

Lab 3

**Adrian Goh Jun Wei
(U1721134D)**

**Parametric Surfaces
and Solids**



(1) 3D-plane

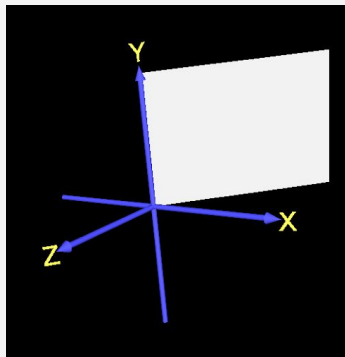


Fig 1.1

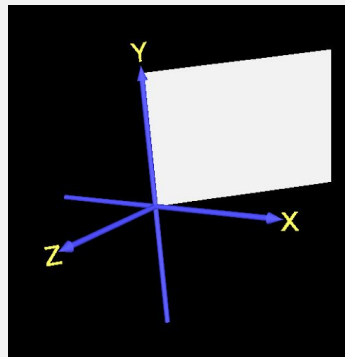


Fig 1.2

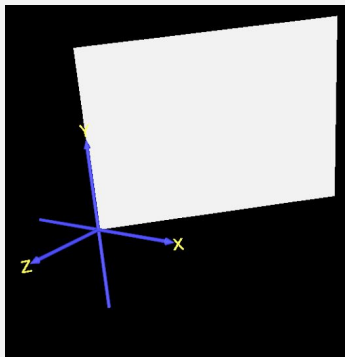


Fig 1.3

The files can be found in the directory **/3D-plane**

- Fig 1.1: 3D-plane.wrl
- Fig 1.2: 3D-plane-resolution.wrl
- Fig 1.3: 3D-plane-domain.wrl

For the 3D-plane (Fig 1.1):

- Parametric representation is defined as
$$\begin{aligned} \mathbf{x} &= \mathbf{u}, \\ \mathbf{y} &= \mathbf{v}, \\ \mathbf{z} &= -\mathbf{u} \end{aligned}$$
- \mathbf{u}, \mathbf{v} is given a parameter domain **[0 1 0 1]**
- Sampling resolution is **[75 75]**

The rendering in Fig 1.1 was repeated with a sampling resolution of **[300 300]** to give Fig 1.2. With a higher resolution, the plane takes a longer time to render.

The rendering in Fig 1.1 was repeated with a parameter domain of **[0 2 0 2]** to give Fig 1.3. As such, the length of each side of the plane is twice as long.

(2) 3D-triangle

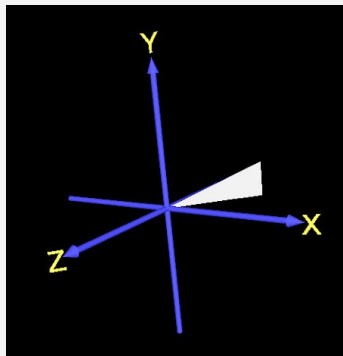


Fig 2.1

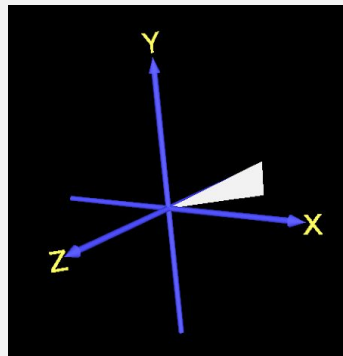


Fig 2.2

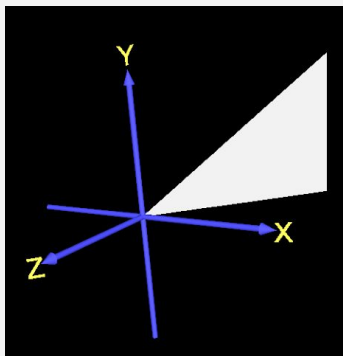


Fig 2.3

The files can be found in the directory **/3D-triangle**

- Fig 2.1: 3D-triangle.wrl
- Fig 2.2: 3D-triangle-resolution.wrl
- Fig 2.3: 3D-triangle-domain.wrl

For the 3D-triangle (Fig 2.1):

- Parametric representation is defined as
$$\begin{aligned} \mathbf{x} &= \mathbf{u}, \\ \mathbf{y} &= \mathbf{u} * \mathbf{v}, \\ \mathbf{z} &= -\mathbf{u} \end{aligned}$$
- \mathbf{u}, \mathbf{v} is given a parameter domain **[0 0.5 0 0.5]**
- Sampling resolution is **[75 75]**

The rendering in Fig 2.1 was repeated with a sampling resolution of **[300 300]** to give Fig 2.2. With a higher resolution, the triangle takes a longer time to render.

The rendering in Fig 2.1 was repeated with a parameter domain of **[0 1 0 1]** to give Fig 2.3. Since the height of the triangle is defined as $\mathbf{u} * \mathbf{v}$, it will increase by 4 times from $(1 \times 1 = 1)$ to $(2 \times 2 = 4)$ while the base only increases by 2x. Thus, the shape of the triangle changes and is no longer similar to the original triangle (Fig 2.1)

(3) bilinear-surface

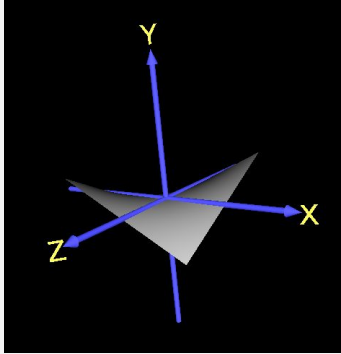


Fig 3.1

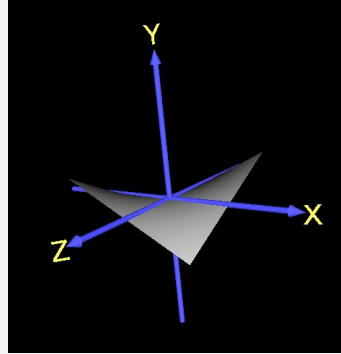


Fig 3.2

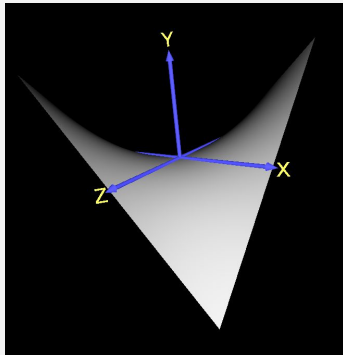


Fig 3.3

The files can be found in the directory **/bilinear-surface**

- Fig 3.1: *bilinear-surface.wrl*
- Fig 3.2: *bilinear-surface-resolution.wrl*
- Fig 3.3: *bilinear-surface-domain.wrl*

For the bilinear surface (Fig 3.1):

- Parametric representation is defined as
$$\begin{aligned} \mathbf{x} &= \mathbf{u}, \\ \mathbf{y} &= \mathbf{u} * \mathbf{v}, \\ \mathbf{z} &= -\mathbf{v} \end{aligned}$$
- \mathbf{u}, \mathbf{v} is given a parameter domain **[-0.5 0.5 -0.5 0.5]**
- Sampling resolution is **[75 75]**

The rendering in Fig 3.1 was repeated with a sampling resolution of **[300 300]** to give Fig 3.2. With a higher resolution, the surface takes a longer time to render.

The rendering in Fig 3.1 was repeated with a parameter domain of **[-1 1 -1 1]** to give Fig 3.3.

(4) sphere

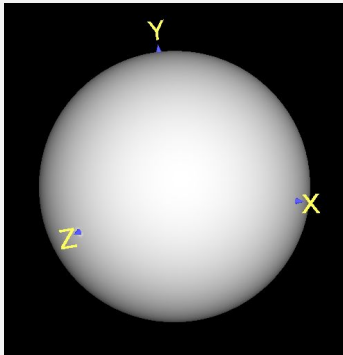


Fig 4.1

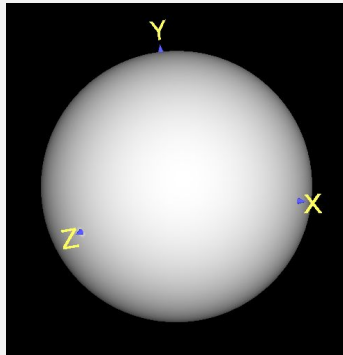


Fig 4.2

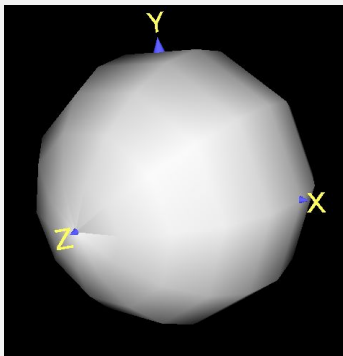


Fig 4.3

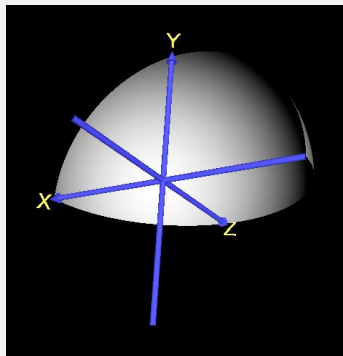


Fig 4.4

The files can be found in the directory **/sphere**

- Fig 4.1: sphere.wrl
- Fig 4.2: sphere-resolution-increase.wrl
- Fig 4.3: sphere-resolution-decrease.wrl
- Fig 4.4: sphere-domain.wrl

For the sphere (Fig 4.1):

- Parametric representation is defined as
$$\begin{aligned}x &= \cos(2\pi u) \sin(\pi v), \\y &= \sin(2\pi u) \sin(\pi v), \\z &= \cos(\pi v)\end{aligned}$$
- u, v is given a parameter domain **[0 1 0 1]**
- Sampling resolution is **[75 75]**

The rendering in Fig 4.1 was repeated with a sampling resolution of **[300 300]** to give Fig 4.2. With a higher resolution, the surface takes a longer time to render. As curve surfaces are made of multiple flat surfaces joining together, the circle looks less curvy (Fig 4.3) with a lower resolution of **[10 10]**

The rendering in Fig 4.1 was repeated with a parameter domain of **[0 0.5 0 0.5]** to give Fig 4.4. Range of x, y, z are $[-1, 1]$, $[0, 1]$, and $[0, 1]$ respectively. Thus, only a portion of the sphere is rendered.

(5) ellipsoid

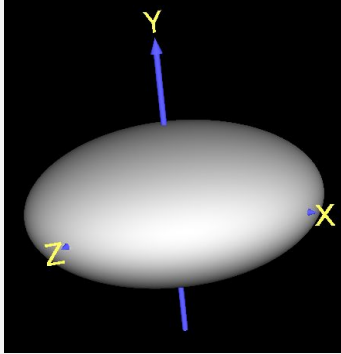


Fig 5.1

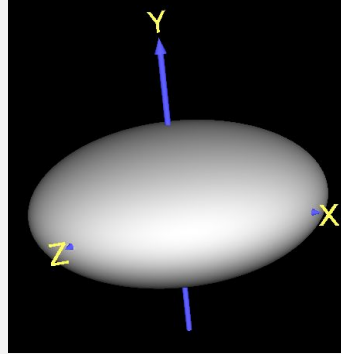


Fig 5.2

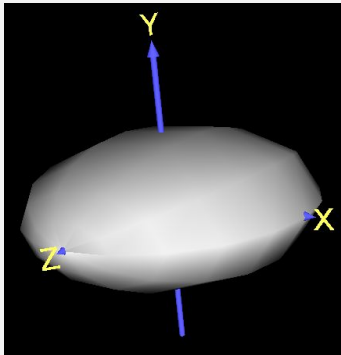


Fig 5.3

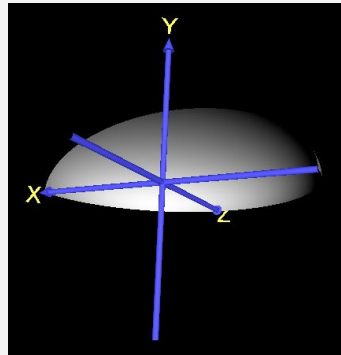


Fig 5.4

The files can be found in the directory **/ellipsoid**

- Fig 5.1: ellipsoid.wrl
- Fig 5.2: ellipsoid-resolution-increase.wrl
- Fig 5.3: ellipsoid-resolution-decrease.wrl
- Fig 5.4: ellipsoid-domain.wrl

For the ellipsoid (Fig 5.1):

- Parametric representation is defined as
$$\begin{aligned}x &= \cos(2\pi u) \sin(\pi v), \\y &= 0.5 \sin(2\pi u) \sin(\pi v), \\z &= \cos(\pi v)\end{aligned}$$
- u, v is given a parameter domain **[0 1 0 1]**
- Sampling resolution is **[75 75]**

The rendering in Fig 5.1 was repeated with a sampling resolution of **[300 300]** to give Fig 5.2. With a higher resolution, the surface takes a longer time to render. As curve surfaces are made of multiple flat surfaces joining together, the circle looks less curvy (Fig 5.3) with a lower resolution of **[10 10]**

The rendering in Fig 5.1 was repeated with a parameter domain of **[0 0.5 0 0.5]** to give Fig 5.4. Range of x, y, z are $[-1, 1]$, $[0, 0.5]$, and $[0, 1]$ respectively. Thus, only a portion of the ellipsoid is rendered.

(6) cone

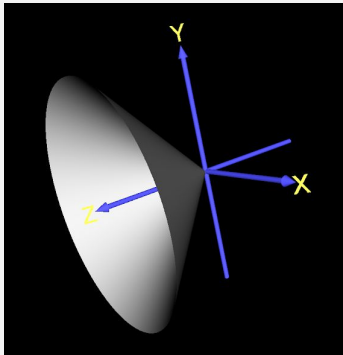


Fig 6.1

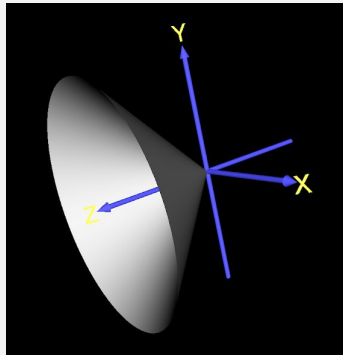


Fig 6.2

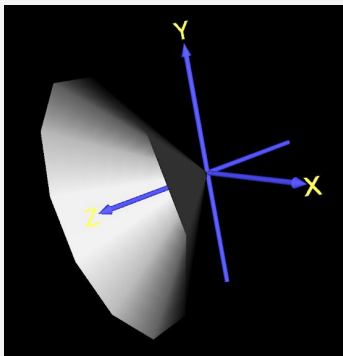


Fig 6.3

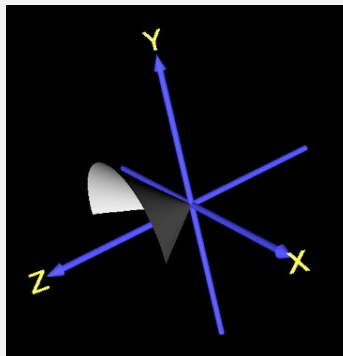


Fig 6.4

The files can be found in the directory **/cone**

- Fig 6.1: cone.wrl
- Fig 6.2: cone-resolution-increase.wrl
- Fig 6.3: cone-resolution-decrease.wrl
- Fig 6.4: cone-domain.wrl

For the cone (Fig 6.1):

- Parametric representation is defined as
$$\mathbf{x} = \mathbf{v} \cdot \cos(2 \cdot \pi \cdot \mathbf{u}),$$
$$\mathbf{y} = \mathbf{v} \cdot \sin(2 \cdot \pi \cdot \mathbf{u}),$$
$$\mathbf{z} = \mathbf{v}$$
- \mathbf{u}, \mathbf{v} is given a parameter domain **[0 1 0 1]**
- Sampling resolution is **[75 75]**

The rendering in Fig 6.1 was repeated with a sampling resolution of **[300 300]** to give Fig 6.2. With a higher resolution, the surface takes a longer time to render. As curve surfaces are made of multiple flat surfaces joining together, the circle looks less curvy (Fig 6.3) with a lower resolution of **[10 10]**

The rendering in Fig 6.1 was repeated with a parameter domain of **[0 0.5 0 0.5]** to give Fig 6.4. Range of x, y, z are $[-0.5, 0.5]$, $[0, 0.5]$, and $[0, 0.5]$ respectively. Thus, half the cone is rendered, and height of cone is halved.

(7) solid-box

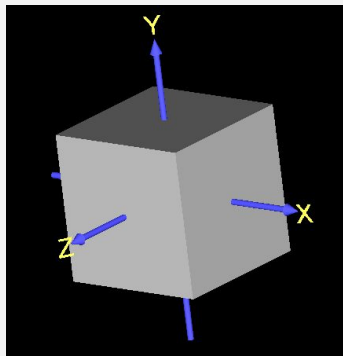


Fig 7.1

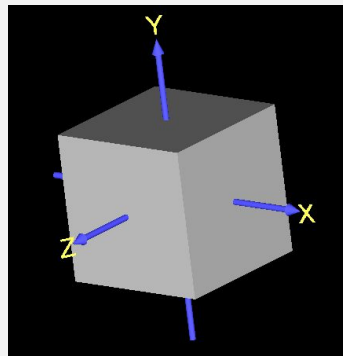


Fig 7.2

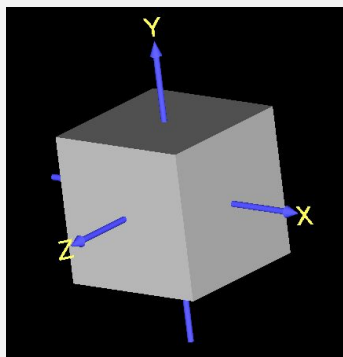


Fig 7.3

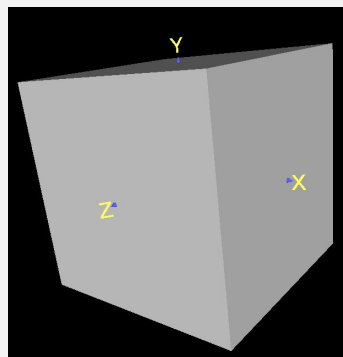


Fig 7.4

The files can be found in the directory **/solid-box**

- Fig 7.1: solid-box.wrl
- Fig 7.2: solid-box-resolution-increase.wrl
- Fig 7.3: solid-box-resolution-decrease.wrl
- Fig 7.4: solid-box-domain.wrl

For the solid box (Fig 7.1):

- Parametric representation is defined as
$$\begin{aligned} \mathbf{x} &= \mathbf{u}, \\ \mathbf{y} &= \mathbf{v}, \\ \mathbf{z} &= \mathbf{w} \end{aligned}$$
- $\mathbf{u}, \mathbf{v}, \mathbf{w}$ are all given a parameter domain **[-0.5 0.5]**
- Sampling resolution is **[75 75 75]**

The rendering in Fig 7.1 was repeated with a sampling resolution of **[300 300]** to give Fig 7.2. With a higher resolution, the surface takes a longer time to render. As the surfaces are all flat, the circle looks the same with a lower resolution of **[10 10]**

The rendering in Fig 7.1 was repeated with a parameter domain of **[-1 1 -1 1 -1 1]** to give Fig 7.4. Range of x, y, z are all $[-1, 1]$ respectively. Thus, the length of the sides are all doubled.

(8) solid-sphere

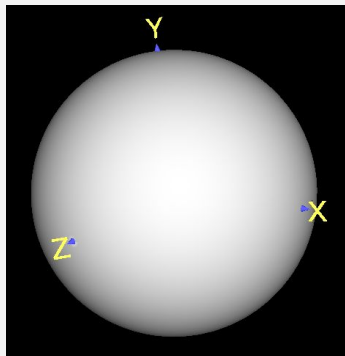


Fig 8.1

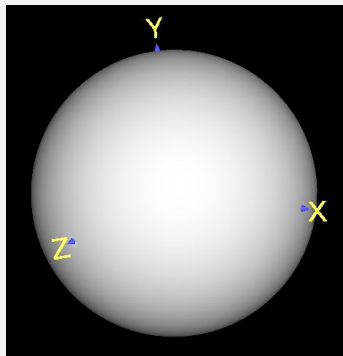


Fig 8.2

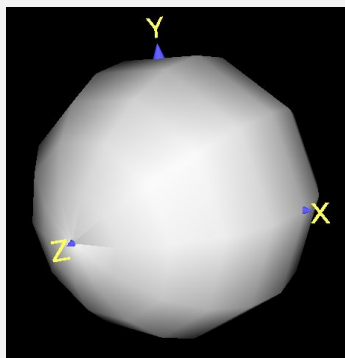


Fig 8.3

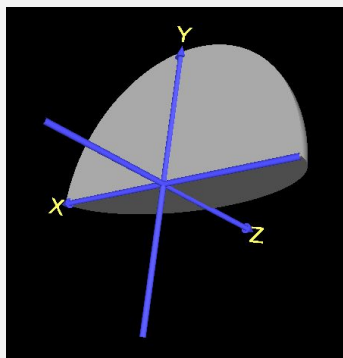


Fig 8.4

The files can be found in the directory **/solid-sphere**

- Fig 8.1: solid-sphere.wrl
- Fig 8.2: solid-sphere-resolution-increase.wrl
- Fig 8.3: solid-sphere-resolution-decrease.wrl
- Fig 8.4: solid-sphere-domain.wrl

For the solid sphere (Fig 8.1):

- Parametric representation is defined as
$$\begin{aligned}x &= \cos(2\pi u) \sin(\pi v), \\y &= \sin(2\pi u) \sin(\pi v), \\z &= w \cos(\pi v)\end{aligned}$$
- **u, v, w** are all given a parameter domain **[0 1]**
- Sampling resolution is **[75 75 75]**

The rendering in Fig 8.1 was repeated with a sampling resolution of **[300 300]** to give Fig 8.2. With a higher resolution, the surface takes a longer time to render. As curve surfaces are made of multiple flat surfaces joining together, the sphere looks less curvy (Fig 8.3) with a lower resolution of **[10 10]**

The rendering in Fig 8.1 was repeated with a parameter domain of **[0 0.5 0 0.5 0 0.5]** to give Fig 8.4. Range of x, y, z are [-1, 1], [0, 1], and [0, 1] respectively. Thus, only a portion of the sphere is rendered.

(9) solid-cylinder

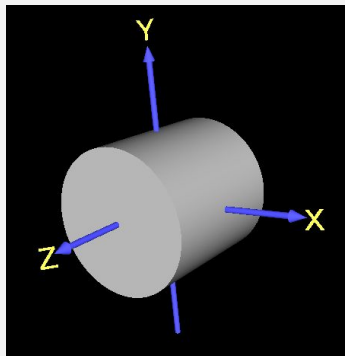


Fig 9.1

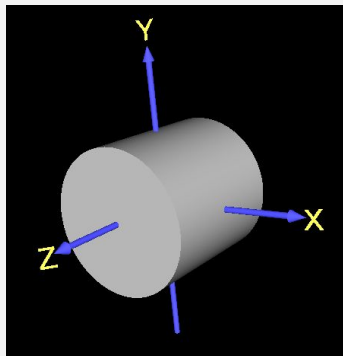


Fig 9.2

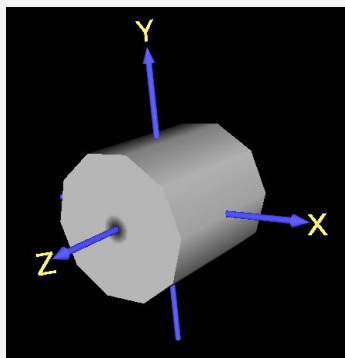


Fig 9.3

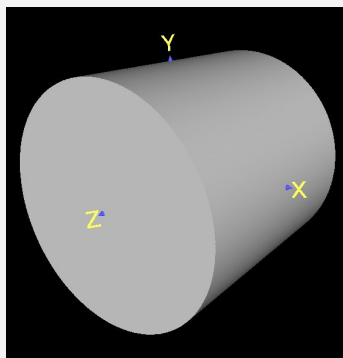


Fig 9.4

The files can be found in the directory **/solid-cylinder**

- Fig 9.1: solid-cylinder.wrl
- Fig 9.2: solid-cylinder-resolution-increase.wrl
- Fig 9.3: solid-cylinder-resolution-decrease.wrl
- Fig 9.4: solid-cylinder-domain.wrl

For the solid cylinder (Fig 9.1):

- Parametric representation is defined as
$$\mathbf{x} = \mathbf{v} * \cos(2 * \pi * \mathbf{u})$$
$$\mathbf{y} = \mathbf{v} * \sin(2 * \pi * \mathbf{u})$$
$$\mathbf{z} = \mathbf{w}$$
- **u, v, w** are all given a parameter domain **[-0.5 0.5]**
- Sampling resolution is **[75 75 75]**

The rendering in Fig 9.1 was repeated with a sampling resolution of **[300 300]** to give Fig 9.2. With a higher resolution, the surface takes a longer time to render. As curve surfaces are made of multiple flat surfaces joining together, the cylinder looks less curvy (Fig 9.3) with a lower resolution of **[10 10]**

The rendering in Fig 9.1 was repeated with a parameter domain of **[-1 1 -1 1 -1 1]** to give Fig 9.4. Range of x, y, z are all **[-1, 1]** respectively. Thus, the cylinder's radius and length are all doubled.

(10) solid-cone

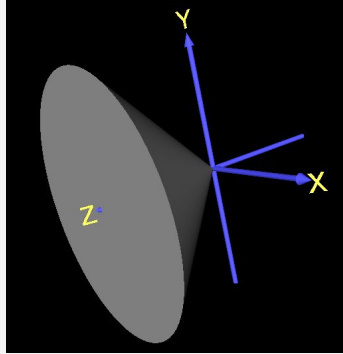


Fig 10.1

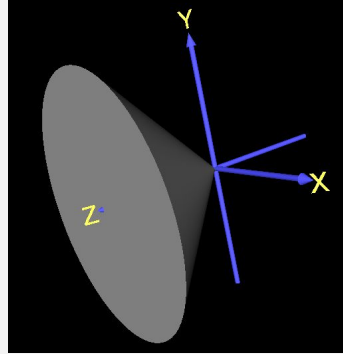


Fig 10.2

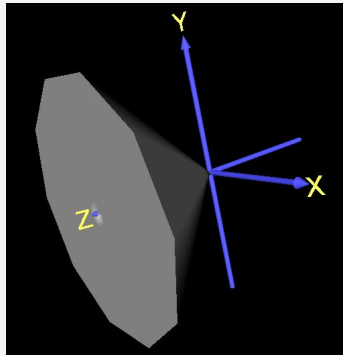


Fig 10.3

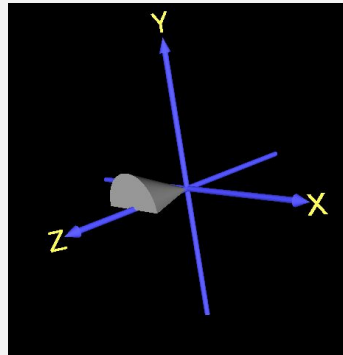


Fig 10.4

The files can be found in the directory **/solid-cone**

- Fig 10.1: *solid-cone.wrl*
- Fig 10.2: *solid-cone-resolution-increase.wrl*
- Fig 10.3: *solid-cone-resolution-decrease.wrl*
- Fig 10.4: *solid-cone-domain.wrl*

For the solid cone (Fig 10.1):

- Parametric representation is defined as

$$\mathbf{x} = \mathbf{w} * \mathbf{v} * \cos(2 * \pi * \mathbf{u})$$

$$\mathbf{y} = \mathbf{w} * \mathbf{v} * \sin(2 * \pi * \mathbf{u})$$

$$\mathbf{z} = \mathbf{w}$$

- $\mathbf{u}, \mathbf{v}, \mathbf{w}$ are all given a parameter domain **[0 1]**
- Sampling resolution is **[75 75 75]**

The rendering in Fig 10.1 was repeated with a sampling resolution of **[300 300]** to give Fig 10.2. With a higher resolution, the surface takes a longer time to render. As curve surfaces are made of multiple flat surfaces joining together, the cone looks less curvy (Fig 10.3) with a lower resolution of **[10 10]**

The rendering in Fig 10.1 was repeated with a parameter domain of **[0 0.5 0 0.5 0 0.5]** to give Fig 10.4. Range of x, y, z are $[-0.25, 0.25]$, $[0, 0.25]$, and $[0, 0.5]$ respectively. Thus, half the cone is rendered, cone's radius (along x and y axis) is divided by 4 and cone's height (along z axis) is divided by 2.

(11a) sinx

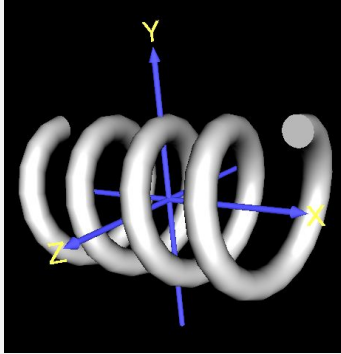


Fig 11.1

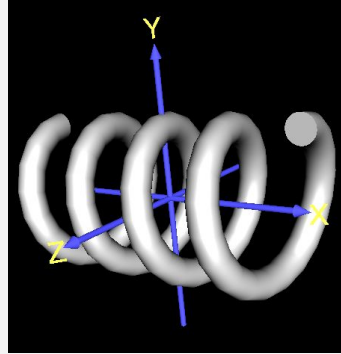


Fig 11.2

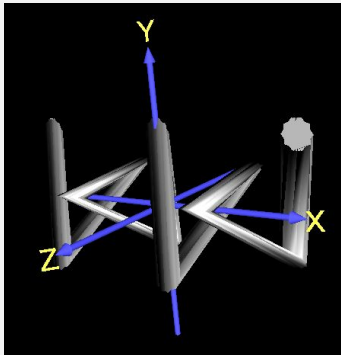


Fig 11.3

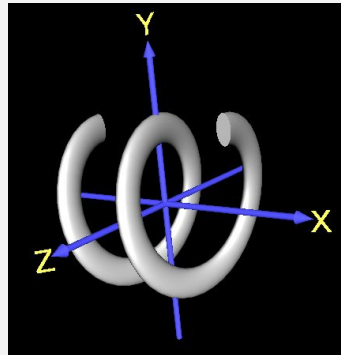


Fig 11.4

The files can be found in the directory **/sinx**

- Fig 11.1: *sinx.wrl*
- Fig 11.2: *sinx-resolution-increase.wrl*
- Fig 11.3: *sinx-resolution-decrease.wrl*
- Fig 11.4: *sinx-domain.wrl*

For the spiral (Fig 11.1):

- Parametric representation is defined as

$$\mathbf{x} = (0.1 * \mathbf{v} * \cos(2 * \pi * \mathbf{u})) + \mathbf{w}$$

$0.1 * \mathbf{v} * \cos(2 * \pi * \mathbf{u})$ is used to defined the circular shape of the end of the object. \mathbf{w} is used to allow it to have a spiral looking shape along the x-axis

$$\mathbf{y} = (0.1 * \sin(2 * \pi * \mathbf{u}) + 0.5) * \cos(4 * \pi * \mathbf{w})$$

$$\mathbf{z} = (0.1 * \sin(2 * \pi * \mathbf{u}) + 0.5) * \sin(4 * \pi * \mathbf{w})$$

$0.1 * \sin(2 * \pi * \mathbf{u})$ is used to defined the circular shape of the end of the object. Adding **0.5** let the radius of the circle of 0.5 unit around the x-axis. As the object revolves around the x-axis in a counter-clockwise manner from y-axis to z-axis, y is multiplied by $\cos(4 * \pi * \mathbf{w})$ while z is multiplied by $\sin(4 * \pi * \mathbf{w})$. $4 * \pi$ is used instead of $2 * \pi$ to make it revolves around x-axis twice.

- \mathbf{u} , \mathbf{v} , \mathbf{w} are all given a parameter domain **[-1 1]**
- Sampling resolution is **[75 75 75]**

(11b) $\sin x$

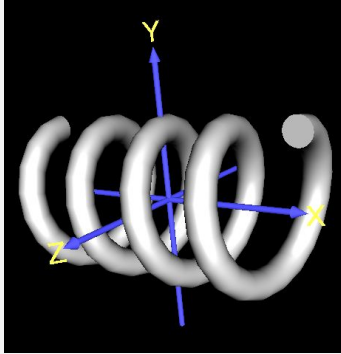


Fig 11.1

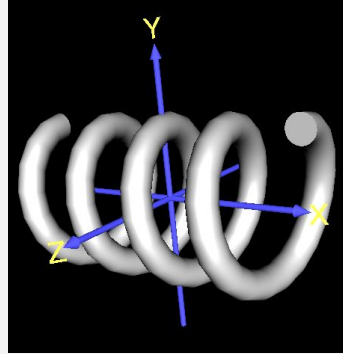


Fig 11.2

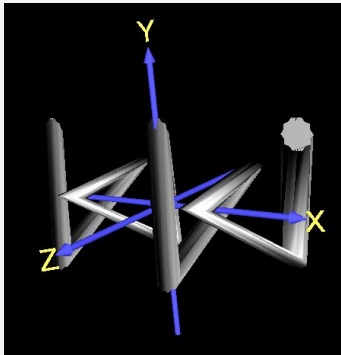


Fig 11.3

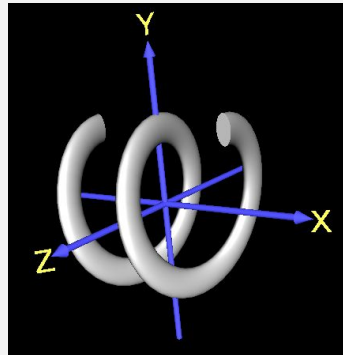


Fig 11.4

The rendering in Fig 11.1 was repeated with a sampling resolution of **[300 300 300]** to give Fig 11.2. With a higher resolution, the surface takes a longer time to render. However, as curve surfaces are made of multiple flat surfaces and polygons joining together, the object looks more curvy.

On the other hand, with a sampling resolution of **[10 10 10]**, the object appears more distorted and sharp (Fig 11.3). This is because object 10 samples are taken for w , thus resulting in 10 sharp turns on the object, as it moves through the x -axis. In addition, the end of the object is no longer circular because 10 samples of u are taken.

The rendering in Fig 11.1 was repeated with a parameter domain of **[-0.5 0.5 -0.5 0.5 -0.5 0.5]** to give Fig 11.4. Referring to its parametric representation, the end of the spiral object is no longer round but ellipse-shaped as v is halved. Also, the number of oscillation on each side of the x -axis is also halved as the range of w is halved.