

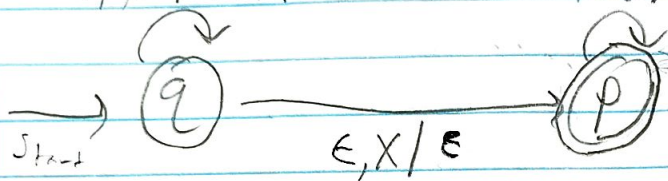
HW 6 Alex Mandzyuk

1) a)

$$P = (\{q, p\}, \{0, 1\}, \{z_0, x\}, \delta, q, z_0, \{p\})$$

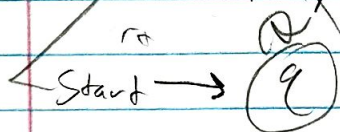
$$\begin{array}{l} 0, z_0 / x z_0 \\ 0, x / x x \\ 1, x / x x \end{array}$$

$$\begin{array}{l} \epsilon, x / \epsilon \\ 1, x / x x \\ 1, z_0 / \epsilon \end{array}$$



b) $P_N =$

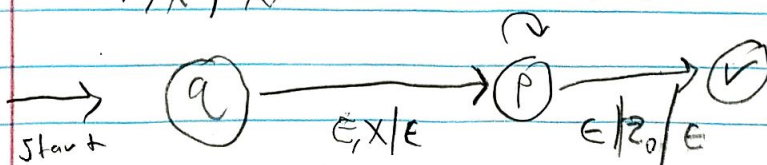
$$\begin{array}{l} 0, z_0 / x z_0 \\ 0, x / x x \\ 1, x / x x \\ \epsilon, x / \epsilon \\ 1, z_0 / \epsilon \end{array}$$



b) $P_N (\{q, p, \checkmark\}, \{0, 1\}, \{z_0, x\}, \delta, q, z_0)$

$$\begin{array}{l} 0, z_0 / x z_0 \\ 0, x / x x \\ 1, x / x x \end{array}$$

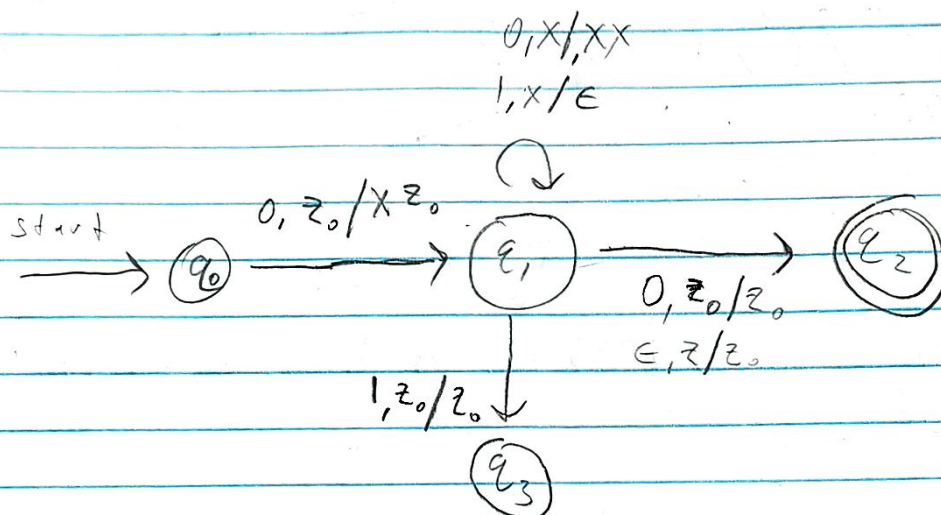
$$\begin{array}{l} \epsilon, x / \epsilon \\ 1, x / x x \\ 1, z_0 / z_0 \end{array}$$



2) 6.2.1 b, c

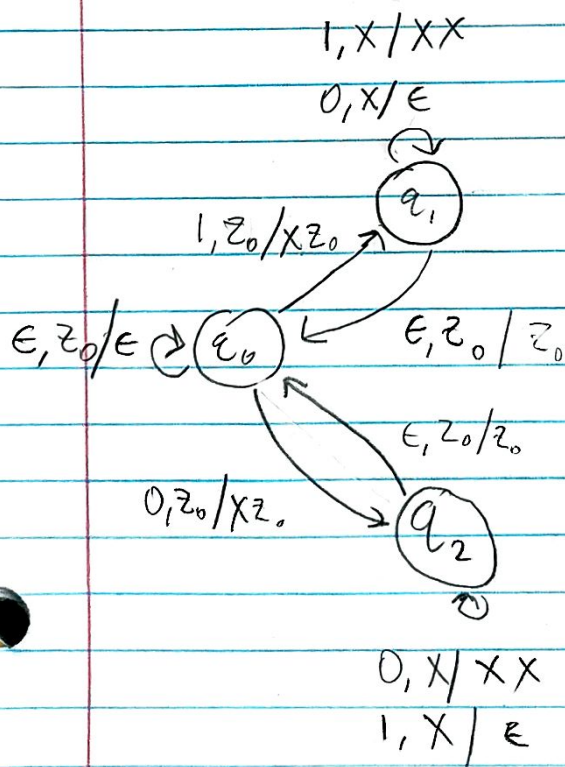
b) Set of all strings s.t. no prefix has more 1's than 0's. Accepted by final state

$$P_F = (\{q_0, q_1, q_2, q_3\}, \{0, 1\}, \{z_0, x\}, \delta, q_0, z_0, \{q_2\})$$



c) Set of all strings of 0's and 1's with an equal number of 0's and 1's

Accepted by empty stack



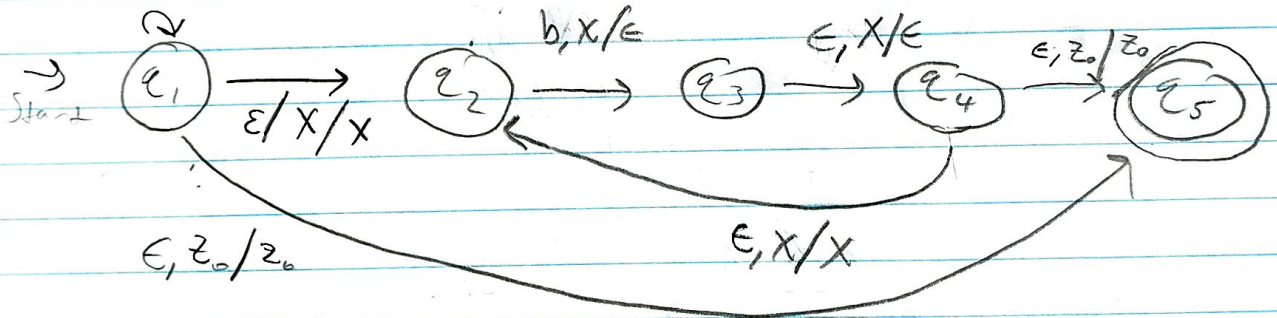
$$P_N = (\{q_0, q_1, q_2\}, \{0, 1\}, \{z_0, x\}, \delta, q_0, z_0)$$

aaabbb

3) $L = \{w \mid w \text{ is of the form } a^{2n}b^n, n \geq 0\}$

$a, z_0 / X z_0$

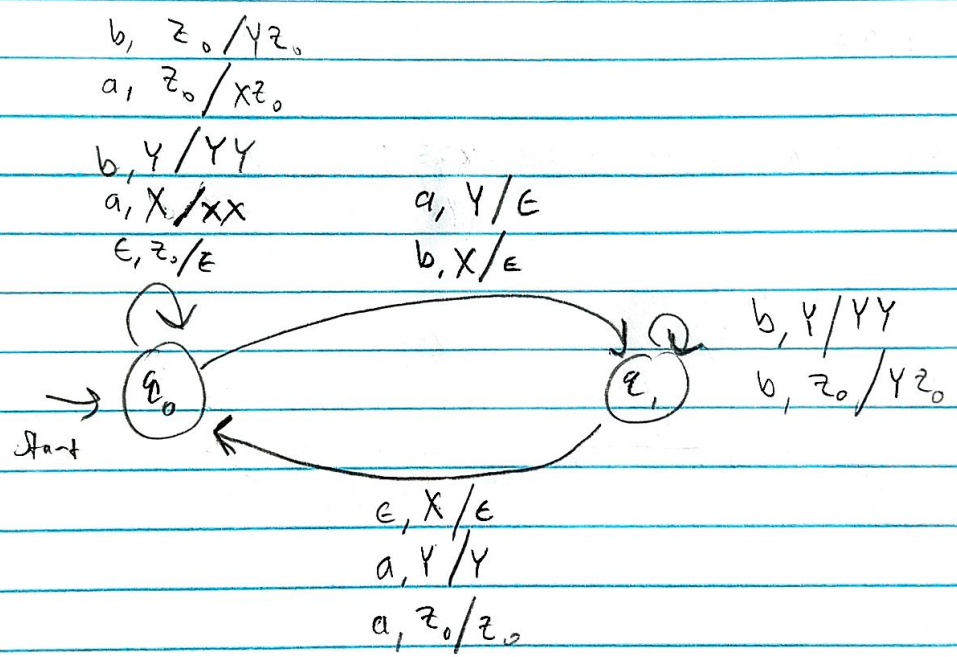
$a, X / XX$



$P_F = (\{q_1, q_2, q_3, q_4, q_5\}, \{a, b\}, \{X, z_0\}, \delta, q_1, z_0, \{q_5\})$

Accepting by final state

4 $P_N = (\{q_0, q_1\}, \{a, b\}, \{X, Y, Z_0\}, \delta, q_0, Z_0)$



Accept by empty stack

5) Convert the grammar

$$S \rightarrow aAA$$

$$A \rightarrow aS / bS / a$$

to a PDA that accepts the
same language by empty stack

$$P = (\{q_0, q_1\}, \{a, b\}, \{a, b, A\}, \delta, q_0, S)$$

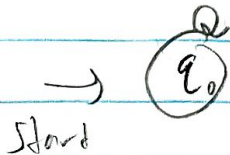
$$a, A / \epsilon$$

$$b, A / S$$

$$a, A / S$$

$$a, S / AA$$

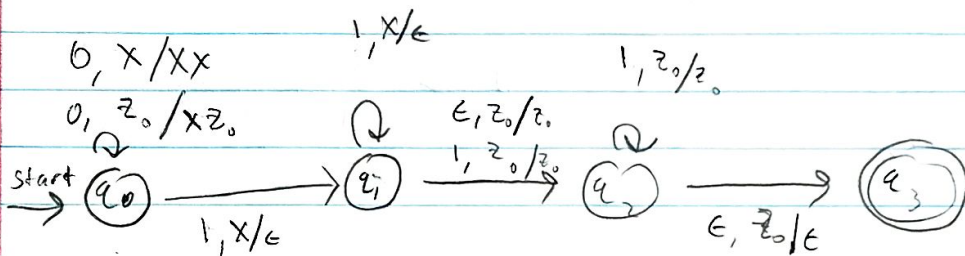
$$\epsilon, \epsilon / \epsilon$$



6) Give deterministic PDA to accept:

a) $\{0^n 1^m \mid n \leq m\}$ by final state

P: $(\{q_0, q_1, q_2, q_3\}, \{0, 1\}, \{z_0, X\}, \delta, q_0, z_0, \{q_3\})$



b) $\{0^n 1^m \mid n \geq m\}$ by final state

P: $(\{q_0, q_1, q_2, q_3\}, \{0, 1\}, \{z_0, X\}, \delta, q_0, z_0, \{q_3\})$

