

Supplementary text and tables

Comparison with the group contribution method of Mavrovouniotis

Although most of the *interaction factors* and *structural groups* used in the new group contribution method are based on the *interaction factors* and *structural groups* used in the group contribution method of Mavrovouniotis (1, 2), significant changes were made in the development of this new group contribution method. 20 new *structural groups* (all noted in Table 1) were introduced into the method to allow for the calculation of ΔG_{est}° for a wider variety of compounds and reactions. Additionally, some of the groups used in the Mavrovouniotis group contribution method were combined into more general *structural groups*. In the Mavrovouniotis method, primary, secondary, and tertiary hydroxyl groups and a hydroxyl group attached to a benzene ring were all treated as separate *structural groups*. After fitting with the four hydroxyl groups delineated, $\Delta_{gr} G_i^{\circ}$ values for the hydroxyl groups were found to be similar, with a maximum difference of 4 kcal/mol and average difference of 2.28 kcal/mol between the values (Table SI). Primary, secondary, and tertiary phosphates were also treated as separate groups in the Mavrovouniotis method, and the $\Delta_{gr} G_i^{\circ}$ values initially calculated for these three phosphate groups were also very similar with a maximum difference of 2 kcal/mol and an average difference of 1.2 kcal/mol. In order to simplify the group contribution method, all hydroxyl groups and all phosphate groups were combined into the single *structural groups* -OH and -O-PO₃²⁻, respectively. Although these changes did result in a 3.3% increase in the SE_{MLR} for the fitting from 1.84 to 1.90 kcal/mol, this increase is acceptable given the corresponding 5.8% reduction in the number of parameters involved in the group contribution model. Note that in both cases, the number of datapoints in the training set involving the generic -OH group or the generic -O-PO₃²⁻ group is not equal to the total number of datapoints involving each of the specific -OH or -O-PO₃²⁻ groups (Table SI). One reason for this apparent discrepancy is that some datapoints contain more than one of the specific -OH or -O-PO₃²⁻ groups. For example, glucose contains a primary and a secondary hydroxyl group which means that glucose is counted among both the 683 datapoints containing primary -OH and the 902 datapoints containing secondary -OH. Another reason for the discrepancy is that some reactions involve the destruction of a primary -OH or -O-PO₃²⁻ along with the simultaneous creation of a secondary -OH or -O-PO₃²⁻, but the generic -OH and -O-PO₃²⁻ cancel out in these reactions.

Changes were also made to the *interaction factors* used in the group contribution method. Three new types of *interaction factors* were introduced in this new group contribution method. These new *interaction factors* are discussed in detail in the methods section of the manuscript. Additionally, some of the *interaction factors* which were included in the group contribution method of Mavrovouniotis were not included in the final implementation of the new group contribution method: (i) the *NAD(P)H factor*, (ii) the *CoA factor*, and (iii) the *origin factor*. As implemented by Mavrovouniotis, the *NAD(P)H factor* was added to $\Delta_r G_{est}^{\circ}$ of all reactions involving NAD(P) and NAD(P)H as cofactors in order to improve the agreement between $\Delta_r G_{est}^{\circ}$ and $\Delta_r G_{obs}^{\circ}$ for reactions. Similarly, the *CoA factor* was added to all reactions involving the addition or removal of

CoA. Finally, the *origin factor* was added to $\Delta_f G_{est}^{\circ}$ of every compound that was decomposed into structural subgroups. These interaction factors were not included in the new group contribution method because all three had high T-tests and an insignificant effect on the SE_{MLR} of the fitting (Table SII).

All of these changes introduced in this new group contribution method have not only expanded the applicability of the method to calculate ΔG_{est}° for a wider range of compounds and reactions, but also improved the accuracy of the method. For the compounds and reactions in the training set for which ΔG_{est}° can be calculated using the Mavrovouniotis group contribution method, the standard deviation of the residuals is 3.92 kcal/mol, compared to a standard deviation of 1.98 kcal/mol when the new group contribution method is used to calculate ΔG_{est}° for the same reactions and compounds.

F-test calculation details

The validity of the linear model proposed in the group contribution hypothesis was assessed using a statistical F-test. An F-test indicates whether or not the variability in the ΔG_{obs}° values that make up the training set that is captured by the group contribution model is statistically significant compared to the variability not captured by the model (the variances between ΔG_{obs}° and ΔG_{est}°) (3). The F value for the model is calculated as follows (3):

$$F = \frac{(\Delta \mathbf{G}_{est}^{\circ})' (\Delta \mathbf{G}_{est}^{\circ}) / N_{gr}}{(SE_{MLR})^2} \quad (1)$$

The location of this F value in the F-cumulative distribution function is then determined,, and if the location of the F value corresponds to a probability value greater than 90%, the linear model is accepted (3).

T-test calculation details

While the F-test is used to test if the entire group contribution model is statistically significant compared to the uncertainty in the model, the t-test is used to determine if each $\Delta_{gr} G_i^{\circ}$ in the group contribution model is statistically significant compared to the uncertainty in $\Delta_{gr} G_i^{\circ}$, $SE_{gr,i}$ (3). The t-value for each parameter is calculated as follows (3):

$$t_i = \frac{\Delta_{gr} G_i^{\circ}}{SE_{gr,i}} \quad (2)$$

The $\Delta_{gr} G_i^{\circ}$ of a group is considered to be statistically significant compared to the $SE_{gr,i}$ for the group if the location of the t_i value in the student t-cumulative distribution corresponds to a probability value less than 5% (3). Only *interaction factors* with t-tests over 5% were removed from the group contribution method. While t-tests were performed on the *structural groups* as well, *structural groups* with high t-tests were not

removed from the model because they were required for the complete decomposition of the molecular structures involved in the training set.

Table S1. Generalized alcohol and phosphate structural subgroups

Description of molecular substructure	$\Delta_{gr}G^\circ$ kcal/mol	SE_{gr} kcal/mol	Frequency
Alcohol groups			
-OH (generalized) [†]	-41.5	0.126	1117
-OH (primary)	-40.8	0.125	683
-OH (secondary)	-43.2	0.165	902
-OH (tertiary)	-44.8	0.510	314
-OH (attached to a benzene ring)	-41.5	0.562	28
Phosphate groups			
-O-PO ₃ ²⁻ (generalized) [†]	-254	0.159	380
-O-PO ₃ ²⁻ (primary)	-253	0.155	483
-O-PO ₃ ²⁻ (secondary)	-254	0.229	207
-O-PO ₃ ²⁻ (tertiary)	-252	1.83	2

[†]These are the groups actually included in the final version of the method

Table S2. Mavrovouniotis interaction factors that were removed

Interaction factor	$\Delta_{gr}G^\circ$ kcal/mol	SE_{gr} kcal/mol	t-test	Frequency	SE_{MLR} with/without
Origin term	0.352	0.850	0.68	660	1.90/1.90
NADH	0.605	0.427	0.16	690	1.90/1.90
CoA	1.64	0.777	0.03	165	1.90/1.90

1. Mavrovouniotis, M. L. 1990. Group contributions for estimating standard Gibbs energies of formation of biochemical-compounds in aqueous-solution. *Biotechnology and Bioengineering* 36:1070-1082.
2. Mavrovouniotis, M. L. 1991. Estimation of standard Gibbs energy changes of biotransformations. *Journal of Biological Chemistry* 266:14440-14445.
3. Neter, J., W. Wasserman, and M. H. Kutner. 1990. *Applied linear statistical models : regression, analysis of variance, and experimental designs*. Irwin, Homewood, IL.