Introduction to Statistics Hypothesis Testing

Hypothesis Testing

What is Hypothesis?

An idea or explanation of something that is based on a few known facts but that has not yet been proved to be true or correct.

-- Oxford Dictionary

What is Hypothesis?

Testing a known assumption that is generally accepted as the truth.

Testing a claim that is supposed to change the current facts.

Null Vs Alternate Hypothesis

 H_{o}

 H_a

- There is no change from the stated facts.
- Chocolate bars weigh 100 gms or more

 \leq

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- The stated facts are incorrect
- Chocolate bars weigh less than 100 gms







Statistical Significance

Statistical Significance

 H_{o}

We expect this to happen.

It happened.

 H_{a}

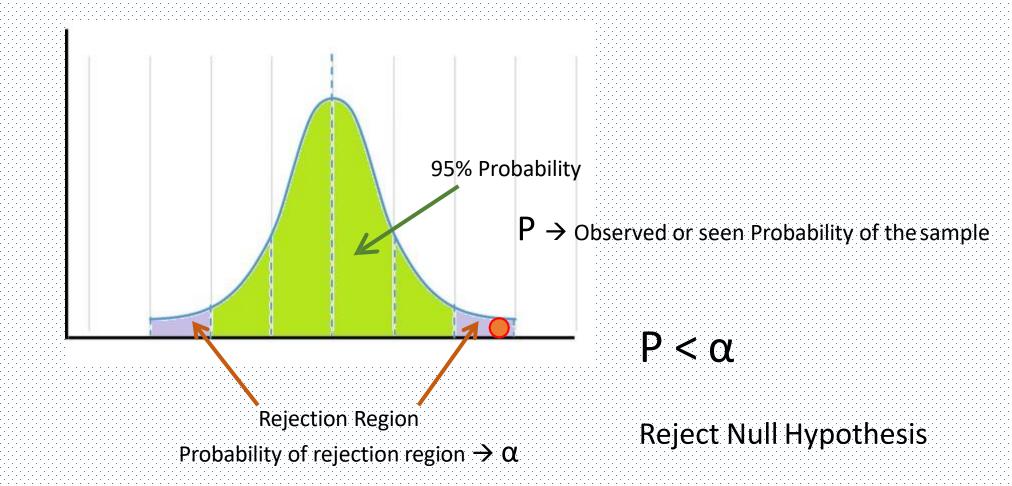
We don't expect this.

Still it happened.

Nothing changes.
Null Hypothesis is true.
Status quo remains.

Null Hypothesis rejected.
Status quo or claim is rejected

Important terms - Statistical Significance



Hypothesis Testing

Current average waiting period for the customers who call the customer service helpline is 100 seconds with a standard deviation of 20 seconds. Certain changes were recently done to the IVR menu options as well as the overall customer service processes. After a week, the management picked-up a sample of 100 calls and found that the average waiting period was 95 seconds. Have the process implementations resulted in the waiting period reduction?

 $\mathbf{H}_{\mathbf{O}}$: null hypothesis: There is no change in the waiting period.

 $\mathbf{H}_{\mathbf{a}}$: alternate hypothesis: The waiting period has reduced.

Significance Level; $\alpha = 0.05$ or 5%

1. State Population parameters and Sample statistics

$$\mu = 100; \quad \sigma = 20; \quad N = 100; \quad \overline{X} = 95;$$

2. Compute Sample Standard Deviation and Z-Value

$$\sigma_{\overline{x}} = \frac{\sigma}{\sqrt{n}}$$
 $z = \frac{\overline{x} - \mu}{\sigma_{\overline{x}}}$

3. Compute ρ using Z-Score for the Z-value

$$\rho = 0.62\%$$

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Reject Null

Population parameters and Sample statistics

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3. Compute ρ using Z-Score for the Z-value

$$\rho = 0.62\%$$

Thank You!