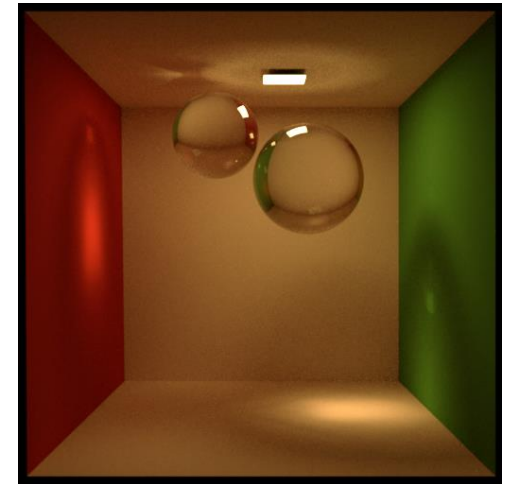
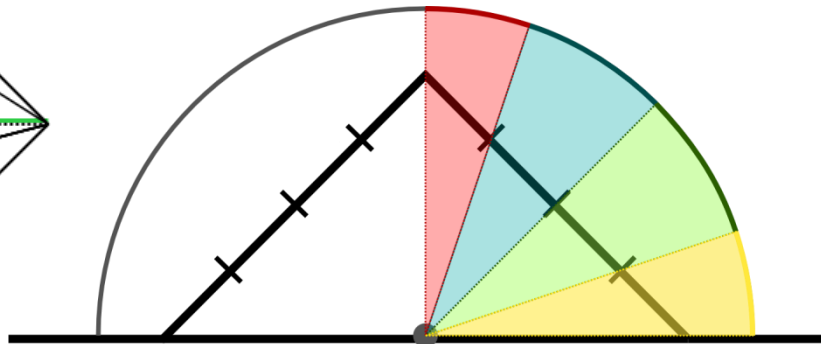
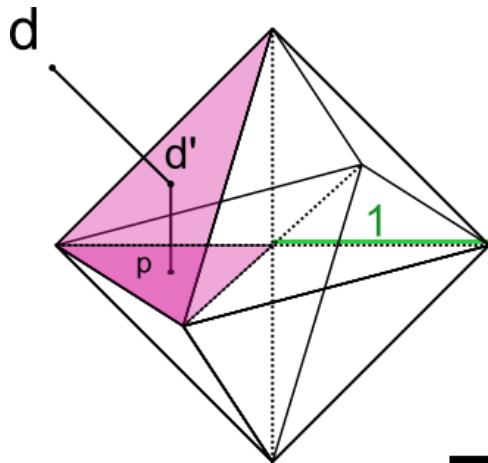


Irradiance Importance Sampling

Bachelorarbeit
Alisa Jung

Institut für Visualisierung und Datenanalyse, Lehrstuhl für Computergrafik



Goal

- Photorealistic Images
- Improve Path Tracing

Rendering Equation:

$$L_o(x, \omega_o) = L_e(x, \omega_o) + \int_{\mathcal{S}^2} L_i(x, \omega_i) \cdot f_s(\omega_i, x, \omega_o) \cdot \cos(\omega_i) d\sigma(\omega_i)$$

→ Monte-Carlo Integration:

$$\int_{\mathcal{S}^2} L_i(x, \omega_i) \cdot f_s(\omega_i, x, \omega_o) \cdot \cos(\omega_i) d\sigma(\omega_i) \approx \frac{1}{N} \sum_{k=1}^N \frac{L_i(x, \omega_k) \cdot f_s(\omega_k, x, \omega_o) \cdot \cos(\omega_k)}{p(\omega_k)}$$

Importance Sampling: Options

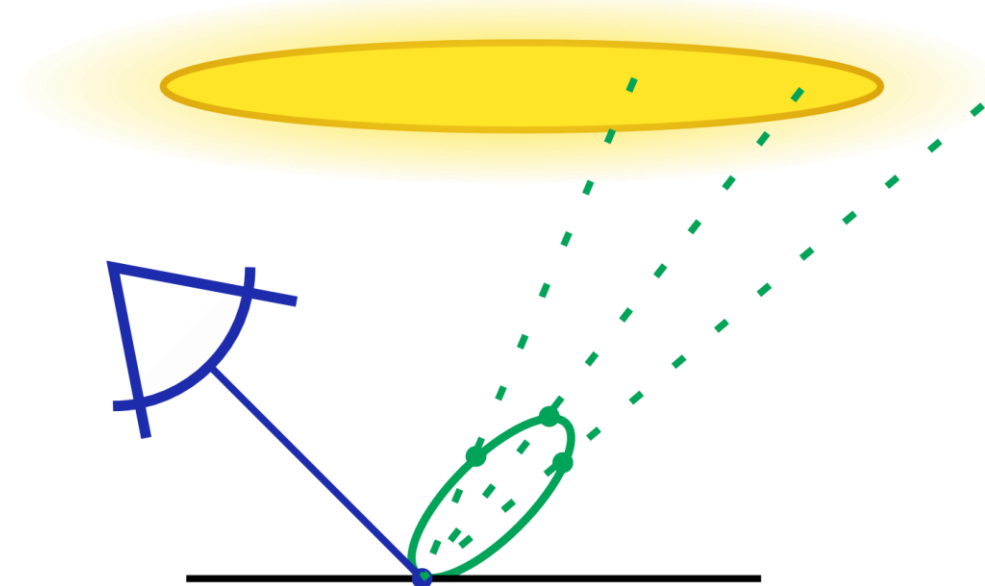
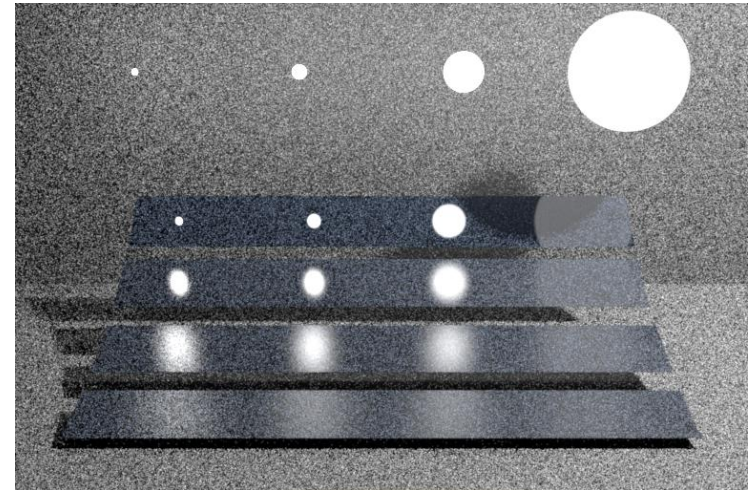
$$\int_{\mathcal{S}^2} L_i(x, \omega_i) \cdot f_s(\omega_i, x, \omega_o) \cdot \cos(\omega_i) d\sigma(\omega_i)$$

■ The cosine: $p \propto \cos$

Importance Sampling: Options

$$\int_{\mathcal{S}^2} L_i(x, \omega_i) \cdot f_s(\omega_i, x, \omega_o) \cdot \cos(\omega_i) d\sigma(\omega_i)$$

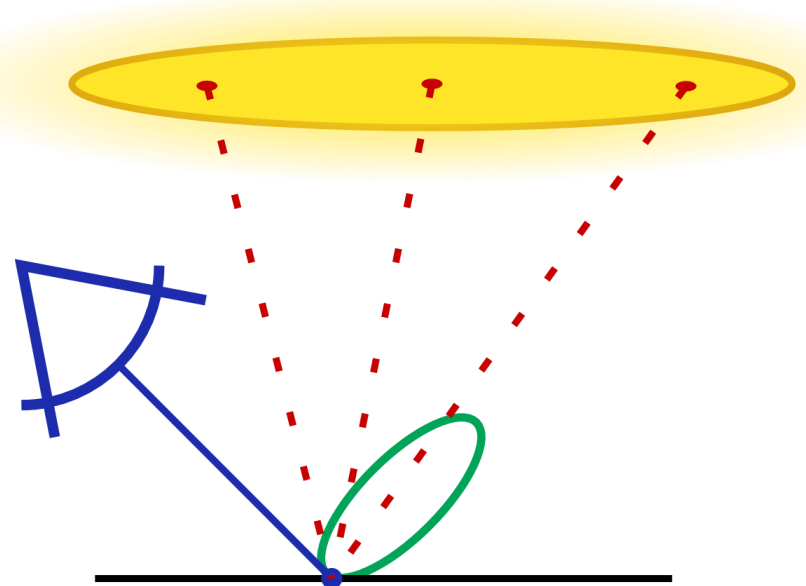
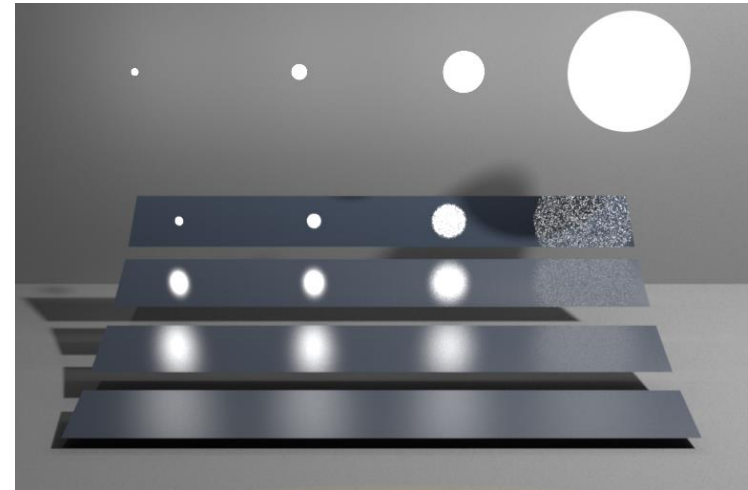
- The cosine: $p \propto \cos$
- The BSDF: $p \propto f_s$



Importance Sampling: Options

$$\int_{\mathcal{S}^2} L_i(x, \omega_i) \cdot f_s(\omega_i, x, \omega_o) \cdot \cos(\omega_i) d\sigma(\omega_i)$$

- The cosine: $p \propto \cos$
- The BSDF: $p \propto f_s$
- Incident Radiance (L_i):
 - Next event estimation
(connection to light source)



Importance Sampling: Options

$$\int_{\mathcal{S}^2} L_i(x, \omega_i) \cdot f_s(\omega_i, x, \omega_o) \cdot \cos(\omega_i) d\sigma(\omega_i)$$

- The cosine: $p \propto \cos$
- The BSDF: $p \propto f_s$
- Incident Radiance (L_i):
 - Next event estimation
(connection to light source)
 - **Caches for incident radiance**

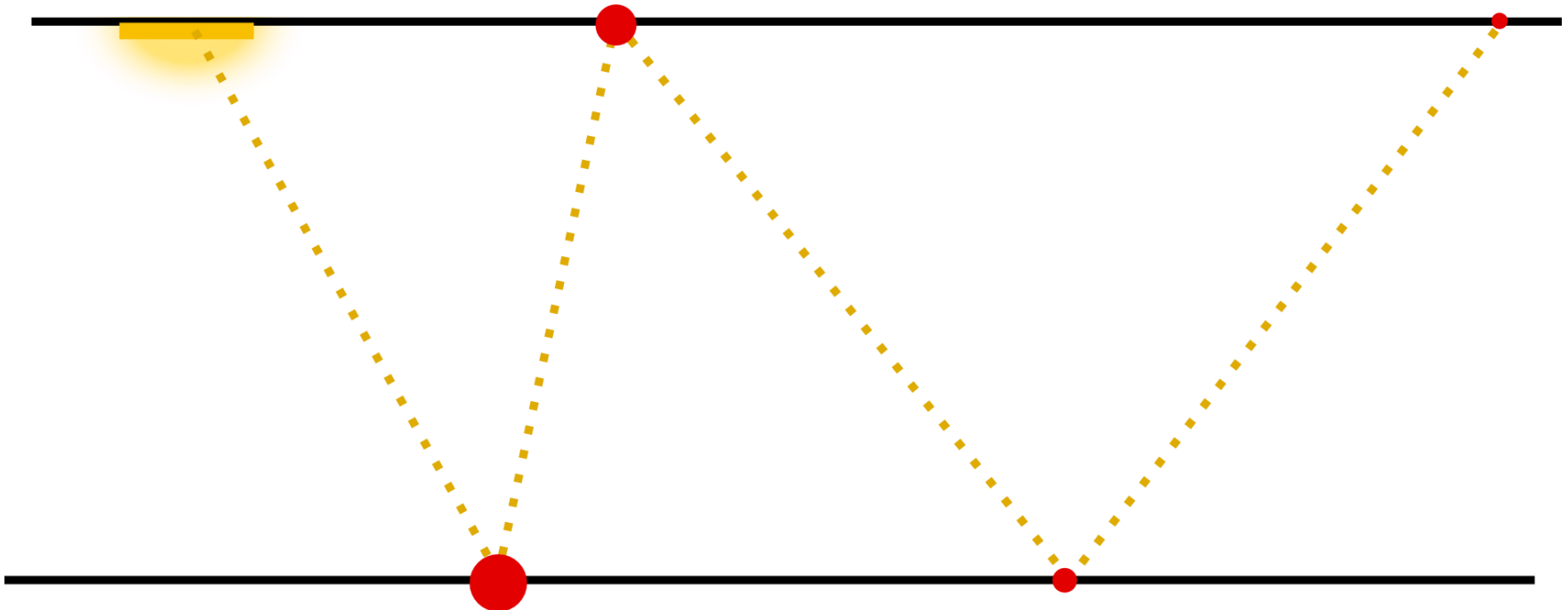
Steps

- Preprocessing → Create Caches
- Rendering
 - Create paths using...
 - Caches
 - BSDF
 - NEE
 - Combine with Multiple Importance Sampling

Preprocessing: Photon Mapping

■ Photon:

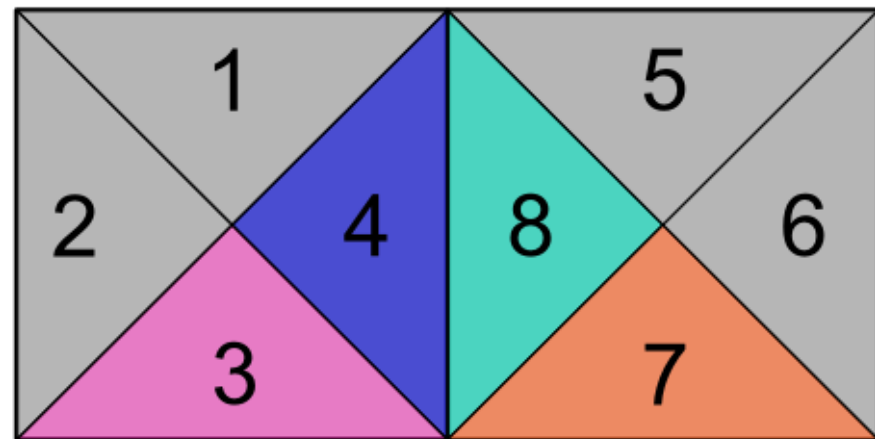
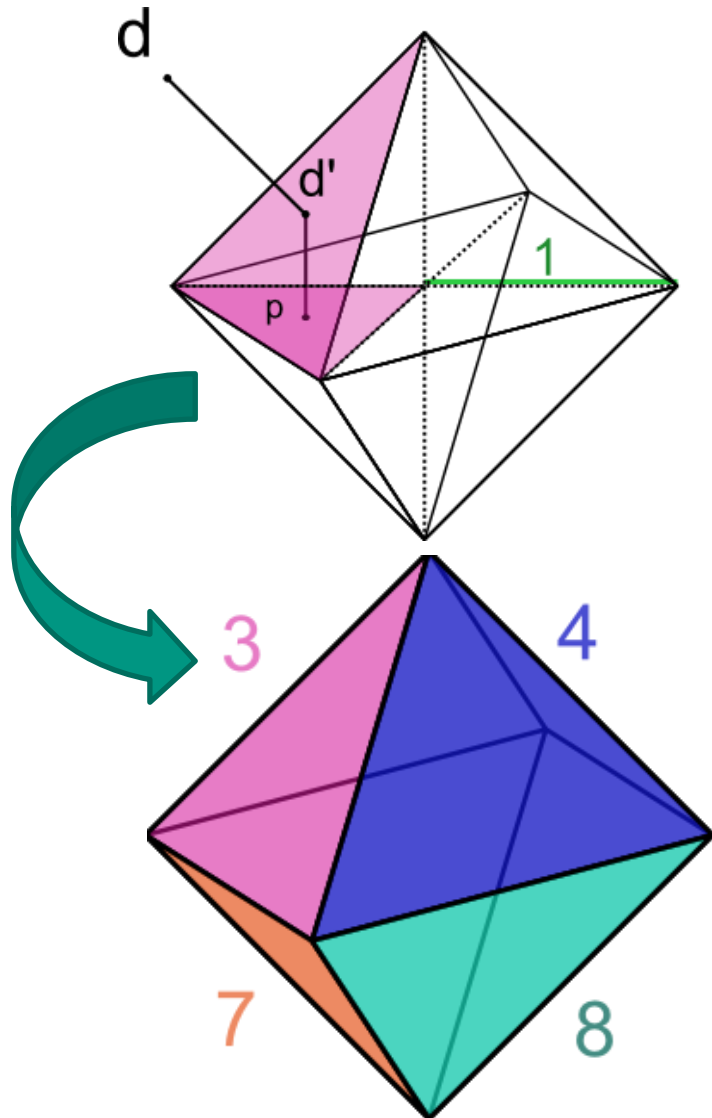
- Position
- Incident direction
- Energy



Preprocessing: Photon Mapping

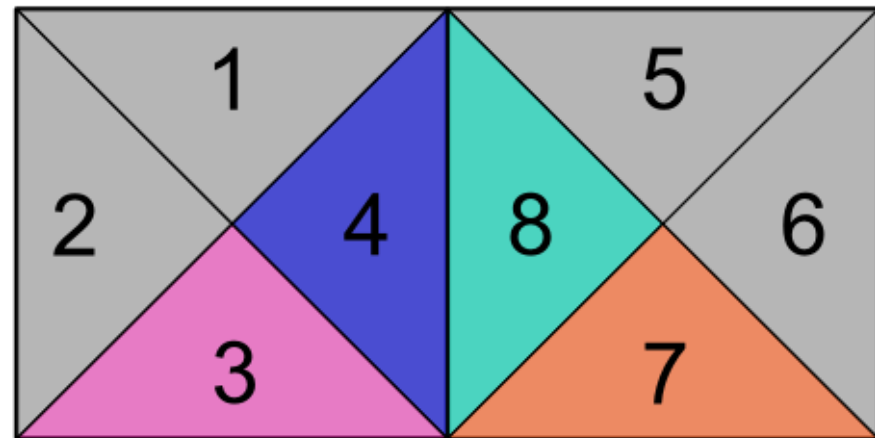
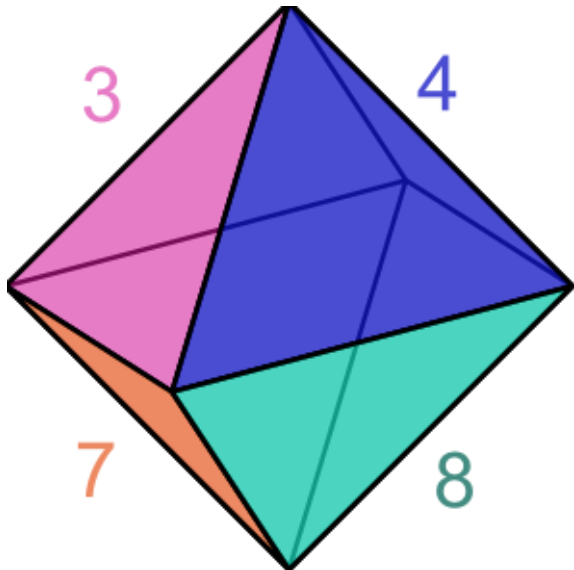
- Photon:
 - Position
 - Incident direction
 - Energy
- Cancel Paths
 - Russian Roulette
 - Energy contribution too small
- k-d tree for fast nearest-neighbour search

Cache Parameterization: Octahedron



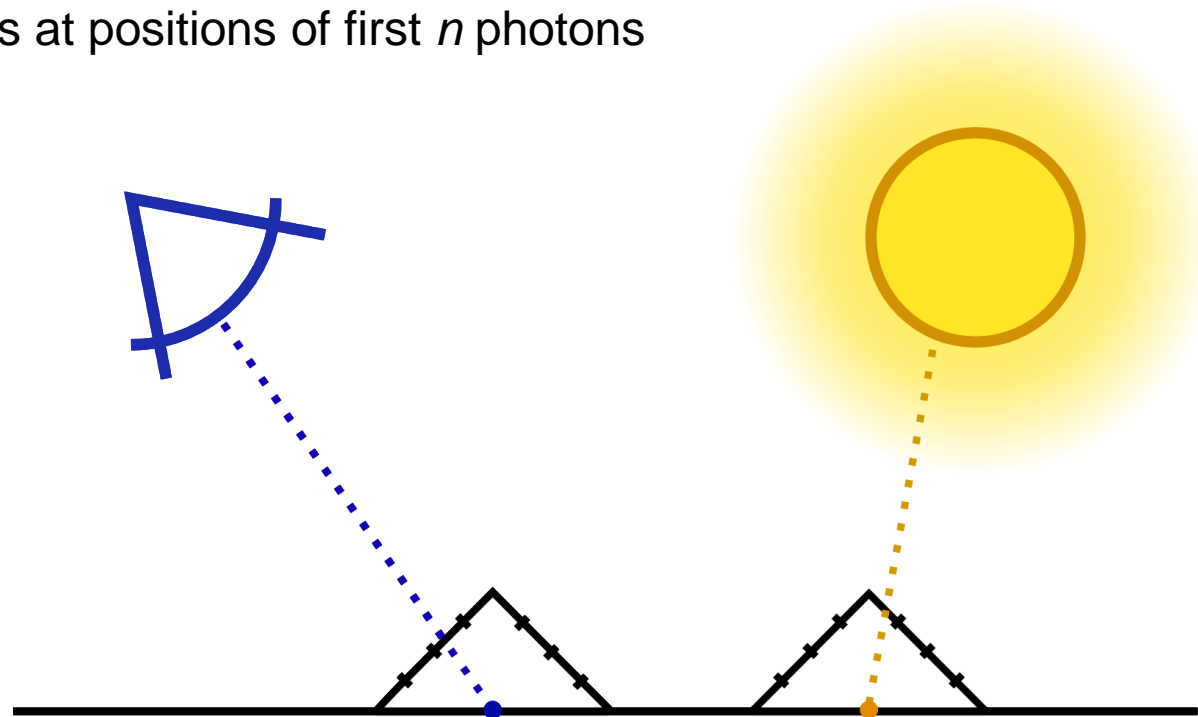
Cache Parameterization: Octahedron

- Simple extension to both hemispheres
- Simple conversion direction \Leftrightarrow texel
- Texels cover similar solid angles



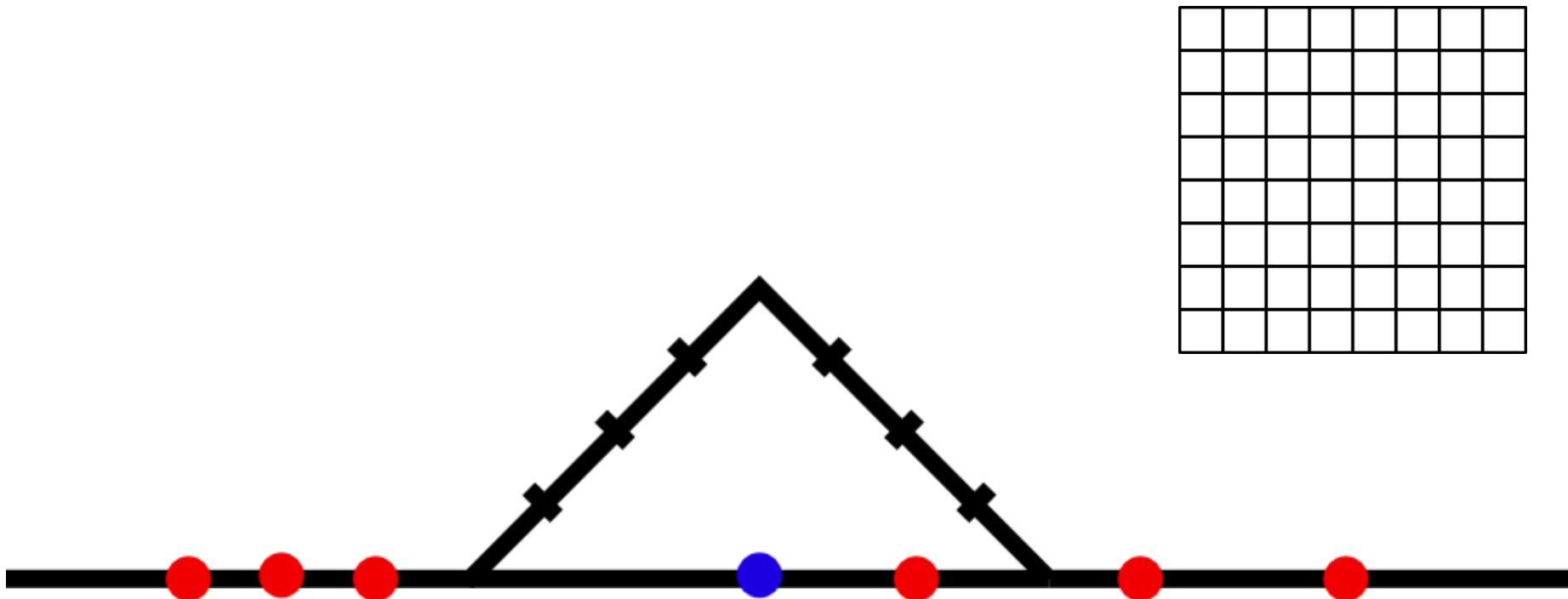
Preprocessing: Placing Caches

- From Camera rays:
 - One Cache per every 8x8 pixel block
- From Photons:
 - Place Caches at positions of first n photons



Preprocessing: Filling Caches

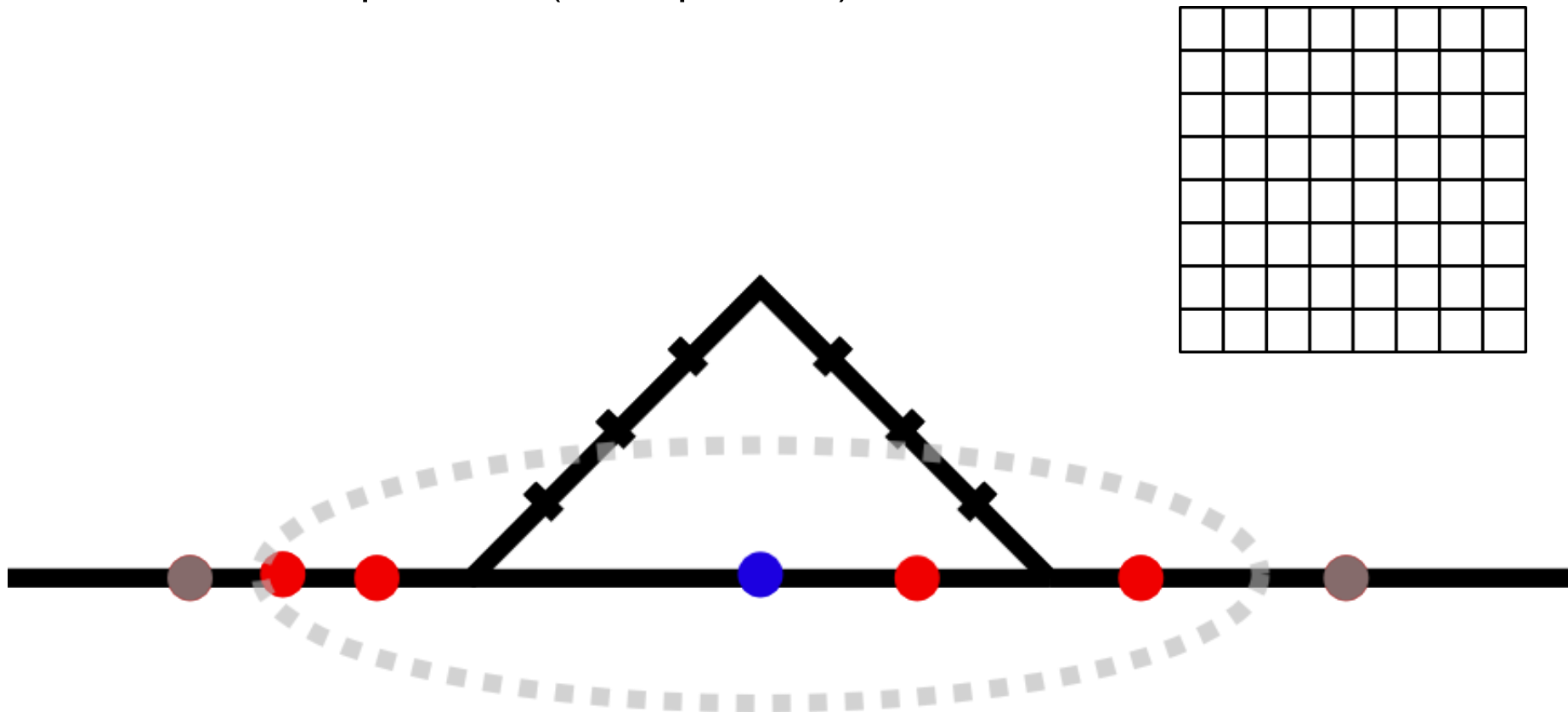
For every cache: Start with empty environment map (right)



Preprocessing: Filling Caches

For every cache:

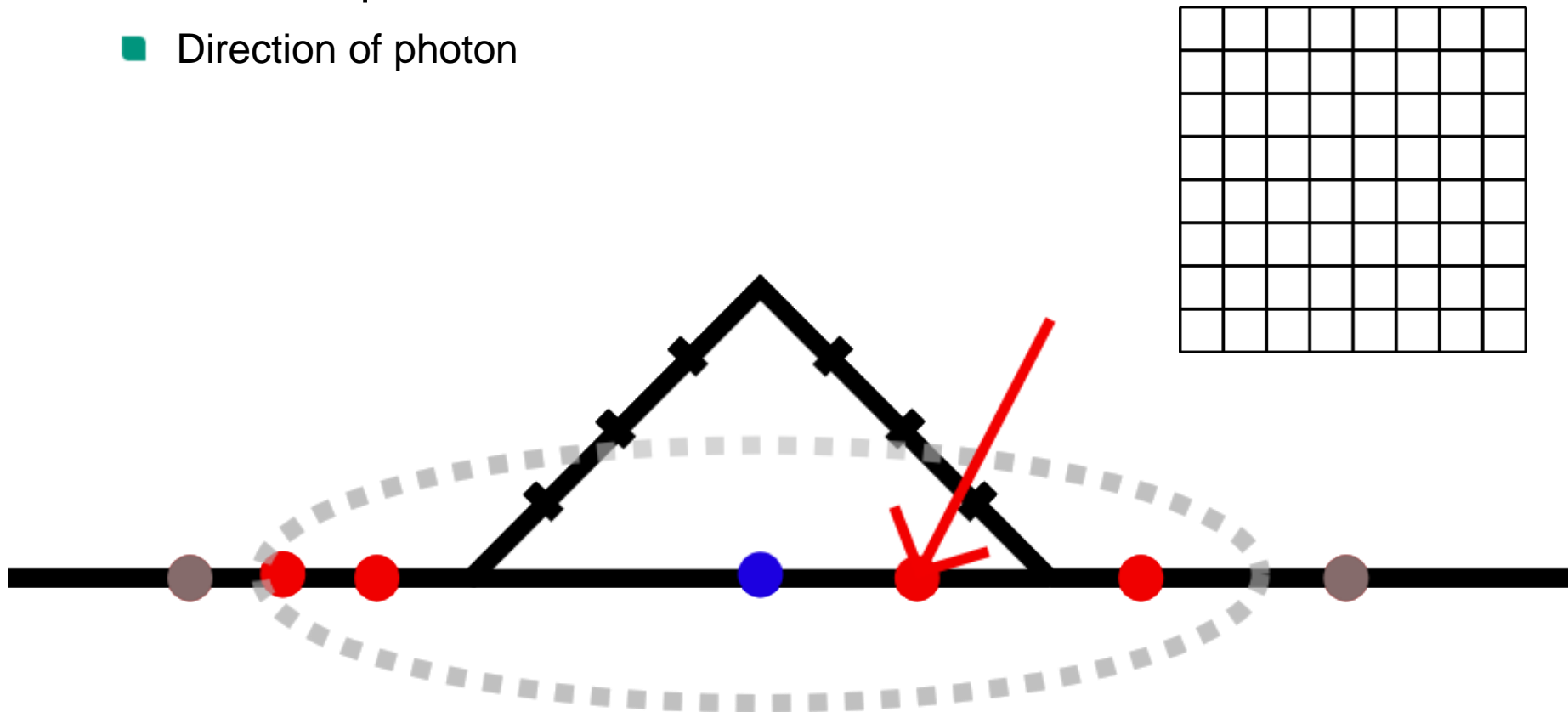
- For closest k photons: (Example: $k=4$)



Preprocessing: Filling Caches

For every cache:

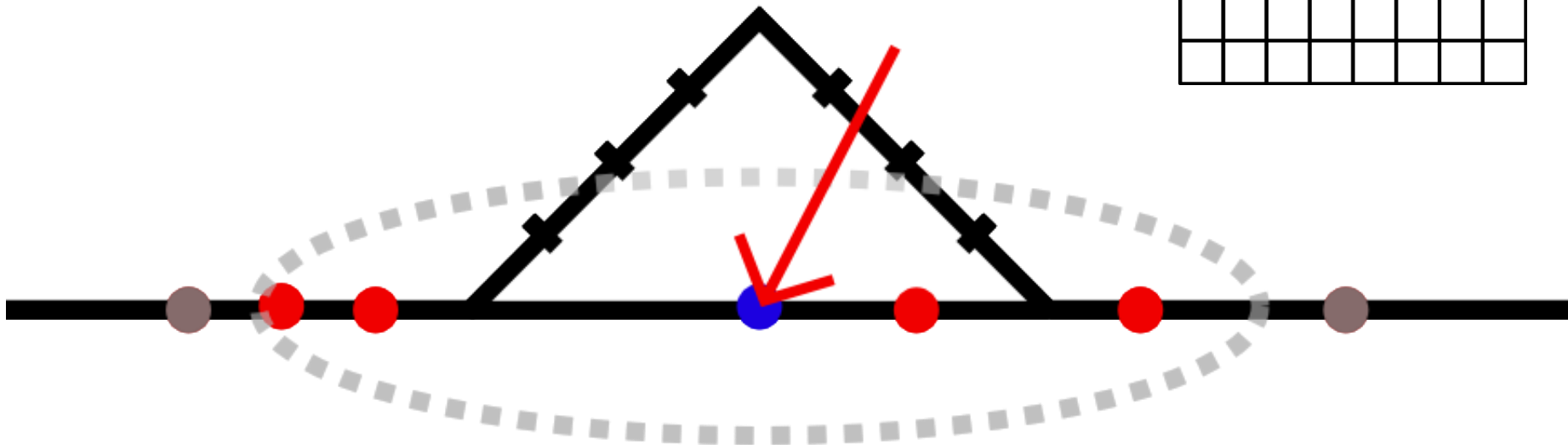
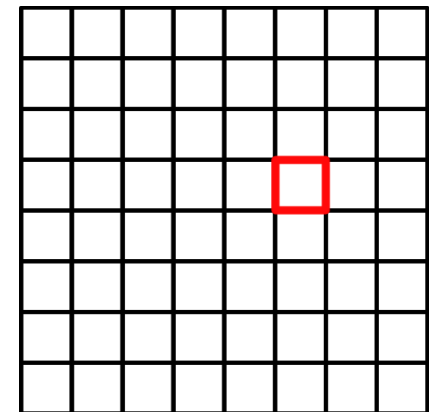
- For closest k photons:
 - Direction of photon



Preprocessing: Filling Caches

For every cache:

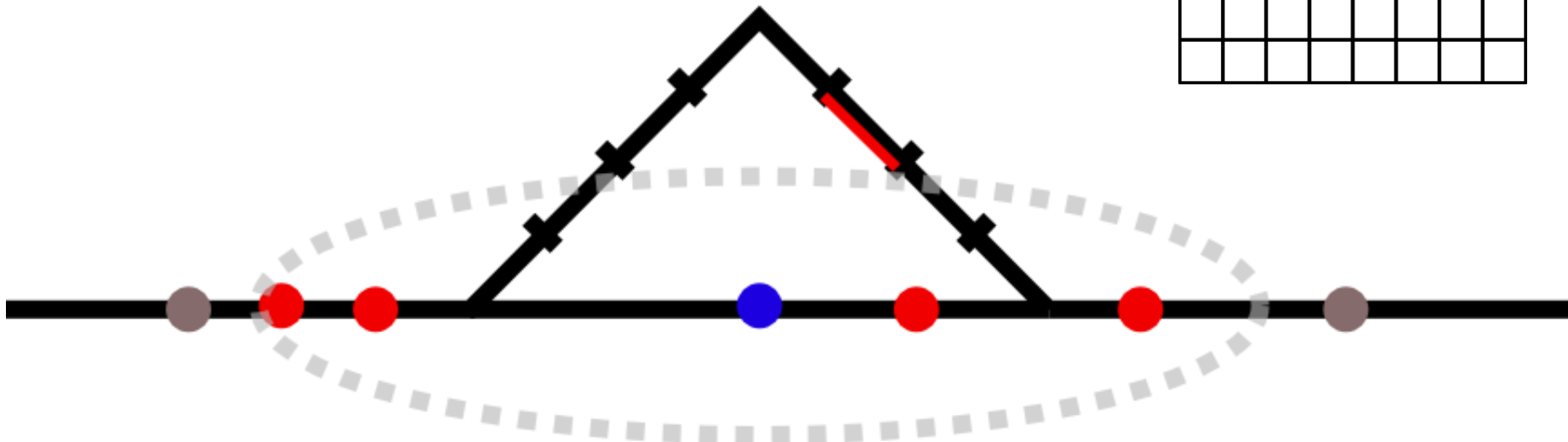
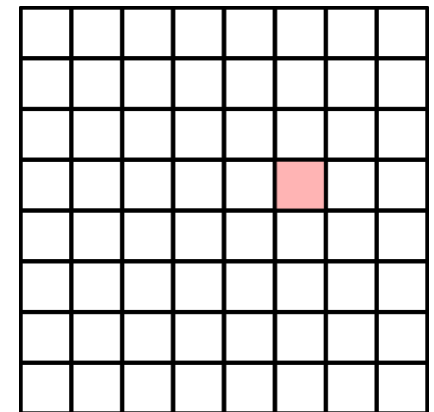
- For closest k photons:
 - Direction of photon \rightarrow texel coordinate



Preprocessing: Filling Caches

For every cache:

- For closest k photons:
 - Direction of photon \rightarrow texel coordinate
 - Add energy of photon to texel

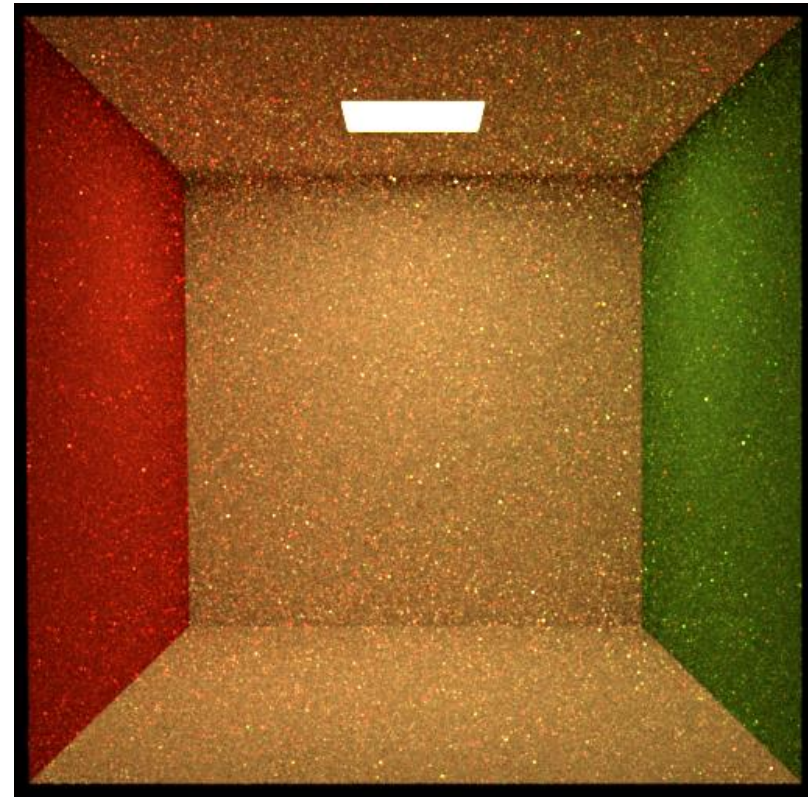
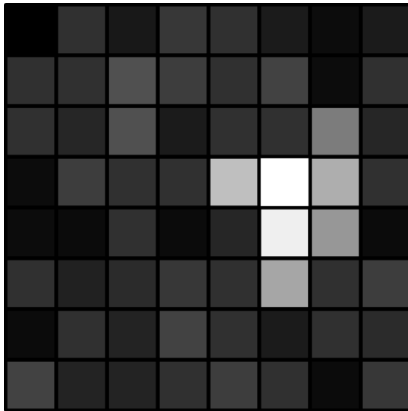


Preprocessing: Filling Caches

For every cache:

- For closest k photons:
 - Direction of photon \rightarrow texel coordinate
 - Add energy of photon to texel

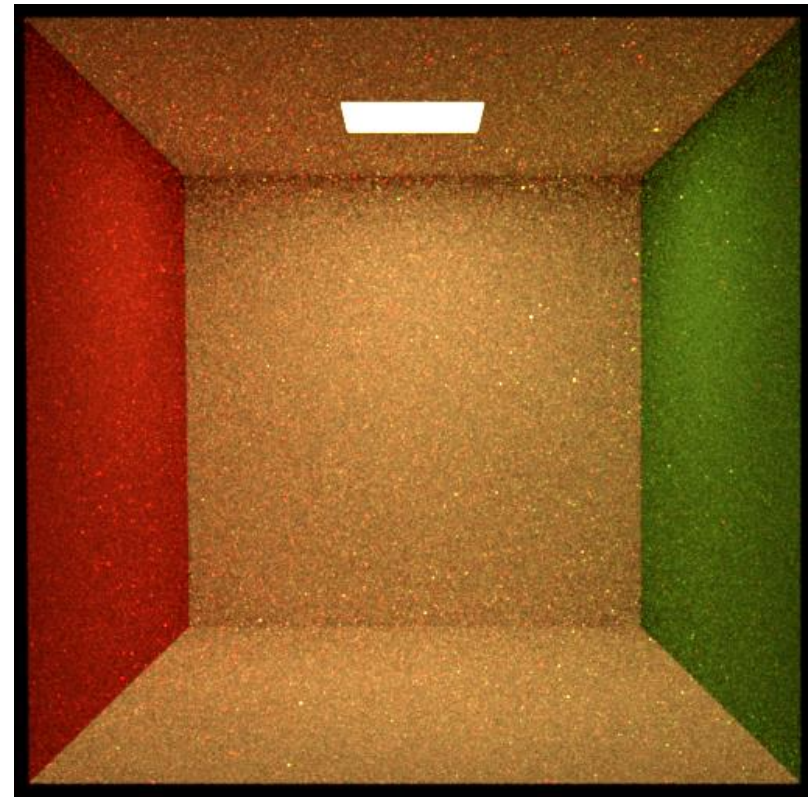
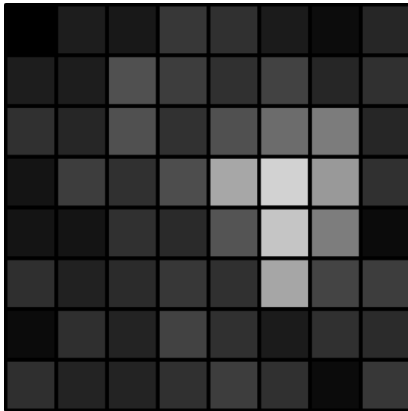
Resulting Environment Map:



Preprocessing: Filling Caches

For every cache:

- For closest k photons:
 - Direction of photon \rightarrow texel coordinate
 - Add energy of photon to texel
- Bilinear + Gaussian Filter



Preprocessing: Filling Caches

For every cache:

- For closest k photons:
 - Direction of photon \rightarrow texel coordinate
 - Add energy of photon to texel
- Bilinear + Gaussian Filter

Result:

Map filled with **relative energy** per incident direction

Preprocessing: Relative Energy \rightarrow PDF

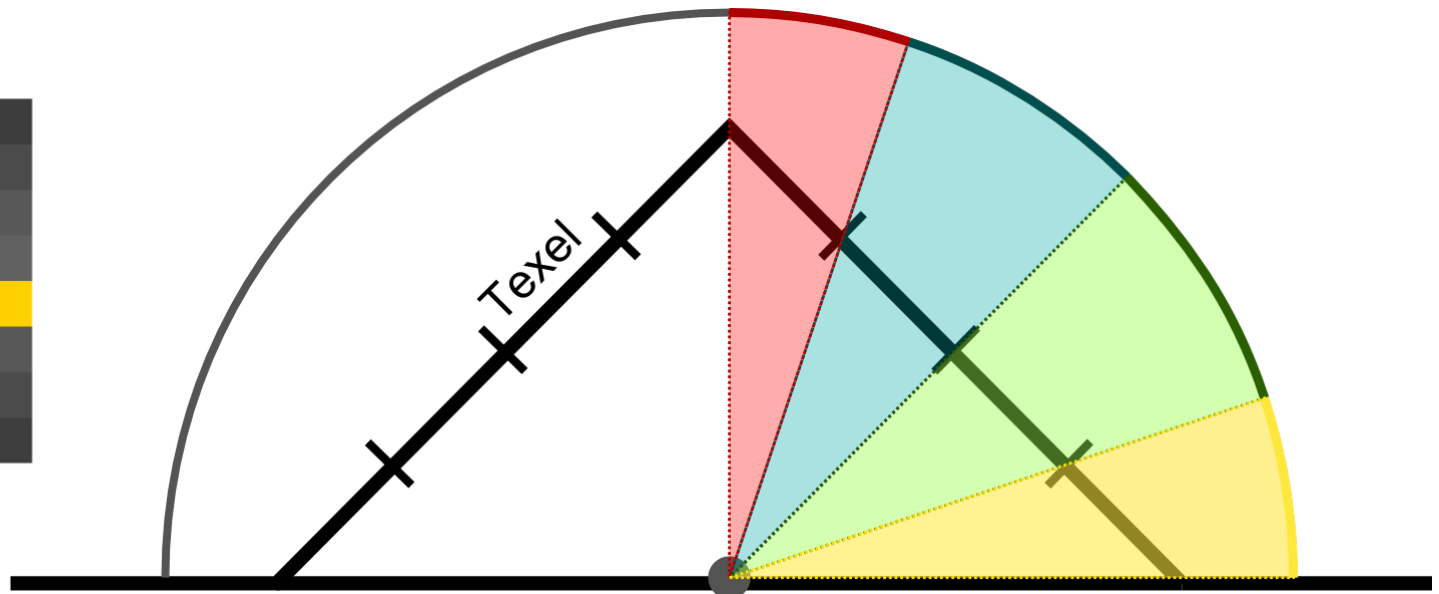
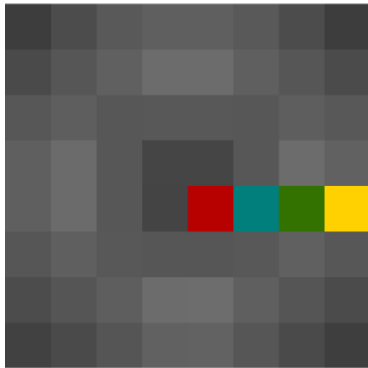
- Normalize sum of all texels to 1
- Monte Carlo Integration \rightarrow Set all 0 texels to small value
- Normalize again

Result:

Map filled with PDF for incident radiance, **measured over texel space**

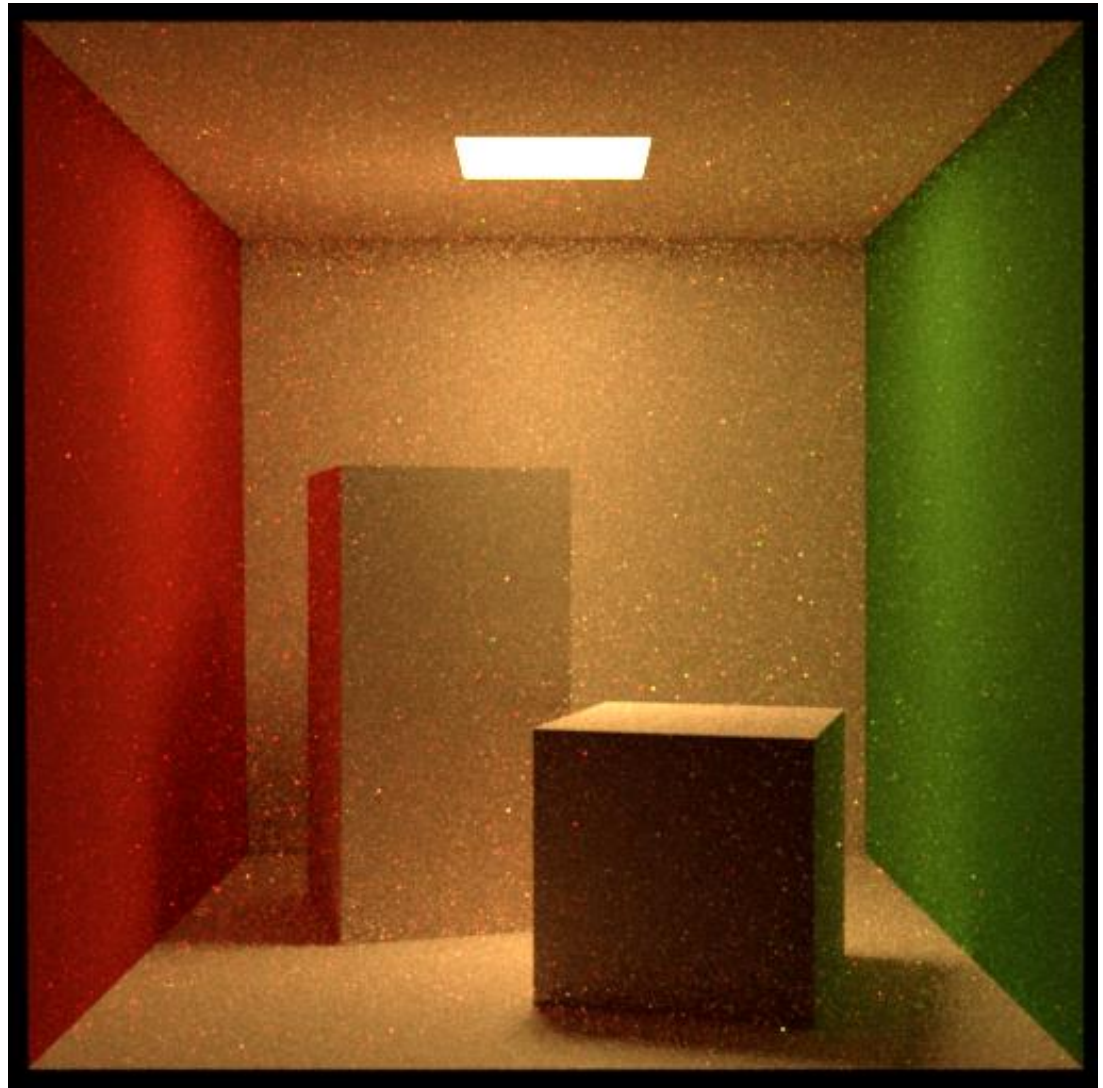
Preprocessing: PDF \rightarrow PDF over solid angle

- Problem: Texels cover different amount of solid angle
 - More solid angle near the center
 - Less solid angle near the edges



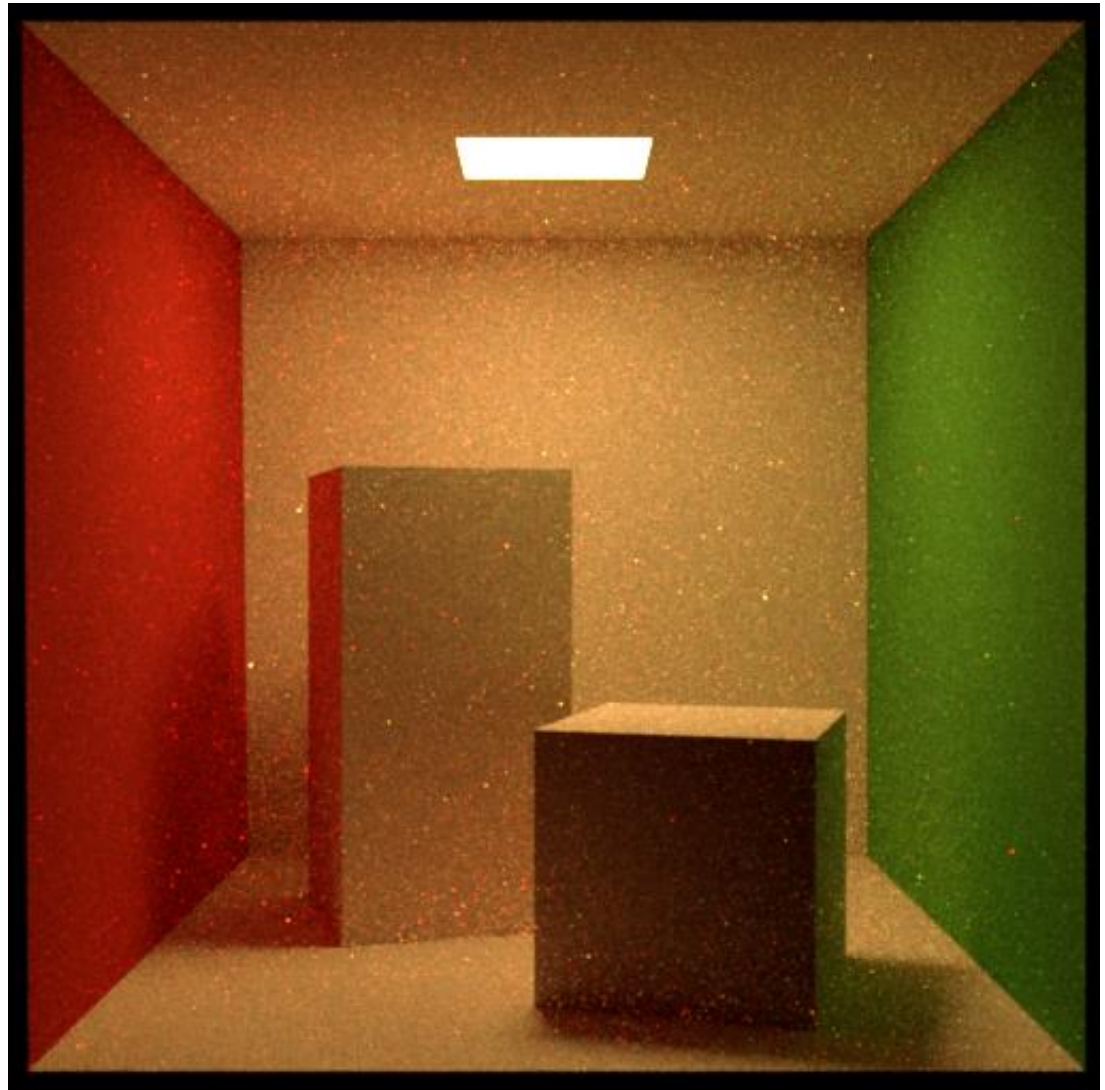
Preprocessing: PDF \rightarrow PDF over solid angle

Wrong: convert with
Factor $\frac{\text{number of texels}}{2\pi}$



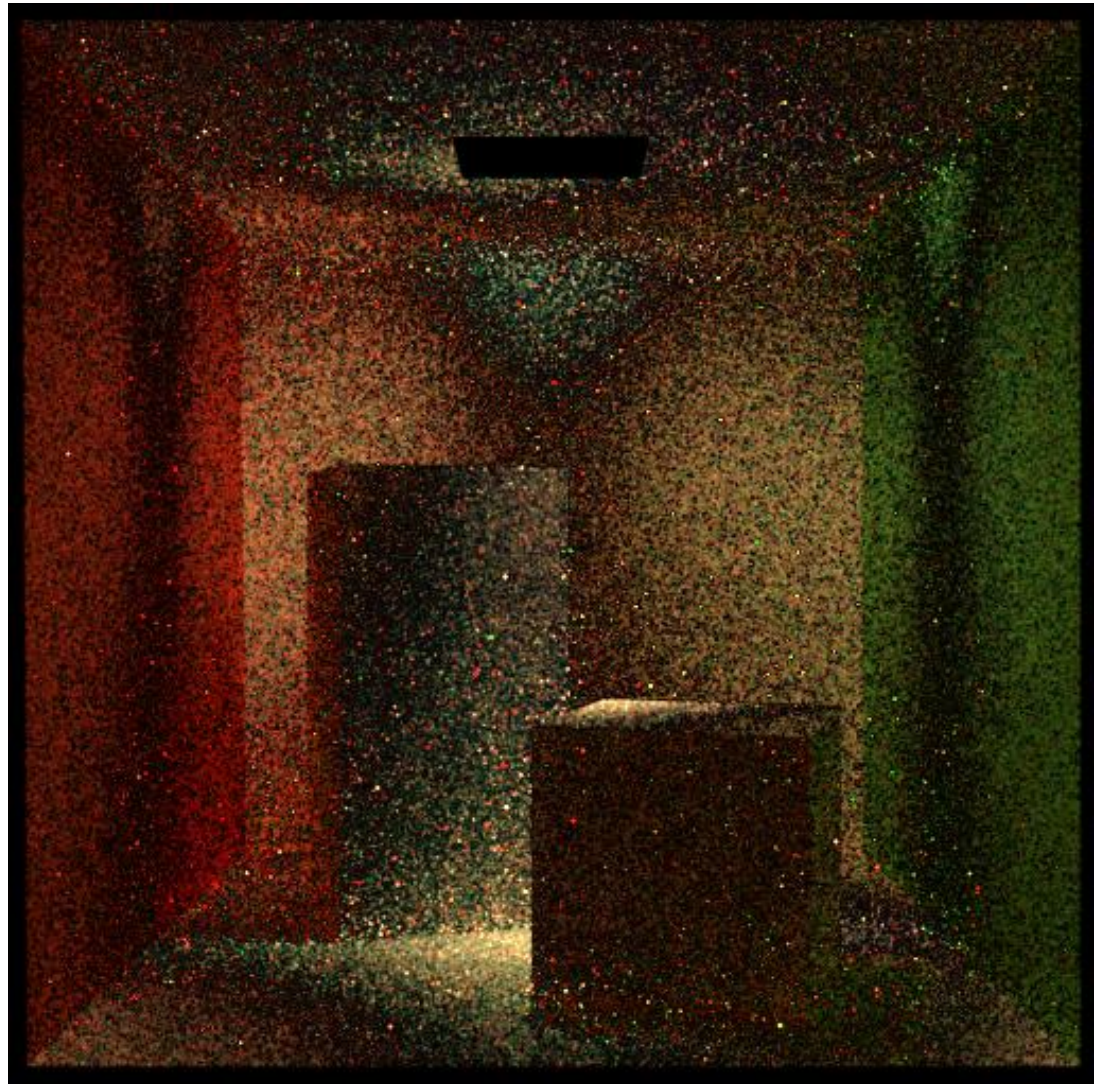
Preprocessing: PDF \rightarrow PDF over solid angle

Correct conversion
to solid angle



Preprocessing: PDF \rightarrow PDF over solid angle

Difference



Final Cache

- Octahedron map with PDF over solid angle
- Octahedron map with CDF for sampling
- k-d tree for faster lookup

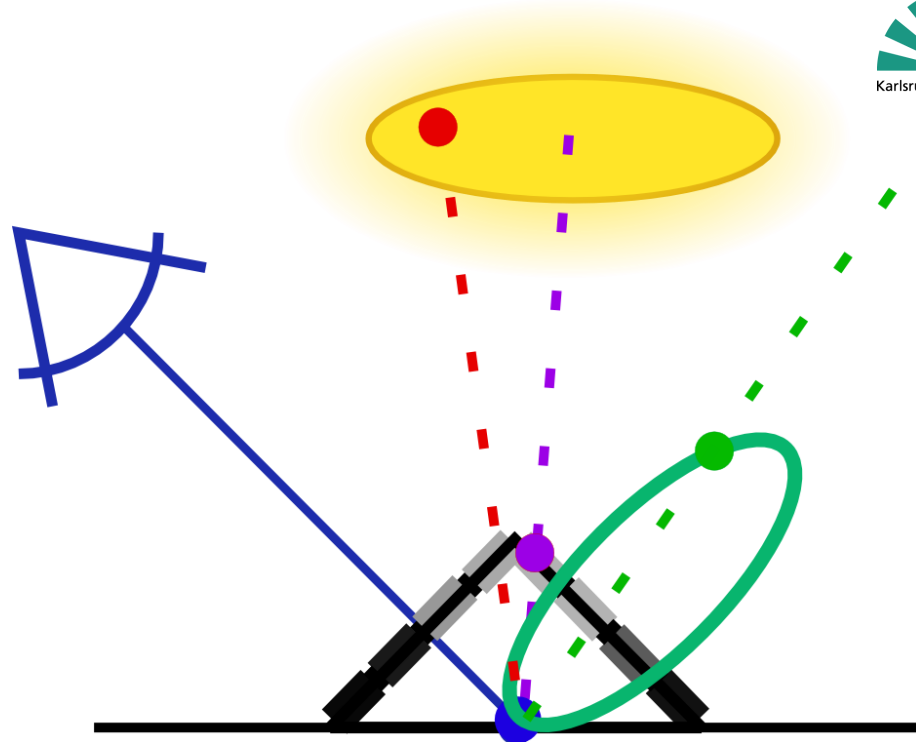
Rendering

Sample paths using...

■ Caches

■ BSDF

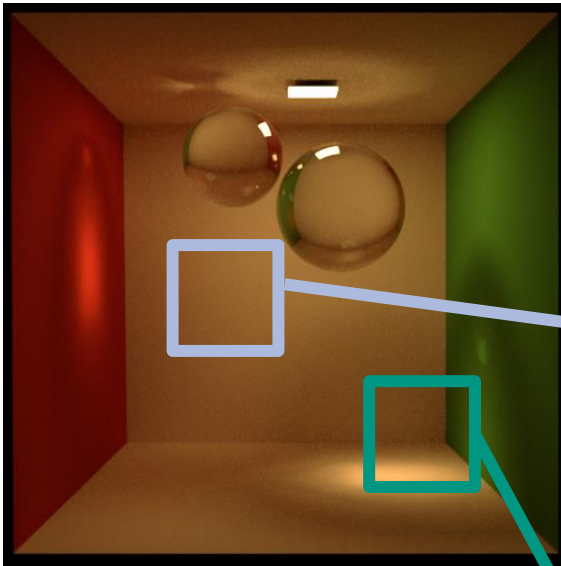
■ NEE




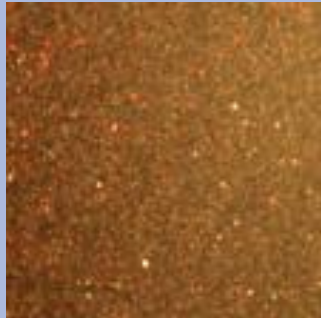
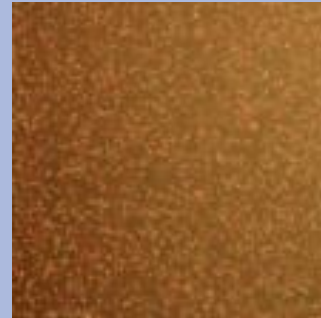



➔ Combine with Multiple Importance Sampling

➔ No Cache available? ➔ switch to BSDF sampling

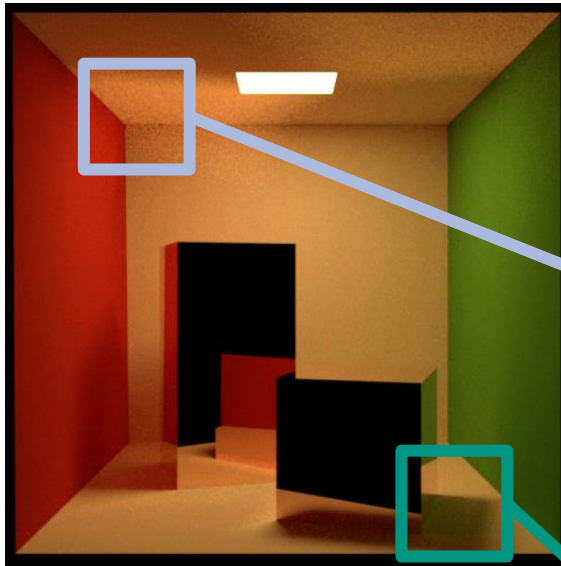
Results









256 samples per pixel
1 Mio. photons
20,000 caches
2000 photons per cache
16x16 texels per cache
42MB memory consumption

Caches + NEE	Caches + BSDF	NEE + BSDF
		
		

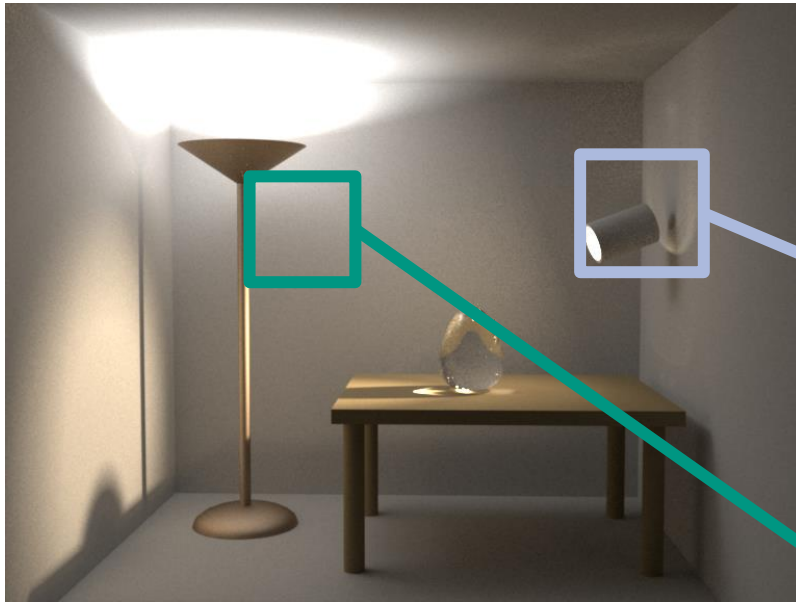
Results



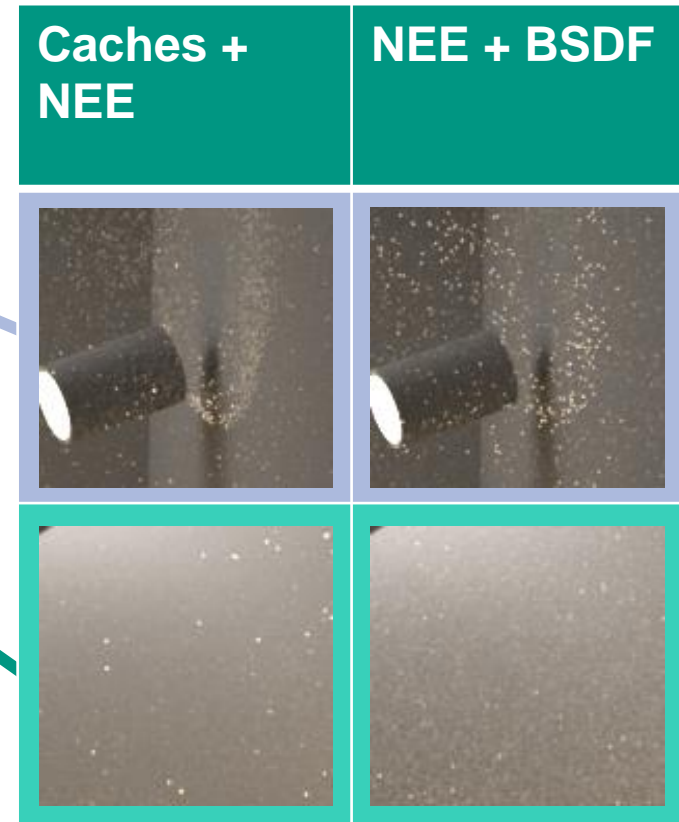
Caches + NEE	Caches + BSDF	NEE + BSDF
		
		

128 samples per pixel
800k photons
20k caches
1k photons per cache
16x16 texels per cache
42MB memory consumption

Results

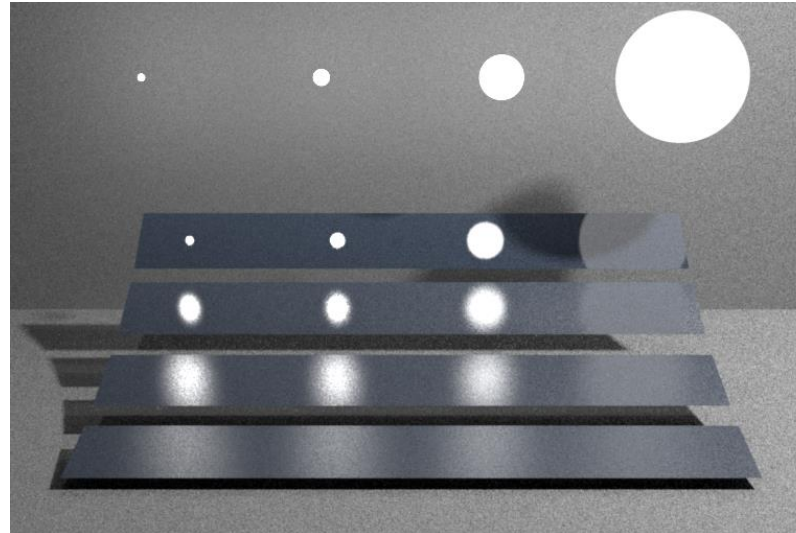


4096 samples per pixel
1.5 Mio. photons
30k caches
2k photons per cache
16x16 texels per cache
Xxx memory consumption
3300 triangles



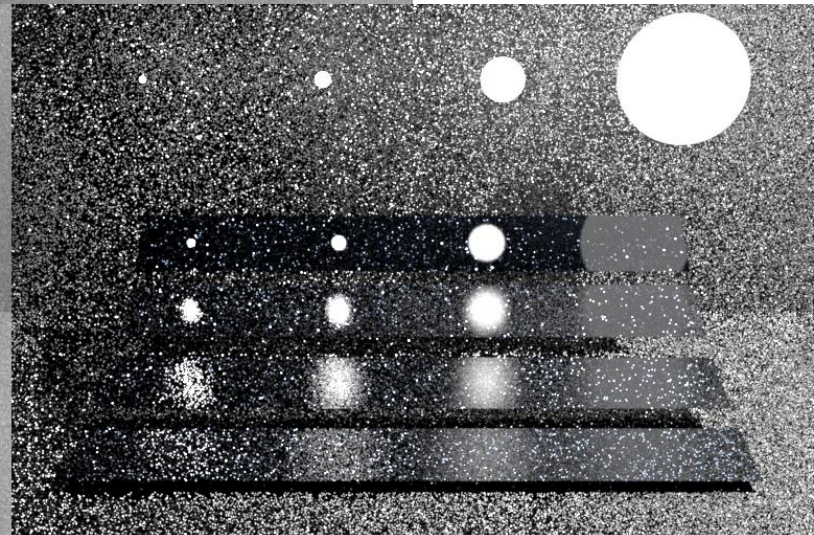
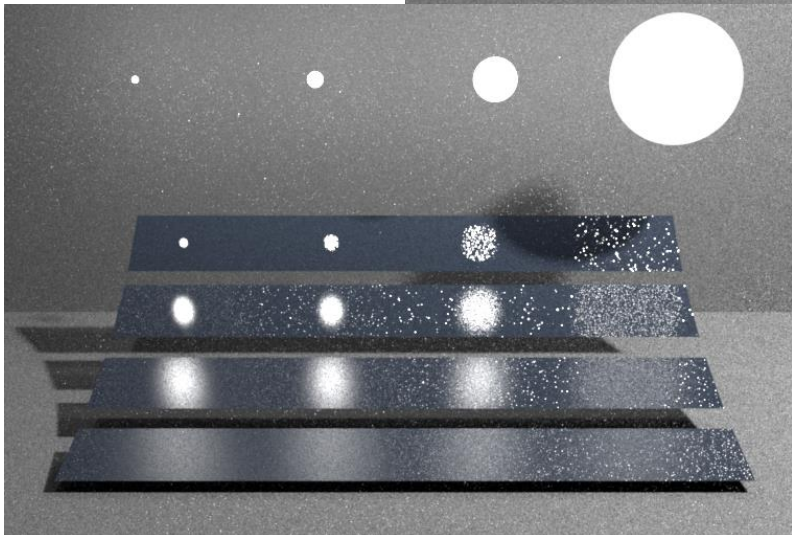
Results

NEE + BSDF

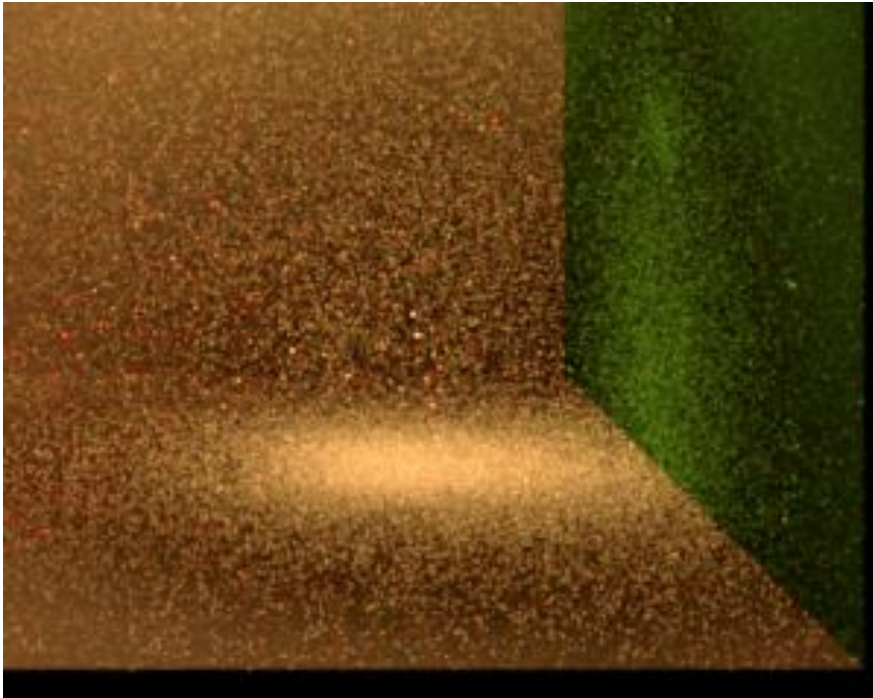


64 samples per pixel
1 Mio. photons
20k caches
2k photons per cache
16x16 cache resolution
Caches + BSDF

Caches + NEE



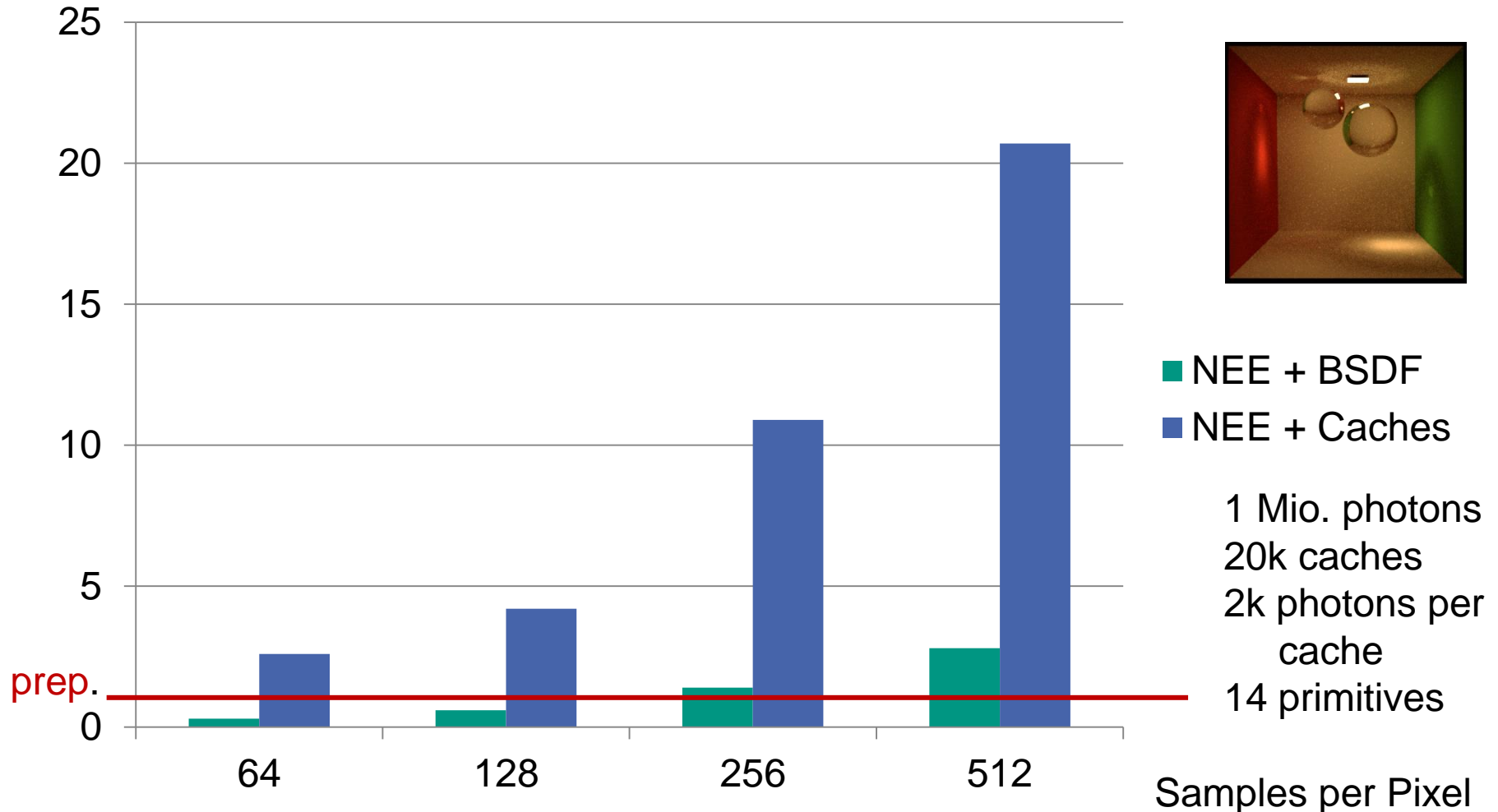
Different Cache Configurations: #photons



few photons in scene
(~ 10 000)

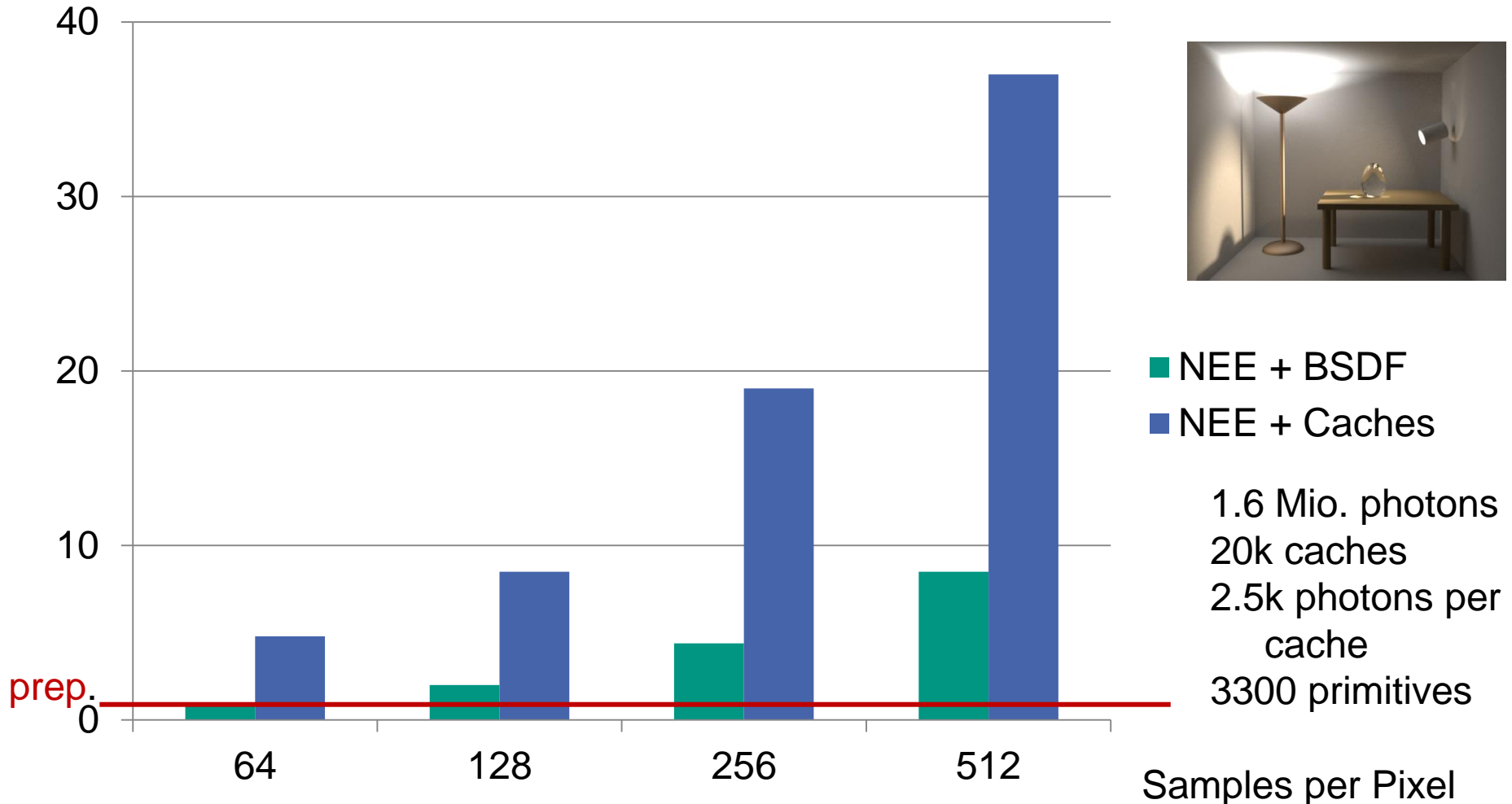
Render Times: Glass Sphere

[minutes]



Render Times: Glass Egg

[minutes]



Equal Time Comparison

NEE + Caches

NEE + Caches
128spp
8.4 min

NEE + BSDF
512spp
8.2 min



Equal Time Comparison

NEE + BSDF

NEE + Caches
128spp
8.4 min

NEE + BSDF
512spp
8.2 min



Conclusion

- Equally good image in similar time
- Better image with same sample-per-pixel - count

Conclusion

On-line Learning of Parametric Mixture Models for Light Transport Simulation

Jiří Vorba^{1*}

Ondřej Karlík^{1*}

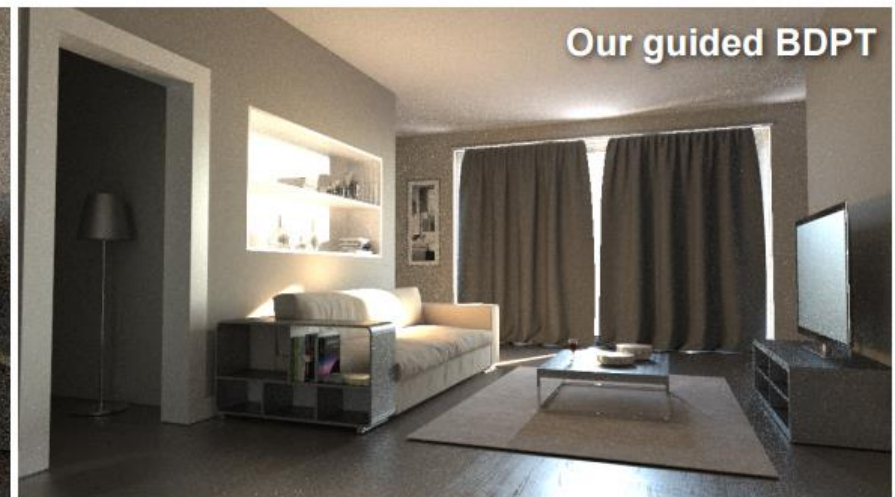
Martin Šik^{1*}

Tobias Ritschel^{2†}

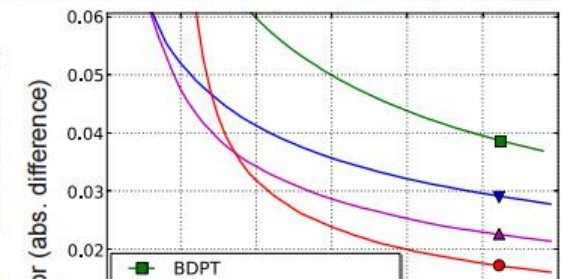
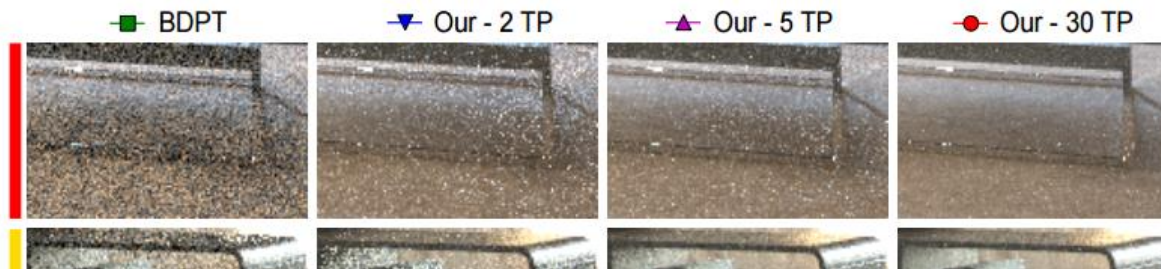
Jaroslav Křivánek^{1‡}
¹Charles University in Prague

²MPI Informatik, Saarbrücken


Bidirectional path tracing (BDPT)



Our guided BDPT



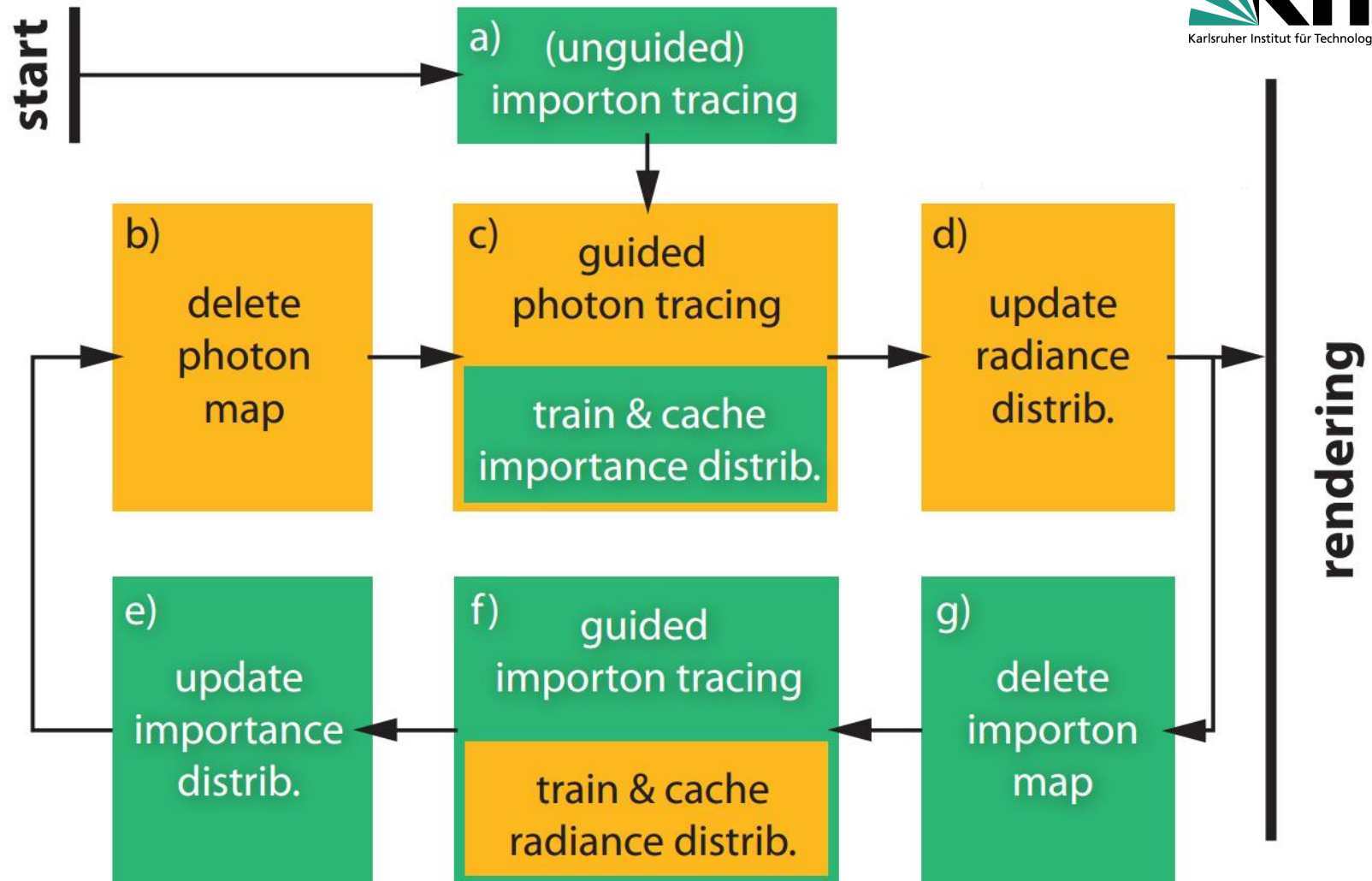
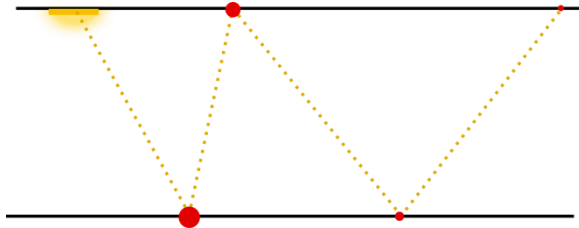


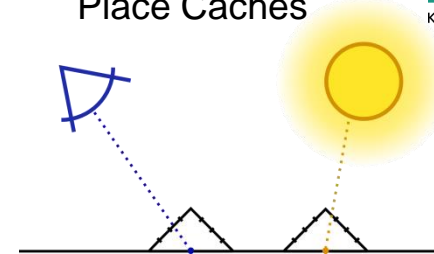
Figure 2: *The training phase preceding the rendering phase.*

Source: „On-line Learning of Parametric Mixture Models for Light Transport Simulation“ (previous slide)
<http://cgg.mff.cuni.cz/~jaroslav/papers/2014-onlineis/>

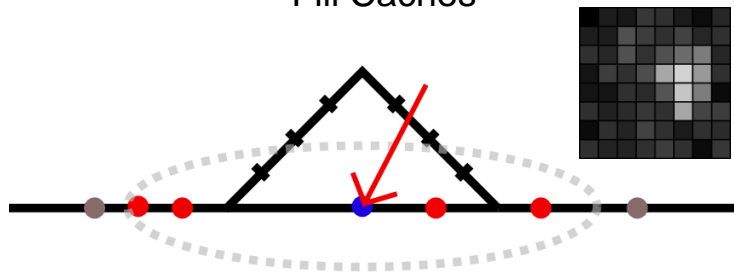
Photon Mapping



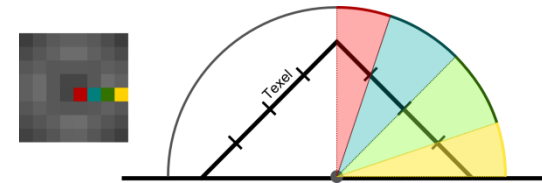
Place Caches



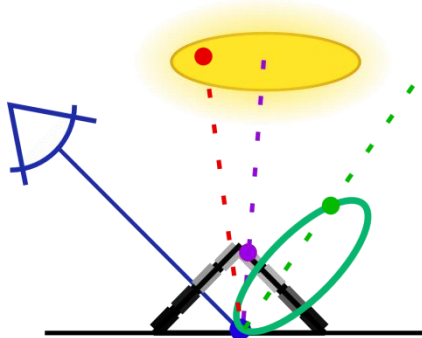
Fill Caches



PDF over solid angle



Path Tracing



<https://github.com/Baconkeks/Irradiance-Importance-Sampling>