INFO-F403 Introduction to Language Theory and Compilation

Chapeaux Thomas Dagnely Pierre

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Lexèmes

Définition des tokens

Lexical units	regular expressions
INT	([0-9])*
FLOAT	([0-9])*.DOT.([0-9])*
BOOL	(0+1+true+false+")
STRING	'.([A-Za-z]+[0-9])*.'
FAC	!
MUL	*
DIV	/
MINUS	-
ADD	+
LT	<
GT	>
LE	<=
GE	>=
EQUIV	==
DIF	!=
AND	&&
OR	
NOT	not
LT-S	lt
GT-S	gt
LE-S	le
GE-S	ge
EQ-S	eq
NE-S	ne

	_
Lexical units	regular expressions
EQUAL	=
DOT	
SEMICOLON	;
COMA	,
OPEN-PAR	(
CLOSE-PAR)
OPEN-BRAC	{
CLOSE-BRAC	}
OPEN-COND	IF
CLOSE-COND	ELSE
ADD-COND	ELSE IF
NEG-COND	UNLESS
RET	return
FUNCT-DEF	SUB
ID	STRING
FUNCT-NAME	&.STRING
PERL-DEF	defined
PERL-INT	int
PERL-LENG	length
PERL-SCAL	scalar
PERL-SUBS	substr
PERL-PRIN	print
COMM	#.STRING
VARIABLE	\$.STRING

coma peut définir l'opérateur coma ou juste un coma entre deux param, mais même lexical unit, c'est le parser qui se charge du reste

COMM ne sera plus utilisé par la suite, on les supprime avant de faire l'analyse lexicale

Automates

Définition des automates finis

DFA

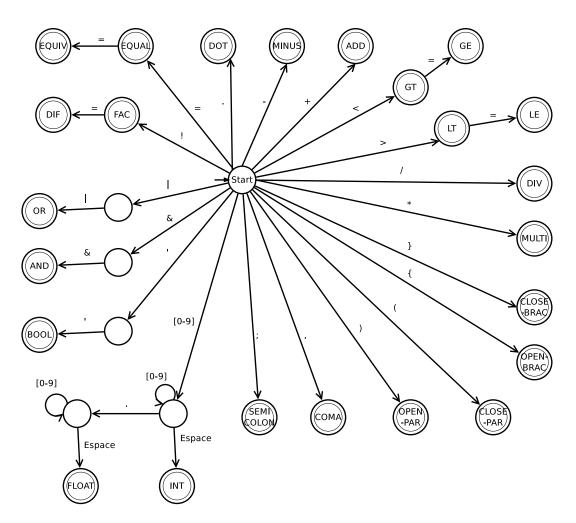


Figure 1: automate "non alphabétique"

La plupart des noeuds pointent vers le token ID, trop lourd a représenter, donc met une petite fleche bleu à la place.

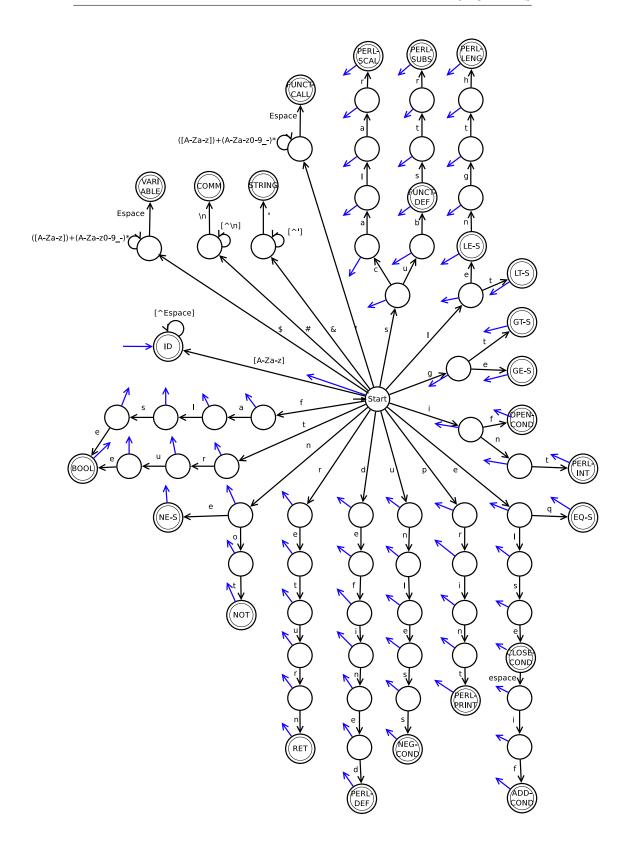


Figure 2: automate "alphabétique"

Grammaire

3.1 Grammaire de base

Nous utilisons pour définir la grammaire la version simplifiée de l'assistant :

```
<PROGRAM>
                             \rightarrow <FUNCT-LIST> <INSTRUCT-LIST>
                              \rightarrow <FUNCT-LIST>
                              \rightarrow <INSTRUCT-LIST>
       <FUNCT-LIST>
                             \rightarrow <FUNCT>
                             \rightarrow <FUNCT-LIST> <FUNCT>
             <FUNCT>
                             \rightarrow funct-def id <FUNCT-ARG> open-brac <INSTRUCT-LIST> close-brac
       <FUNCT-ARG>
                             \rightarrow <ARG-LIST>
          <ARG-LIST>
                             \rightarrow <ARG-LIST> coma variable
                             \rightarrow variable
                              \rightarrow epsilon
   <INSTRUCT-LIST>
                             \rightarrow <INSTRUCT-LIST> <INSTRUCT> semicolon
                             \rightarrow <INSTRUCT> semicolon
      <FUNCT-CALL>
                             \rightarrow funct-name <FUNCT-CALL-ARG>
<FUNCT-CALL-ARG>
                             \rightarrow <FUNCT-CALL-ARG> coma <EXP>
                             \rightarrow <EXP>
                             \rightarrow epsilon
         <INSTRUCT>
                             \rightarrow variable equal \langle EXP \rangle
                              \rightarrow <EXP>
                              \rightarrow ret \langleEXP\rangle
                             \rightarrow <COND>
               <COND>
                             \rightarrowopen-cond <<br/>EXP> open-brac <<br/>INSTRUCT-LIST> close-brac <<br/>COND-END>
                             \rightarrowadd-cond <<br/>EXP> open-brac <<br/>INSTRUCT-LIST> close-brac <<br/>COND-END>
         <COND-END>
                              \rightarrow close-cond open-brac <INSTRUCT-LIST> close-brac
                             \rightarrow epsilon
       <SIMPLE-EXP>
                             \rightarrow int
                             \rightarrow <FUNCT-CALL>
                             \rightarrow variable
                             \rightarrow string
                 <EXP>
                             \rightarrow <SIMPLE-EXP>
                             \rightarrow open-par \langle EXP \rangle close-par
                              \rightarrow <EXP> add <EXP>
                              \rightarrow <EXP> minus <EXP>
                              \rightarrow <EXP> multi <EXP>
                              \rightarrow <EXP> div <EXP>
                              \rightarrow <EXP> equiv <EXP>
                              \rightarrow <EXP> gt <EXP>
```

3.2 Suppression des symboles inutiles

on vire les non-productifs et inaccessibles. Y en a pas donc ca va vite.

3.3 Gestion des priorités et associativité

Cela ne concerne que la règle EXP, on la transforme donc en :

```
 \begin{array}{lll} \langle \mathrm{EXP} \rangle & \rightarrow \langle \mathrm{EXP-2} \rangle & \mathrm{equiv} \ \langle \mathrm{EXP-2} \rangle \ \langle \mathrm{EXP-2} \rangle \\ & \rightarrow \langle \mathrm{EXP-2} \rangle & \mathrm{gt} \ \langle \mathrm{EXP-2} \rangle \ \langle \mathrm{EXP-2} \rangle \\ & \rightarrow \langle \mathrm{EXP-2} \rangle & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{add} \ \langle \mathrm{EXP-3} \rangle \ \langle \mathrm{EXP-2} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{minus} \ \langle \mathrm{EXP-3} \rangle \ \langle \mathrm{EXP-2} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \rightarrow \langle \mathrm{SIMPLE-EXP} \rangle & \mathrm{mul} \ \langle \mathrm{SIMPLE-EXP} \rangle \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{SIMPLE-EXP} \rangle & \mathrm{div} \ \langle \mathrm{SIMPLE-EXP} \rangle \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{SIMPLE-EXP} \rangle & \rightarrow \langle \mathrm{SIMPLE-EXP} \rangle \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{SIMPLE-EXP} \rangle & \mathrm{div} \ \langle \mathrm{SIMPLE-EXP} \rangle \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{SIMPLE-EXP} \rangle & \mathrm{div} \ \langle \mathrm{SIMPLE-EXP} \rangle \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{SIMPLE-EXP} \rangle & \mathrm{div} \ \langle \mathrm{SIMPLE-EXP} \rangle \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{SIMPLE-EXP} \rangle & \mathrm{div} \ \langle \mathrm{SIMPLE-EXP} \rangle \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{SIMPLE-EXP} \rangle & \mathrm{div} \ \langle \mathrm{SIMPLE-EXP} \rangle \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{SIMPLE-EXP} \rangle & \mathrm{div} \ \langle \mathrm{SIMPLE-EXP} \rangle \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{SIMPLE-EXP} \rangle & \mathrm{div} \ \langle \mathrm{SIMPLE-EXP} \rangle \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{SIMPLE-EXP} \rangle & \mathrm{div} \ \langle \mathrm{SIMPLE-EXP} \rangle \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle & \mathrm{div} \ \langle \mathrm{EXP-3} \rangle \\ & \rightarrow \langle \mathrm{EX
```

3.4 left factoring

Cela ne concerne que EXP, EXP-2, EXP-3 et PROGRAM :

```
<PROGRAM>
                     \rightarrow <FUNCT-LIST> <PROG-TAIL>
                     \rightarrow <INSTRUCT-LIST>
<PROG-TAIL>
                     \rightarrow <INSTRUCT-LIST>
                     \rightarrow epsilon
         \langle \text{EXP} \rangle
                     \rightarrow <EXP-2> <EXP-TAIL>
  <EXP-TAIL>
                     \rightarrow equiv \langleEXP-2\rangle \langleEXP-TAIL\rangle
                     \rightarrow gt <EXP-2> <EXP-TAIL>
                     \rightarrow epsilon
                     \rightarrow <EXP-3> <EXP-2-TAIL>
       <EXP-2>
<EXP-2-TAIL>
                    \rightarrow add <EXP-3> <EXP-2-TAIL>
                     \rightarrow minus <EXP-3> <EXP-2-TAIL>
                     \rightarrow epsilon
                     \rightarrow <SIMPLE-EXP> <EXP-3-TAIL>
       \langle \text{EXP-3} \rangle
<EXP-3-TAIL>
                     \rightarrow mul <SIMPLE-EXP> <EXP-3-TAIL>
                     \rightarrow div <SIMPLE-EXP> <EXP-3-TAIL>
                     \rightarrow epsilon
```

3.5 Left recursion

 ${\it concerne FUNCT-LIST, ARG-LIST, INSTRUCT-LIST, FUNCT-CALL-ARG:}$

```
\langle FUNCT\text{-}LIST \rangle \rightarrow \langle FUNCT\text{-}LIST\text{-}BEG \rangle \langle FUNCT\text{-}LIST\text{-}END \rangle
       \langle \text{FUNCT-LIST-BEG} \rangle \rightarrow \langle \text{FUNCT} \rangle
                                   \rightarrow <FUNCT> <FUNCT-LIST-END>
       <FUNCT-LIST-END>
                                     \rightarrow EPSILON
                 <ARG-LIST>
                                    \rightarrow <ARG-LIST-BEG> <ARG-LIST-END>
           <ARG-LIST-BEG>
                                    \rightarrow variable
                                     \rightarrow epsilon
           <ARG-LIST-END>
                                    \rightarrowcoma variable <ARG-LIST-END>
                                     \rightarrow epsilon
          <INSTRUCT-LIST>
                                     \rightarrow <INSTRUCT> semicolon <INSTRUCT-LIST>
                                     \rightarrow epsilon
      <FUNCT-CALL-ARG>
                                   \rightarrow <FUNCT-CALL-ARG-BEG> <FUNCT-CALL-ARG-END>
<FUNCT-CALL-ARG-BEG>
                                    \rightarrow <EXP>
                                     \rightarrow epsilon
<FUNCT-CALL-ARG-END>
                                    \rightarrow coma <EXP> <FUNCT-CALL-ARG-END>
                                     \rightarrow epsilon
```

3.6 Suppresion des productions unitaires

La règle FUNCT-ARG (< FUNCT-ARG> \to < ARG-LIST>) est dans ce cas On la remplace donc directement par ARG-LIST.

Seul FUNCT est touché et devient : (<FUNCT> \to funct-def id <FUNCT-ARG> open-brac <INSTRUCT-LIST> close-brac)

3.7 Suppression des ambiguïté

Il reste encore une ambiguïté avec cette grammaire, au niveau de FUNCT-CALL-ARG :

Soit:

```
 < FUNCT-CALL> \qquad \rightarrow funct-name < FUNCT-CALL-ARG> \\ < FUNCT-CALL-ARG> \qquad \rightarrow < FUNCT-CALL-ARG-BEG> < FUNCT-CALL-ARG-END> \\ < FUNCT-CALL-ARG-BEG> \qquad \rightarrow < EXP> \\ \rightarrow epsilon \\ < FUNCT-CALL-ARG-END> \qquad \rightarrow coma < EXP> < FUNCT-CALL-ARG-END> \\ \rightarrow epsilon \\ \vdots \\ < SIMPLE-EXP> \qquad \rightarrow < FUNCT-CALL> \\ \vdots \\ < EXP> \qquad \rightarrow < SIMPLE-EXP> \\ \vdots \\ < EXP> \qquad \vdots
```

On voit qu'on a un problème car les fonction peuvent appeler des fonctions en paramètres.

On peut ainsi se retrouver avec une fonction du type :

Il est alors impossible de savoir si 3 est le deuxième argument de bar ou de foo. On rajoute alors des parenthèses pour lever cette ambiguïté.

voir si on peut faire ça, on si existe un moyen de résoudre ça en modifiant la grammaire

3.8 Grammaire finale

```
<PROGRAM>
                                    \rightarrow <\!\!\text{FUNCT-LIST}\!\!> <\!\!\text{PROG-TAIL}\!\!>
                                    \rightarrow <INSTRUCT-LIST>
               <PROG-TAIL>
                                   \rightarrow <INSTRUCT-LIST>
                                    \rightarrow epsilon
              <FUNCT-LIST>
                                    \rightarrow <FUNCT-LIST-BEG> <FUNCT-LIST-END>
       <FUNCT-LIST-BEG>
                                    \rightarrow <FUNCT>
       <FUNCT-LIST-END>
                                    \rightarrow <FUNCT> <FUNCT-LIST-END>
                                    \rightarrow epsilon
                    <FUNCT>
                                   \rightarrow funct-def id <ARG-LIST> open-brac <INSTRUCT-LIST> close-brac
                 <ARG-LIST>
                                   \rightarrow <ARG-LIST-BEG> <ARG-LIST-END>
           <ARG-LIST-BEG>
                                   \rightarrow variable
                                    \rightarrow epsilon
           <ARG-LIST-END>
                                    \rightarrow coma variable <ARG-LIST-END>
                                    \rightarrow epsilon
         <INSTRUCT-LIST>
                                    \rightarrow <INSTRUCT> semicolon <INSTRUCT-LIST>
                                    \rightarrow epsilon
                                    \rightarrow funct-name open-par <FUNCT-CALL-ARG> close-par
            <FUNCT-CALL>
      <FUNCT-CALL-ARG>
                                   \rightarrow <FUNCT-CALL-ARG-BEG> <FUNCT-CALL-ARG-END>
<FUNCT-CALL-ARG-BEG>
                                   \rightarrow <EXP>
                                    \rightarrow epsilon
<FUNCT-CALL-ARG-END>
                                    \rightarrow coma <EXP> <FUNCT-CALL-ARG-END>
                                    \rightarrow epsilon
                <INSTRUCT>
                                   \rightarrow variable equal \langle EXP \rangle
                                    \rightarrow ret \langleEXP\rangle
                                    \rightarrow <COND>
                                   → open-cond <EXP> open-brac <INSTRUCT-LIST> close-brac <COND-END>
                      <COND>
                                    \rightarrow close-cond open-brac <
INSTRUCT-LIST> close-brac
               <COND-END>
                                    \rightarrow add-cond <EXP> open-brac <INSTRUCT-LIST> close-brac <COND-END>
                                    \rightarrow epsilon
             <SIMPLE-EXP>
                                    \rightarrow <FUNCT-CALL>
                                    \rightarrow variable
                                    \rightarrow \mathrm{int}
                                    \rightarrow string
                                    \rightarrow open-par <EXP> close-par
                        \langle \text{EXP} \rangle
                                   \rightarrow <EXP-2> <EXP-TAIL>
                 <EXP-TAIL>
                                    \rightarrow equiv <EXP-2> <EXP-TAIL>
                                    \rightarrow gt <EXP-2> <EXP-TAIL>
                                    \rightarrow epsilon
                      \langle \text{EXP-2} \rangle
                                   \rightarrow <EXP-3> <EXP-2-TAIL>
               <EXP-2-TAIL>
                                   \rightarrow add \langleEXP-3\rangle \langleEXP-2-TAIL\rangle
                                    \rightarrow minus <EXP-3> <EXP-2-TAIL>
                                    \rightarrow epsilon
                      \langle \text{EXP-3} \rangle
                                    \rightarrow <SIMPLE-EXP> <EXP-3-TAIL>
               <EXP-3-TAIL>
                                    \rightarrow mul <SIMPLE-EXP> <EXP-3-TAIL>
                                    \rightarrow div <SIMPLE-EXP> <EXP-3-TAIL>
                                    \rightarrow epsilon
```

Scanner

reconnait plus de token que ceux supporté par la grammaire. beacuse passé de grammaire complète à grammaire simplifié

Parser

- 5.1 Table de parsing
- 5.2 First and follow

Poubelle

6.1 Grammaire complète : bug

On se base sur la BNF donné par l'assistant et on l'adapte à notre version de perl

 $PROGRAM \rightarrow PROGRAM FUNCT-LIST$

 \rightarrow PROGRAM INSTRUCT

 \rightarrow FUNCT-LIST

 \rightarrow INSTRUCT

 \rightarrow EPSILON

 $\text{FUNCT-LIST} \quad \to \text{FUNCT}$

 \rightarrow FUNCT FUNCT-LIST

 \rightarrow EPSILON

FUNCT \rightarrow FUNCT-DEF ID OPEN-BRAC INSTRUCT RETURN CLOSE-BRAC

ightarrow FUNCT-DEF ID OPEN-PAR CLOSE-PAR OPEN-BRAC INSTRUCT RETURN CLOSE-BRAC

ightarrow FUNCT-DEF ID OPEN-PAR PARAM CLOSE-PAR OPEN-BRAC INSTRUCT RETURN CLOSE-BRAC

 ${\tt FUNCT\text{-}CALL} \quad \to {\tt USER\text{-}FUNCT\text{-}CALL}$

 $\rightarrow \text{PERL-FUNCT-CALL}$

USER-FUNCT-CALL \rightarrow ID OPEN-PAR CLOSE-PAR

 \rightarrow ID OPEN-PAR PARAM CLOSE-PAR

 \rightarrow ID PARAM

 \rightarrow ID

 $\begin{array}{ccc} \text{PERL-FUNCT-CALL} & \rightarrow \text{PERL-DEF EXP} \end{array}$

 \rightarrow PERL-INT EXP

 \rightarrow PERL-LENG EXP

 \rightarrow PERL-SCAL EXP

 \rightarrow PERL-SUBS EXP COMA INT COMA INT

 \rightarrow PERL-SUBS EXP COMA INT

 \rightarrow PERL-PRIN LIST

LIST \rightarrow STRING

 \rightarrow STRING LIST

 \rightarrow EPSILON

 $PARAM \rightarrow VAR$

 \rightarrow VAR PARAM-END

 \rightarrow EPSILON

PARAM-END \rightarrow COMA VAR

 \rightarrow COMA VAR PARAM-END

 \rightarrow EPSILON

RETURN \rightarrow RET EXP SEMICOLON

 \rightarrow RET EXP-COND SEMICOLON

 \rightarrow RET VAR SEMICOLON

 \rightarrow EPSILON

```
INSTRUCT
                         \rightarrow COND SEMICOLON INSTRUCT
                          \rightarrow EXP SEMICOLON INSTRUCT
                          \rightarrow FUNCT-CALL SEMICOLON INSTRUCT
                          \rightarrow ASSIGNATION SEMICOLON INSTRUCT
                          \rightarrow COND SEMICOLON
                          \rightarrow EXP SEMICOLON
                          \rightarrow FUNCT-CALL SEMICOLON
                          \rightarrow ASSIGNATION SEMICOLON
                          \rightarrow EPSILON
     ASSIGNATION \rightarrow VAR EQUAL VALUE
                          \rightarrow VAR EQUAL EXP
               COND → OPEN-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC COND-END

ightarrow NEG-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC COND-END
                          \rightarrow EXP OPEN-COND EXP-COND
                          \rightarrow EXP NEG-COND EXP-COND
         COND-END

ightarrow ADD-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC
                          \rightarrow ADD-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC COND-END
                          \rightarrow CLOSE-COND OPEN-BRAC INSTRUCT CLOSE-BRAC
                          \rightarrow EPSILON
                 EXP
                         \rightarrow VAR
                          \rightarrow EXP OPERATOR EXP
                          \rightarrow EXP-COMP
                          \rightarrow NOT EXP
                          \rightarrow FAC EXP
                          \rightarrow ADD EXP
                          \rightarrow MINUS EXP
         EXP-COMP
                         \rightarrow EXP OPERATOR-COMP EXP
        OPERATOR \rightarrow MUL
                          \rightarrow \text{DIV}
                          \rightarrow MINUS
                          \rightarrow CONC
                          \rightarrow ADD
                          \rightarrow COMA
                          \rightarrow DOT
OPERATOR-COMP
                         \rightarrow LT
                         \rightarrow GT
                          \rightarrow LE
                          \rightarrow GE
                          \rightarrow EQUIV
                          \rightarrow DIF
                          \rightarrow AND-LOGIC
                          \rightarrow \mathrm{OR}
                          \rightarrow LT-S
                          \rightarrow GT-S
                          \rightarrow LE-S
                          \rightarrow GE-S
                          \rightarrow COMA-LOGIC
                          \rightarrow \text{EQ-S}
                          \rightarrow NE-S
              VALUE \rightarrow INT
                          \rightarrow FLOAT
                          \to \mathrm{BOOL}
                                                                    13
                          \rightarrow STRING
                 VAR \rightarrow VALUE
                          \rightarrow VARIABLE
                          \rightarrow MINUS VAR
                          \rightarrow ADD VAR
```

 \rightarrow OPEN-PAR EXP CLOSE-PAR

6.2 Gestion des priorités

On doit adapter la grammaire pour respecter les priorité et les associativité gauche/droite.

Cela ne modifie que les règles EXP, EXP-COND, OPERATOR et OPERATOR-COND qui deviennent :

```
\langle EXP \rangle
             \rightarrow <EXP> LT <EXP2>
             \rightarrow <EXP> LT-S <EXP2>
             \rightarrow <EXP> GT <EXP2>
             \rightarrow <EXP> GT-S <EXP2>
             \rightarrow <EXP> LE <EXP2>
             \rightarrow <EXP> LE-S <EXP2>
             \rightarrow <EXP> GE <EXP2>
             \rightarrow <EXP> GE-S <EXP2>
             \rightarrow <EXP> EQUIV <EXP2>
             \rightarrow <EXP> EQ-S <EXP2>
             \rightarrow <EXP> NE-S <EXP2>
             \rightarrow <EXP> DIF <EXP2>
             \rightarrow <EXP> DOT <EXP2>
             \rightarrow <EXP> COMA <EXP2>
             \rightarrow <EXP2> EQUAL <EXP>
             \rightarrow NOT <EXP>
             \rightarrow FAC <EXP>
             \rightarrow <EXP2>
\langle \text{EXP2} \rangle
            \rightarrow <EXP> ADD <EXP3>
             \rightarrow <EXP> MINUS <EXP3>
             \rightarrow <EXP> OR <EXP3>
             \rightarrow <EXP3>
<EXP3>
             \rightarrow <EXP> MUL <VAR>
             \rightarrow <EXP> DIV <VAR>
             \rightarrow <EXP> AND <VAR>
             \rightarrow <VAR>
```

6.3 Suppression des symboles inutiles

On doit virer non-productifs et inaccessibles. Ici ok, rien à faire

6.4 left-factoring

On vire ce qui commence pareillement

On obtient la gram suivante :

 $PROGRAM \rightarrow PROGRAM PROG-END$

 $\begin{array}{l} \rightarrow \text{FUNCT-LIST} \\ \rightarrow \text{INSTRUCT} \end{array}$

 \rightarrow EPSILON

 $\begin{array}{ccc} \mathsf{PROG\text{-}END} & \to \mathsf{FUNCT\text{-}LIST} \end{array}$

 $\to {\rm INSTRUCT}$

 $\texttt{FUNCT-LIST} \quad \to \texttt{FUNCT} \ \texttt{FUNCT-LIST-END}$

 $\rightarrow \text{EPSILON}$

 ${\tt FUNCT\text{-}LIST\text{-}END} \quad \to {\tt FUNCT\text{-}LIST}$

 \rightarrow EPSILON

FUNCT \rightarrow FUNCT-DEF ID FUNCT-END

FUNCT-END \rightarrow OPEN-BRAC INSTRUCT RETURN CLOSE-BRAC

 \rightarrow OPEN-PAR FUNCT-END2

FUNCT-END2 \rightarrow CLOSE-PAR OPEN-BRAC INSTRUCT RETURN CLOSE-BRAC

 \rightarrow PARAM CLOSE-PAR OPEN-BRAC INSTRUCT RETURN CLOSE-BRAC

 $FUNCT-CALL \rightarrow USER-FUNCT-CALL$

 \rightarrow PERL-FUNCT-CALL

USER-FUNCT-CALL \rightarrow ID USER-FUNCT-CALL-END

USER-FUNCT-CALL-END \rightarrow OPEN-PAR USER-FUNCT-CALL-END2

 \rightarrow PARAM

 \rightarrow EPSILON

 $\text{USER-FUNCT-CALL-END2} \quad \to \text{CLOSE-PAR}$

 \rightarrow PARAM CLOSE-PAR

 $\begin{array}{ccc} \text{PERL-FUNCT-CALL} & \rightarrow \text{PERL-DEF EXP} \end{array}$

 \rightarrow PERL-INT EXP

 \rightarrow PERL-LENG EXP

 \rightarrow PERL-SCAL EXP

 \rightarrow PERL-SUBS PERL-SUBS-END

 \rightarrow PERL-PRIN LIST

PERL-SUBS-END \rightarrow EXP COMA INT COMA INT

 \rightarrow EXP COMA INT

LIST \rightarrow STRING LIST-END

 $\text{LIST-END} \quad \to \text{LIST}$

 \rightarrow EPSILON

 $PARAM \rightarrow PARAM2$

 \rightarrow EPSILON

 ${\rm PARAM2} \quad \to {\rm PARAM\text{-}END}$

 $\rightarrow \text{EPSILON}$

 ${\tt PARAM\text{-}END} \quad \to {\tt COMA} \ {\tt VAR} \ {\tt PARAM\text{-}END2}$

 \rightarrow EPSILON

 $PARAM\text{-}END2 \longrightarrow PARAM\text{-}END$

 $\rightarrow \text{EPSILON}$

RETURN \rightarrow RET RETURN-END

 $\rightarrow \text{EPSILON}$

RETURN-END \rightarrow EXP SEMICOLON

 \rightarrow EXP-COND SEMICOLON

 \rightarrow VAR SEMICOLON

 \rightarrow ADD VAR

 \rightarrow OPEN-PAR EXP CLOSE-PAR

INSTRUCT \rightarrow COND INSTRUCT-END \rightarrow EXP INSTRUCT-END \rightarrow FUNCT-CALL INSTRUCT-END \rightarrow ASSIGNATION INSTRUCT-END \rightarrow EPSILON ${\tt INSTRUCT\text{-}END} \quad \to {\tt SEMICOLON} \ {\tt INSTRUCT\text{-}END2}$ INSTRUCT-END2 \rightarrow INSTRUCT $\rightarrow \text{EPSILON}$ ASSIGNATION \rightarrow VAR EQUAL ASSIGNATION-END ASSIGNATION-END \rightarrow VALUE $\rightarrow \text{EXP}$ COND → OPEN-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC COND-END ightarrow NEG-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC COND-END \rightarrow EXP COND-END2 COND-END2 \rightarrow OPEN-COND EXP-COND \rightarrow NEG-COND EXP-COND ightarrow ADD-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC COND-END3 COND-END ightarrow CLOSE-COND OPEN-BRAC INSTRUCT CLOSE-BRAC \rightarrow EPSILON COND-END3 \rightarrow COND-END \rightarrow EPSILON $\langle EXP \rangle$ \rightarrow <EXP> <EXP-END> \rightarrow <EXP2> EQUAL <EXP> \rightarrow NOT <EXP> \rightarrow FAC <EXP> \rightarrow <EXP2> <EXP-END> \rightarrow LT <EXP2> \rightarrow LT-S <EXP2> \rightarrow GT <EXP2> \rightarrow GT-S <EXP2> \rightarrow LE <EXP2> \rightarrow LE-S <EXP2> \rightarrow GE < EXP2> \rightarrow GE-S <EXP2> \rightarrow EQUIV <EXP2> \rightarrow EQ-S <EXP2> \rightarrow NE-S <EXP2> \rightarrow DIF \langle EXP2 \rangle \rightarrow DOT <EXP2> \rightarrow COMA <EXP2> $\langle \text{EXP2} \rangle$ \rightarrow <EXP> <EXP2-END> \rightarrow <EXP3> $\langle \text{EXP2-END} \rangle \rightarrow \text{ADD} \langle \text{EXP3} \rangle$ \rightarrow MINUS <EXP3> \rightarrow OR <EXP3> $\langle EXP3 \rangle$ \rightarrow <EXP> <EXP3-END> \rightarrow <VAR> <EXP3-END> \rightarrow MUL <VAR> \rightarrow DIV <VAR> \rightarrow AND <VAR> $\text{VALUE} \quad \to \text{INT}$ $\rightarrow {\rm FLOAT}$ 16 \rightarrow BOOL \rightarrow STRING $VAR \rightarrow VALUE$ $\rightarrow \text{VARIABLE}$ \rightarrow MINUS VAR

6.5 récursion gauche

On doit juste changer les règles PROGRAM et EXP qui deviennent:

 ${\tt PROGRAM} \quad \to {\tt PROG \ PROG-TAIL}$

 $\begin{array}{cc} \text{PROG} & \rightarrow \text{FUNCT-LIST} \end{array}$

 $\rightarrow \text{INSTRUCT}$

 \rightarrow EPSILON

 $\begin{array}{ccc} \mathsf{PROG\text{-}TAIL} & \to \mathsf{PROG\text{-}END} \ \mathsf{PROG\text{-}TAIL} \end{array}$

 \rightarrow EPSILON

 $\langle \text{EXP} \rangle \rightarrow \langle \text{EXP-TAIL} \rangle$

 ${\rm E} \quad \rightarrow <\!\!{\rm EXP2}\!\!> {\rm EQUAL} <\!\!{\rm EXP}\!\!>$

 \rightarrow NOT < EXP>

 \rightarrow FAC < EXP>

 $\rightarrow <\!\!\text{EXP2}\!\!>$

 $\texttt{EXP-TAIL} \quad \to \texttt{EXP-END} \ \texttt{EXP-TAIL}$

 $\rightarrow \text{EPSILON}$

6.6 Grammaire finale

 $PROGRAM \quad \to PROG \ PROG\text{-}TAIL$

 $\mbox{PROG} \quad \rightarrow \mbox{FUNCT-LIST}$

 $\begin{array}{l} \rightarrow \text{INSTRUCT} \\ \rightarrow \text{EPSILON} \end{array}$

 $PROG-TAIL \rightarrow PROG-END PROG-TAIL$

 \rightarrow EPSILON

PROG-END \rightarrow FUNCT-LIST

 $\rightarrow \text{INSTRUCT}$

FUNCT-LIST \rightarrow FUNCT FUNCT-LIST-END

 $\rightarrow \text{EPSILON}$

 ${\tt FUNCT\text{-}LIST\text{-}END} \quad \to {\tt FUNCT\text{-}LIST}$

 \rightarrow EPSILON

FUNCT \rightarrow FUNCT-DEF ID FUNCT-END

FUNCT-END \rightarrow OPEN-BRAC INSTRUCT RETURN CLOSE-BRAC

 \rightarrow OPEN-PAR FUNCT-END2

FUNCT-END2 \rightarrow CLOSE-PAR OPEN-BRAC INSTRUCT RETURN CLOSE-BRAC

 \rightarrow PARAM CLOSE-PAR OPEN-BRAC INSTRUCT RETURN CLOSE-BRAC

 ${\tt FUNCT\text{-}CALL} \quad \to {\tt USER\text{-}FUNCT\text{-}CALL}$

 $\rightarrow \text{PERL-FUNCT-CALL}$

USER-FUNCT-CALL \rightarrow ID USER-FUNCT-CALL-END

USER-FUNCT-CALL-END \rightarrow OPEN-PAR USER-FUNCT-CALL-END2

 $\rightarrow \mathrm{PARAM}$

 \rightarrow EPSILON

USER-FUNCT-CALL-END2 \rightarrow CLOSE-PAR

 \rightarrow PARAM CLOSE-PAR

 $\begin{array}{ccc} \text{PERL-FUNCT-CALL} & \rightarrow \text{PERL-DEF EXP} \end{array}$

 $\begin{array}{l} \rightarrow \text{ PERL-INT EXP} \\ \rightarrow \text{ PERL-LENG EXP} \\ \rightarrow \text{ PERL-SCAL EXP} \end{array}$

 \rightarrow PERL-SUBS PERL-SUBS-END

 \rightarrow PERL-PRIN LIST

PERL-SUBS-END \rightarrow EXP COMA INT COMA INT

 \rightarrow EXP COMA INT

LIST \rightarrow STRING LIST-END

 $\text{LIST-END} \quad \to \text{LIST}$

 $\rightarrow \text{EPSILON}$

 $PARAM \rightarrow PARAM2$

 \rightarrow EPSILON

 $PARAM2 \rightarrow PARAM-END$

 \rightarrow EPSILON

PARAM-END \rightarrow COMA VAR PARAM-END2

 $\rightarrow \text{EPSILON}$

 $PARAM-END2 \rightarrow PARAM-END$

 $\rightarrow \text{EPSILON}$

RETURN \rightarrow RET RETURN-END

 \rightarrow EPSILON

RETURN-END \rightarrow EXP SEMICOLON

 \rightarrow EXP-COND SEMICOLON

 \rightarrow VAR SEMICOLON

 \rightarrow ADD VAR

 \rightarrow OPEN-PAR EXP CLOSE-PAR

```
INSTRUCT \rightarrow COND INSTRUCT-END
                            \rightarrow EXP INSTRUCT-END
                            \rightarrow FUNCT-CALL INSTRUCT-END
                            \rightarrow ASSIGNATION INSTRUCT-END
                            \rightarrow EPSILON
    {\tt INSTRUCT\text{-}END} \quad \to {\tt SEMICOLON} \ {\tt INSTRUCT\text{-}END2}
   INSTRUCT-END2 \rightarrow INSTRUCT
                            \rightarrow EPSILON
      ASSIGNATION \rightarrow VAR EQUAL ASSIGNATION-END
ASSIGNATION-END \rightarrow VALUE
                            \rightarrow \text{EXP}
                 COND
                          → OPEN-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC COND-END

ightarrow NEG-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC COND-END
                            \rightarrow EXP COND-END2
         COND-END2
                            \rightarrow OPEN-COND EXP-COND
                            \rightarrow NEG-COND EXP-COND

ightarrow ADD-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC COND-END3
          COND-END

ightarrow CLOSE-COND OPEN-BRAC INSTRUCT CLOSE-BRAC
                            \rightarrow EPSILON
         COND-END3 \rightarrow COND-END
                            \rightarrow EPSILON
               \langle EXP \rangle
                            \rightarrow <E> <EXP-TAIL>
                       E \rightarrow \langle EXP2 \rangle EQUAL \langle EXP \rangle
                            \rightarrow NOT <EXP>
                            \rightarrow FAC <EXP>
                            \rightarrow <EXP2>
            EXP-TAIL \rightarrow EXP-END EXP-TAIL
                            \rightarrow EPSILON
         \langle \text{EXP-END} \rangle \rightarrow \text{LT} \langle \text{EXP2} \rangle
                            \rightarrow LT-S <EXP2>
                            \rightarrow GT <EXP2>
                            \rightarrow GT-S <EXP2>
                            \rightarrow LE <EXP2>
                            \rightarrow LE-S <EXP2>
                            \rightarrow GE <EXP2>
                            \rightarrow GE-S <
EXP2>
                            \rightarrow EQUIV <EXP2>
                            \rightarrow EQ-S <EXP2>
                            \rightarrow NE-S <EXP2>
                            \rightarrow DIF <EXP2>
                            \rightarrow DOT <EXP2>
                            \rightarrow COMA <EXP2>
              \langle \text{EXP2} \rangle \rightarrow \langle \text{EXP} \rangle \langle \text{EXP2-END} \rangle
                            \rightarrow <EXP3>
       <EXP2-END>
                            \rightarrow ADD <EXP3>
                            \rightarrow MINUS <EXP3>
                            \rightarrow OR <EXP3>
              \langle EXP3 \rangle
                           \rightarrow <EXP> <EXP3-END>
                            \rightarrow < VAR >
       <EXP3-END>
                            \rightarrow MUL <VAR>
                            \rightarrow DIV <VAR>
                            \rightarrow AND <VAR>
                                                                20
                VALUE
                          \rightarrow INT
                            \rightarrow FLOAT
                            \rightarrow BOOL
                            \rightarrow STRING
                   VAR \rightarrow VALUE
                            \rightarrow VARIABLE
                            \rightarrow MINUS VAR
```

EXPRESSION (?)	VARIABLE OPERATOR VARIABLE
	EXPRESSION OPERATOR VARIABLE
XPRESSION-COND (?)	VARIABLE OPERATOR-COMP VARIABLE
()	EXPRESSION OPERATOR-COMP VARIABLE
ASSIGNATION	VARIABLE EQUAL VALUE
CONDITION (?)	((OPEN-COND+NEG-COND)EXPRESSION-COND OPEN-BRAC INSTRUCTIONS* CLOSE-BRAC
	(ADD-COND EXPRESSION-COND OPEN-BRAC INSTRUCTIONS* CLOSE-BRAC)*
	(CLOSE-COND EXPRESSION-COND OPEN-BRAC INSTRUCTIONS* CLOSE-BRAC))
	+ EXPRESSION (OPEN-COND + NEG-COND) EXPRESSION-COND
INSTRUCTIONS	((CONDITION SEMICOLON)* + (EXPRESSION SEMICOLON)* + (FUNCTION-CALL
	$SEMICOLON)^* + (ASSIGNATION SEMICOLON)^*)^*$
PARAM	DOLLAR VARIABLE (COMA DOLLAR VARIABLE)*
USER-FUNCT-CALL	AND FUNCTION-NAME (OPEN-PAR CLOSE-PAR + OPEN-PAR PARAM CLOSE-PAR
	+ PARAM) SEMICOLON
PERL-FUNCT-CALL	${\it defined EXPRESSION + int EXPRESSION + length EXPRESSION}$
	scalar EXPRESSION + substr EXPRESSION COMA INT COMA INT
	scalar EXPRESSION + substr EXPRESSION COMA INT
	+ print (?liste de string)
FUNCTION-CALL	USER-FUNCT-CALL + PERL-FUNCT-CALL
FUNCTION	FUNCTION-ID FUNCTION-NAME (OPEN-PAR CLOSE PAR + OPEN-PAR PARAM CLOSE-PAR)
	OPEN-BRAC INSTRUCTIONS (RETURN EXPRESSION + RETURN EXPRESSION-COND
	+ RETURN VARIABLE) SEMICOLON CLOSE-BRAC
FUNCTION-LIST	FUNCTION*
PROGRAM	(FUNCTION-LIST + INSTRUCTIONS)*

Grammaire après gestion des priorité et associativité :

 $PROGRAM \rightarrow PROGRAM FUNCT-LIST$

 \rightarrow PROGRAM INSTRUCT

 $\rightarrow \text{FUNCT-LIST}$

 $\to {\rm INSTRUCT}$

 \rightarrow EPSILON

 $\text{FUNCT-LIST} \quad \to \text{FUNCT}$

 \rightarrow FUNCT FUNCT-LIST

 \rightarrow EPSILON

FUNCT \rightarrow FUNCT-ID FUNCT-NAME OPEN-BRAC INSTRUCT RETURN CLOSE-BRAC

 \rightarrow FUNCT-ID FUNCT-NAME OPEN-PAR CLOSE PAR OPEN-BRAC INSTRUCT RETURN CLOSE-BRA

ightarrow FUNCT-ID FUNCT-NAME OPEN-PAR PARAM CLOSE-PAR OPEN-BRAC INSTRUCT RETURN CL

 ${\tt FUNCT\text{-}CALL} \quad \to {\tt USER\text{-}FUNCT\text{-}CALL}$

 \rightarrow PERL-FUNCT-CALL

USER-FUNCT-CALL \rightarrow FUNCT-NAME OPEN-PAR CLOSE-PAR

 \rightarrow FUNCT-NAME OPEN-PAR PARAM CLOSE-PAR

 \rightarrow FUNCT-NAME PARAM

 $\rightarrow \text{FUNCT-NAME}$

 $\begin{array}{ccc} \text{PERL-FUNCT-CALL} & \rightarrow \text{PERL-DEF EXP} \end{array}$

 \rightarrow PERL-INT EXP

 \rightarrow PERL-LENG EXP

 \rightarrow PERL-SCAL EXP

 \rightarrow PERL-SUBS EXP COMA INT COMA INT

 \rightarrow PERL-SUBS EXP COMA INT

 \rightarrow PERL-PRIN LIST

 $\operatorname{LIST} \quad \to \operatorname{STRING}$

 \rightarrow STRING LIST

 $\rightarrow \text{EPSILON}$

 $PARAM \rightarrow VAR$

 \rightarrow VAR PARAM-END

 \rightarrow EPSILON

 ${\tt PARAM\text{-}END} \quad \to {\tt COMA~VAR}$

 \rightarrow COMA VAR PARAM-END

 \rightarrow EPSILON

RETURN \rightarrow RET EXP SEMICOLON

 \rightarrow RET EXP-COND SEMICOLON

 \rightarrow RET VAR SEMICOLON

 $\rightarrow \text{EPSILON}$

 \rightarrow OPEN-PAR EXP CLOSE-PAR

```
INSTRUCT \rightarrow COND SEMICOLON INSTRUCT
                   \rightarrow EXP SEMICOLON INSTRUCT
                   \rightarrow FUNCT-CALL SEMICOLON INSTRUCT
                   → ASSIGNATION SEMICOLON INSTRUCT
                   \rightarrow COND SEMICOLON
                   \rightarrow EXP SEMICOLON
                   \rightarrow FUNCT-CALL SEMICOLON
                   \rightarrow ASSIGNATION SEMICOLON
                   \rightarrow EPSILON
ASSIGNATION
                  \rightarrow VAR EQUAL VALUE
                   \rightarrow VAR EQUAL EXP
         COND
                   → OPEN-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC COND-END

ightarrow NEG-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC COND-END
                   \rightarrow EXP OPEN-COND EXP-COND
                   \rightarrow EXP NEG-COND EXP-COND
   COND-END

ightarrow ADD-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC
                   \rightarrow ADD-COND EXP-COND OPEN-BRAC INSTRUCT CLOSE-BRAC COND-END
                   \rightarrow CLOSE-COND OPEN-BRAC INSTRUCT CLOSE-BRAC
                   \rightarrow EPSILON
        <EXP>
                   \rightarrow <EXP> LT <EXP2>
                   \rightarrow <EXP> LT-S <EXP2>
                   \rightarrow <EXP> GT <EXP2>
                    \rightarrow <EXP> GT-S <EXP2>
                   \rightarrow <EXP> LE <EXP2>
                   \rightarrow <EXP> LE-S <EXP2>
                   \rightarrow <EXP> GE <EXP2>
                   \rightarrow <EXP> GE-S <EXP2>
                   \rightarrow <EXP> EQUIV <EXP2>
                   \rightarrow <EXP> DIF <EXP2>
                   \rightarrow <\!\! \mathrm{EXP2}\!\! > \mathrm{EQUAL} <\!\! \mathrm{EXP}\!\! >
                   \rightarrow NOT <EXP>
                   \rightarrow FAC <EXP>
                   \rightarrow <EXP2>
       \langle \text{EXP2} \rangle
                   \rightarrow <EXP> ADD <EXP3>
                   \rightarrow <EXP> MINUS <EXP3>
                   \rightarrow <EXP> OR <EXP3>
                   \rightarrow <EXP3>
                   \rightarrow <EXP> MUL <VAR>
       \langle EXP3 \rangle
                   \rightarrow <EXP> DIV <VAR>
                   \rightarrow <\!\! \mathrm{EXP}\!\! > \mathrm{AND} <\!\! \mathrm{VAR}\!\! >
                   \rightarrow <VAR>
        VALUE \rightarrow INT
                   \rightarrow FLOAT
                   \rightarrow BOOL
                   \rightarrow STRING
            VAR \rightarrow VALUE
                   \rightarrow MINUS VAR
                   \rightarrow ADD VAR
```