ECE 657A - Assignment 1

Date Submitted: February 04, 2022

```
In [85]: # Data Manipulation
import pandas as pd
import numpy as np

# Charting
import seaborn as sns
sns.set(style="ticks", color_codes=True)
import matplotlib.pyplot as plt
from scipy import stats

# Misc
import warnings
warnings.filterwarnings("ignore")
```

Question 1: Assessment of Data

Abalone Dataset

We begin by looking at the features of the dataset itself.

```
In [86]: # Columns/Features of Dataset
abalone_columns = ['Sex','Length','Diameter','Height','Whole weight','Shucked weight
# Loading the Data set
abalone_df=pd.read_csv('abalone.csv',names=abalone_columns)
```

1. Exploratory Data Analysis

```
In [87]: abalone_df.head() #Top 5 rows of the dataframe
```

Shucked Out[87]: Whole Viscera Shell Rings Sex Length Diameter Height weight weight weight weight 0 0.455 0.365 0.095 0.5140 0.1010 15 M 0.2245 0.150 7 1 0.350 0.265 0.090 0.2255 0.0995 0.0485 0.070 2 F 0.530 0.420 0.135 0.6770 0.2565 0.1415 0.210 9 3 Μ 0.440 0.365 0.125 0.5160 0.2155 0.1140 0.155 10 7 0.330 0.255 0.080 0.2050 0.0895 0.0395 0.055

	Length	Diameter	Height	Whole weight	Shucked weight	Viscera weight	Shell weight
count	4177.000000	4177.000000	4177.000000	4177.000000	4177.000000	4177.000000	4177.000000
mean	0.523992	0.407881	0.139516	0.828742	0.359367	0.180594	0.238831
std	0.120093	0.099240	0.041827	0.490389	0.221963	0.109614	0.139203
min	0.075000	0.055000	0.000000	0.002000	0.001000	0.000500	0.001500
25%	0.450000	0.350000	0.115000	0.441500	0.186000	0.093500	0.130000
50%	0.545000	0.425000	0.140000	0.799500	0.336000	0.171000	0.234000
75%	0.615000	0.480000	0.165000	1.153000	0.502000	0.253000	0.329000
max	0.815000	0.650000	1.130000	2.825500	1.488000	0.760000	1.005000
4							

In [89]:

abalone_df.info() #info about the datatype of columns

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 4177 entries, 0 to 4176
Data columns (total 9 columns):
```

#	Column	Non-Null Count	Dtype
0	Sex	4177 non-null	object
1	Length	4177 non-null	float64
2	Diameter	4177 non-null	float64
3	Height	4177 non-null	float64
4	Whole weight	4177 non-null	float64
5	Shucked weight	4177 non-null	float64
6	Viscera weight	4177 non-null	float64
7	Shell weight	4177 non-null	float64
8	Rings	4177 non-null	int64
dtyp	es: float64(7),	int64(1), object	(1)
memo	ry usage: 293.8+	KB	

1.1 Feature Analysis

1.1.1 Univariate Analysis

Initially, we take up each column separately and then explore the ranges of the columns

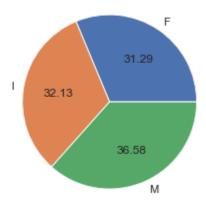
1.1.1.1 Gender distribution

We look at the categorical data first and it's distribution on the entire dataset. We have made a pie chart to explain the total distribution of the category 'Sex' on the dataset.

```
abalone_df.groupby('Sex').size().plot(kind='pie', autopct='%.2f')
plt.ylabel("")
plt.title("Percentage distribution of the category (SEX)")
```

Out[90]: Text(0.5, 1.0, 'Percentage distribution of the category (SEX)')

Percentage distribution of the category (SEX)

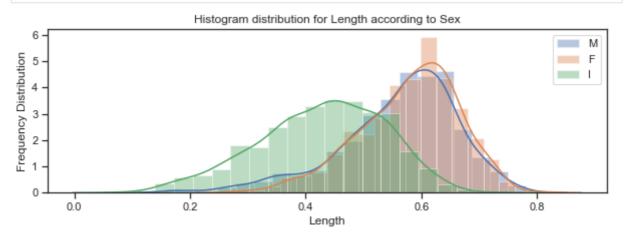


We find that all three categories - M,F,I are almost equally distributed among the dataset with a little extra records for the M category.

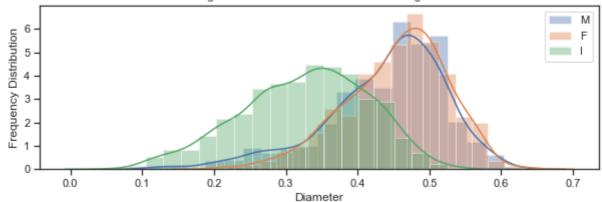
```
In [91]: #Creating a function to plot similar Histogram for showing distribution according to
    def plot_histogram_against_sex(field, b):
        plt.figure(figsize=(10,3))
        sns.distplot(abalone_df.loc[abalone_df['Sex']=='M'][field],bins=b,kde=True,label
        sns.distplot(abalone_df.loc[abalone_df['Sex']=='F'][field],bins=b,kde=True,label
        sns.distplot(abalone_df.loc[abalone_df['Sex']=='I'][field],bins=b,kde=True,label
        plt.legend()
        plt.title("Histogram distribution for {} according to Sex".format(field))
        plt.xlabel(field)
        plt.ylabel("Frequency Distribution")
        plt.show()
```

Then, we move on to exploring range and distribution frequency of various features on the basis of sex. We are doing that by plotting histograms for the features. We are plotting histograms because this is singular feature analysis.

```
plot_histogram_against_sex("Length",20) # Histogram of Length on basis of sex plot_histogram_against_sex("Diameter",20) # Histogram of diameter on basis of sex plot_histogram_against_sex("Height",20) # Histogram of height on basis of sex
```







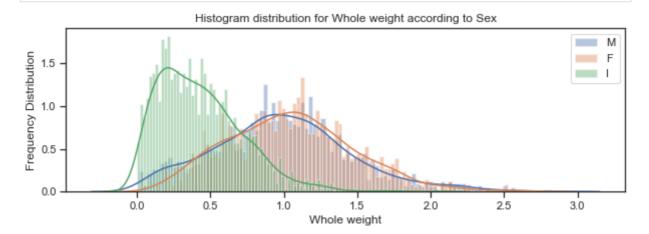
Histogram distribution for Height according to Sex 15.0 Frequency Distribution F 12.5 10.0 7.5 5.0 2.5 0.0 0.8 1.0 0.0 0.2 0.4 0.6 1.2 Height

1.1.1.2 Weight measurements analysis

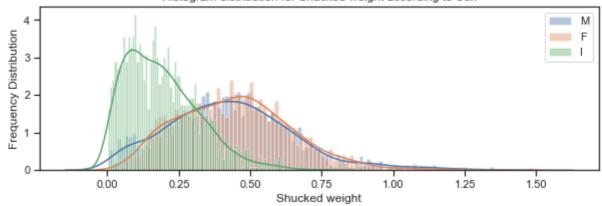
Now, we explore the weight categories similarly using the histogram plot.

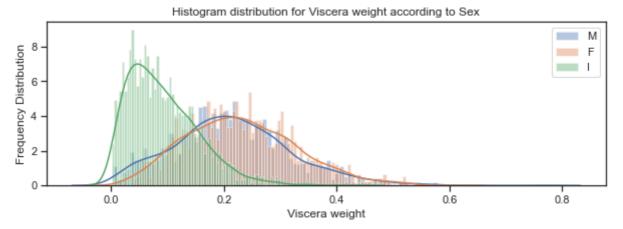
In [93]:

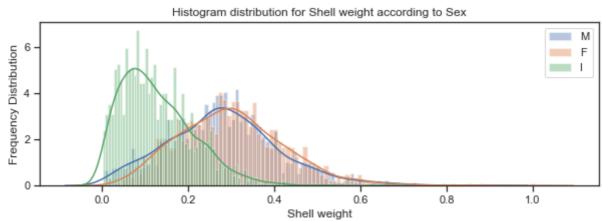
plot_histogram_against_sex("Whole weight",100) # Histogram of Whole weight on basis plot_histogram_against_sex("Shucked weight",100) # Histogram of Shucked weight on ba plot_histogram_against_sex("Viscera weight",100) # Histogram of Viscera weight on ba plot_histogram_against_sex("Shell weight",100) # Histogram of Shell weight on basis









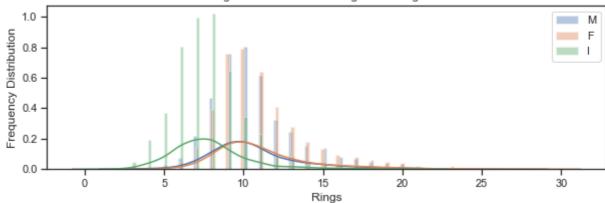


1.1.1.3 Rings distribution

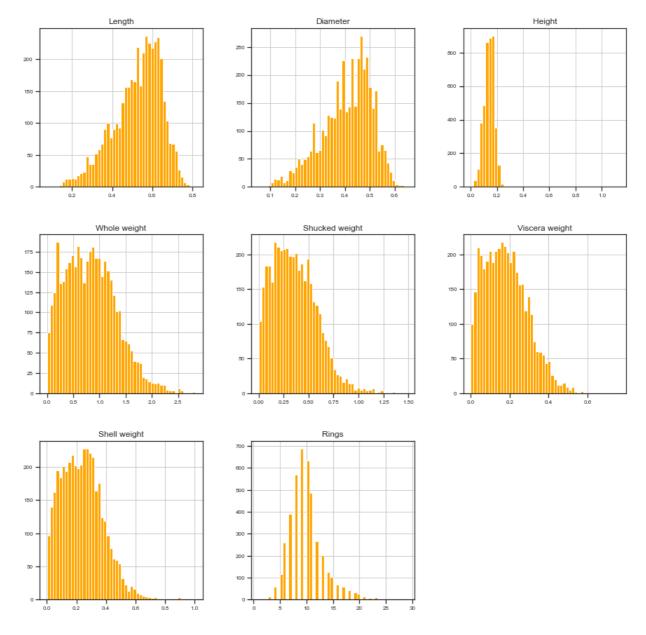
Rings frequency distribution is explored separately because this is our target value in the dataset.

```
In [94]: # Histogram of Rings on basis of sex
plot_histogram_against_sex("Rings",100)
```





We also look at the data frequency distribution by plotting all the histograms at once to show their ranges and variations.

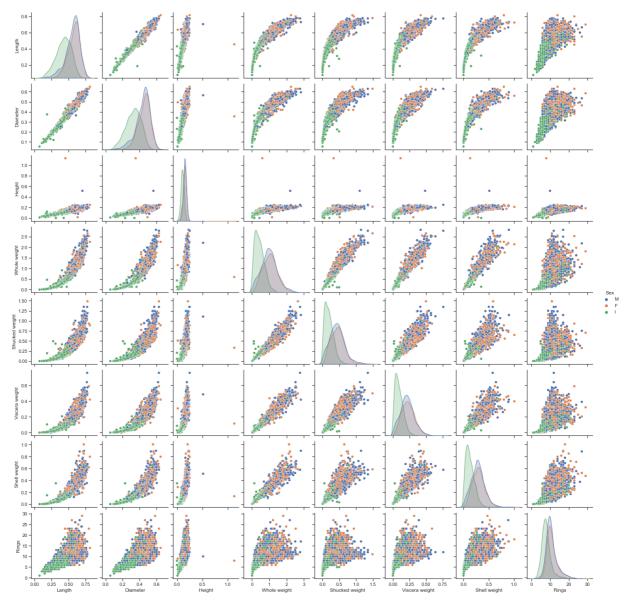


1.1.2 Bivariate Analysis

This analysis is being done to compare any two features together and see their relations with each other. To do so, we will make pair plots on the basis of the 'Sex' category column for all other features

In [96]:
Plotting the Pair-plots for all numerical columns with respect to each other categ
sns.pairplot(abalone_df, hue="Sex", vars=('Length','Diameter','Height','Whole weight

Out[96]: <seaborn.axisgrid.PairGrid at 0x218b0c84850>

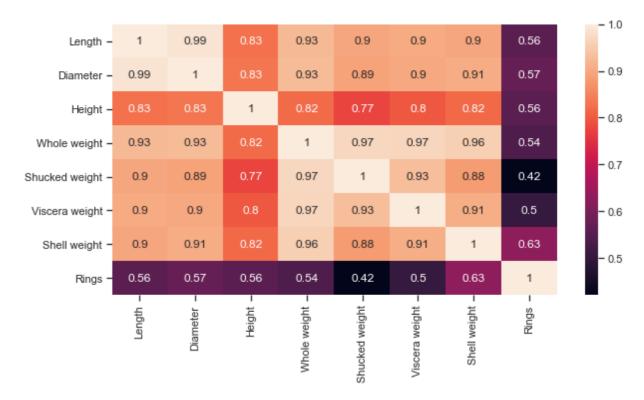


By looking at the pairplots, we can see that some fields like whole weight, shucked weight, viscera weight and shell weight are correlated because they are creating an almost linear graph when they are plotted together on a graph. The fields Length and Diameter are also closely correlated because they have a perfect linear graph when plotted together.

The pair plots showed the correlation quite strongly but to emphasize it more prominently we shall make a heatmap to find very clearly what fields are correlated.

```
In [97]: plt.figure(figsize=(10,5))
    sns.heatmap(abalone_df.corr(method='pearson'),annot=True)
```

Out[97]: <AxesSubplot:>



As expected and seen from the pairplots plotted above, we can see that weight categories are correlated. But the most correlated fields are Diameter and Length.

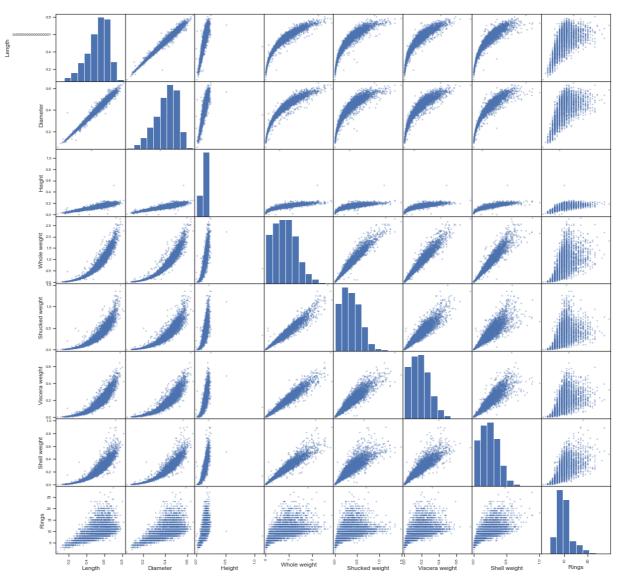
2. Do we have any missing data?

```
In [98]:
           abalone_df.isnull().sum()
                             0
Out[98]:
          Length
                             0
                             0
          Diameter
          Height
                             0
          Whole weight
                             0
          Shucked weight
                             0
          Viscera weight
                             0
          Shell weight
                             0
          Rings
          dtype: int64
```

To check for missing values we used the is_null function with sum function. Since the output values of all columns are zeroes, we can conclude that there is no missing data in the dataset

We will also plot a scatterplot to show whether or not there is any missing data

```
In [99]: scatterplot = pd.plotting.scatter_matrix(abalone_df, alpha=0.4, figsize=(20,20))
```



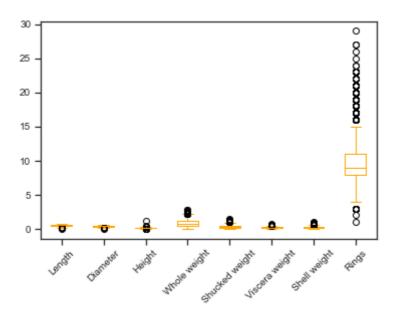
Since, in the scatter plot, we can't seem to find any missing holes or missing chunks of data, we will conclude there is no missing data.

3. Diversity of Data

We will make a boxplot to plot the range of all features to see how diverse the data is in terms of the range distribution.

```
temp_df = abalone_df.drop(columns=['Sex'])#dropping sex as it is a categorical colum
pd.plotting.boxplot(temp_df , grid=False, rot=45, fontsize=10, color="orange")
```

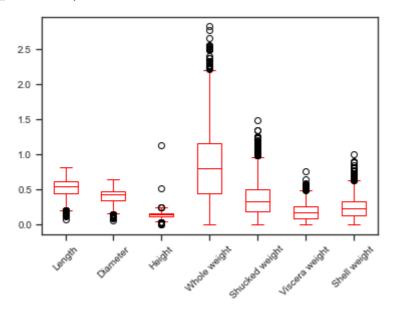
Out[100... <AxesSubplot:>



We will drop the 'Rings' column as clearly seen in the above graph that it's range is totally different from our other features.

```
temp_df1 = temp_df.drop(columns=['Rings'])
pd.plotting.boxplot(temp_df1, grid=False, rot=45, fontsize=10, color="red")
```

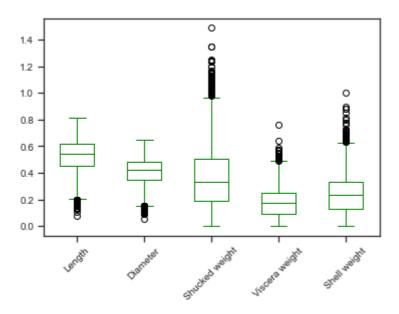
Out[101... <AxesSubplot:>



Here, in the above graph we see that columns whole weight and height have a quite a varying range from the other columns. So, we will drop whole weight and height columns to see the diversity of other columns more clearly.

```
temp_df2 = temp_df1.drop(columns=['Whole weight','Height'])
pd.plotting.boxplot(temp_df2, grid=False, rot=45, fontsize=10, color="green")
```

Out[102... <AxesSubplot:>

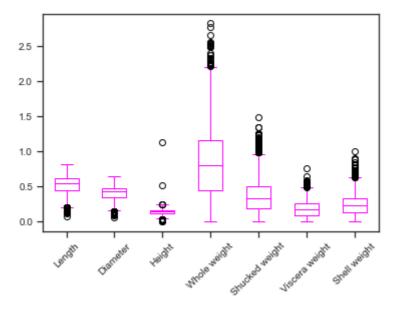


Analyzing from the past 3 graphs where the range is quite varying for all features, we conclude that normalization is required for this dataset.

4. Outliers

```
abalone_features_df = abalone_df.drop(columns=['Sex','Rings']) # removing category a
pd.plotting.boxplot(abalone_features_df, grid=False, rot=45, fontsize=10, color="mag")
```

Out[103... <AxesSubplot:>



We can clearly see some outliers in the ranges, to show it more prominently we'll plot separate boxplots for range.

```
In [104... plt.figure(figsize=(30, 15))
    rows = 3
    cols = 4
    i = 0

i += 1
    plt.subplot(rows, cols, i)
    _ = sns.boxplot(abalone_features_df['Length'], color="orange")
```

```
i += 1
plt.subplot(rows, cols, i)
 = sns.boxplot(abalone_features_df['Diameter'], color="green")
i += 1
plt.subplot(rows, cols, i)
_ = sns.boxplot(abalone_features_df['Height'], color="magenta")
i += 1
plt.subplot(rows, cols, i)
_ = sns.boxplot(abalone_features_df['Whole weight'], color="blue")
i += 1
plt.subplot(rows, cols, i)
_ = sns.boxplot(abalone_features_df['Shucked weight'], color="red")
i += 1
plt.subplot(rows, cols, i)
_ = sns.boxplot(abalone_features_df['Viscera weight'], color="yellow")
i += 1
plt.subplot(rows, cols, i)
_ = sns.boxplot(abalone_features_df['Shell weight'], color="purple")
```

There are clearly prominent outliers in each of the feature as can be seen from the boxplots. The outliers can be just errors as they cannot be naturally occuring. It can be instantiated with an example from the outliers of the height features, all the values of abalone fish height lie in 0 to 0.2 but one height has value more than 1.

0.3 0.4 0.5

5. Is our data set balanced?

0.4 0.5 0.6 Length

0.6 0.8 1.0 Shucked weight 0.7

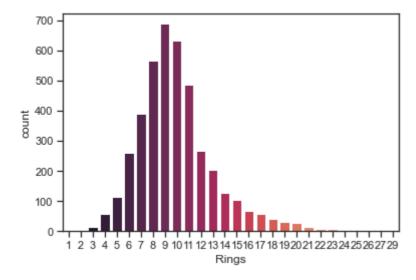
0.2 0.3

```
abalone_df.Sex.unique()

abalone_df['Sex'] = abalone_df['Sex'].replace(['M'],'0')
abalone_df['Sex'] = abalone_df['Sex'].replace(['F'],'1')
abalone_df['Sex'] = abalone_df['Sex'].replace(['I'],'2')
```

To check for the balance in the dataset, we will plot a count plot to see the distribution. If it is a proper bell curve, then it is a balanced set, otherwise it is not.

```
In [106... sns.countplot(x=abalone_df['Rings'],data=abalone_df, palette='rocket')
Out[106... <AxesSubplot:xlabel='Rings', ylabel='count'>
```



We can clearly see that the count plot that is made is a bit skewed and doesn't make a proper bell curve which means data is unbalanced.

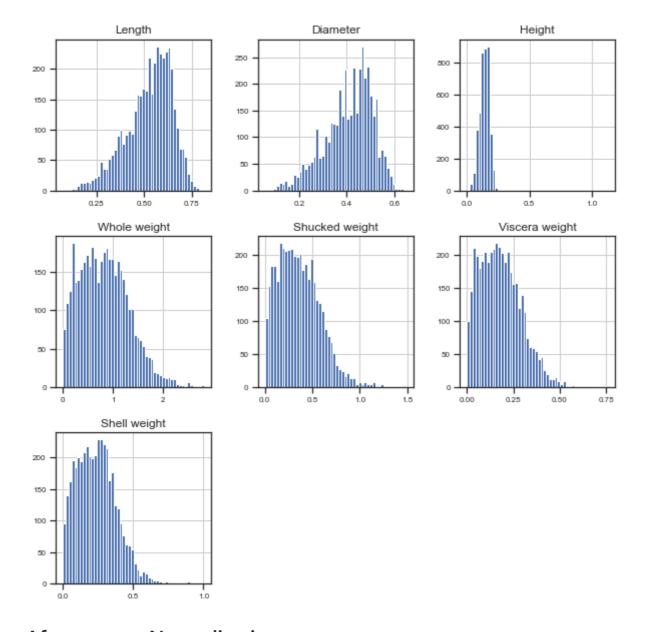
Yes, the dataset is still usable as it not totally unbalanced but slightly unbalanced as can be seen from the slight skewness of the graph.

6. Normalization

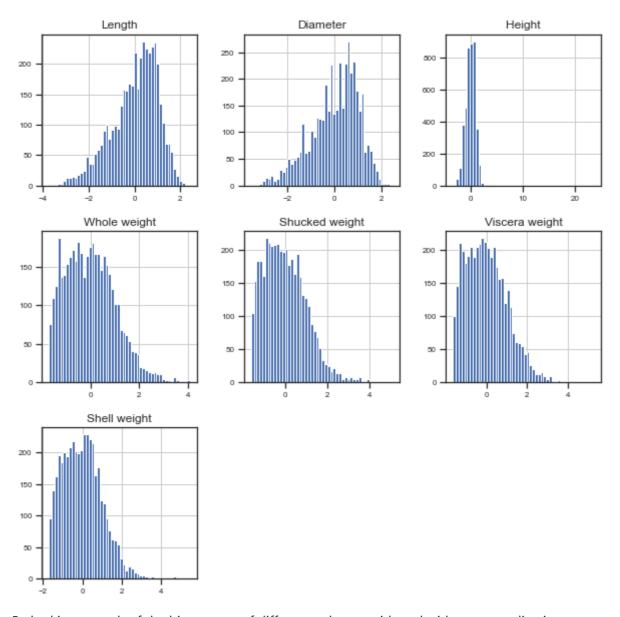
Before Normalization

We shall now begin with the normalization of different numerical features of dataset excluding the target values.

To begin, we plot the histogram plots for checking the shape and range distribution of all features



After z-score Normalization



By looking at each of the histograms of different columns with and without normalization respectively, we deduce that the shape of the graph remains preserved although the range around which all datapoints were centered has changed.

Min-max Normalization

```
In [109...
          abalone_for_normalization = abalone_df.drop(columns=['Sex'])
          #Minmax normalization
          from sklearn.preprocessing import MinMaxScaler, StandardScaler
          cols = list(abalone_for_normalization.columns)
          scaler minmax = MinMaxScaler()
          features_data_x = abalone_for_normalization.drop('Rings', axis = 1).values
          target_y = abalone_for_normalization['Rings'].values
          X_minmax = scaler_minmax.fit_transform(features_data_x)
In [110...
          #Dataframe of minmax normalized data
          abalone_minmax = pd.DataFrame(data=np.column_stack((X_minmax,target_y)),columns=cols
          abalone_minmax.head()
Out[110...
                                             Whole
                                                         Shucked
                                                                       Viscera
                                                                                    Shell
                                                                                          Rings
              Length Diameter
                                Height
                                            weight
                                                          weight
                                                                       weight
                                                                                  weight
```

	Length	Diameter	Height	Whole weight	Shucked weight	Viscera weight	Shell weight	Rings
0	0.513514	0.521008	0.084071	0.181335	0.150303	0.132324	0.147982	15.0
1	0.371622	0.352941	0.079646	0.079157	0.066241	0.063199	0.068261	7.0
2	0.614865	0.613445	0.119469	0.239065	0.171822	0.185648	0.207773	9.0
3	0.493243	0.521008	0.110619	0.182044	0.144250	0.149440	0.152965	10.0
4	0.344595	0.336134	0.070796	0.071897	0.059516	0.051350	0.053313	7.0

It is very clear that the normalization still preserve the shape of the data for all predictors, however, on different scale. all data points were shifted to be centered around the zero and with unit variance)

6(a) Is normalization needed?

Yes, normalization is absolutely needed for this dataset as the ranges of different features are varying too much.

6(b,c) Unormalized Comparison of three values

To clearly observe the difference that normalization makes on dataset, we take specific columns choosing Diameter as a meaningful feature and then comparing it with other two features whole weight and shell weight under different normalization techniques.

```
In [111... # Plot one feature value, sorted from low to high, against two others
    x=['Diameter']; y=['Whole weight','Shell weight']

In [112... abalone_temp = abalone_df[x+y]
    abalone_temp.sort_values(by=x, inplace=True)
    display(abalone_temp.describe())
```

```
Diameter Whole weight Shell weight
count 4177.000000
                      4177.000000
                                  4177.000000
          0.407881
                         0.828742
                                       0.238831
mean
                         0.490389
  std
          0.099240
                                       0.139203
 min
          0.055000
                         0.002000
                                       0.001500
 25%
          0.350000
                         0.441500
                                       0.130000
 50%
          0.425000
                         0.799500
                                       0.234000
 75%
          0.480000
                         1.153000
                                       0.329000
          0.650000
 max
                         2.825500
                                       1.005000
```

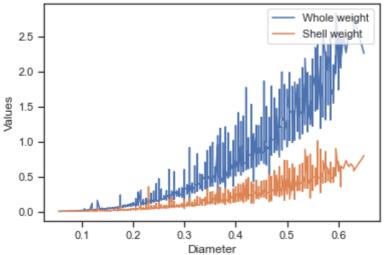
```
abalone_temp.plot(x=x[0], y=y)

plt.legend(loc='upper right')
   plt.title('Increasing {} level compared to {} and {} before normalization'.format(x[
   plt.xlabel('Diameter')
```

```
plt.ylabel('Values')
plt.legend(loc='upper right')
```

Out[113... <matplotlib.legend.Legend at 0x218b88ea610>

Increasing Diameter level compared to Whole weight and Shell weight before normalization



When we look at Whole weight and Shucked weight as they correlate with Rings we see a major need for normalization.

Using Z-Score Normalization

We implement z-score normalization using the sklearn.stats package applied to the entire dataset. Then we once again select our columns of interest. Note that the x and y variables do not need to be updated since they are just the names of the columns being used and they do not change across the three examples.

```
abalone_zscore['Rings'] = abalone_df['Rings']
abalone_zscore['Sex'] = abalone_df['Sex']
abalone_zscore.head()
```

Out[114...

	Length	Diameter	Height	Whole weight	Shucked weight	Viscera weight	Shell weight	Rings	Sex
0	-0.574558	-0.432149	-1.064424	-0.641898	-0.607685	-0.726212	-0.638217	15	0
1	-1.448986	-1.439929	-1.183978	-1.230277	-1.170910	-1.205221	-1.212987	7	0
2	0.050033	0.122130	-0.107991	-0.309469	-0.463500	-0.356690	-0.207139	9	1
3	-0.699476	-0.432149	-0.347099	-0.637819	-0.648238	-0.607600	-0.602294	10	0
4	-1.615544	-1.540707	-1.423087	-1.272086	-1.215968	-1.287337	-1.320757	7	2

```
abalone_temp = abalone_zscore[x+y]
abalone_temp.sort_values(by=x, inplace=True)
display(abalone_temp.describe())
```

	Diameter	Whole weight	Shell weight
count	4.177000e+03	4.177000e+03	4.177000e+03
mean	1.053077e-15	4.231446e-16	7.601719e-16
std	1.000120e+00	1.000120e+00	1.000120e+00

	Diameter	Whole weight	Shell weight
min	-3.556267e+00	-1.686092e+00	-1.705134e+00
25%	-5.833158e-01	-7.897577e-01	-7.819095e-01
50%	1.725193e-01	-5.963767e-02	-3.470794e-02
75%	7.267984e-01	6.613049e-01	6.478319e-01
max	2.440025e+00	4.072271e+00	5.504642e+00

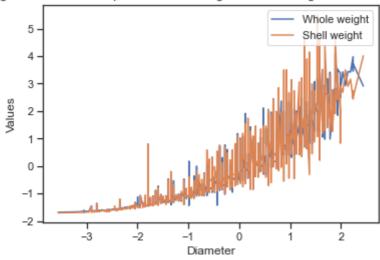
```
In [116...
```

```
plt.figure()
abalone_temp.sort_values(by=x, inplace=True)
abalone_temp.plot(x=x[0], y=y)
plt.legend(loc='upper right')
plt.title('Increasing {} level compared to {} and {} after z-score normalization'.fo
plt.xlabel('Diameter')
plt.ylabel('Values')
plt.legend(loc='upper right')
```

Out[116... <matplotlib.legend.Legend at 0x218b89284c0>

<Figure size 432x288 with 0 Axes>

Increasing Diameter level compared to Whole weight and Shell weight after z-score normalization



Using min-max Normalization

This we simply implement ourselves since the formula is straightforward. the min() and max() functions will produce vectors of the respective values for every feature, then the formula below will normalize all the values of the new abalone minmax matrix appropriately.

In [117...

abalone_minmax.head()

Out[117...

	Length	Diameter	Height	Whole weight	Shucked weight	Viscera weight	Shell weight	Rings
0	0.513514	0.521008	0.084071	0.181335	0.150303	0.132324	0.147982	15.0
1	0.371622	0.352941	0.079646	0.079157	0.066241	0.063199	0.068261	7.0
2	0.614865	0.613445	0.119469	0.239065	0.171822	0.185648	0.207773	9.0
3	0.493243	0.521008	0.110619	0.182044	0.144250	0.149440	0.152965	10.0

	Length	Diameter	Height	Whole weight	Shucked weight	Viscera weight	Shell weight	Rings
4	0.344595	0.336134	0.070796	0.071897	0.059516	0.051350	0.053313	7.0

We can already see a significant difference here from the zscore summary tables, there are no very small or very large numbers any longer, these result from he large differences in scale and variance of the two feautures which zscore preserves.

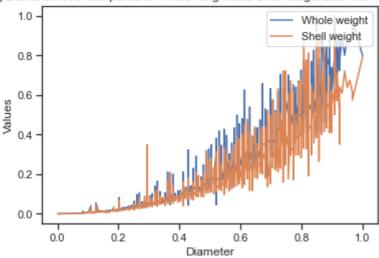
```
plt.figure()
    abalone_minmax.sort_values(by=x, inplace=True)
    abalone_minmax.plot(x=x[0], y=y)

plt.legend(loc='upper right')
    plt.title('Increasing {} level compared to {} and {} after min-max normalization'.fo
    plt.xlabel('Diameter')
    plt.ylabel('Values')
    plt.legend(loc='upper right')
```

Out[118... <matplotlib.legend.Legend at 0x218b8935ca0>

<Figure size 432x288 with 0 Axes>

Increasing Diameter level compared to Whole weight and Shell weight after min-max normalization



We can clearly see that by applying any of the z-score or min-max normalizations, the range graphs of whole weight and shell weight overlap. Hence, normalization is required.

Wine Quality Data Set

```
In [119...
#Columns/Features
D = ['fixed acidity', 'volatile acidity', 'citric acid', 'residual sugar', 'chloride
L = 'quality'
C = 'color'
DL = D + [L]
DC = D + [C]
DLC = DL + [C]
#Loading Data set
wine_r = pd.read_csv("winequality-red.csv", sep=';')
#Loading Data set
wine_w = pd.read_csv("winequality-white.csv", sep=';')
wine_w = pd.read_csv("winequality-white.csv", sep=';')
wine_w = wine_w.copy()
wine_w[C] = np.zeros(wine_w.shape[0],dtype=int)
```

```
wine_r[C]= np.ones(wine_r.shape[0],dtype=int)
wine = pd.concat([wine_w,wine_r])

#Let's see what kind of features we have.
wine.info()
print(wine.shape, wine_r.shape, wine_w.shape)
```

```
<class 'pandas.core.frame.DataFrame'>
Int64Index: 6497 entries, 0 to 1598
Data columns (total 13 columns):
    Column
#
                           Non-Null Count
                                           Dtype
                           -----
0
    fixed acidity
                           6497 non-null
                                           float64
    volatile acidity
                           6497 non-null
                                           float64
1
2
                           6497 non-null
                                           float64
    citric acid
3
    residual sugar
                           6497 non-null
                                           float64
4
    chlorides
                           6497 non-null
                                           float64
5
    free sulfur dioxide
                           6497 non-null
                                           float64
6
    total sulfur dioxide 6497 non-null
                                           float64
7
                           6497 non-null
                                           float64
    density
8
                           6497 non-null
                                           float64
    рΗ
9
                           6497 non-null
                                           float64
    sulphates
                           6497 non-null
10 alcohol
                                           float64
                           6497 non-null
                                           int64
11
    quality
                           6497 non-null
                                           int32
12 color
dtypes: float64(11), int32(1), int64(1)
memory usage: 685.2 KB
(6497, 13) (1599, 13) (4898, 13)
```

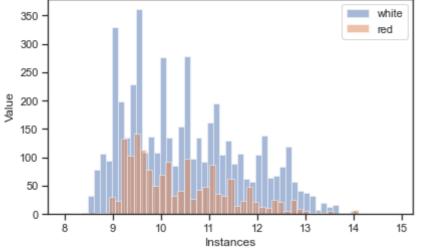
```
In [121...
    plt.figure(figsize=(6,6))
    col='alcohol'
    aw = wine_w.hist(column=col, bins=50, alpha=0.5, label="white")
    wine_r.hist(column=col, bins=50, alpha=0.5, label="red", ax=aw)

plt.title('The distribution of {} concentration in the white wine (0) and the red wi plt.xlabel('Instances')
    plt.ylabel('Value')
    plt.legend(loc='upper right')
    plt.grid()

plt.tight_layout()
    plt.show()
```

<Figure size 432x432 with 0 Axes>





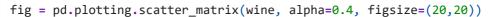
In [120...

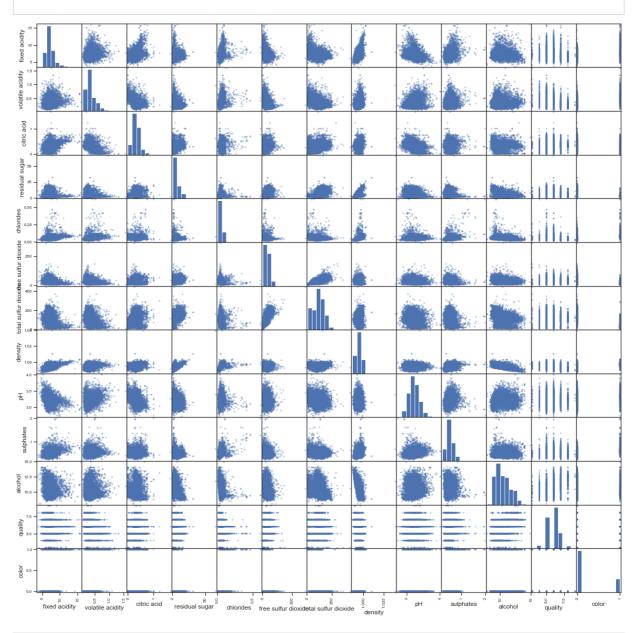
Out[122... fixed acidity volatile acidity 0 citric acid 0 residual sugar 0 chlorides 0 free sulfur dioxide 0 total sulfur dioxide 0 density 0 рΗ 0 sulphates 0 alcohol 0 quality 0 color

dtype: int64

It seems there are no zeros or null entries in the dataset. To be more sure we can look at a scatterplot of all the data, and we see that there do not seem to be any large holes or irregular missing blocks. The bands of points for quality and color are the result of those features having a discrete set of values, they are categorical variables.

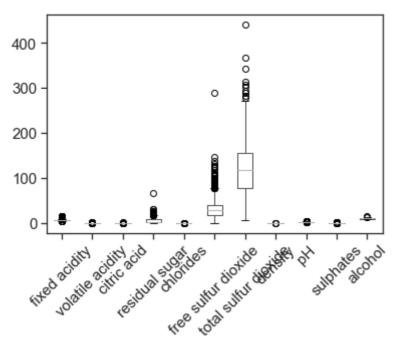
In [123...





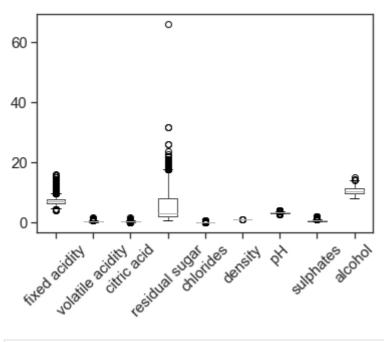
```
x = wine.drop(columns=['color', 'quality'])
pd.plotting.boxplot(x, grid=False, rot=45, fontsize=15)
```

Out[124... <AxesSubplot:>

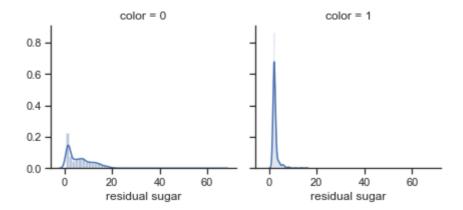


In [125...
 x = wine.drop(columns=['color', 'quality', 'free sulfur dioxide', 'total sulfur diox
 pd.plotting.boxplot(x, grid=False, rot=45, fontsize=15)
 #Even then, the remaining features have a wide range, so normalization will be criti

Out[125... <AxesSubplot:>



```
In [126...
#Finding the outliers
g = sns.FacetGrid(wine, col="color")
g.map(sns.distplot, 'residual sugar', hist=True, kde=True)
g.add_legend();
#For the red wine, we can see less sugar on average comparing with its percentage in
#Also, it is clear that we have some outliers in the white wine with max value of 65
```

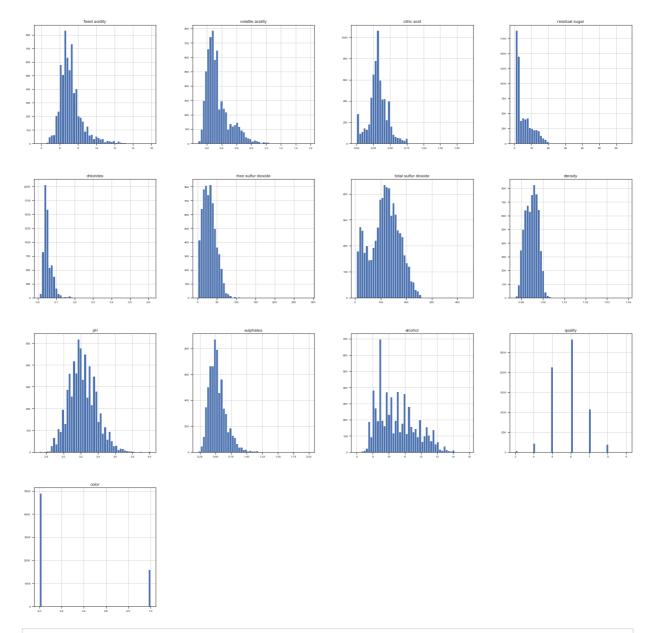


Similar to the residual sugar distribution, we can see for the white wine the range of the free sulfur dioxide extends till 289 mg/dm³ which is pretty far away from its average of 35mg/dm³. On the other hand, the range of the same feature in the red wine samples is: max = 72 and min = 1 and average of 15.

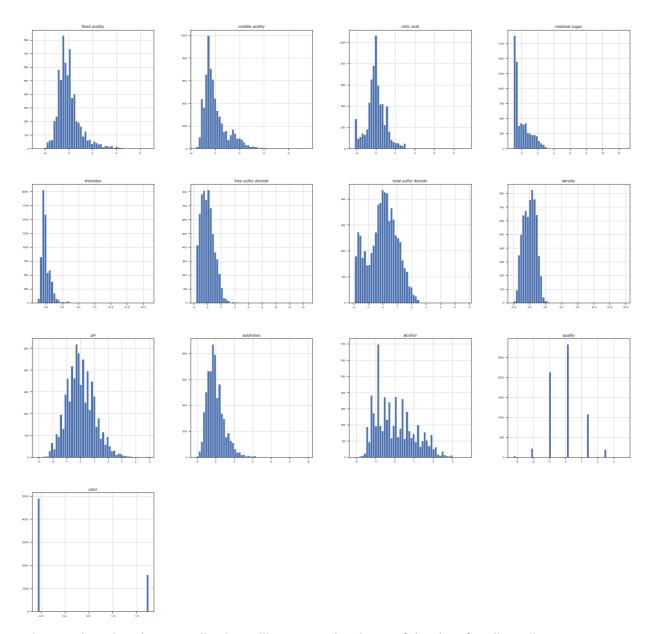
```
In [127... #is our dataset for wine quality balanced wine.quality.unique()
```

Out[127... array([6, 5, 7, 8, 4, 3, 9], dtype=int64)

It looks like that we have only 7 levels of quality among all wine samples we have! Thus, most of the wine samples of both types (white and red) classified with quality in the range of {5,6,7}.



```
from scipy import stats
    # Normalization with zscore
plt.figure()
wine_znormalized = wine.apply(stats.zscore) # Repeated ahead
wine_znormalized.hist(figsize=(30, 30), bins=50, xlabelsize=8, ylabelsize=8)
```



It is very clear that the normalization still preserve the shape of the data for all predictors, however, on different scale. all data points were shifted to be centered around the zero and with unit variance)

We implement z-score normalization using the sklearn.stats package applied to the entire dataset. Then we once again select out the columns of interest. Note that the x and y variables do not need to be updated since they are just the names of the columns being used and they do not change across the three examples.

```
# Plot one feature value, sorted from low to high, against two others
x=['alcohol']; y=['pH','density']
w_aqc = wine[x+y]
w_aqc.sort_values(by=x, inplace=True)
display(w_aqc.describe())
```

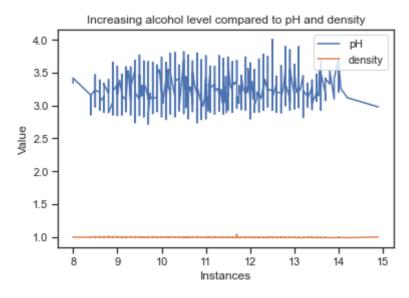
	alcohol	рН	density
count	6497.000000	6497.000000	6497.000000
mean	10.491801	3.218501	0.994697
std	1.192712	0.160787	0.002999
min	8.000000	2.720000	0.987110

	alcohol	рН	density
25%	9.500000	3.110000	0.992340
50 %	10.300000	3.210000	0.994890
75%	11.300000	3.320000	0.996990
max	14.900000	4.010000	1.038980

```
In [131...
w_aqc.plot(x=x[0], y=y)
# w_aqc.hist(column=y, bins=10, alpha=.5)

plt.legend(loc='upper right')
plt.title('Increasing {} level compared to {} and {}'.format(x[0],y[0],y[1]))
plt.xlabel('Instances')
plt.ylabel('Value')
plt.legend(loc='upper right')
```

Out[131... <matplotlib.legend.Legend at 0x218a4545490>



```
In [132...
wine_zscore = wine.loc[:, ~wine.columns.isin(['quality', 'color'])].apply(stats.zsco
wine_zscore["quality"] = wine["quality"]
wine_zscore["color"] = wine["color"]
w_aqc_zscore = wine_zscore[x+y]

w_aqc_zscore.sort_values(by=x, inplace=True)
display(w_aqc_zscore.describe())
```

	alcohol	рН	density
count	6.497000e+03	6.497000e+03	6.497000e+03
mean	-3.439863e-15	2.998610e-15	-5.780439e-15
std	1.000077e+00	1.000077e+00	1.000077e+00
min	-2.089350e+00	-3.100615e+00	-2.530192e+00
25%	-8.316152e-01	-6.748622e-01	-7.859527e-01
50%	-1.608231e-01	-5.287424e-02	6.448888e-02
75%	6.776670e-01	6.313125e-01	7.648525e-01

	alcohol	рН	density
max	3.696231e+00	4.923029e+00	1.476879e+01

```
In [133... wine_zscore.head()

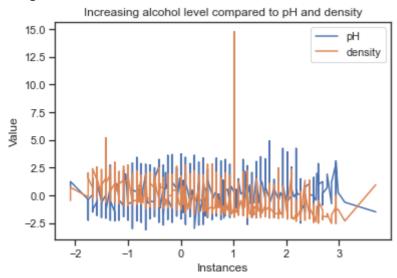
Out[133... fixed volatile citric residual chlorides sulfur sulfur density pH s
```

	fixed acidity	volatile acidity	citric acid	residual sugar	chlorides	sulfur dioxide	total sulfur dioxide	density	рН	s
0	-0.166089	-0.423183	0.284686	3.206929	-0.314975	0.815565	0.959976	2.102214	-1.359049	-
1	-0.706073	-0.240949	0.147046	-0.807837	-0.200790	-0.931107	0.287618	-0.232332	0.506915	-
2	0.682458	-0.362438	0.559966	0.306208	-0.172244	-0.029599	-0.331660	0.134525	0.258120	-
3	-0.011808	-0.666161	0.009406	0.642523	0.056126	0.928254	1.243074	0.301278	-0.177272	-
4	-0.011808	-0.666161	0.009406	0.642523	0.056126	0.928254	1.243074	0.301278	-0.177272	-

```
In [134...
    plt.figure()
    w_aqc_zscore.sort_values(by=x, inplace=True)
    w_aqc_zscore.plot(x=x[0], y=y)
    plt.legend(loc='upper right')
    plt.title('Increasing {} level compared to {} and {}'.format(x[0],y[0],y[1]))
    plt.xlabel('Instances')
    plt.ylabel('Value')
    plt.legend(loc='upper right')
```

Out[134... <matplotlib.legend.Legend at 0x218a4215fa0>

<Figure size 432x288 with 0 Axes>



Using min-max Normalization

This we simply implement ourselves since the formula is straightforward. the min() and max() functions will produce vectors of the respective values for every feature, then the formula below will normalize all the values of the new wine-minmax matrix appropriately.

```
In [135...
wine_minmax = (wine-wine.min())/(wine.max()-wine.min())
wine_minmax["quality"] = wine["quality"]
```

```
wine_minmax["color"] = wine["color"]

w_aqc_minmax = wine_minmax[x+y]
display(w_aqc_minmax.describe())
```

	alcohol	рН	density		
count	6497.000000	6497.000000	6497.000000		
mean	0.361131	0.386435	0.146262		
std	0.172857	0.124641	0.057811		
min	0.000000	0.000000	0.000000		
25%	0.217391	0.302326	0.100829		
50%	0.333333	0.379845	0.149990		
75%	0.478261	0.465116	0.190476		
max	1.000000	1.000000	1.000000		

In [136...

wine_minmax.head()

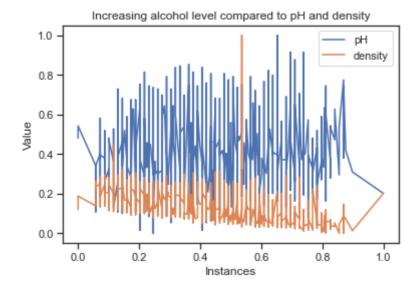
Out[136...

	fixed acidity	volatile acidity	citric acid	residual sugar	chlorides	free sulfur dioxide	total sulfur dioxide	density	рН	sulphat
0	0.264463	0.126667	0.216867	0.308282	0.059801	0.152778	0.377880	0.267785	0.217054	0.1292
1	0.206612	0.146667	0.204819	0.015337	0.066445	0.045139	0.290323	0.132832	0.449612	0.1516
2	0.355372	0.133333	0.240964	0.096626	0.068106	0.100694	0.209677	0.154039	0.418605	0.1235
3	0.280992	0.100000	0.192771	0.121166	0.081395	0.159722	0.414747	0.163678	0.364341	0.1011
4	0.280992	0.100000	0.192771	0.121166	0.081395	0.159722	0.414747	0.163678	0.364341	0.1011
								_		

We can already see a significant difference here from the zscore summary tables, there are no very small or very large numbers any longer, these result from he large differences in scale and variance of the two feautures which zscore preserves.

```
plt.figure()
    w_aqc_minmax.sort_values(by=x, inplace=True)
    w_aqc_minmax.plot(x=x[0], y=y)

plt.legend(loc='upper right')
    plt.title('Increasing {} level compared to {} and {}'.format(x[0],y[0],y[1]))
    plt.xlabel('Instances')
    plt.ylabel('Value')
    plt.legend(loc='upper right')
```



2. Classification for KNN

2.1. Abalone

```
# Using three datasets: unnormalized, zscore normalized and minmax normalized abalone_dataframe_unnormal = abalone_df abalone_dataframe_zscore = abalone_zscore abalone_dataframe_minmax = abalone_minmax abalone_target = "Rings" # Target variable
```

1. Divide the data into a training set and a test set (80%, 20%) Note: set the random seed for splitting, use random state=27 in the sci-kit learn train test split function to get the same split every time you run the program.

```
# Creating functions to generate a train-test split and analyzing the train test spl
from sklearn.model_selection import train_test_split

def generate_train_test_splits(df,target):
    X = df.drop(target, axis = 1)
    y = df[target]

# Train and test split
    X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.20, random return X_train, X_test, y_train, y_test

def analyze_train_test_splits(*args):
    for split in args:
        display(split.count())
```

```
# Train, test set for zscore normalized
abalone_zscore_X_train, abalone_zscore_X_test, abalone_zscore_y_train, abalone_zscor
# Train, test set for minmax normalized
abalone_minmax_X_train, abalone_minmax_X_test, abalone_minmax_y_train, abalone_minma

print("\n*** Analysis for zscore normalized ***\n")
analyze_train_test_splits(abalone_zscore_X_train, abalone_zscore_X_test, abalone_zscore_X_test)
```

```
print("\n*** Analysis for minmax normalized ***\n")
analyze_train_test_splits(abalone_minmax_X_train, abalone_minmax_X_test, abalone_min
```

```
*** Analysis for zscore normalized ***
Length
                3341
Diameter
                3341
               3341
Height
               3341
Whole weight
Shucked weight 3341
Viscera weight 3341
Shell weight
               3341
                3341
Sex
dtype: int64
               836
Length
Diameter
               836
               836
Height
              836
Whole weight
Shucked weight 836
Viscera weight 836
               836
Shell weight
Sex
                836
dtype: int64
3341
836
*** Analysis for minmax normalized ***
Length
                3341
Diameter
               3341
               3341
Height
Whole weight
               3341
Shucked weight 3341
Viscera weight 3341
Shell weight 3341
dtype: int64
Length
               836
               836
Diameter
               836
Height
              836
Whole weight
Shucked weight 836
Viscera weight 836
Shell weight
              836
dtype: int64
3341
836
```

2. Start by training the model with the classifier's default parameters. Use the train set and test the model on the test set. Note that different values of k will lead to different results.

```
In [141...
# Defining wrapper functions for knn classification for reusability

from sklearn.neighbors import KNeighborsClassifier
from sklearn.metrics import classification_report,confusion_matrix, accuracy_score

# The below function accepts train-test splits, value of k, method(for weighted KNN)
def knn_classify(X_train, X_test, y_train, y_test,n=None,method=None):
    knn_args = {}

# Assessing the arguments
if n is not None:
    knn_args['n_neighbors'] = n

if method == "e":
    knn_args['weights'] = "distance"
```

```
if method == "m":
                  knn_args['weights'] = "distance"
                  knn_args['metric'] = "manhattan"
              # Run KNN based upon arguments passed to the current function
              knn = KNeighborsClassifier(**knn_args) # Defining model
              knn.fit(X train, y train) # Running the model
              predictions = knn.predict(X_test) # Making predictions
              accuracy = accuracy_score(y_test, predictions) # Calculating accuracy
              return accuracy
          # The below function is just to analyze the predictions, confusion matrix
          def knn analyze(predictions,y test):
              print("\n*** Confusion Matrix ***\n")
              print(confusion_matrix(y_test,predictions))
              print("\n*** Classification Report ***\n")
              print(classification_report(y_test,predictions))
              accuracy = accuracy_score(y_test,predictions)
              print("\n*** Accuracy ***\n")
              print(accuracy)
In [142...
          # Calculating accuracy for default value of k i.e. 5
          abalone_zscore_accuracy = knn_classify(abalone_zscore_X_train, abalone_zscore_X_test
          abalone_minmax_accuracy = knn_classify(abalone_minmax_X_train, abalone_minmax_X_test
In [143...
          print("Accuracy for zscore = {}".format(abalone_zscore_accuracy))
          print("Accuracy for minmax = {}".format(abalone_minmax_accuracy))
         Accuracy for zscore = 0.22009569377990432
         Accuracy for minmax = 0.215311004784689
```

3. To find the best value for k, you need to compute accuracy for a range of values of k so you can "tune" the classifier. Using these scores, plot a figure of accuracy vs k. Report the best k in terms of classification accuracy.

```
#k_values = [1,5,10,15,20,25,30,35]
k_values = range(4,100)
abalone_zscore_accuracies = []
abalone_minmax_accuracies = []

for k in k_values:
    acc1 = knn_classify(abalone_zscore_X_train, abalone_zscore_X_test, abalone_zscore_acc2 = knn_classify(abalone_minmax_X_train, abalone_minmax_X_test, abalone_minma
    abalone_zscore_accuracies.append(acc1)
    abalone_minmax_accuracies.append(acc2)

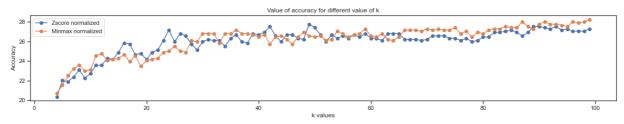
# Multiplying accuracies by 100 for better comparison
abalone_zscore_accuracies = [x*100 for x in abalone_zscore_accuracies]
abalone_minmax_accuracies = [x*100 for x in abalone_minmax_accuracies]
```

```
plt.figure(figsize=(20,3))
plt.plot(k_values, abalone_zscore_accuracies, marker='o')
```

```
plt.plot(k_values, abalone_minmax_accuracies, marker='o')

plt.xlabel("k values")
plt.ylabel("Accuracy")
plt.title("Value of accuracy for different value of k")
plt.legend(["Zscore normalized","Minmax normalized"])
```

Out[145... <matplotlib.legend.Legend at 0x218a39cf970>



```
In [146... # Finding the maximum accuracy
    zscore_max_accuracy = max(abalone_zscore_accuracies)
    minmax_max_accuracy = max(abalone_minmax_accuracies)

# Finding the best value of k
    zscore_best_k = k_values[abalone_zscore_accuracies.index(zscore_max_accuracy)]
    minmax_best_k = k_values[abalone_minmax_accuracies.index(minmax_max_accuracy)]

print("*** Best value of k for zscore = {} ***".format(zscore_best_k))
    print("*** Best value of k for minmax = {} ***".format(minmax_best_k))

*** Best value of k for zscore = 49 ***
    *** Best value of k for minmax = 99 ***
```

4. Improving on KNN: You can try to improve on your classification results using the method of weighted KNN. The KNeighborsClassifier class has an option for weighted KNN where points that are nearby to the query point are more important for the classification than others. Compare the three different weighting schemes (default, manhattan, euclidean) by plotting accuracy vs k for all three of them on the same figure to see the effect.

```
In [147...
          # Storing the accuracies for different k-values and different weighting parameters f
          abalone zscore accuracies manhattan = []
          abalone_zscore_accuracies_euclidean = []
          abalone_minmax_accuracies_manhattan = []
          abalone_minmax_accuracies_euclidean = []
          # Using 'knn_classify' wrapper function defined above
          for k in k values:
              acc1_m = knn_classify(abalone_zscore_X_train, abalone_zscore_X_test, abalone_zsc
              acc1_e = knn_classify(abalone_zscore_X_train, abalone_zscore_X_test, abalone_zsc
              acc2_m = knn_classify(abalone_minmax_X_train, abalone_minmax_X_test, abalone_min
              acc2_e = knn_classify(abalone_minmax_X_train, abalone_minmax_X_test, abalone_min
              abalone_zscore_accuracies_manhattan.append(acc1_m)
              abalone_zscore_accuracies_euclidean.append(acc1_e)
              abalone_minmax_accuracies_manhattan.append(acc2_m)
              abalone_minmax_accuracies_euclidean.append(acc2_e)
```

```
In [148...
          # Multiplying accuracies by 100 for better comparison
          abalone zscore accuracies manhattan = [x*100 \text{ for } x \text{ in abalone zscore accuracies manhattan}]
          abalone_zscore_accuracies_euclidean = [x*100 for x in abalone_zscore_accuracies_eucl
          abalone_minmax_accuracies_manhattan = [x*100 for x in abalone_minmax_accuracies_manh
          abalone_minmax_accuracies_euclidean = [x*100 for x in abalone_minmax_accuracies_eucl
In [149...
          def accuracy_plot(default,manhattan,euclidean):
              plt.figure(figsize=(20,3))
              plt.plot(k_values, default, label='Default', marker='o')
              plt.plot(k_values, manhattan, label="Manhattan", marker='o')
              plt.plot(k_values, euclidean, label="Euclidean", marker='o')
              plt.xlabel("k values")
              plt.ylabel("Accuracy")
              plt.title("Value of accuracy for different value of k")
              plt.legend(["Default", "Manhattan", "Euclidean"])
              plt.show()
          print("*** Plot for Zscore normalized values ***")
          accuracy plot(abalone_zscore_accuracies,abalone_zscore_accuracies_manhattan,abalone_
          print("*** Plot for Minmax normalized values ***")
          accuracy_plot(abalone_minmax_accuracies,abalone_minmax_accuracies_manhattan,abalone_
         *** Plot for Zscore normalized values ***
         *** Plot for Minmax normalized values ***
                                                    k values
In [150...
          # Finding the maximum accuracy
          zscore_max_accuracy_manhattan = max(abalone_zscore_accuracies_manhattan)
          zscore_max_accuracy_euclidean = max(abalone_zscore_accuracies_euclidean)
          print("*** Best accuracy from zscore = {} ***".format(max(zscore_max_accuracy,zscore
          minmax max accuracy manhattan = max(abalone minmax accuracies manhattan)
          minmax_max_accuracy_euclidean = max(abalone_minmax_accuracies_euclidean)
          print("*** Best accuracy from minmax = {} ***".format(max(minmax max accuracy,minmax
          # Finding the best value of k
          zscore_best_k_manhattan = k_values[abalone_zscore_accuracies_manhattan.index(zscore_
          zscore_best_k_euclidean = k_values[abalone_zscore_accuracies_euclidean.index(zscore_
```

minmax_best_k_manhattan = k_values[abalone_minmax_accuracies_manhattan.index(minmax_ minmax_best_k_euclidean = k_values[abalone_minmax_accuracies_euclidean.index(minmax_

```
print("*** Best value of k for zscore for manhattan distance metric= {} ***".format(
print("*** Best value of k for zscore for euclidean distance metric= {} ***".format(
print("*** Best value of k for minmax for manhattan distance metric= {} ***".format(
print("*** Best value of k for minmax for euclidean distance metric= {} ***".format(
```

```
*** Best accuracy from zscore = 28.11004784688995 ***
*** Best accuracy from minmax = 28.4688995215311 ***
*** Best value of k for zscore for manhattan distance metric= 87 ***
*** Best value of k for zscore for euclidean distance metric= 89 ***
*** Best value of k for minmax for manhattan distance metric= 76 ***
*** Best value of k for minmax for euclidean distance metric= 79 ***
```

5 Ablation Study on Normalization: An ablation study is where some aspect of the model or analysis is dropped, in order to see what its effect was on the entire outcome. We can do a simple form of ablation here by removing normalization from our pipeline. Replot the three curves from the previous question on weighted KNN, but this time remove the normalization step from the preprocessing. Comment on the difference, was normalization effective or necessary in this case?

```
In [151...
```

```
# Splitting unnormalized data into training and testing set
abalone_unnormal_X_train, abalone_unnormal_X_test, abalone_unnormal_y_train, abalone
# Calculating accuracy
abalone_unnormal_accuracy = knn_classify(abalone_unnormal_X_train, abalone_unnormal_
abalone_unnormal_accuracies = []
for k in k values:
    acc1 = knn_classify(abalone_unnormal_X_train, abalone_unnormal_X_test, abalone_u
    abalone_unnormal_accuracies.append(acc1)
abalone_unnormal_accuracies = [x*100 for x in abalone_unnormal_accuracies]
plt.figure(figsize=(20,3))
plt.plot(k_values, abalone_unnormal_accuracies, marker='o')
plt.title("Value of accuracy for different value of k (Unnormalized data)")
plt.xlabel("k values")
plt.ylabel("Accuracy")
plt.show()
# Trying manhatten and euclidean metrics for unnormalized data
abalone unnormal accuracies manhattan = []
abalone unnormal accuracies euclidean = []
for k in k_values:
    acc1_m = knn_classify(abalone_unnormal_X_train, abalone_unnormal_X_test, abalone
    acc1_e = knn_classify(abalone_unnormal_X_train, abalone_unnormal_X_test, abalone
    abalone_unnormal_accuracies_manhattan.append(acc1_m)
    abalone unnormal accuracies euclidean.append(acc1 e)
abalone_unnormal_accuracies_manhattan = [x*100 for x in abalone_unnormal_accuracies_
abalone unnormal accuracies euclidean = [x*100 \text{ for } x \text{ in abalone unnormal accuracies}]
print("*** Plot for Unnormalized values ***")
accuracy_plot(abalone_unnormal_accuracies,abalone_unnormal_accuracies_manhattan,abal
```

```
# Finding the maximum accuracy
unnormal_max_accuracy = max(abalone_unnormal_accuracies)
unnormal_max_accuracy_manhattan = max(abalone_unnormal_accuracies_manhattan)
unnormal_max_accuracy_euclidean = max(abalone_unnormal_accuracies_euclidean)

print("*** Best accuracy from unnormalized data = {} ***".format(max(unnormal_max_ac

# Finding the best value of k
unnormal_best_k = k_values[abalone_unnormal_accuracies.index(unnormal_max_accuracy)]
unnormal_best_k_manhattan = k_values[abalone_unnormal_accuracies_manhattan.index(unn
unnormal_best_k_euclidean = k_values[abalone_unnormal_accuracies_euclidean.index(unn
print("*** Best value of k for unnormalized distance metric= {} ***".format(unnormal
print("*** Best value of k for unnormalized for manhattan distance metric= {} ***".f

*** Best accuracy from unnormalized data = 29.5454545454547 ***

*** Best value of k for unnormalized data = 29.5454545454547 ***

*** Best value of k for unnormalized data = 29.545454545454547 ***
```

*** Best value of k for unnormalized for manhattan distance metric= 50 ***

*** Best value of k for unnormalized for euclidean distance metric= 37 ***

Conclusion:

Best accuracy from zscore = 26.674641148325357

Best accuracy from minmax = 26.794258373205743

Best accuracy from unnormalized data = 28.708133971291865

It is evident that we are achieving more accuracy with unnormalized value therefore normalization is not effective here

2.2. Wine

```
# There are 2 target variables defined here
wine_target1 = "quality"
wine_target2 = "color"

# Shuffle the wine dataset because the dataset would be divided into 2 parts: one fo
wine = wine.sample(frac=1).reset_index(drop=True)

# Using three datasets: unnormalized, zscore normalized and minmax normalized for ea
wine_quality_dataframe_unnormal = wine.drop(wine_target2,axis=1)
wine_quality_dataframe_zscore = wine_zscore.drop(wine_target2,axis=1)
wine_quality_dataframe_minmax = wine_minmax.drop(wine_target2,axis=1)
wine_color_dataframe_unnormal = wine.drop(wine_target1,axis=1)
```

```
wine_color_dataframe_zscore = wine_zscore.drop(wine_target1,axis=1)
wine_color_dataframe_minmax = wine_minmax.drop(wine_target1,axis=1)
```

1. Divide the data into a training set and a test set (80%, 20%) Note: set the random seed for splitting, use random state=27 in the sci-kit learn train test split function to get the same split every time you run the program.

```
In [154...
         ''' <u>Q</u>uality '''
          # Train, test set for zscore and minmax normalized
          wine_quality_zscore_X_train, wine_quality_zscore_X_test, wine_quality_zscore_y_train
          wine_quality_minmax_X_train, wine_quality_minmax_X_test, wine_quality_minmax_y_train
          print("\n*** Analysis for zscore normalized ***\n")
          analyze_train_test_splits(wine_quality_zscore_X_train, wine_quality_zscore_X_test, w
          print("\n*** Analysis for minmax normalized ***\n")
          analyze_train_test_splits(wine_quality_minmax_X_train, wine_quality_minmax_X_test, w
          ''' Color '''
          # Train, test set for zscore and minmax normalized
          wine_color_zscore_X_train, wine_color_zscore_X_test, wine_color_zscore_y_train, wine
          wine_color_minmax_X_train, wine_color_minmax_X_test, wine_color_minmax_y_train, wine
          print("\n*** Analysis for zscore normalized ***\n")
          analyze_train_test_splits(wine_color_zscore_X_train, wine_color_zscore_X_test, wine_
          print("\n*** Analysis for minmax normalized ***\n")
          analyze_train_test_splits(wine_color_minmax_X_train, wine_color_minmax_X_test, wine_
         *** Analysis for zscore normalized ***
         fixed acidity
                                 5197
                                5197
         volatile acidity
                                5197
         citric acid
                                5197
         residual sugar
         chlorides
                                 5197
         free sulfur dioxide 5197 total sulfur dioxide 5197
         density
                                 5197
                                 5197
         рΗ
         sulphates
                                 5197
         alcohol
                                5197
         dtype: int64
                              1300
1300
         fixed acidity
         volatile acidity
         citric acid
                                 1300
         residual sugar
                               1300
         chlorides
                                 1300
         free sulfur dioxide 1300
         total sulfur dioxide
                                 1300
                                 1300
         density
                                 1300
         рΗ
         sulphates
                                 1300
         alcohol
                                 1300
         dtype: int64
         5197
         *** Analysis for minmax normalized ***
         fixed acidity
                                 5197
         volatile acidity
                                5197
                                5197
         citric acid
         residual sugar
                                5197
         chlorides
                                 5197
```

free sulfur dioxide 5197

```
total sulfur dioxide 5197
density
                           5197
                          5197
рΗ
                          5197
sulphates
                          5197
alcohol
dtype: int64
dtype: int64
fixed acidity 1300
volatile acidity 1300
citric acid 1300
residual sugar 1300
chlorides 1300
free sulfur dioxide 1300
total sulfur dioxide 1300
                          1300
density
                          1300
рΗ
sulphates
                          1300
alcohol
                           1300
dtype: int64
5197
1300
*** Analysis for zscore normalized ***
fixed acidity 5197
volatile acidity 5197
citric acid 5197
citric acid 519/
residual sugar 5197
free sulfur dioxide
                          5197
total sulfur dioxide 5197
density
                          5197
рΗ
                          5197
sulphates
                          5197
alcohol
                          5197
dtype: int64
fixed acidity 1300
volatile acidity 1300
citric acid 1300
residual sugar 1300
chlorides 1300
free sulfur dioxide
                          1300
total sulfur dioxide 1300
density
                          1300
рΗ
                          1300
sulphates
                          1300
alcohol
                           1300
dtype: int64
5197
*** Analysis for minmax normalized ***
fixed acidity
                          5197
                         5197
volatile acidity
citric acid
                          5197
residual sugar 5197
chlorides
                          5197
free sulfur dioxide
                          5197
total sulfur dioxide 5197
density
                           5197
                           5197
рН
sulphates
                          5197
alcohol
                          5197
dtype: int64
fixed acidity 1300 volatile acidity 1300 citnic acid
citric acid residual sugar 1300
chlorides
                          1300
free sulfur dioxide 1300
total sulfur dioxide 1300
```

```
density 1300
pH 1300
sulphates 1300
alcohol 1300
dtype: int64
5197
1300
```

2. Start by training the model with the classifier's default parameters. Use the train set and test the model on the test set. Note that different values of k will lead to different results.

```
In [155...
          # Calculating accuracy for default value of k i.e. 5 using 'knn_classify' wrapper fu
          wine_quality_zscore_accuracy = knn_classify(wine_quality_zscore_X_train, wine_qualit
          wine_quality_minmax_accuracy = knn_classify(wine_quality_minmax_X_train, wine_qualit
          wine_color_zscore_accuracy = knn_classify(wine_color_zscore_X_train, wine_color_zsco
          wine_color_minmax_accuracy = knn_classify(wine_color_minmax_X_train, wine_color_minm
In [156...
          print("*** For Quality ***")
          print("Accuracy for zscore = {}".format(wine_quality_zscore_accuracy))
          print("Accuracy for minmax = {}".format(wine_quality_minmax_accuracy))
          print("*** For Color ***")
          print("Accuracy for zscore = {}".format(wine_color_zscore_accuracy))
          print("Accuracy for minmax = {}".format(wine color minmax accuracy))
         *** For Quality ***
         Accuracy for zscore = 0.56
         Accuracy for minmax = 0.5615384615384615
         *** For Color ***
         Accuracy for zscore = 0.9953846153846154
         Accuracy for minmax = 0.9923076923076923
```

3. To find the best value for k, you need to compute accuracy for a range of values of k so you can "tune" the classifier. Using these scores, plot a figure of accuracy vs k. Report the best k in terms of classification accuracy.

```
In [157...
          #k values = [5,10,15,20,25,30,35]
          k \text{ values} = range(4,100)
          wine_quality_zscore_accuracies = []
           wine_quality_minmax_accuracies = []
           wine_color_zscore_accuracies = []
           wine_color_minmax_accuracies = []
           for k in k values:
               acc1 = knn classify(wine quality zscore X train, wine quality zscore X test, win
               acc2 = knn_classify(wine_quality_minmax_X_train, wine_quality_minmax_X_test, win
               wine_quality_zscore_accuracies.append(acc1)
               wine_quality_minmax_accuracies.append(acc2)
               acc1 = knn_classify(wine_color_zscore_X_train, wine_color_zscore_X_test, wine_color_zscore_X_test)
               acc2 = knn_classify(wine_color_minmax_X_train, wine_color_minmax_X_test, wine_color_minmax_X_test)
               wine color zscore accuracies.append(acc1)
               wine_color_minmax_accuracies.append(acc2)
```

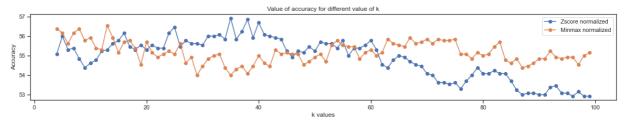
```
# Multiplying accuracies by 100 for better comparison
wine_quality_zscore_accuracies = [x*100 for x in wine_quality_zscore_accuracies]
wine_quality_minmax_accuracies = [x*100 for x in wine_quality_minmax_accuracies]
wine_color_zscore_accuracies = [x*100 for x in wine_color_zscore_accuracies]
wine_color_minmax_accuracies = [x*100 for x in wine_color_minmax_accuracies]
```

```
plt.figure(figsize=(20,3))
  plt.plot(k_values, wine_quality_zscore_accuracies, marker='o')
  plt.plot(k_values, wine_quality_minmax_accuracies, marker='o')

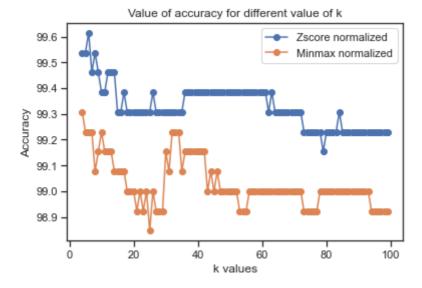
plt.xlabel("k values")
  plt.ylabel("Accuracy")
  plt.title("Value of accuracy for different value of k")
  plt.legend(["Zscore normalized","Minmax normalized"])
  plt.show()

plt.plot(k_values, wine_color_zscore_accuracies, marker='o')
  plt.plot(k_values, wine_color_minmax_accuracies, marker='o')

plt.xlabel("k values")
  plt.ylabel("Accuracy")
  plt.ylabel("Accuracy")
  plt.title("Value of accuracy for different value of k")
  plt.legend(["Zscore normalized","Minmax normalized"])
```



Out[158... <matplotlib.legend.Legend at 0x218b5e72940>



```
# Finding the maximum accuracy
quality_zscore_max_accuracy = max(wine_quality_zscore_accuracies)
quality_minmax_max_accuracy = max(wine_quality_minmax_accuracies)

color_zscore_max_accuracy = max(wine_color_zscore_accuracies)
color_minmax_max_accuracy = max(wine_color_minmax_accuracies)

# Finding the best value of k
quality_zscore_best_k = k_values[wine_quality_zscore_accuracies.index(quality_zscore)
```

```
quality_minmax_best_k = k_values[wine_quality_minmax_accuracies.index(quality_minmax_color_zscore_best_k = k_values[wine_color_zscore_accuracies.index(color_zscore_max_acolor_minmax_best_k = k_values[wine_color_minmax_accuracies.index(color_minmax_max_aprint("*** [Quality] Best_value of k for zscore = {} ***".format(quality_zscore_best_print("*** [Quality] Best_value of k for minmax = {} ***".format(quality_minmax_best_print("*** [Color] Best_value of k for zscore = {} ***".format(color_zscore_best_k)) print("*** [Color] Best_value of k for minmax = {} ***".format(color_minmax_best_k))
*** [Quality] Best_value of k for zscore = 35 ***
*** [Quality] Best_value of k for zscore = 6 ***
*** [Color] Best_value of k for zscore = 6 ***
*** [Color] Best_value of k for minmax = 4 ***
```

4. Improving on KNN: You can try to improve on your classification results using the method of weighted KNN. The KNeighborsClassifier class has an option for weighted KNN where points that are nearby to the query point are more important for the classification than others. Compare the three different weighting schemes (default, manhattan, euclidean) by plotting accuracy vs k for all three of them on the same figure to see the effect.

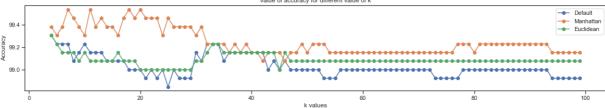
```
In [160...
          ## Storing the accuracies for different k-values and different weighting parameters
          wine_quality_zscore_accuracies_manhattan = []
          wine_quality_zscore_accuracies_euclidean = []
          wine_quality_minmax_accuracies_manhattan = []
          wine_quality_minmax_accuracies_euclidean = []
          wine_color_zscore_accuracies_manhattan = []
          wine_color_zscore_accuracies_euclidean = []
          wine_color_minmax_accuracies_manhattan = []
          wine_color_minmax_accuracies_euclidean = []
          # Using 'knn_classify' wrapper function defined above
          for k in k_values:
              ''' Quality '''
              acc1_m = knn_classify(wine_quality_zscore_X_train, wine_quality_zscore_X_test, w
              acc1_e = knn_classify(wine_quality_zscore_X_train, wine_quality_zscore_X_test, w
              acc2_m = knn_classify(wine_quality_minmax_X_train, wine_quality_minmax_X_test, w
              acc2_e = knn_classify(wine_quality_minmax_X_train, wine_quality_minmax_X_test, w
              wine quality zscore accuracies manhattan.append(acc1 m)
              wine_quality_zscore_accuracies_euclidean.append(acc1_e)
              wine_quality_minmax_accuracies_manhattan.append(acc2_m)
              wine_quality_minmax_accuracies_euclidean.append(acc2_e)
              ''' Color '''
              acc1_m = knn_classify(wine_color_zscore_X_train, wine_color_zscore_X_test, wine_
              acc1_e = knn_classify(wine_color_zscore_X_train, wine_color_zscore_X_test, wine_
              acc2_m = knn_classify(wine_color_minmax_X_train, wine_color_minmax_X_test, wine_
              acc2_e = knn_classify(wine_color_minmax_X_train, wine_color_minmax_X_test, wine_
              wine_color_zscore_accuracies_manhattan.append(acc1_m)
              wine_color_zscore_accuracies_euclidean.append(acc1_e)
```

```
wine_color_minmax_accuracies_manhattan.append(acc2_m)
wine_color_minmax_accuracies_euclidean.append(acc2_e)
```

```
In [161...
          # Multiplying accuracies by 100 for better comparison
          wine_quality_zscore_accuracies_manhattan = [x*100 for x in wine_quality_zscore_accur
          wine_quality_zscore_accuracies_euclidean = [x*100 for x in wine_quality_zscore_accur
          wine_quality_minmax_accuracies_manhattan = [x*100 \text{ for } x \text{ in } wine_quality_minmax_accurates_manhattan]
          wine_quality_minmax_accuracies_euclidean = [x*100 \text{ for } x \text{ in wine_quality_minmax_accur}]
          wine_color_zscore_accuracies_manhattan = [x*100 for x in wine_color_zscore_accuracie
          wine_color_zscore_accuracies_euclidean = [x*100 for x in wine_color_zscore_accuracie
          wine_color_minmax_accuracies_manhattan = [x*100 for x in wine_color_minmax_accuracie
          wine_color_minmax_accuracies_euclidean = [x*100 for x in wine_color_minmax_accuracie
In [162...
          def accuracy plot(default,manhattan,euclidean):
               plt.figure(figsize=(20,3))
               plt.plot(k_values, default, label='Default', marker='o')
               plt.plot(k_values, manhattan, label="Manhattan", marker='o')
               plt.plot(k_values, euclidean, label="Euclidean", marker='o')
               plt.xlabel("k values")
               plt.ylabel("Accuracy")
               plt.title("Value of accuracy for different value of k")
               plt.legend(["Default","Manhattan","Euclidean"])
               plt.show()
          print("*** Plot for Zscore normalized values (Quality) ***")
          accuracy_plot(wine_quality_zscore_accuracies,wine_quality_zscore_accuracies_manhatta
          print("*** Plot for Minmax normalized values (Quality) ***")
          accuracy_plot(wine_quality_minmax_accuracies,wine_quality_minmax_accuracies manhatta
          print("*** Plot for Zscore normalized values (Color) ***")
          accuracy_plot(wine_color_zscore_accuracies,wine_color_zscore_accuracies_manhattan,wi
          print("*** Plot for Minmax normalized values (Color) ***")
          accuracy_plot(wine_color_minmax_accuracies,wine_color_minmax_accuracies_manhattan,wi
             Plot for Zscore normalized values (Quality) ***
                                                                                              Manhattai

    Euclidean

          *** Plot for Minmax normalized values (Quality) ***
                   - Andrews Committee Committee
          67.5
          65.0
                                                                                              Default
          62.5
          60.0
          57.5
             Plot for Zscore normalized values (Color) ***
          99.7
           99.6
          99.4
```



In [163... # ***** Finding the maximum accuracy ''' Quality ''' quality_zscore_max_accuracy_manhattan = max(wine_quality_zscore_accuracies_manhattan quality_zscore_max_accuracy_euclidean = max(wine_quality_zscore_accuracies_euclidean print("*** [Quality] Best accuracy from zscore = {} ***".format(max(quality_zscore_m quality_minmax_max_accuracy_manhattan = max(wine_quality_minmax_accuracies_manhattan quality_minmax_max_accuracy_euclidean = max(wine_quality_minmax_accuracies_euclidean print("*** [Quality] Best accuracy from minmax = {} ***".format(max(quality_minmax_m ''' Color ''' color_zscore_max_accuracy_manhattan = max(wine_color_zscore_accuracies_manhattan) color_zscore_max_accuracy_euclidean = max(wine_color_zscore_accuracies_euclidean) print("*** [Color] Best accuracy from zscore = {} ***".format(max(color_zscore_max_a color_minmax_max_accuracy_manhattan = max(wine_color_minmax_accuracies_manhattan) color_minmax_max_accuracy_euclidean = max(wine_color_minmax_accuracies_euclidean) print("*** [Color] Best accuracy from minmax = {} ***".format(max(color_minmax_max_a print("\n\n") # ***** Finding the best value of k ''' Quality ''' quality_zscore_best_k_manhattan = k_values[wine_quality_zscore_accuracies_manhattan. quality_zscore_best_k_euclidean = k_values[wine_quality_zscore_accuracies_euclidean. quality_minmax_best_k_manhattan = k_values[wine_quality_minmax_accuracies_manhattan. quality_minmax_best_k_euclidean = k_values[wine_quality_minmax_accuracies_euclidean. print("*** [Quality] Best value of k for zscore for manhattan distance metric= {} ** print("*** [Quality]] Best value of k for zscore for euclidean distance metric= $\{\}$ ** print("*** [Quality] Best value of k for minmax for manhattan distance metric= {} ** print("*** [Quality] Best value of k for minmax for euclidean distance metric= {} ** ''' Color ''' color_zscore_best_k_manhattan = k_values[wine_color_zscore_accuracies_manhattan.inde color_zscore_best_k_euclidean = k_values[wine_color_zscore_accuracies_euclidean.inde color_minmax_best_k_manhattan = k_values[wine_color_minmax_accuracies_manhattan.inde color_minmax_best_k_euclidean = k_values[wine_color_minmax_accuracies_euclidean.inde print("*** [Color] Best value of k for zscore for manhattan distance metric= {} ***" print("*** [Color] Best value of k for zscore for euclidean distance metric= {} ***"

print("*** [Color] Best value of k for minmax for manhattan distance metric= {} ***"
print("*** [Color] Best value of k for minmax for euclidean distance metric= {} ***"

```
*** [Quality] Best accuracy from minmax = 69.76923076923077 ***

*** [Color] Best accuracy from zscore = 99.76923076923076 ***

*** [Color] Best accuracy from minmax = 99.53846153846155 ***

*** [Quality] Best value of k for zscore for manhattan distance metric= 64 ***

*** [Quality] Best value of k for zscore for euclidean distance metric= 39 ***

*** [Quality] Best value of k for minmax for manhattan distance metric= 92 ***

*** [Quality] Best value of k for minmax for euclidean distance metric= 64 ***

*** [Color] Best value of k for zscore for manhattan distance metric= 5 ***

*** [Color] Best value of k for minmax for manhattan distance metric= 4 ***

[Color] Best value of k for minmax for manhattan distance metric= 7 ***

*** [Color] Best value of k for minmax for manhattan distance metric= 4 ***
```

5 Ablation Study on Normalization: An ablation study is where some aspect of the model or analysis is dropped, in order to see what its effect was on the entire outcome. We can do a simple form of ablation here by removing normalization from our pipeline. Replot the three curves from the previous question on weighted KNN, but this time remove the normalization step from the preprocessing. Comment on the difference, was normalization effective or necessary in this case?

```
In [164...
                        # For quality
                         abalone_unnormal_X_train, abalone_unnormal_X_test, abalone_unnormal_y_train, abalone
                         abalone_unnormal_accuracy = knn_classify(abalone_unnormal_X_train, abalone_unnormal_
                         abalone_unnormal_accuracies = []
                         for k in k_values:
                                   acc1 = knn_classify(abalone_unnormal_X_train, abalone_unnormal_X_test, abalone_u
                                   abalone_unnormal_accuracies.append(acc1)
                         abalone_unnormal_accuracies = [x*100 for x in abalone_unnormal_accuracies]
                         plt.figure(figsize=(20,3))
                         plt.plot(k_values, abalone_unnormal_accuracies, marker='o')
                         plt.xlabel("k values")
                         plt.ylabel("Accuracy")
                         plt.show()
                         abalone_unnormal_accuracies_manhattan = []
                         abalone unnormal accuracies euclidean = []
                         for k in k values:
                                   acc1_m = knn_classify(abalone_unnormal_X_train, abalone_unnormal_X_test, abalone
                                   acc1 e = knn classify(abalone unnormal X train, abalone unnormal X test, abalone
                                   abalone_unnormal_accuracies_manhattan.append(acc1_m)
                                   abalone_unnormal_accuracies_euclidean.append(acc1_e)
                         abalone_unnormal_accuracies_manhattan = [x*100 \text{ for } x \text{ in } abalone\_unnormal_accuracies_
                         abalone unnormal accuracies euclidean = [x*100 \text{ for } x \text{ in abalone unnormal accuracies}]
                         print("*** Plot for Unnormalized values ***")
                         accuracy_plot(abalone_unnormal_accuracies,abalone_unnormal_accuracies_manhattan,abal
                         # For color
                         abalone\_unnormal\_X\_train,\ abalone\_unnormal\_X\_test,\ abalone\_unnormal\_y\_train,\ abalone\_unnormal\_y\_t
                         abalone_unnormal_accuracy = knn_classify(abalone_unnormal_X_train, abalone_unnormal_
                         abalone unnormal accuracies = []
                         for k in k_values:
                                   acc1 = knn_classify(abalone_unnormal_X_train, abalone_unnormal_X_test, abalone_u
```

```
abalone_unnormal_accuracies.append(acc1)
abalone_unnormal_accuracies = [x*100 for x in abalone_unnormal_accuracies]
plt.figure(figsize=(20,3))
plt.plot(k values, abalone unnormal accuracies, marker='o')
plt.xlabel("k values")
plt.ylabel("Accuracy")
plt.show()
abalone_unnormal_accuracies_manhattan = []
abalone_unnormal_accuracies_euclidean = []
for k in k_values:
    acc1_m = knn_classify(abalone_unnormal_X_train, abalone_unnormal_X_test, abalone
    acc1_e = knn_classify(abalone_unnormal_X_train, abalone_unnormal_X_test, abalone
    abalone_unnormal_accuracies_manhattan.append(acc1_m)
    abalone_unnormal_accuracies_euclidean.append(acc1_e)
abalone_unnormal_accuracies_manhattan = [x*100 for x in abalone_unnormal_accuracies_
abalone_unnormal_accuracies_euclidean = [x*100 for x in abalone_unnormal_accuracies_
print("*** Plot for Unnormalized values ***")
accuracy_plot(abalone_unnormal_accuracies,abalone_unnormal_accuracies_manhattan,abal
  Plot for Unnormalized values
  Plot for Unnormalized values
```

5 Ablation Study on Normalization: An ablation study is where some aspect of the model or analysis is dropped, in order to see what its effect was on the entire outcome. We can do a simple form of ablation here by removing normalization from our pipeline. Replot the three curves from the previous question on weighted KNN, but this time remove the normalization step from

the preprocessing. Comment on the difference, was normalization effective or necessary in this case?

```
In [168...
         ''' Ouality '''
          print("*** Quality ***")
          # Splitting unnormalized data into training and testing set
          wine_quality_unnormal_X_train, wine_quality_unnormal_X_test, wine_quality_unnormal_y
          # Calculating accuracy
          wine_quality_unnormal_accuracy = knn_classify(wine_quality_unnormal_X_train, wine_qu
          wine quality unnormal accuracies = []
          for k in k_values:
              acc1 = knn_classify(wine_quality_unnormal_X_train, wine_quality_unnormal_X_test,
              wine_quality_unnormal_accuracies.append(acc1)
          wine_quality_unnormal_accuracies = [x*100 for x in wine_quality_unnormal_accuracies]
          plt.figure(figsize=(20,3))
          plt.plot(k_values, wine_quality_unnormal_accuracies, marker='o')
          plt.xlabel("k values")
          plt.ylabel("Accuracy")
          plt.title("Value of accuracy for different value of k (Unnormalized data)")
          # Trying manhatten and euclidean metrics for unnormalized data
          wine_quality_unnormal_accuracies_manhattan = []
          wine_quality_unnormal_accuracies_euclidean = []
          for k in k_values:
              acc1_m = knn_classify(wine_quality_unnormal_X_train, wine_quality_unnormal_X_tes
              acc1_e = knn_classify(wine_quality_unnormal_X_train, wine_quality_unnormal_X_tes
              wine_quality_unnormal_accuracies_manhattan.append(acc1_m)
              wine_quality_unnormal_accuracies_euclidean.append(acc1_e)
          wine_quality_unnormal_accuracies_manhattan = [x*100 \text{ for } x \text{ in wine_quality_unnormal_a}]
          wine_quality_unnormal_accuracies_euclidean = [x*100 \text{ for } x \text{ in } wine_quality_unnormal_a
          print("*** Plot for Unnormalized values ***")
          accuracy_plot(wine_quality_unnormal_accuracies,wine_quality_unnormal_accuracies_manh
          ''' Color '''
          print("*** Color ***")
          # Splitting unnormalized data into training and testing set
          wine_color_unnormal_X_train, wine_color_unnormal_X_test, wine_color_unnormal_y_train
          # Calculating accuracy
          wine color unnormal accuracy = knn classify(wine color unnormal X train, wine color
          wine_color_unnormal_accuracies = []
          for k in k_values:
              acc1 = knn_classify(wine_color_unnormal_X_train, wine_color_unnormal_X_test, win
              wine_color_unnormal_accuracies.append(acc1)
          wine_color_unnormal_accuracies = [x*100 for x in wine_color_unnormal_accuracies]
          plt.figure(figsize=(20,3))
          plt.plot(k values, wine color unnormal accuracies, marker='o')
          plt.xlabel("k values")
          plt.ylabel("Accuracy")
          plt.title("Value of accuracy for different value of k (Unnormalized data)")
          plt.show()
          # Trying manhatten and euclidean metrics for unnormalized data
          wine_color_unnormal_accuracies_manhattan = []
          wine_color_unnormal_accuracies_euclidean = []
```

```
for k in k_values:
              acc1_m = knn_classify(wine_color_unnormal_X_train, wine_color_unnormal_X_test, w
              acc1_e = knn_classify(wine_color_unnormal_X_train, wine_color_unnormal_X_test, w
              wine_color_unnormal_accuracies_manhattan.append(acc1_m)
              wine color unnormal accuracies euclidean.append(acc1 e)
          wine_color_unnormal_accuracies_manhattan = [x*100 for x in wine_color_unnormal_accur
          wine_color_unnormal_accuracies_euclidean = [x*100 \text{ for } x \text{ in } wine_color_unnormal_accur}]
          print("*** Plot for Unnormalized values ***")
          accuracy_plot(wine_color_unnormal_accuracies,wine_color_unnormal_accuracies_manhatta
             Quality ***
         *** Plot for Unnormalized values ***
          60
         *** Color ***
         *** Plot for Unnormalized values ***
In [166...
          ''' Quality '''
          print("*** Quality ***")
          # Finding the maximum accuracy
          unnormal_max_accuracy = max(wine_quality_unnormal_accuracies)
          unnormal_max_accuracy_manhattan = max(wine_quality_unnormal_accuracies_manhattan)
          unnormal_max_accuracy_euclidean = max(wine_quality_unnormal_accuracies_euclidean)
          print("*** Best accuracy from unnormalized data = {} ***".format(max(unnormal_max_ac
          # Finding the best value of k
          unnormal_best_k = k_values[wine_quality_unnormal_accuracies.index(unnormal_max_accur
          unnormal_best_k_manhattan = k_values[wine_quality_unnormal_accuracies_manhattan.inde
          unnormal_best_k_euclidean = k_values[wine_quality_unnormal_accuracies_euclidean.inde
          print("*** Best value of k for unnormalized distance metric= {} ***".format(unnormal
          print("*** Best value of k for unnormalized for manhattan distance metric= {} ***".f
          print("*** Best value of k for unnormalized for euclidean distance metric= {} ***".f
```

```
print("\n\n")
 ''' Color '''
 print("*** Color ***")
 # Finding the maximum accuracy
 unnormal_max_accuracy = max(wine_color_unnormal_accuracies)
 unnormal max accuracy manhattan = max(wine color unnormal accuracies manhattan)
 unnormal_max_accuracy_euclidean = max(wine_color_unnormal_accuracies_euclidean)
 print("*** Best accuracy from unnormalized data = {} ***".format(max(unnormal_max_ac
 # Finding the best value of k
 unnormal best k = k values[wine color unnormal accuracies.index(unnormal max accurac
 unnormal_best_k_manhattan = k_values[wine_color_unnormal_accuracies_manhattan.index(
 unnormal_best_k_euclidean = k_values[wine_color_unnormal_accuracies_euclidean.index(
 print("*** Best value of k for unnormalized distance metric= {} ***".format(unnormal
 print("*** Best value of k for unnormalized for manhattan distance metric= {} ***".f
 print("*** Best value of k for unnormalized for euclidean distance metric= {} ***".f
*** Ouality ***
*** Best accuracy from unnormalized data = 65.0 ***
*** Best value of k for unnormalized distance metric= 7 ***
*** Best value of k for unnormalized for manhattan distance metric= 21 ***
*** Best value of k for unnormalized for euclidean distance metric= 18 ***
*** Color ***
*** Best accuracy from unnormalized data = 96.61538461538461 ***
*** Best value of k for unnormalized distance metric= 15 ***
*** Best value of k for unnormalized for manhattan distance metric= 6 ***
*** Best value of k for unnormalized for euclidean distance metric= 11 ***
Conclusion:
[For quality]
Best accuracy from zscore = 68.61538461538461
Best accuracy from minmax = 68.6923076923077
Best accuracy from unnormalized data = 61.15384615384616
[For color]
Best accuracy from zscore = 99.76923076923076
Best accuracy from minmax = 99.53846153846155
Best accuracy from unnormalized data = 97.15384615384616
It is evident that we are achieving more accuracy with normalized value therefore
normalization is effective here
```

References

- [1] KNeighborsClassifier; https://scikit-learn.org/stable/modules/generated/sklearn.neighbors
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[3] Scatter Plot; Date accessed: 3rd Feb; https://en.wikipedia.org/wiki/Scatter_plot