Code **▼**

Compound Poisson process

2XXXXXXX NAME

This docoument demonstrates how simulate a compound Poisson process.

- Consider a shop where customers arrive in an exponential distribution with rate $\lambda=20$.
 - mean of $Exp(\lambda) = 1/\lambda$.
- The number of customers for each arrival follows a geometric distribution with parameter p=0.4.
 - mean of Geom(p) = 1/p.
- · All random values are independent.

Example of generating exponential random variables:

From time 0 to 1, how many times will customers arrive?

- · Of course, this is random.
- num_arrivals represents the total arrival numbers up to time 1.

```
arrivals <- numeric()
while (sum(arrivals)<1){
  arrivals <- c(arrivals, rexp(1, lambda))
}
(num_arrivals <- length(arrivals) - 1)</pre>
```

```
[1] 18
```

The number of cumstomers in each arrival is determined by a geometric distribution.

```
p = 0.4
(num_customer <- rgeom(1, p) + 1)
```

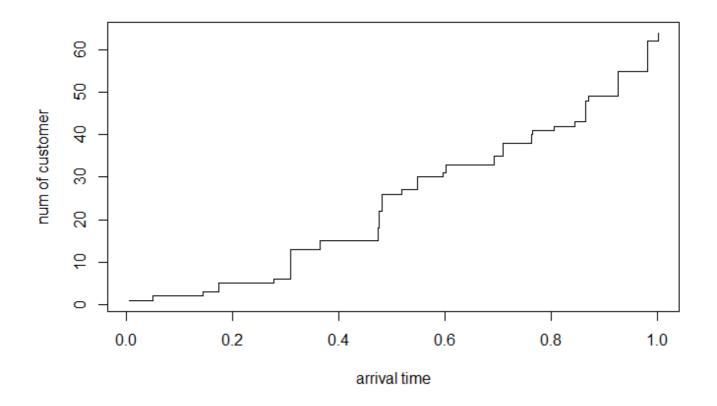
```
[1] 6
```

The following plot represents the customer arrivals:

• To plot stair type graph, use type='s'.

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Your code shoude be here



In this case, the total number of customer up to time 1 is:

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sum(num_customer[1:(length(num_customer)-1)])

[1] 60

Now simulate this procedure 100 times.

- first, compute the total number of customers up to time 1 for each simulation.
- next, compute the mean of the total number of customers.

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Your code shoude be here

[1] 42.4

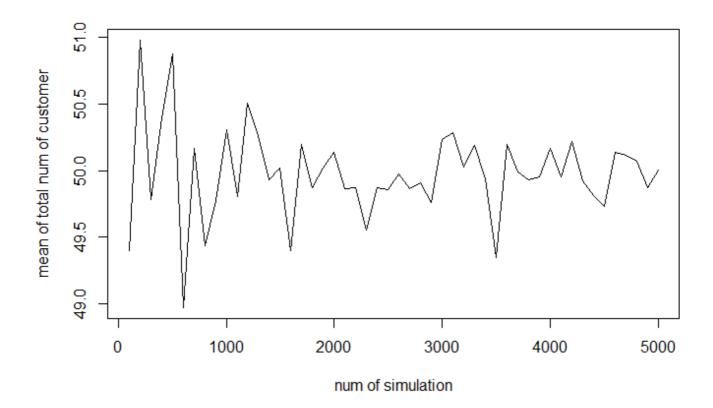
Increase sequentially the simulation number:

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 $num_simuls \leftarrow seq(100, 5000, 100)$

Now plot the mean of the number of total cumstomer with simulation number.

- # Your code shoude be here
- # This takes time.



Question:

- Which value does the mean of total num of customer converge?
- Caluate the theoritical value of the mean of total num of customer.