

Advantages of Pipelined restoring Division:

Simpler Control Logic:

- Pipelined restoring division uses a relatively straightforward sequence of additions, subtractions, and shifts, making the control logic easier to design compared to SRT or Goldschmidt, which involve more complex operations like partial quotient selection or multiplication.

Hardware Friendly:

- It is suitable for fixed-point arithmetic and can be implemented with simple hardware without the need for high-speed multipliers or floating-point units, which are required for Newton-Raphson and Goldschmidt methods.

Disadvantages of pipelined restoring division:

Slower Convergence:

- Pipelined restoring division is typically slower than iterative methods like Newton-Raphson and Goldschmidt, which converge quadratically and are better suited for high-performance systems.

Not Ideal for Floating-Point:

- It's less efficient or practical for floating-point division due to precision and normalization issues. Methods like SRT are more optimized for IEEE floating-point standards.

More Clock Cycles:

- Since Pipelined restoring division performs one operation per bit of the divisor, it can require more clock cycles than Goldschmidt or Newton-Raphson, which compute multiple bits per iteration using multiplication.

The comparison table:

Here is the comparison table that compares our method (pipelined restoring) with other methods such as SRT, Newton-Raphson and Goldschmidt.

Comparison of Division Algorithms:

Feature / Method	Pipelined Restoring Division	SRT (e.g., Radix-4)	Newton-Raphson	Goldschmidt
Basic Principle	Repeated add/subtract & shift	Digit recurrence with lookup table	Iterative reciprocal approximation	Parallel scaling of numerator & denominator
Latency (32-bit)	~32 cycles	~10–20 cycles	~4–6 cycles	~3–5 cycles
Convergence Rate	Linear (1 bit per iteration)	Logarithmic (radix-dependent)	Quadratic	Quadratic
Accuracy (per iteration)	1 bit	$\sim \log_2(\text{radix})$ bits	Doubles each iteration	Doubles each iteration
Iterations Required (32-bit)	~32	~5 (radix-4)	3–4 iterations	3–4 iterations
Initial Approximation	Not required	Table lookup	Required (LUT or estimate)	Required (LUT or estimate)
Hardware Complexity	Low	Medium	High (requires multipliers)	High (optimized for parallelism)
Floating-Point Suitability	Low	Moderate	Excellent	Excellent
Typical Applications	Simple processors, microcontrollers	General-purpose processors	High-performance CPUs	GPUs, SIMD/parallel processors

HANDWORKED EXAMPLE:

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Assumptions:-

$$XLEN = 4$$

STAGE-LIST = 4'b1111 (all stages enabled)

$$DIVidend(a) = 13 = 1101$$

$$DIVisor(b) = 3 = 0011$$

cycle-wise computation Table :-

cycle	dividend (P)	m ($d(P)dividend$ $\gg shift$)	n ($d(P)divisor$)	$q(m \geq n)$	$t(m-n)$	$d(new \text{ dividend})$	quotient[$i+1$]
0	1101	0001	0011	0	0000	0110	0000
1	0110	0011	0011	1	0000	0011	0010
2	0011	0010	0011	0	0000	1001	0010
3	1001	1001	0011	1	0110	0110	0011

Final Result:-

$$\text{Final quotient (quo)} = 0100 = 4$$

$$\text{Final remainder (rem)} = 0001 = 1$$

check:-

$$13 \div 3 = 4, \text{ remainder} = 1 \quad \checkmark$$

CODE AND IMPLEMENTATION:

Github: <https://github.com/AnanthNaik/EE311/tree/main>

Division Algorithms:

1. SRT Division

- Type: Digit recurrence method.
- Process: Iteratively computes the quotient one digit at a time, allowing quotient digits to be in a redundant form (e.g., $\{-1, 0, 1\}$).
- Key Formula:

$$r_{i+1} = r_i - q_i \cdot d \cdot \beta^{-i}$$

$$Q = \sum_{i=1}^n q_i \cdot \beta^{-i}$$

- Where:
 - ◆ r_i is the current remainder
 - ◆ q_i is the quotient digit (can be -1, 0, or +1 in radix-2, or more digits in higher radices).
 - ◆ d is the divisor.
 - ◆ β is the radix (e.g., 2, 4, 8).
 - ◆ Q is the final quotient.
- Process:
 - ◆ Normalize dividend and divisor (make divisor in $[0.5, 1]$).
 - ◆ Initialize $r_0 = \text{dividend}$, $Q = 0$.
 - ◆ Use lookup tables or decision logic to determine q_i from r_i and d .
 - ◆ Update r_{i+1} and accumulate q_i into the final quotient.
 - ◆ Repeat for required precision.
 - ◆ Convert redundant results to binary if needed.
- Features:
 - ◆ Uses lookup tables or decision logic to select quotient digits.
 - ◆ Handles one digit per cycle; moderate speed.

- ◆ Common in FPUs due to balanced performance and complexity.

2. Newton-Raphson Division

- Type: Iterative approximation method.
- Process: Converts division into reciprocal approximation using:

$$x_{n+1} = x_n(2 - B \cdot x_n)$$

$$Q = A \cdot x_n$$

Where, Q is the final quotient.

- Features:
 - ◆ Fast convergence (doubles precision each step).
 - ◆ Requires good initial estimate and multiple multipliers.
 - ◆ Efficient for scalar floating-point units and CPUs.

3. Goldschmidt Division

- Type: Iterative approximation method.
- Process: Simultaneously scales both dividend and divisor to force the divisor toward 1:

$Q = A/B$, $F = \text{scaling factor to bring } B \rightarrow 1$.

$$F_i = 2 - B_i \cdot x_i$$

$$A_{i+1} = A_i \cdot F_i, \quad B_{i+1} = B_i \cdot F_i$$

$$Q = A_n.$$

Where, Q is the final quotient and x_0 is initial approximation.

- Features:
 - ◆ High parallelism; suitable for SIMD/GPU architectures.
 - ◆ Fully multiplication-based; no division or subtraction required in loop.
 - ◆ Converges quickly and efficiently in hardware.