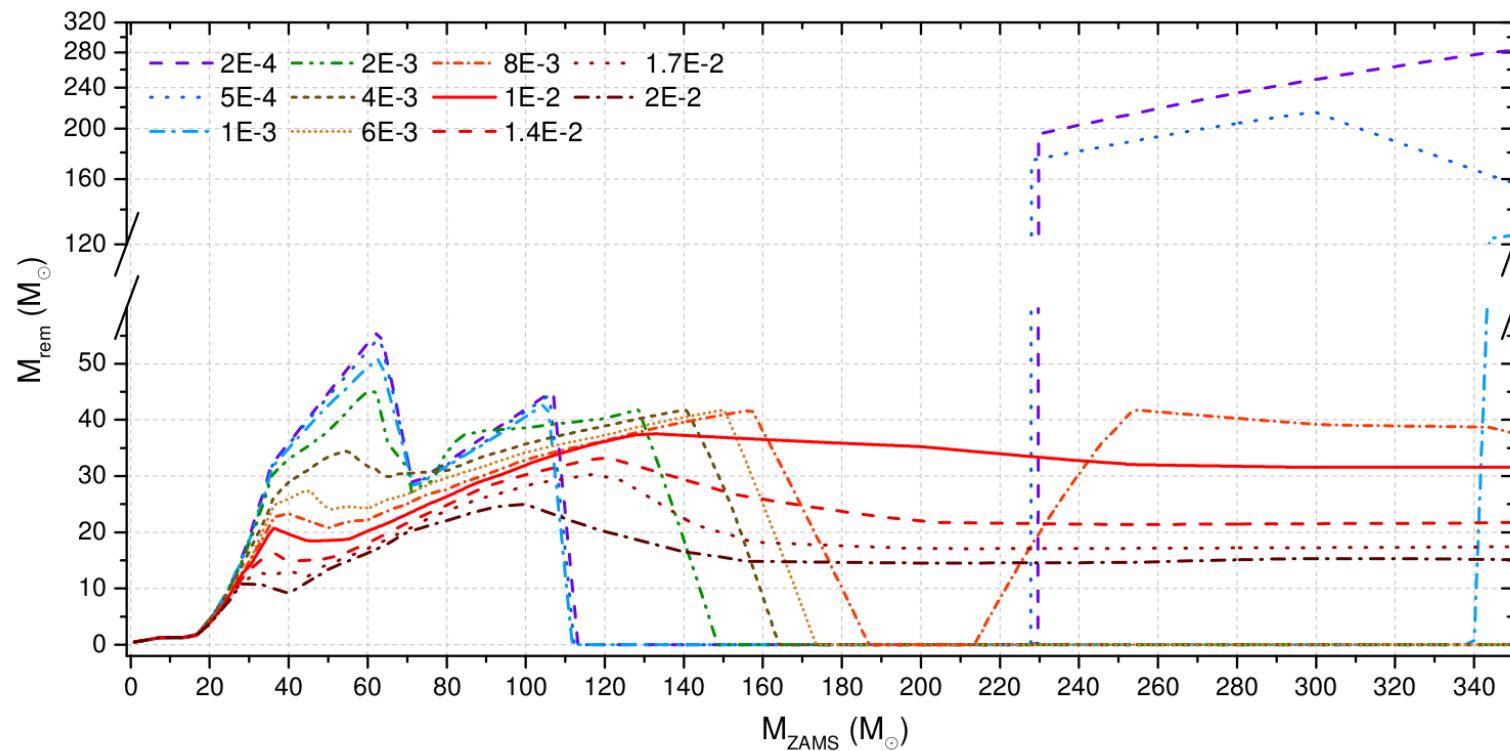
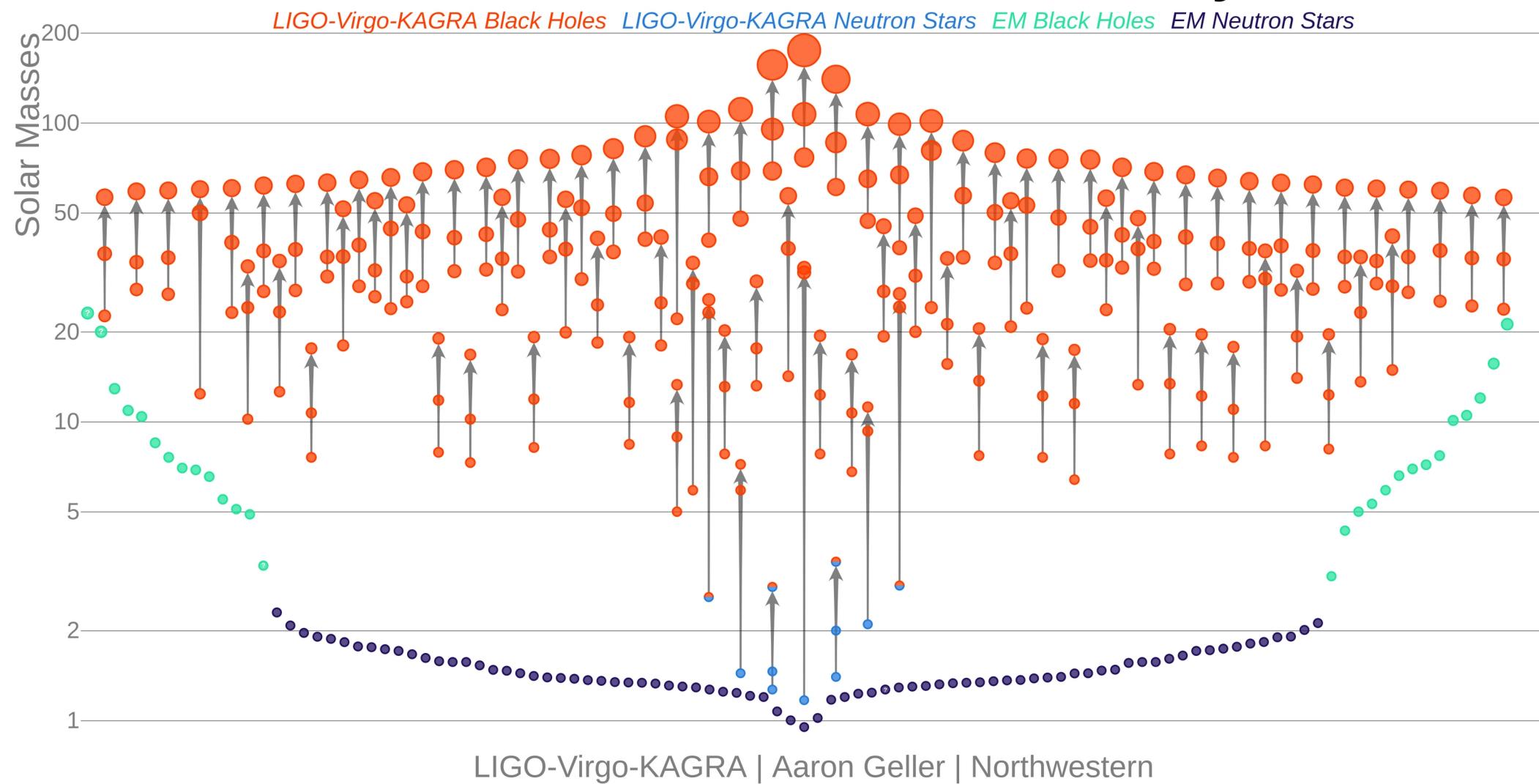


The formation of compact objects from single star evolution

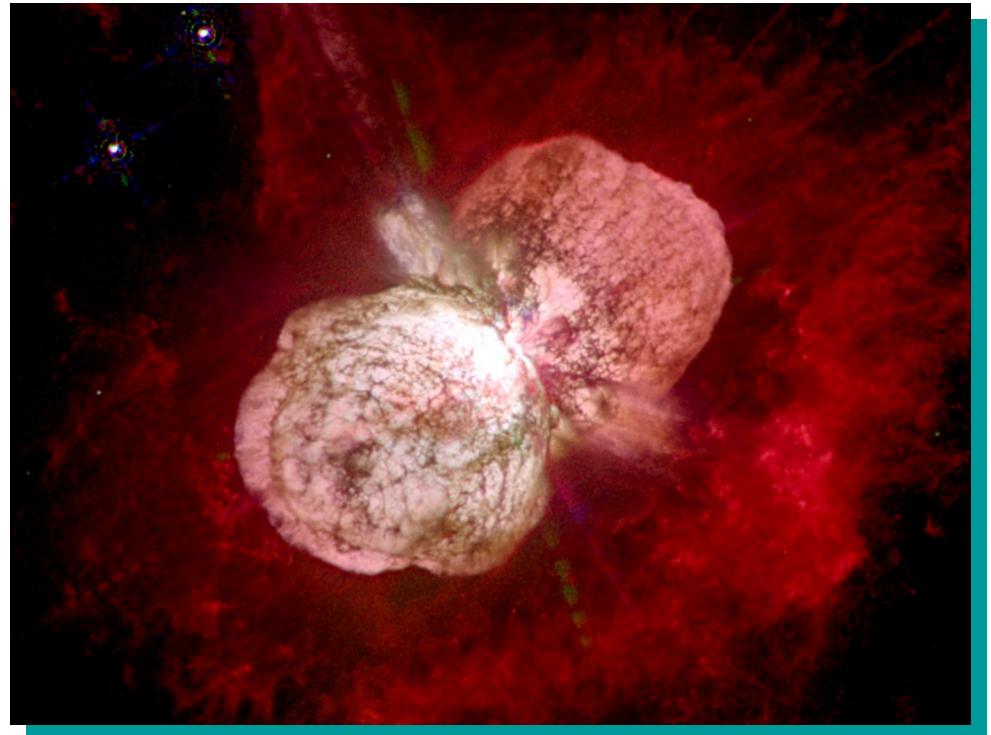
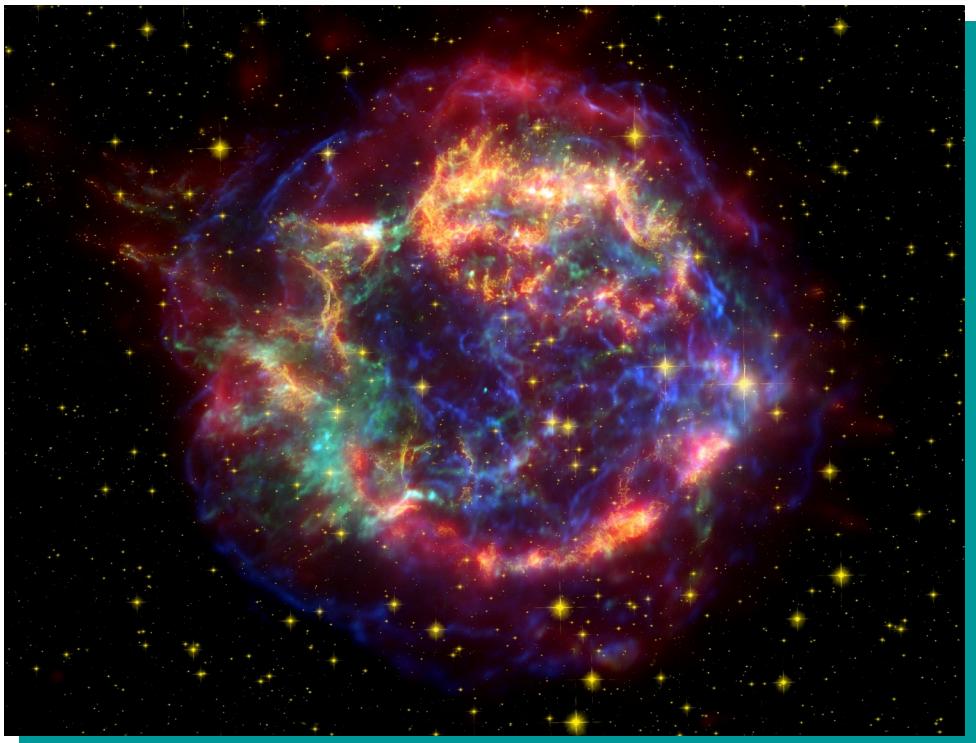


Masses in the Stellar Graveyard



Two critical ingredients:

- 1) PROGENITOR STAR
EVOLUTION
(STELLAR WINDS)
- 2) SUPERNOVA (SN)
EXPLOSION



*Winds ejected by Eta Carinae
(HST, credits: NASA)*

*Chandra + HST + Spitzer
Image of the SN remnant
Cassiopeia A*

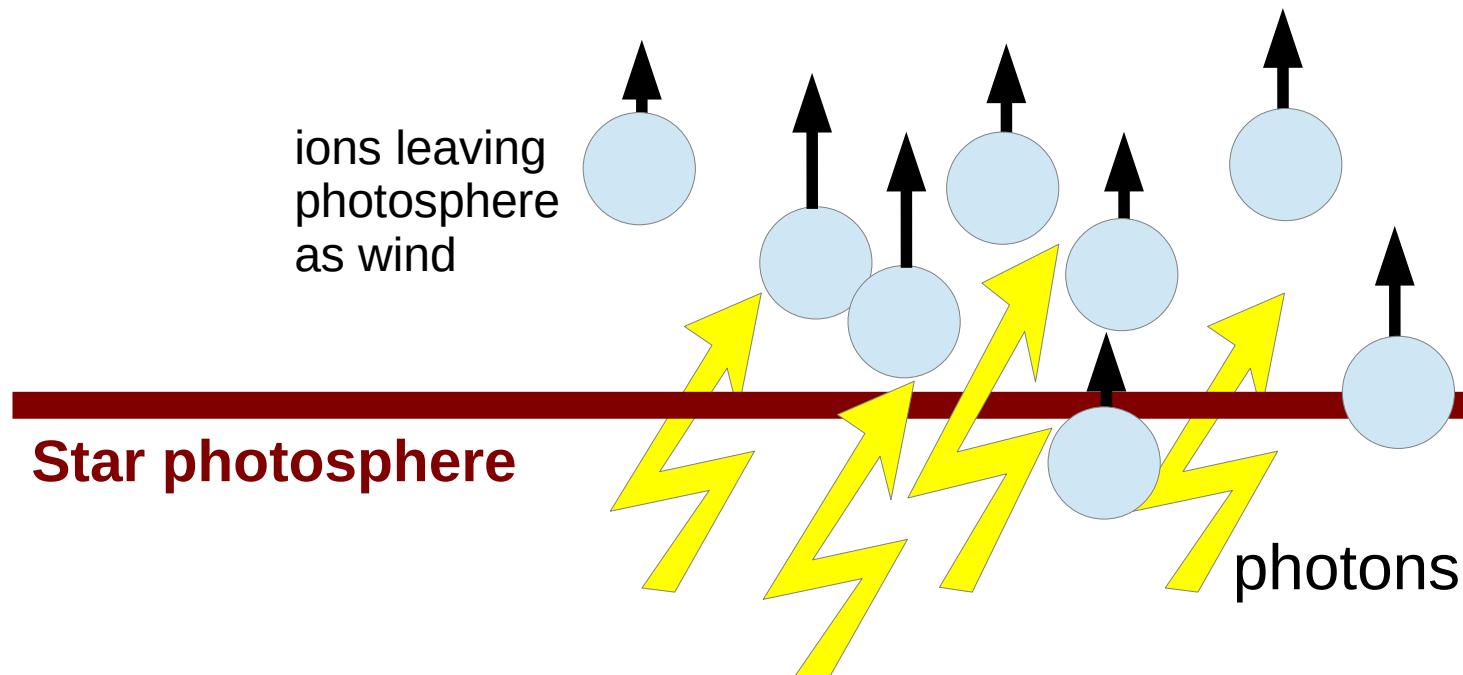
Stellar winds

Massive stars ($>30 M_{\odot}$) might lose $>50\%$ mass by winds
(Vink+ 2001, 2005, 2011; see Vink+ 2016 for a short review)

Photons in atmosphere of a star couple with ions
→ **transfer linear momentum to the ions and unbind them**

Coupling through resonant METAL LINES (especially Fe lines)
→ **MASS LOSS DEPENDS ON METALLICITY**

If star radiation pressure dominated, coupling through electron scattering
→ **MASS LOSS DEPENDS ON LUMINOSITY**



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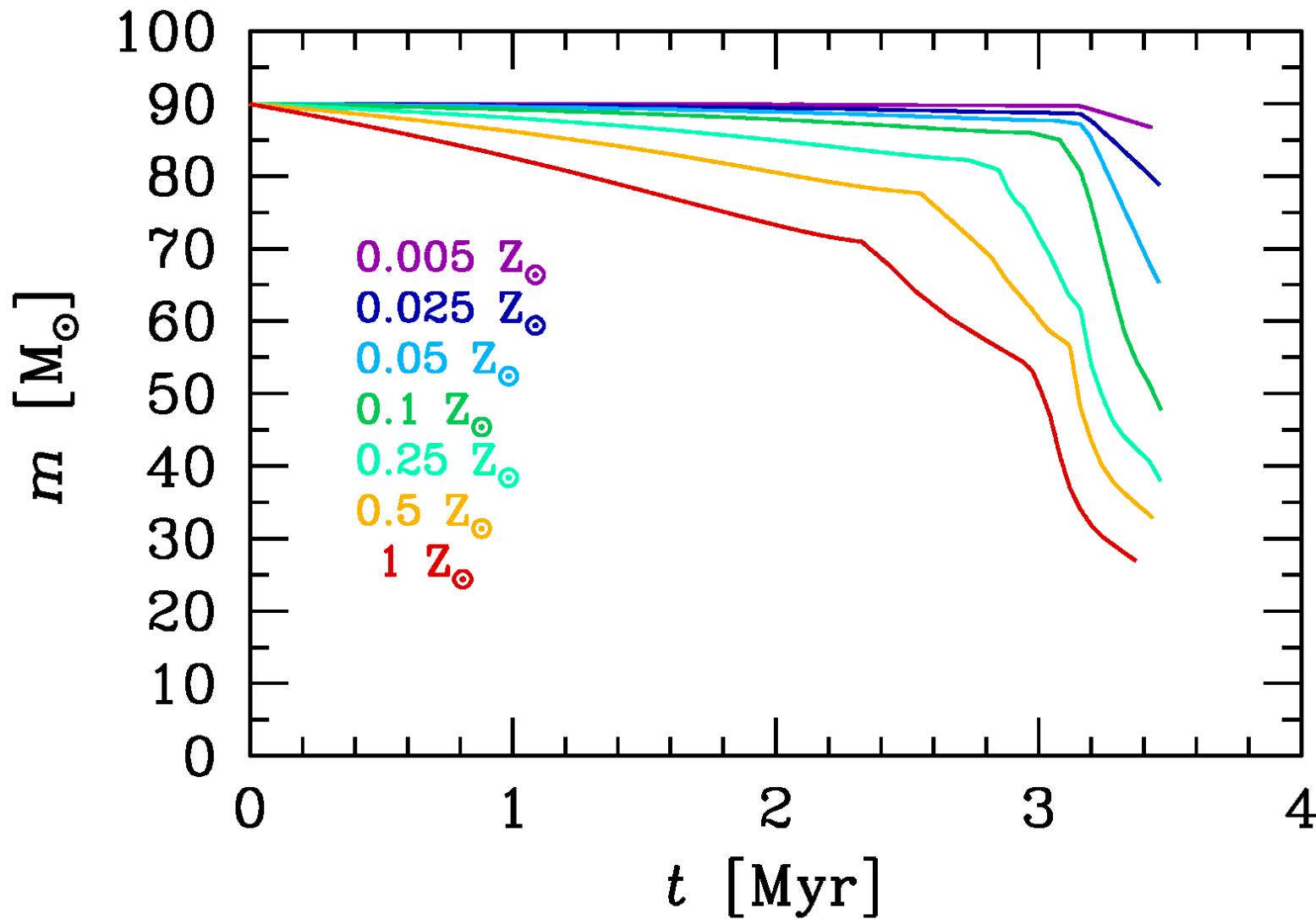
If star radiation pressure dominated, coupling through electron scattering
 → **MASS LOSS DEPENDS ON LUMINOSITY**

$$\dot{M} \propto Z^{\alpha} \quad \alpha \sim 0.5 - 0.9$$

$$\left\{ \begin{array}{l} \alpha = 0.85 \quad [\text{if } \Gamma < 2/3] \\ \alpha = 2.45 - 2.4 \Gamma \quad [\text{if } \Gamma > 2/3] \end{array} \right.$$

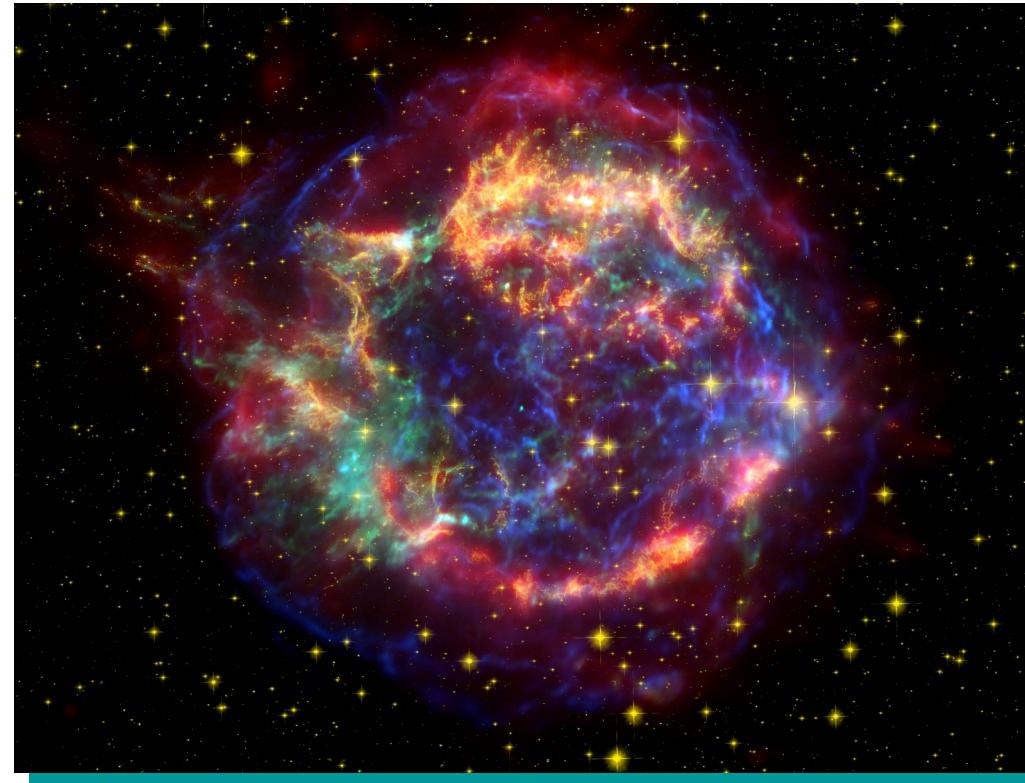
$$\Gamma = \frac{L_*}{L_{\text{Edd}}}$$

Stellar winds



Core-collapse supernovae

Final mass of a star is very important,
because it affects the outcome of a
core-collapse (CC) SUPERNOVA



When Fe core forms in a massive ($> 8 \text{ Msun}$) star

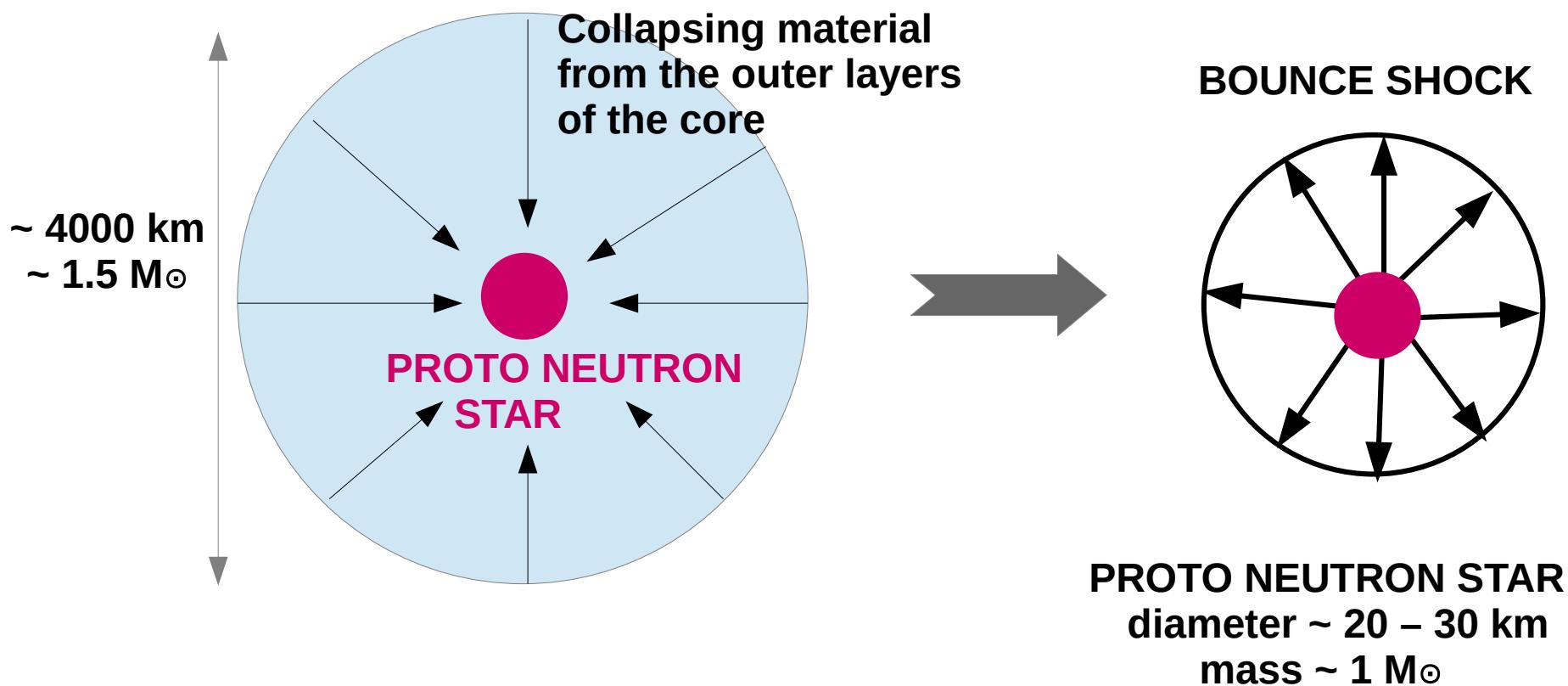
- 1) Fe-group atoms (Ni-62, Fe-58, Fe-56) have maximum binding energy: no more energy released by fusion
→ stellar core starts collapsing because pressure drops
- 2) electron degeneracy pressure tries to stop collapse but if core mass > Chandrasekhar mass ($\sim 1.4 \text{ Msun}$)
electron + proton capture removes electrons
→ electron pressure decreases



- COLLAPSE to NUCLEAR DENSITY ($\sim 10^{17} \text{ kg m}^{-3}$), where neutron degeneracy pressure stops collapse
- PROTO-NEUTRON STAR (PNS) FORMS

Collapse of the core to nuclear density produces **BOUNCE SHOCK**

Fraction of binding energy of core ($E_{b,c} \sim 10^{53}$ erg) is converted into thermal energy (mostly of neutrinos)



Collapse of the core to nuclear density produces **BOUNCE SHOCK**

Fraction of binding energy of core ($E_{b,c} \sim 10^{53}$ erg) is converted into thermal energy (mostly of neutrinos)

SHOCK MUST REVERSE COLLAPSE OF OUTER LAYERS

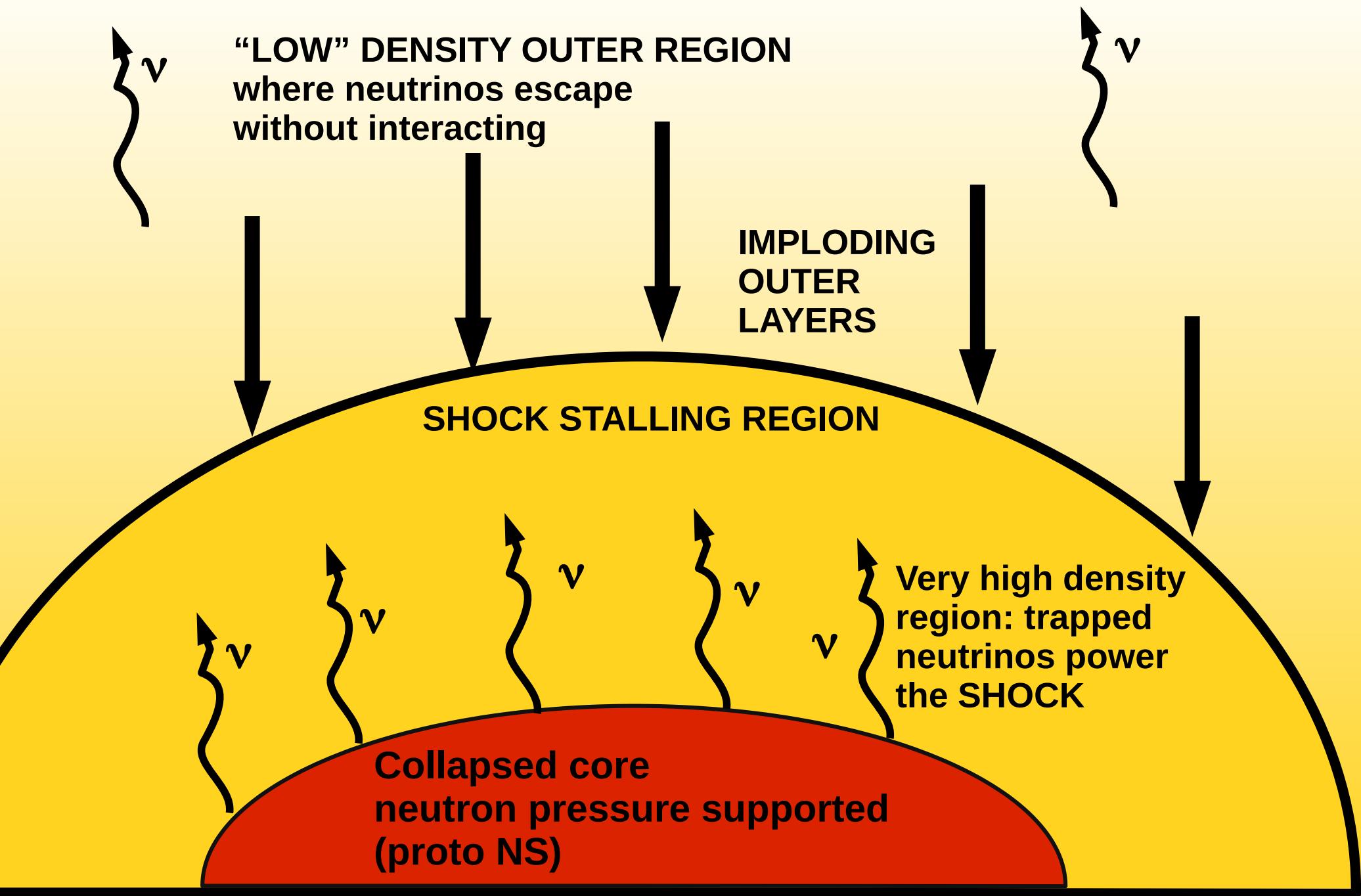
But density must be sufficiently high that neutrinos interact, otherwise neutrinos leak away without transferring energy

- **SHOCK MIGHT STALL**
- **SN FAILS**

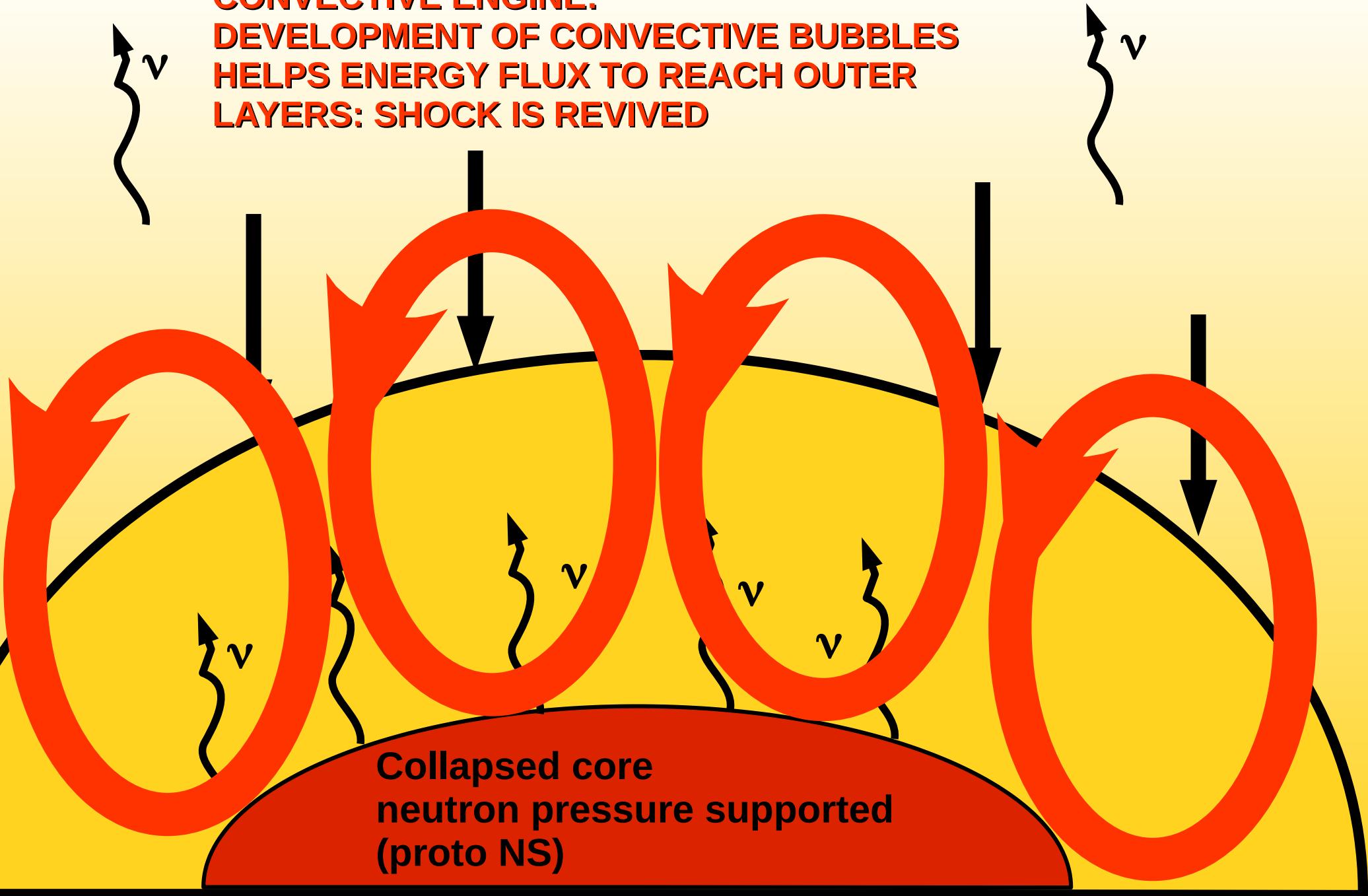
WHAT CAN REVIVE THE SHOCK?

STANDARD MODEL: CONVECTIVE ENGINE

Fryer 2014, http://pos.sissa.it/archive/conferences/237/004/FRAPWS2014_004.pdf



**CONVECTIVE ENGINE:
DEVELOPMENT OF CONVECTIVE BUBBLES
HELPS ENERGY FLUX TO REACH OUTER
LAYERS: SHOCK IS REVIVED**



Supernova shock stops anyway if BOUND MASS is too LARGE (Fryer 1999; Fryer & Kalogera 2001)

Back-of-the-envelope calculation to connect direct collapse and pre-supernova mass:

$$E_{\text{SN}} = \frac{G M_{\text{env}} (M_{\text{env}} + M_{\text{core}})}{R_{\text{env}}}$$

The diagram shows the components of the energy equation. A green arrow points from the term M_{env} in the numerator to the label "envelope mass". Another green arrow points from the term R_{env} in the denominator to the label "envelope radius". A third green arrow points from the term M_{core} in the numerator to the label "proto-NS ~ 1 Msun".

Star cannot explode if envelope binding energy > SN energy

$$M_{\text{env}} \sim 50 M_{\odot} \left(\frac{E_{\text{SN}}}{10^{51} \text{erg}} \right)^{1/2} \left(\frac{R_{\text{env}}}{10 R_{\odot}} \right)^{1/2}$$

If $M_{\text{fin}} > 50 M_{\odot}$ this SN fails and star collapses to a BH

How to study a core-collapse supernova (SN)?

HYDRODYNAMICAL SIMULATIONS

!CAVEAT: only stars with mass 8 – 11 Msun explode easily!!

1D: large statistics (hundreds of models), approximate neutrino transfer (often kinetic bombs or thermal bombs to artificially induce explosion even in more massive stars)

(O'Connor & Ott 2011; Ugliano et al. 2012; Ertl et al. 2016)

2D: explode easily but often contain less physics than 1D and we cannot run large sets

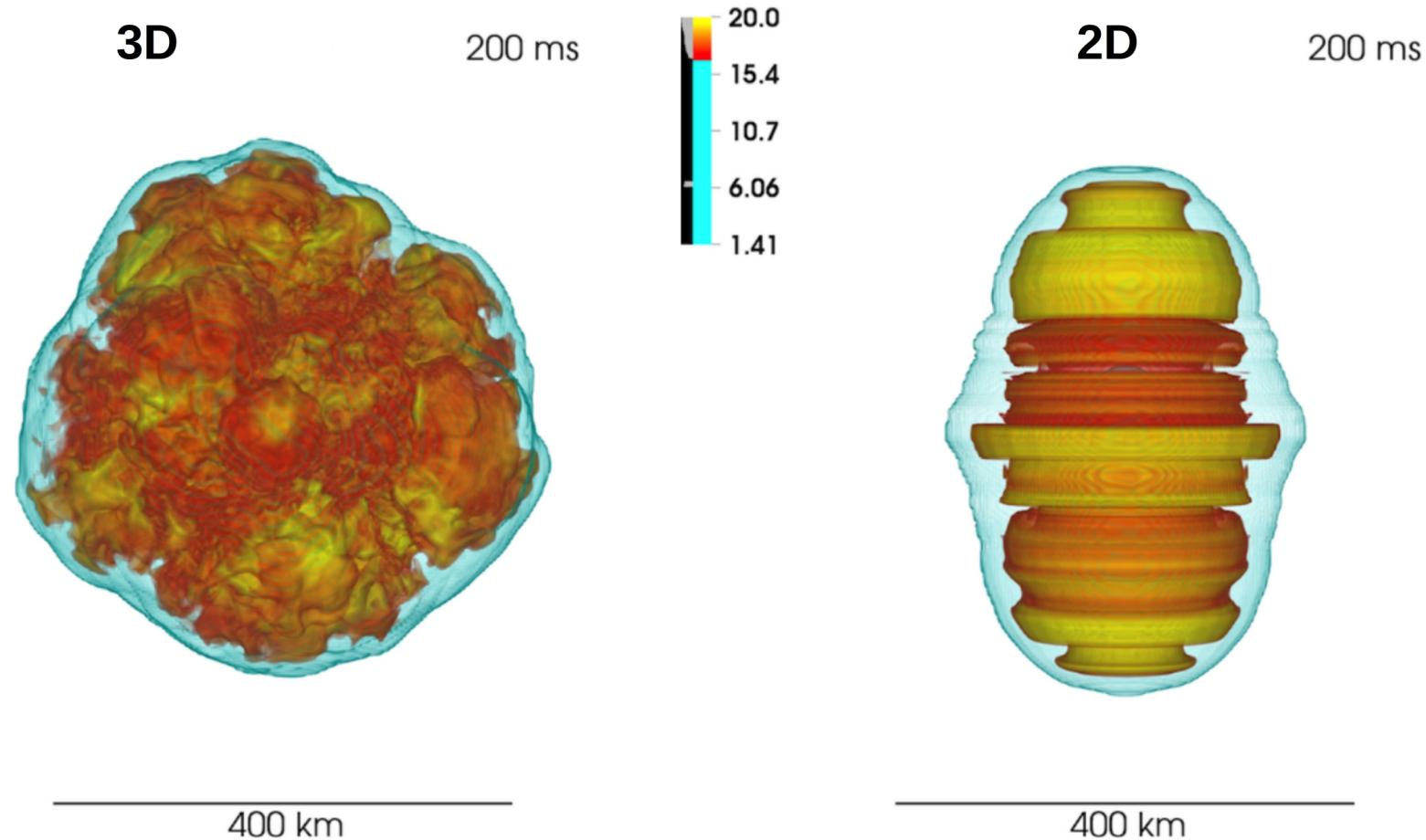
(Marek & Janka 2009; Mueller et al. 2012a, 2012b)

3D: computationally expensive (see 2D)

(Ott et al. 2005; Bondin & Mezzacappa 2007; Couch 2013; Couch & O'Connor 2014)

How to study a core-collapse supernova (SN)?

HYDRODYNAMICAL SIMULATIONS (Couch & O'Connor 2014)



CRITERIA FOR COLLAPSE TO A REMNANT

depends on the "compactness" of the inner layers of the star

1. MASS OF CARBON-OXYGEN CORE

If $M_{\text{CO}} > 8 - 12 \text{ M}_{\odot}$ SN FAILS

(Fryer+ 1999, 2012; Belczynski+ 2010)

2. COMPACTNESS

3. TWO-PARAMETER CRITERION

Core-collapse (CC) SN depends on the "compactness" of the inner layers

COMPACTNESS (= ratio between mass and radius) of a given portion of the stellar core at the onset of collapse

(O'Connor & Ott 2011)

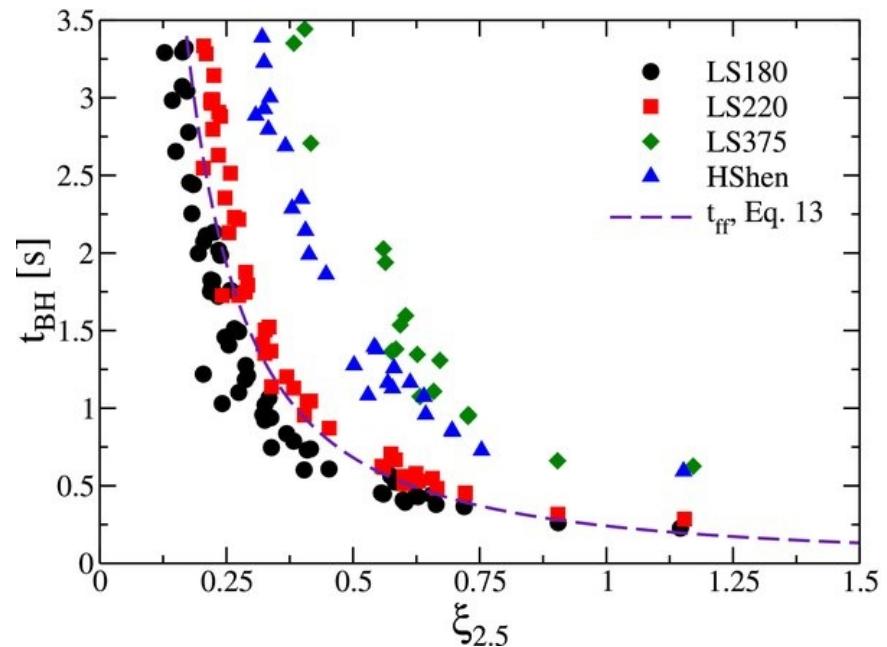
$$\xi_M \equiv \frac{M / M_{\odot}}{R(M) / 1000 \text{ km}}$$

$M = 2.5 M_{\odot}$ is usually adopted

Star collapses if $\xi_{2.5} > 0.2$

(Ugliano+ 2012; Horiuchi+ 2012)

Figure from
O'Connor & Ott 2011

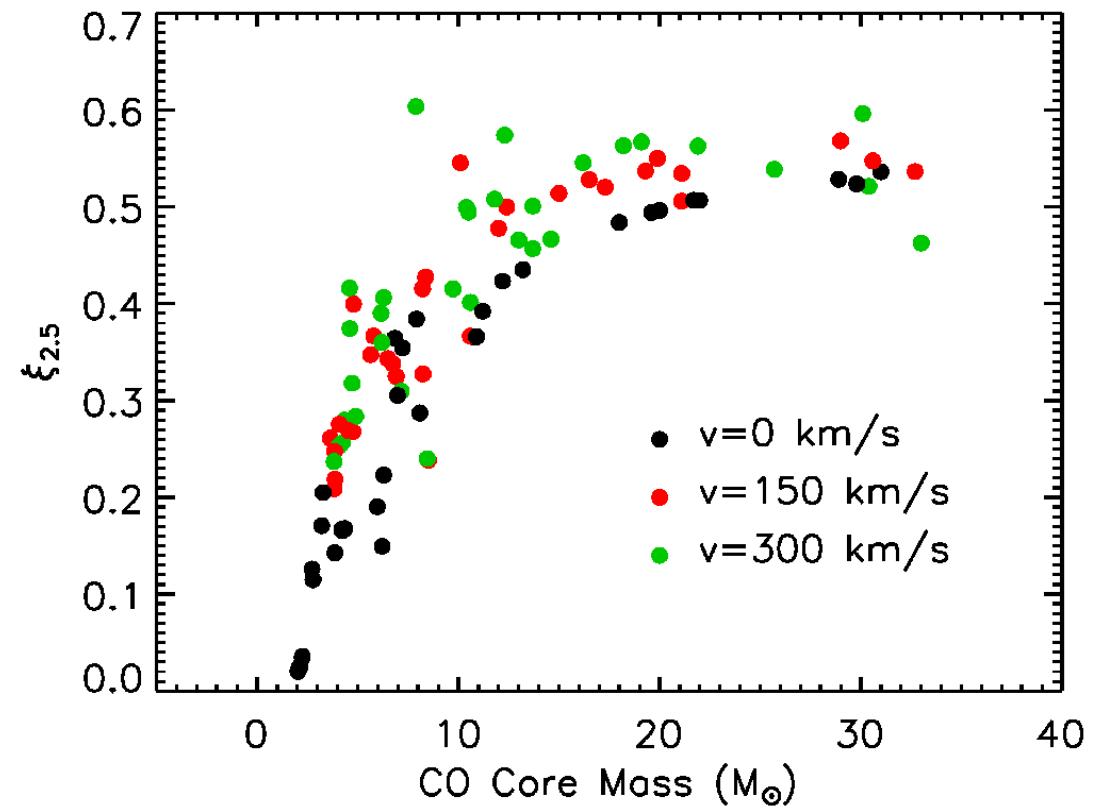


Core-collapse (CC) SN depends on the "compactness" of the inner layers

Compactness correlates well with mass of CO core

→ compactness > 0.2 corresponds to CO core > 8 M_⊙

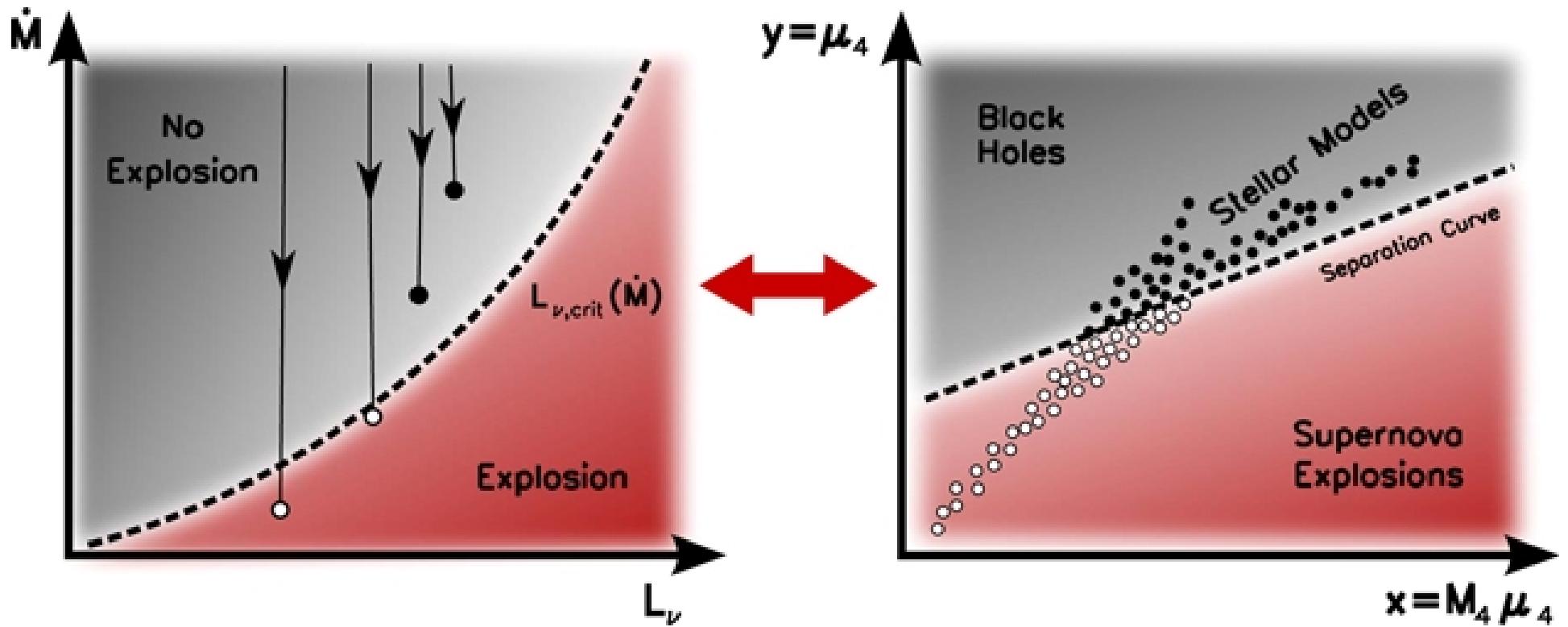
Figure from
Limongi 2017
arXiv:1706.01913



Core-collapse (CC) SN depends on the enclosed mass (M_4) and mass gradient (μ_4) at a dimensionless entropy per nucleon $s = 4$

$$M_4 = m(s=4)/M_\odot$$

$$\mu_4 = \left[\frac{dm/M_\odot}{dr/1000 \text{ km}} \right]_{s=4}$$



Core-collapse (CC) SN depends on the enclosed mass (M_4) and mass gradient (μ_4) at a dimensionless entropy per nucleon $s = 4$

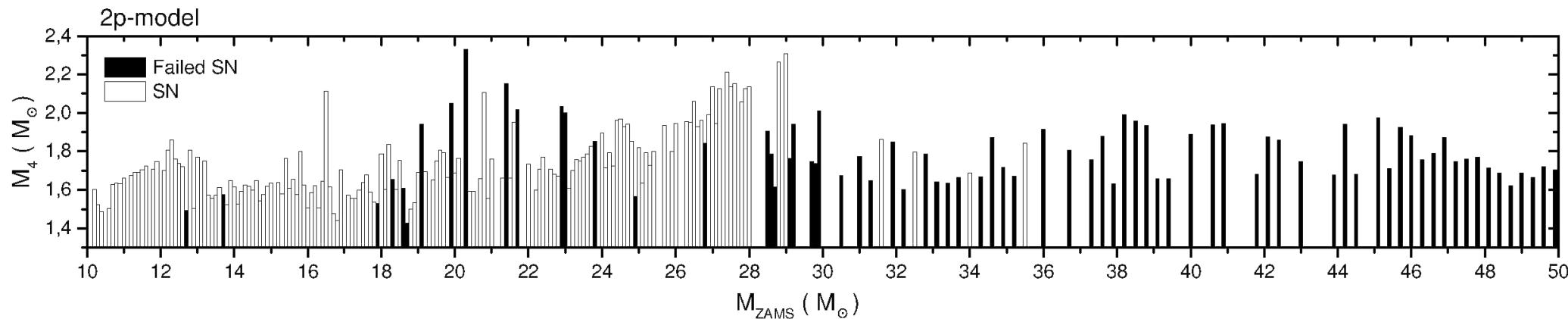


Fig. 21

Spera, MM, Bressan 2015

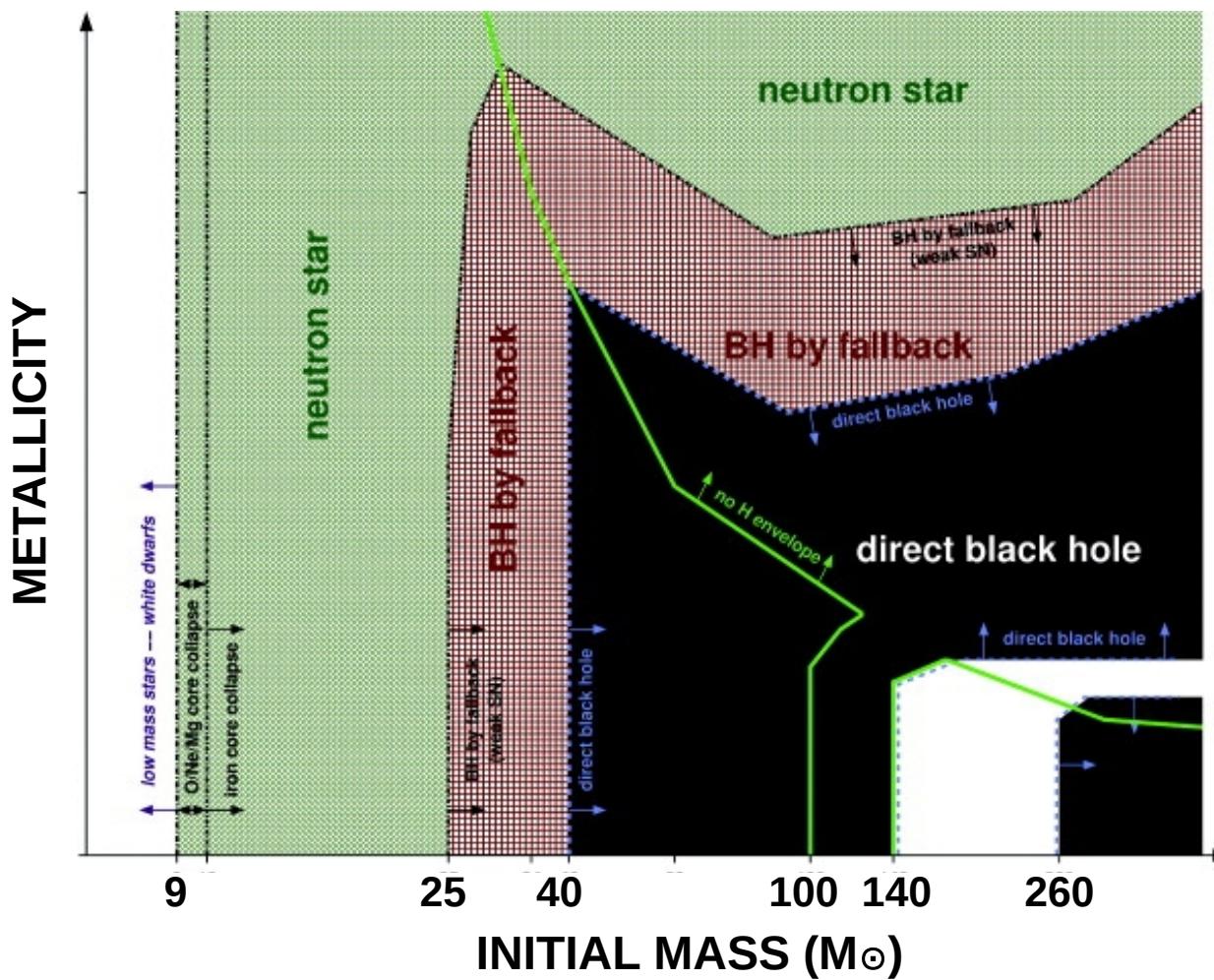
ISLANDS OF DIRECT COLLAPSE AND SN EXPLOSION

Concluding remark:
**MANY MODELS of SN EXPLOSION OUTCOMES
 BUT IF THE STAR IS VERY MASSIVE ($>40 M_\odot$)
 THEY GIVE SIMILAR RESULT**

CC SN depends on the "fallback" of the outer layers of the star:

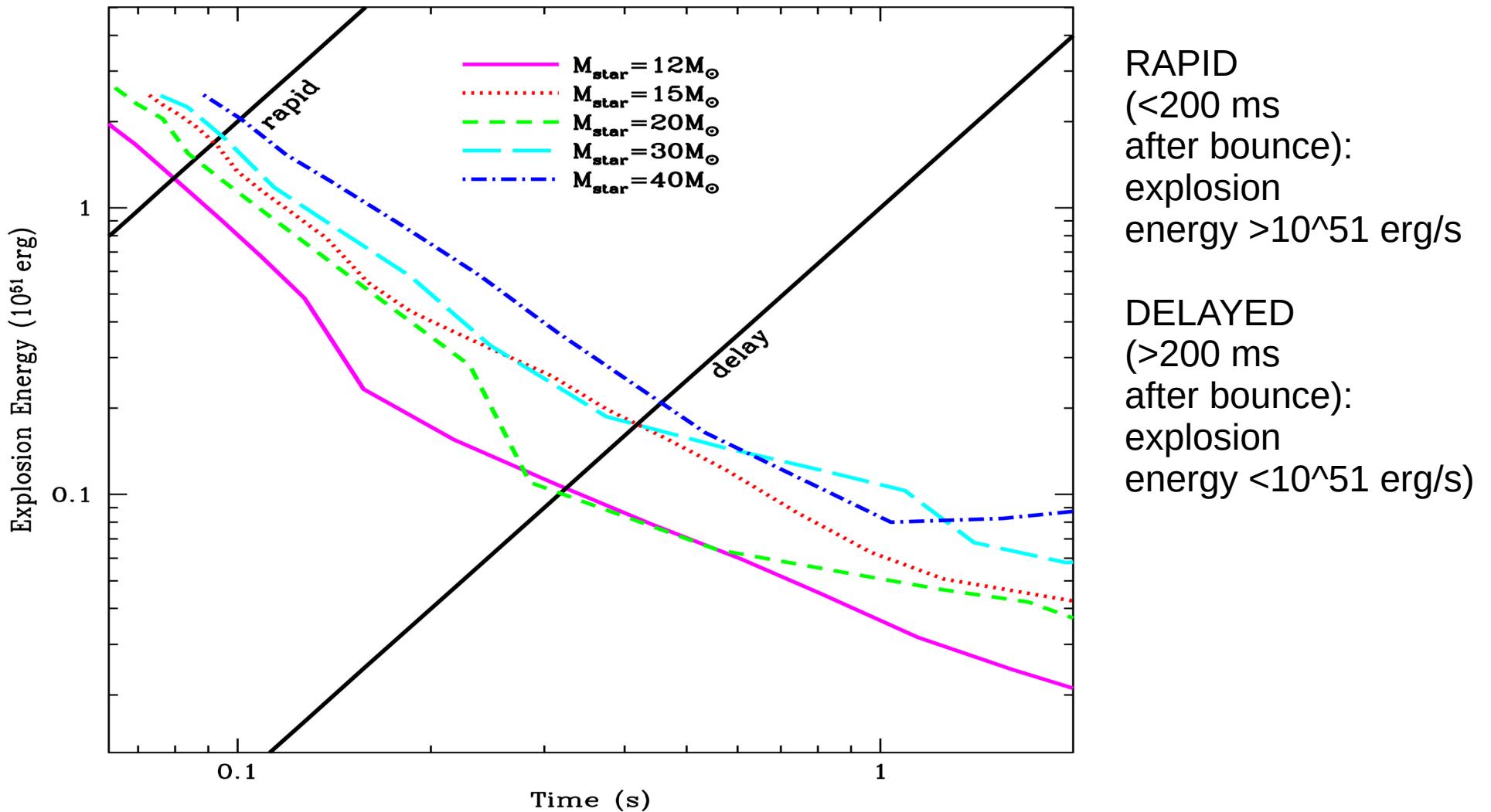
How much material falls back to the proto-NS after the SN

Barely constrained – depends on explosion energy,
angular momentum,
progenitor's mass/metallicity



Heger et al. 2003

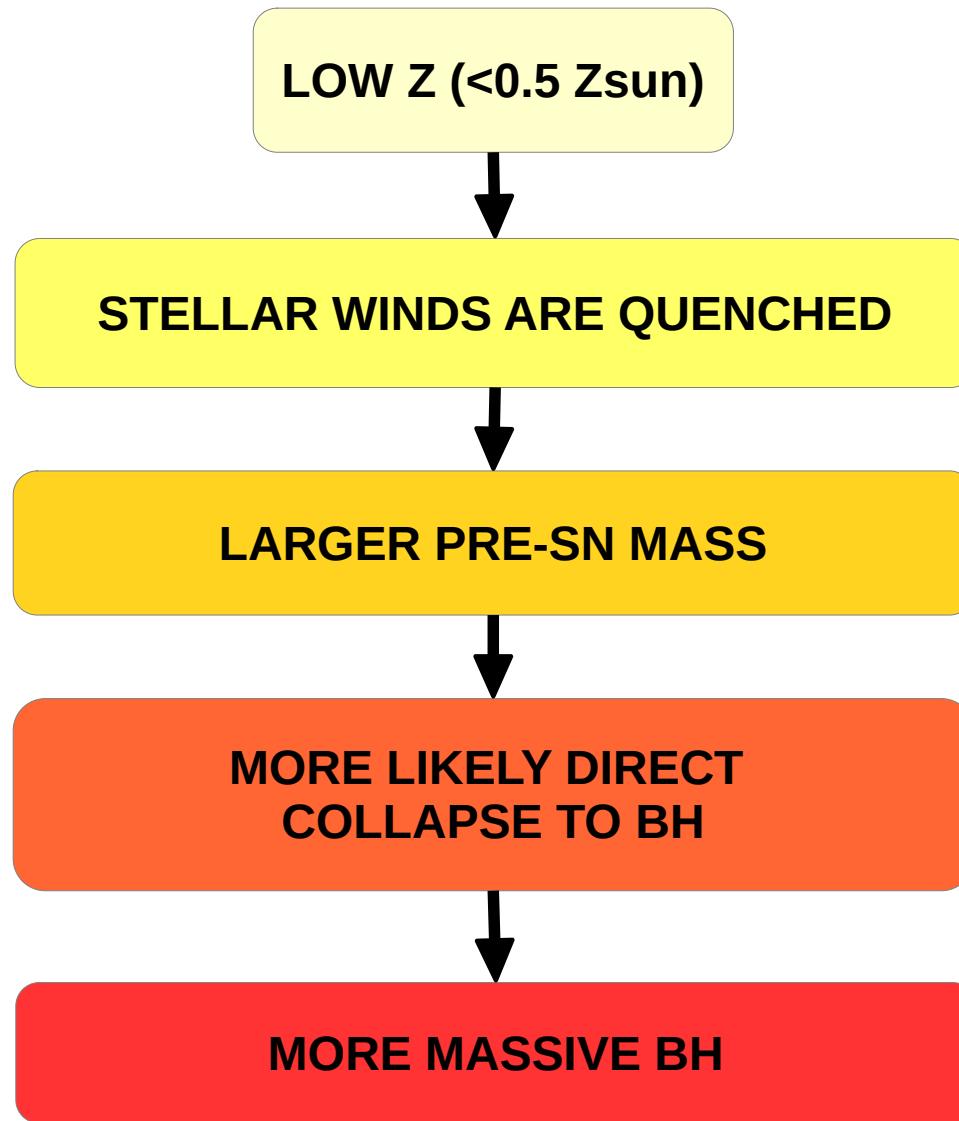
CC SN depends on the rapidity of the explosion:
 (e.g. Fryer+ 2012; Fryer 2014)

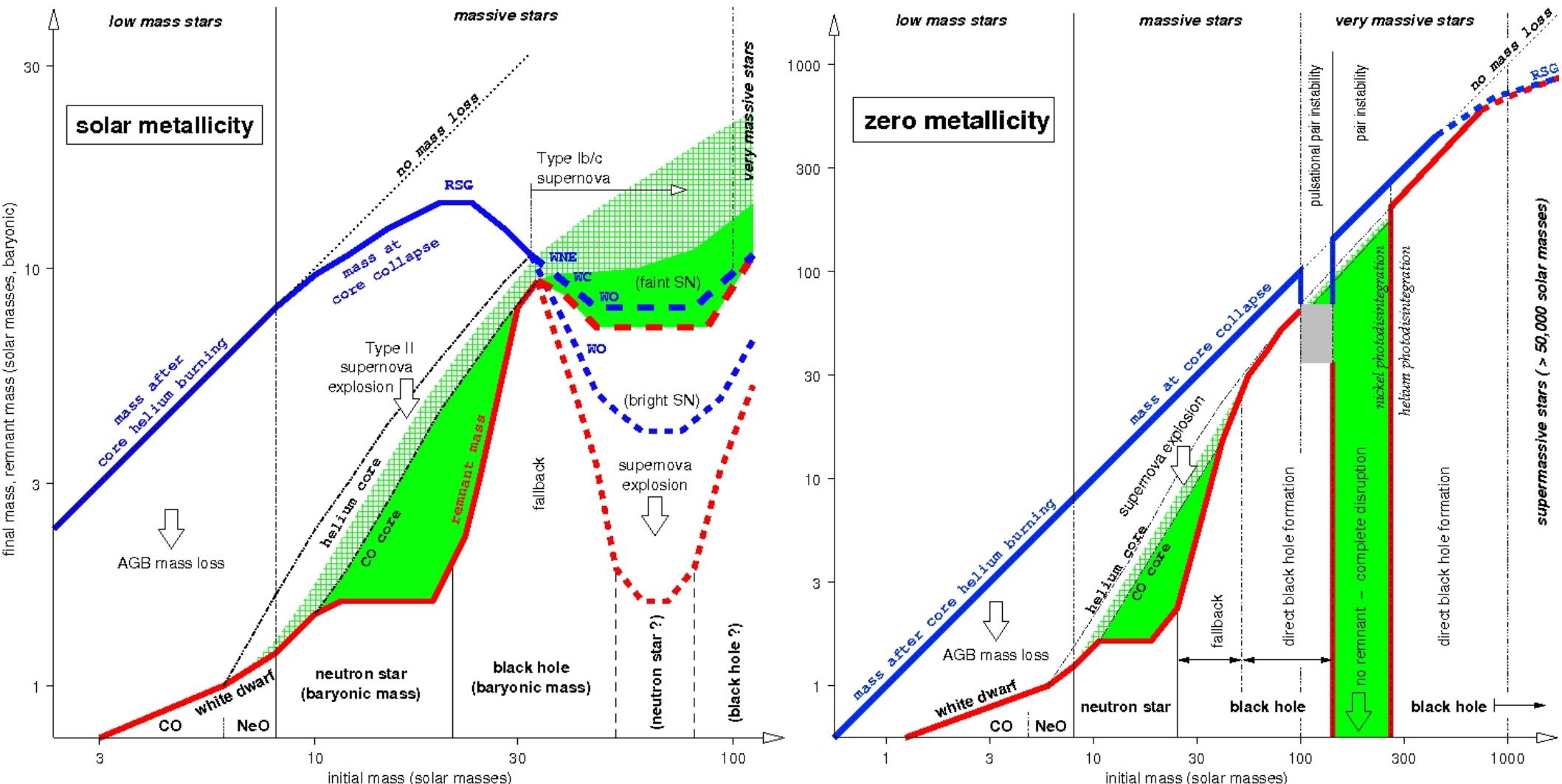


From Fryer 2014,
http://pos.sissa.it/archive/conferences/237/004/FRAPWS2014_004.pdf

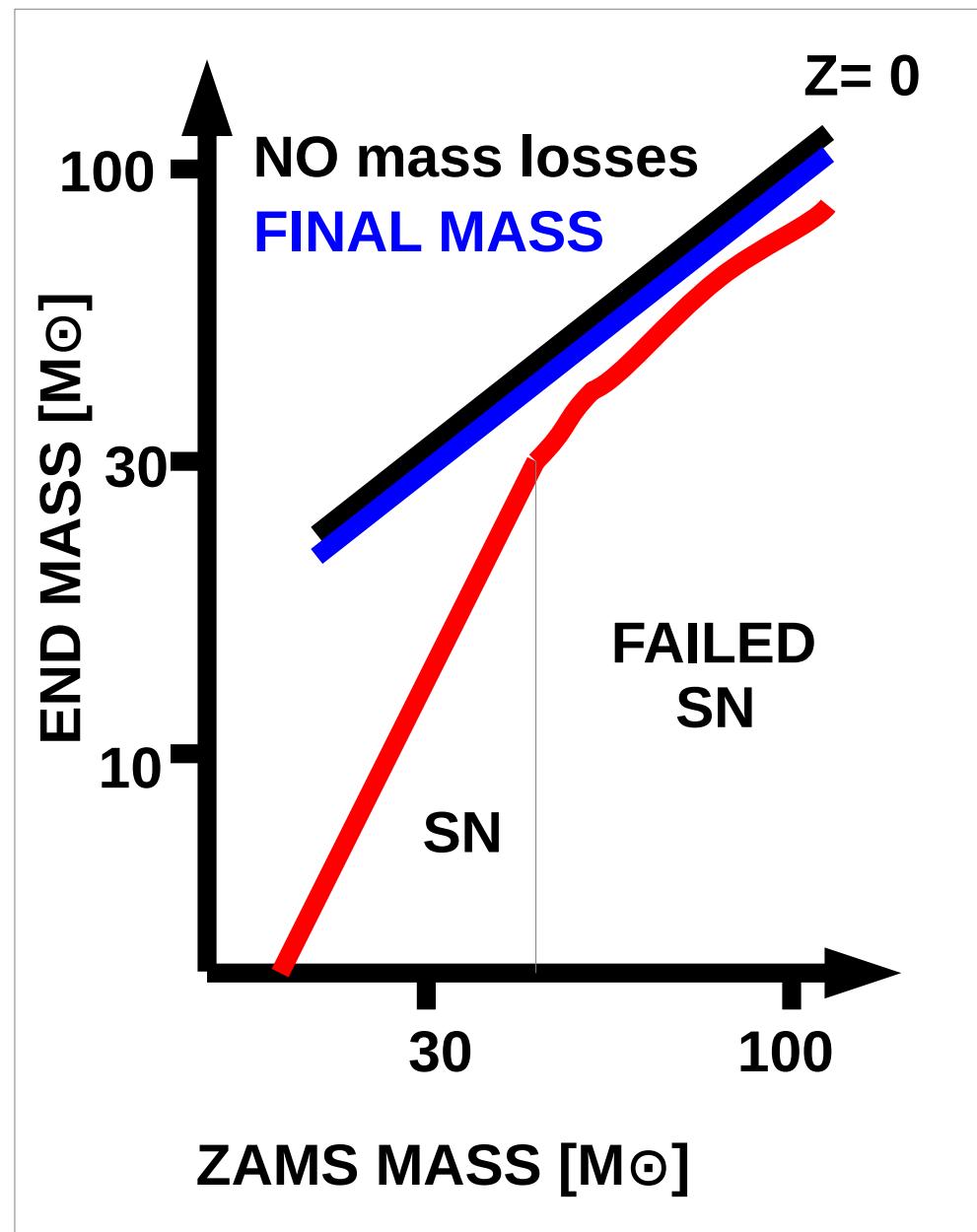
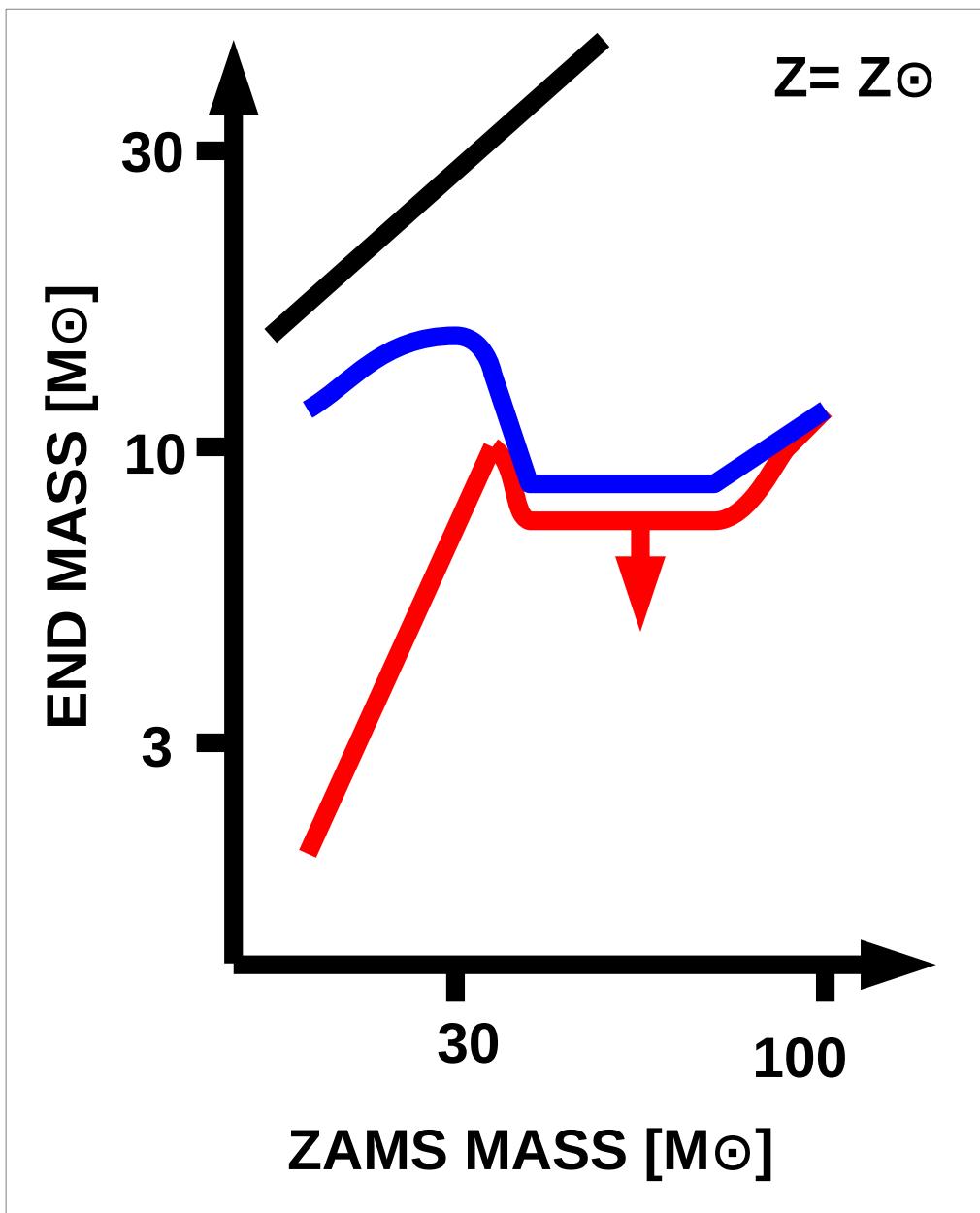
The formation of compact remnants: wrap up

Very complicated. However, as rule of thumb (MM+ 2009, 2013):





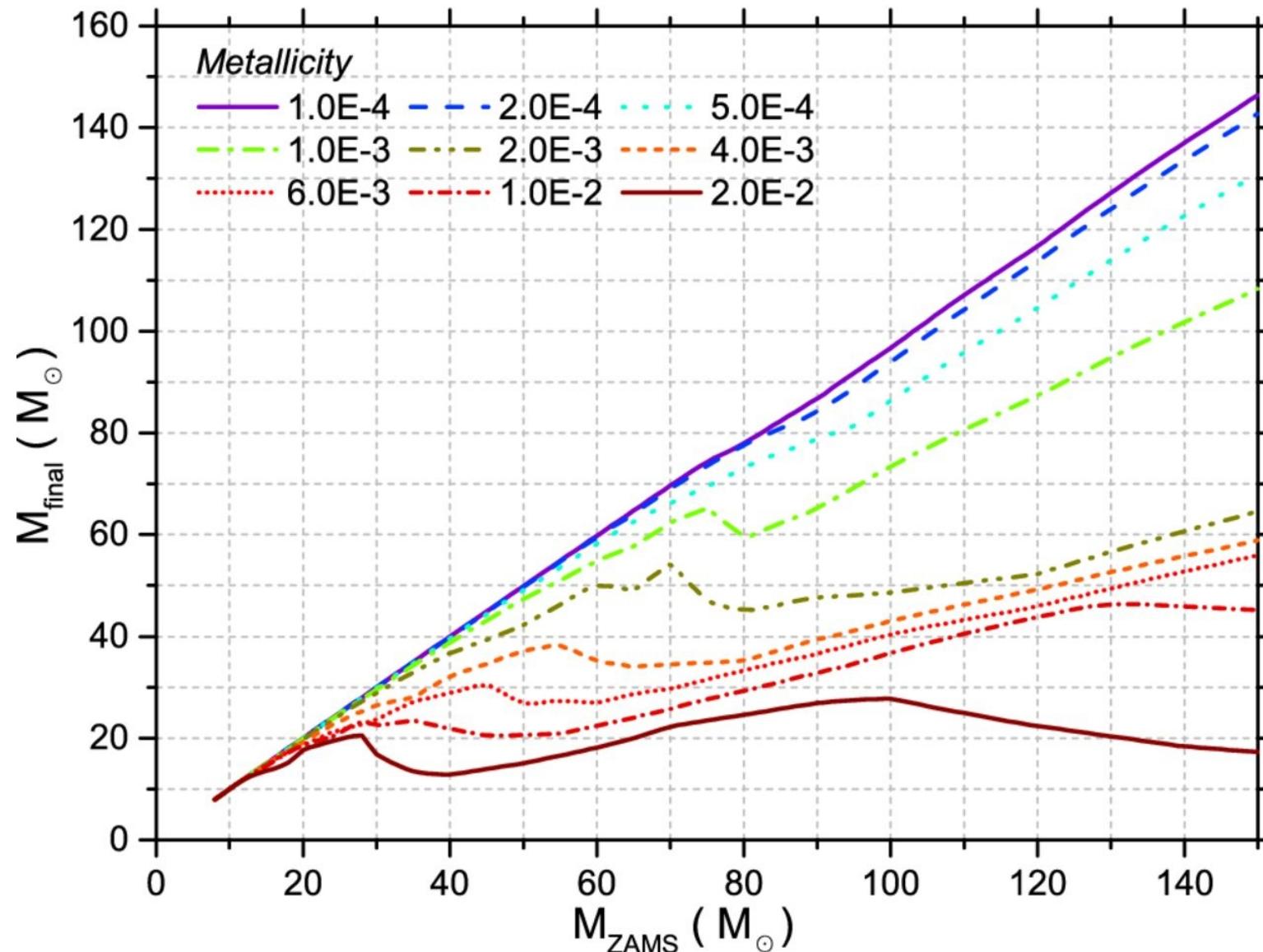
Heger et al. (2003)

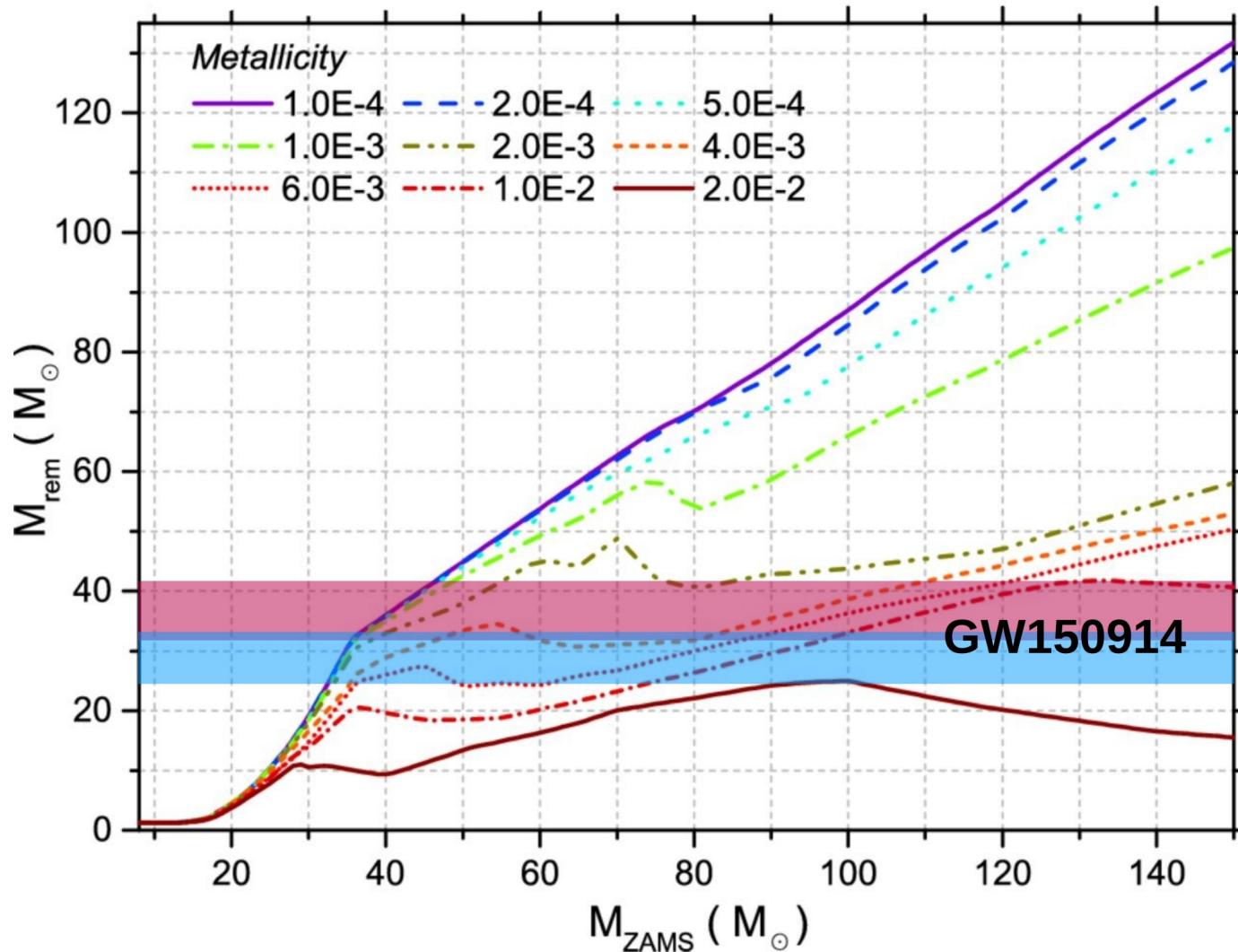


My cartoon from Heger et al. (2003)

What about intermediate metallicities between 0 and solar?

- more difficult because stellar winds are uncertain
- importance of final mass: pre-supernova mass of the star (when CO core built)



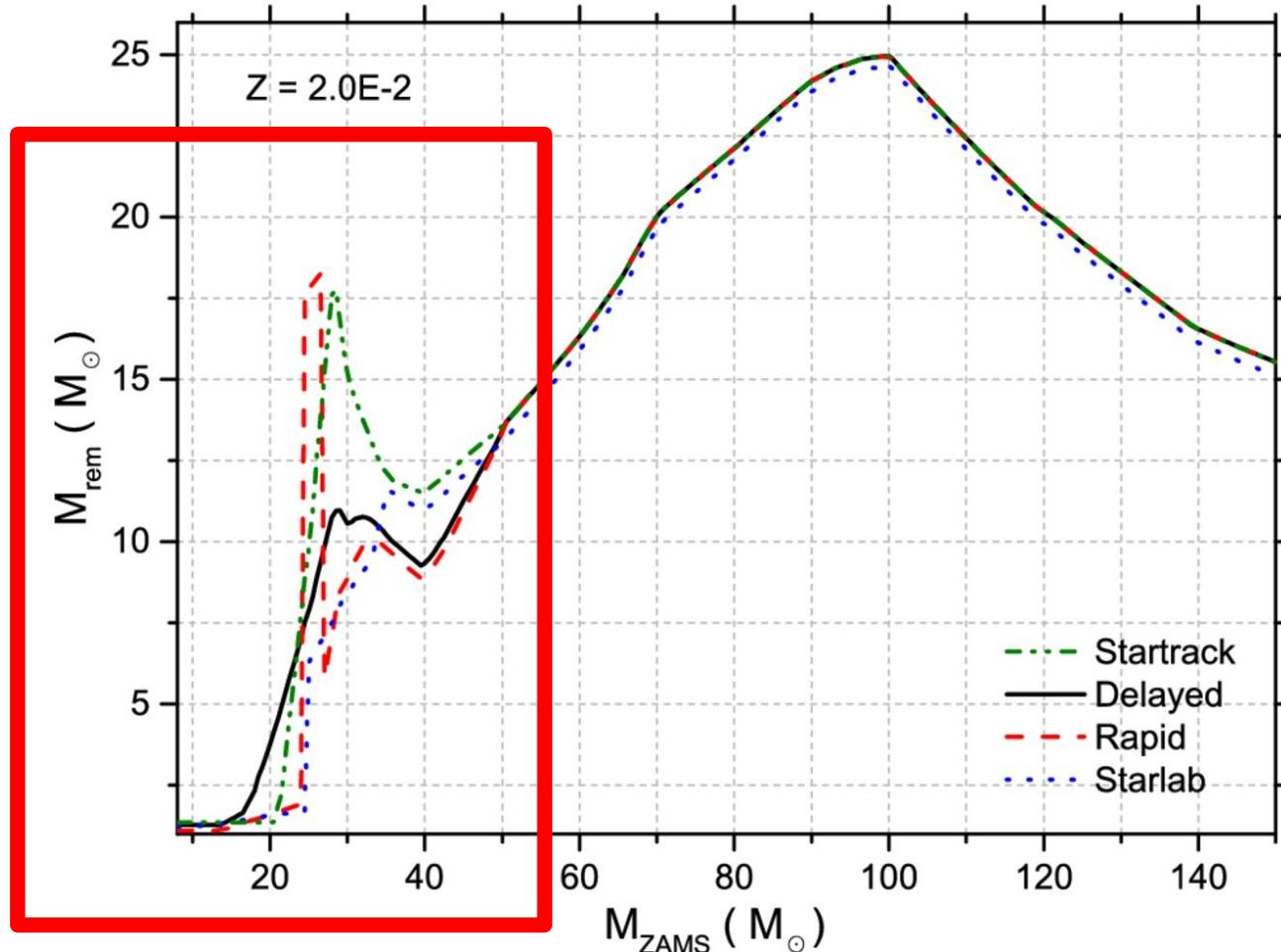


Remnant mass follows same trend as final mass → stellar winds are crucial

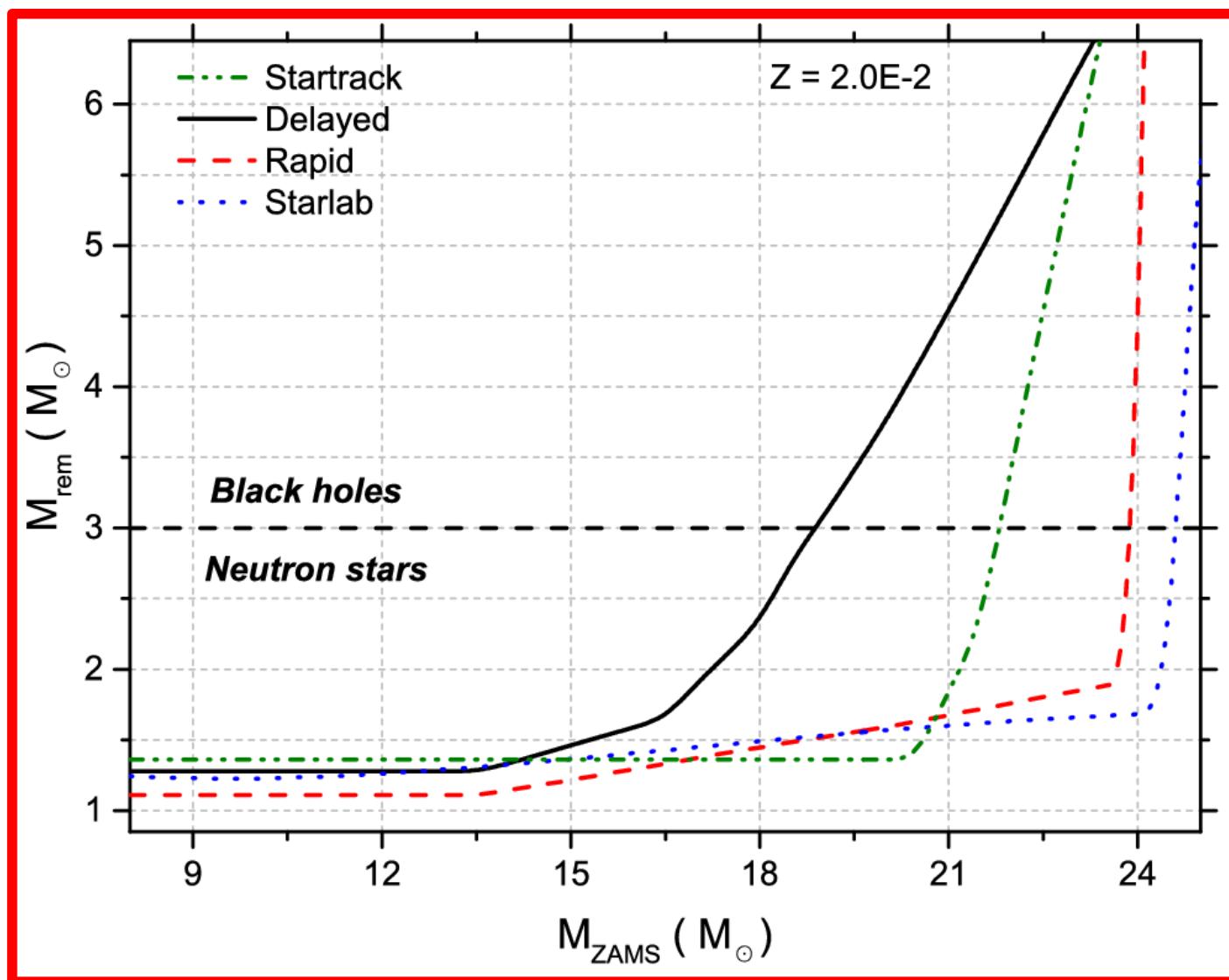
From Spera, MM & Bressan 2015, MNRAS, 451, 4086

See also MM+ 2009, MNRAS, 395, L71; MM+ 2010, MNRAS, 408, 234; Belczynski+ 2010, ApJ, 714, 1217; Fryer+ 2012, ApJ, 749, 91; MM+ 2013, MNRAS, 429, 2298; Belczynski+ 2016, A&A, 594, 97; Spera & MM 2017, MNRAS, 470, 4739

Importance of supernova model for “LOW” STAR MASSES ($< 40 M_{\odot}$)



A lower mass gap in BH mass spectrum?



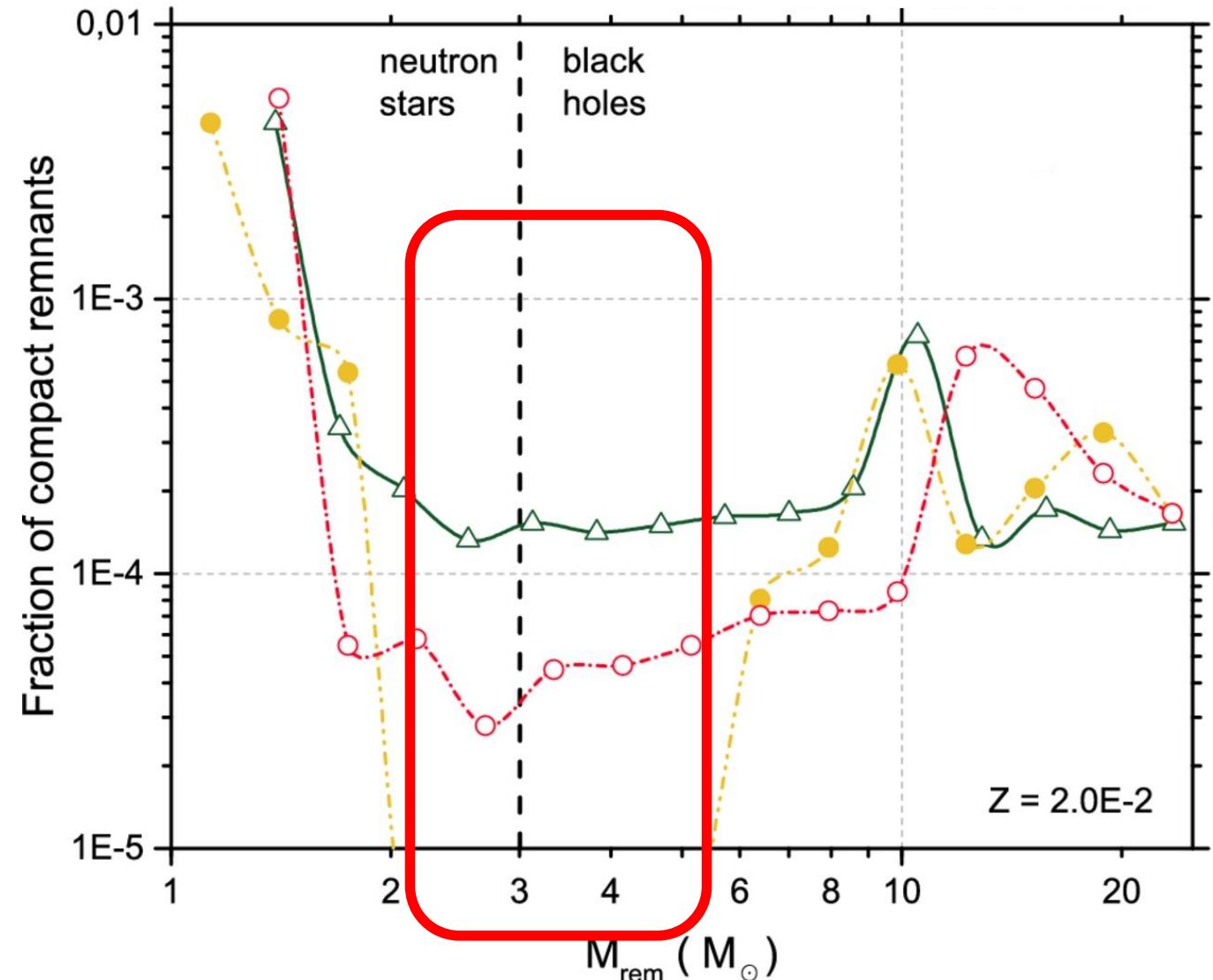
A lower mass gap in BH mass spectrum?

Solar metallicity

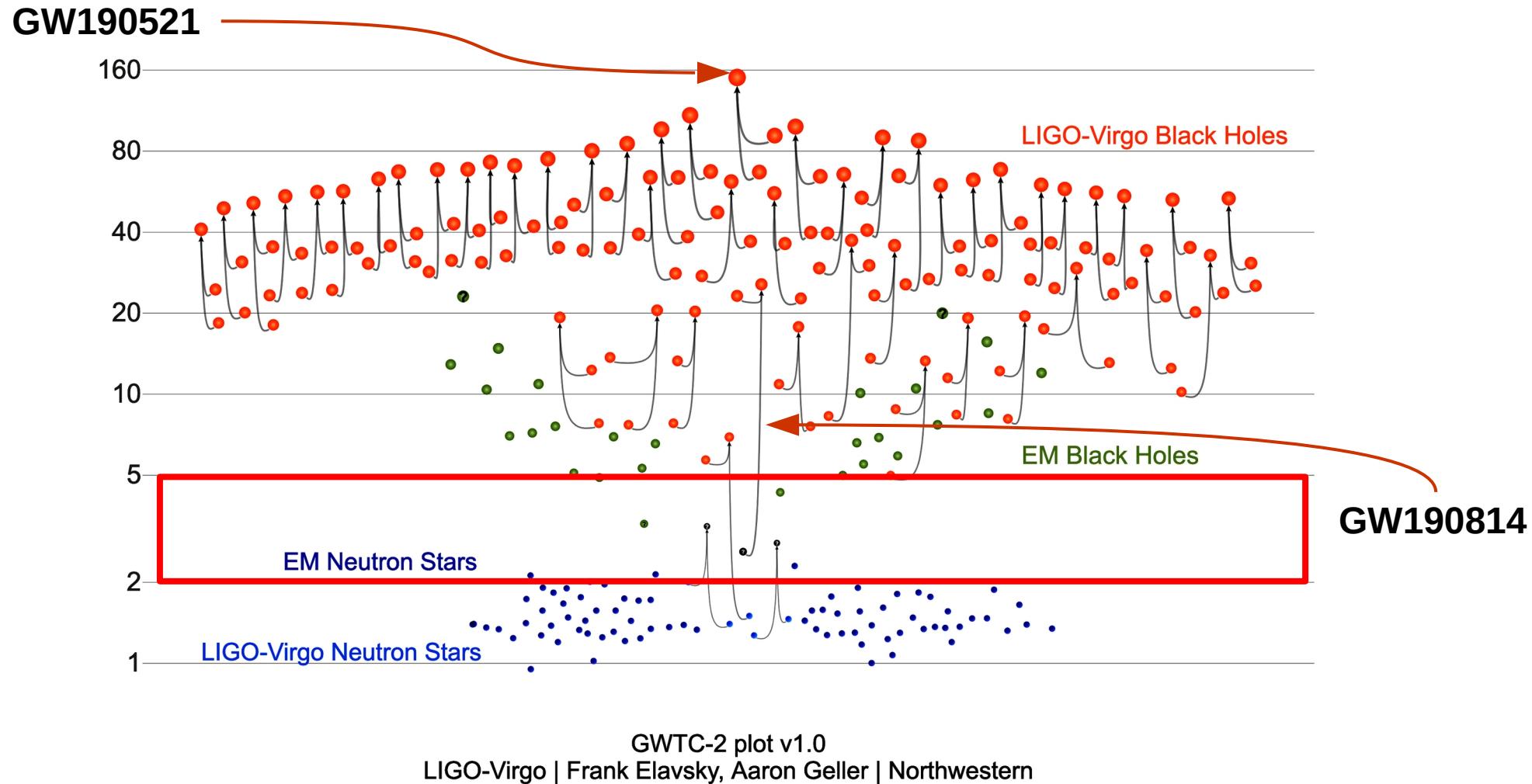
GREEN:
DELAYED
SN (Fryer+ 2012)

RED:
DELAYED
SN (MM+ 2013)

YELLOW:
PROMPT SN
(Fryer+ 2012)



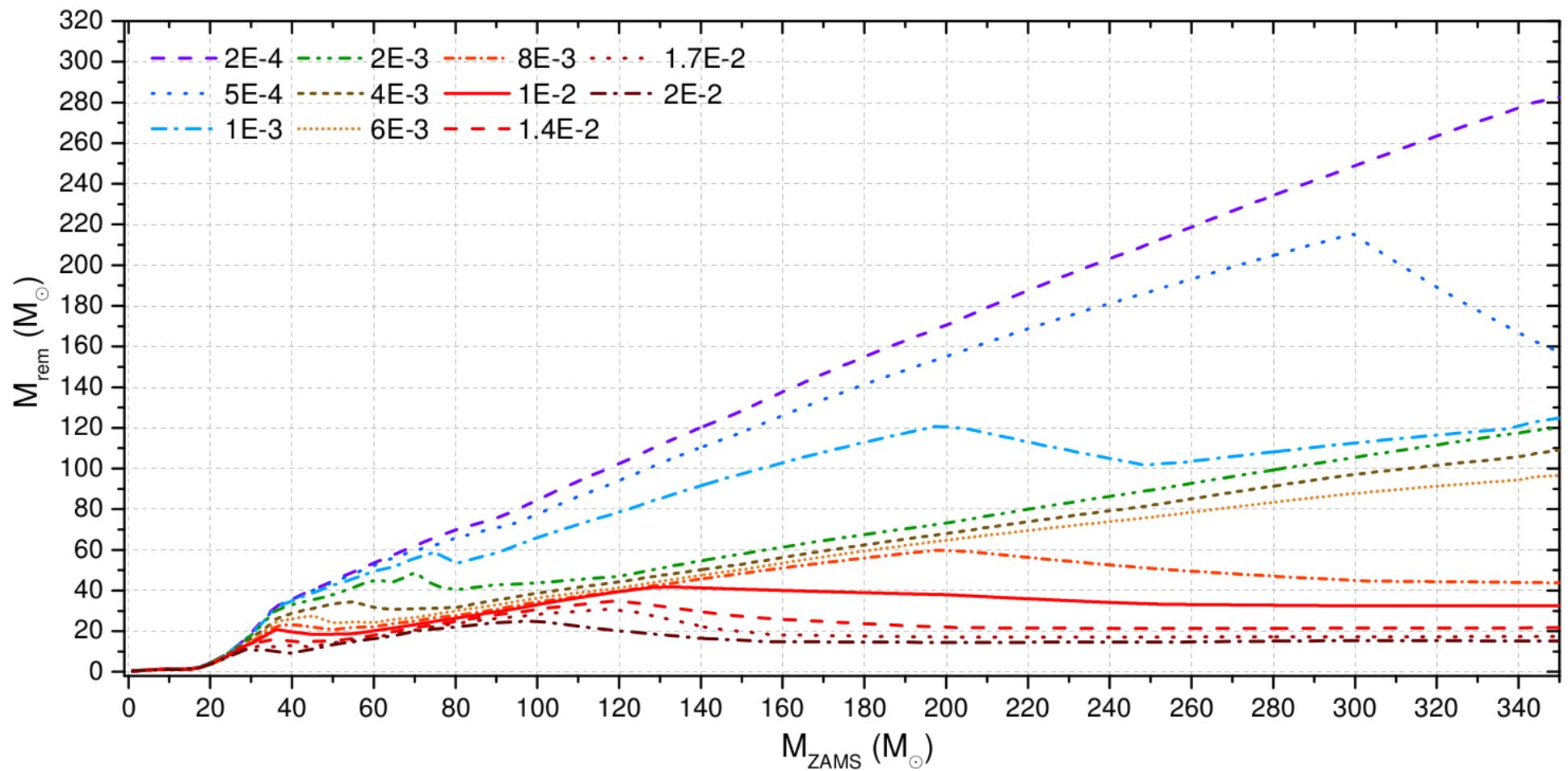
A lower mass gap in BH mass spectrum?



Abbott et al. 2020, GWTC-2, 2020, <https://arxiv.org/abs/2010.14527>

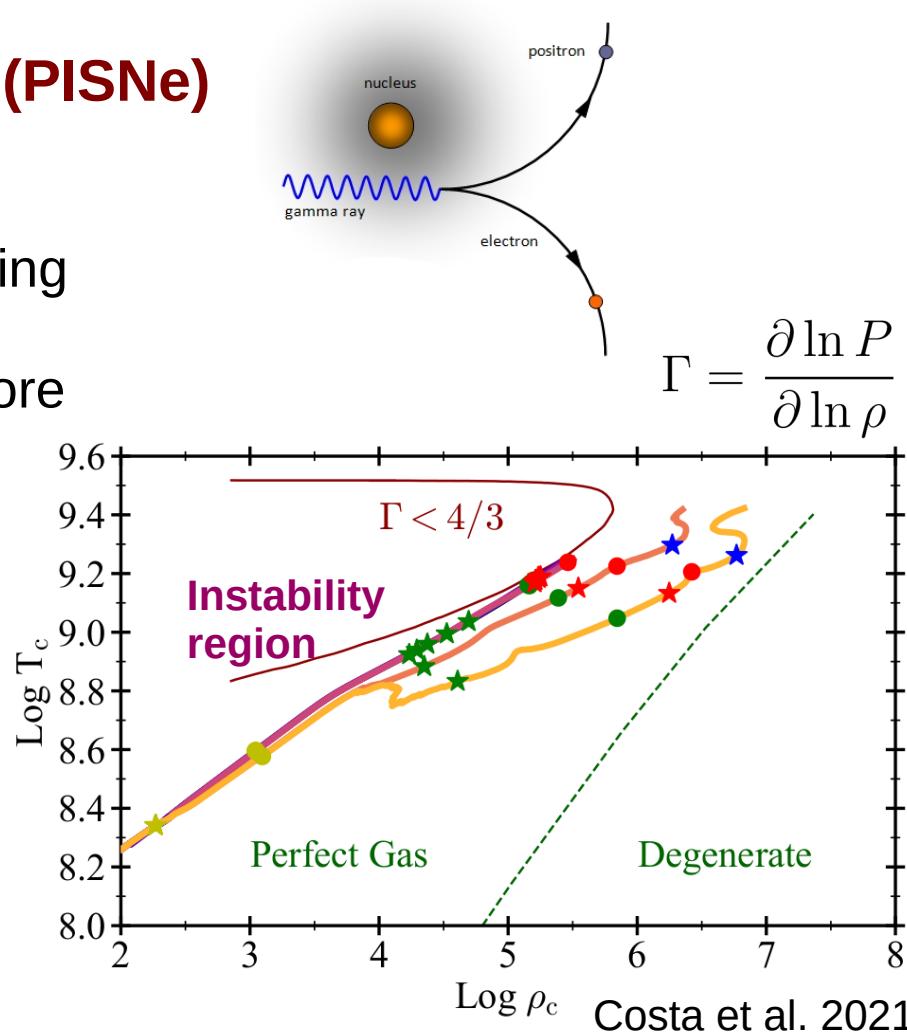
Evolution of very massive stars still uncertain

→ stellar winds are Eddington-limited rather than metallicity dependent



PAIR-INSTABILITY SUPERNOVAE (PISNe)

If star is very massive,
helium core mass > $64 M_{\odot}$ at end of C burning
 → central temperature > 7×10^8 K
 → efficient production of γ -ray radiation in core
 → γ -ray photons scattering atomic nuclei
 produce electron-positron pairs
 (1 Mev, nearly at rest)



The missing pressure of γ -ray photons produces dramatic collapse during O burning, without Fe core

- Temperature increase during collapse ignites all remaining species
- **an explosion is induced that leaves NO remnant**

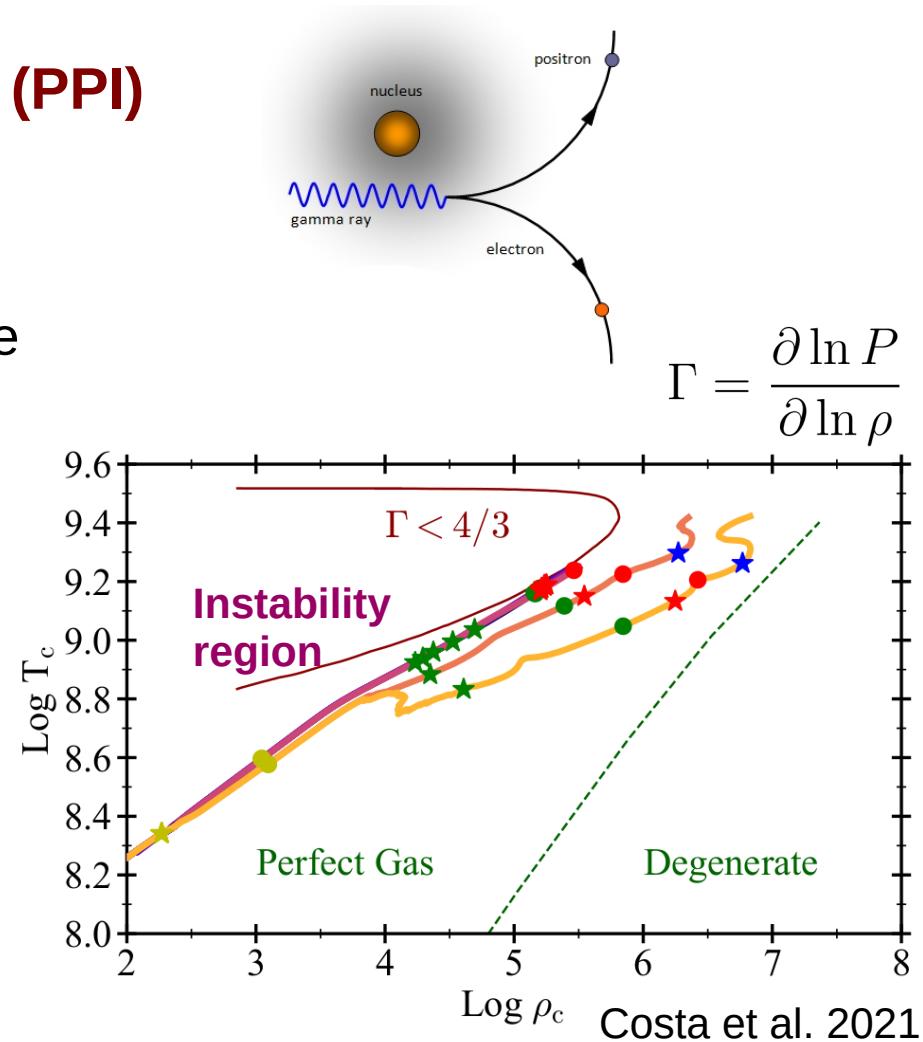
Ober, El Eid & Fricke 1983; Bond, Arnett & Carr 1984;
 Heger et al. 2003; Woosley, Blinnikov & Heger 2007

PULSATIONAL PAIR INSTABILITY (PPI)

- If star is quite massive,
 $64 M_{\odot} > \text{Helium core mass} > 32 M_{\odot}$
 - some production of γ -ray radiation in core
 - γ -ray photons scattering atomic nuclei produce electron-positron pairs (1 Mev, nearly at rest)

The missing pressure of γ -ray photons produces contraction during O burning, without Fe core

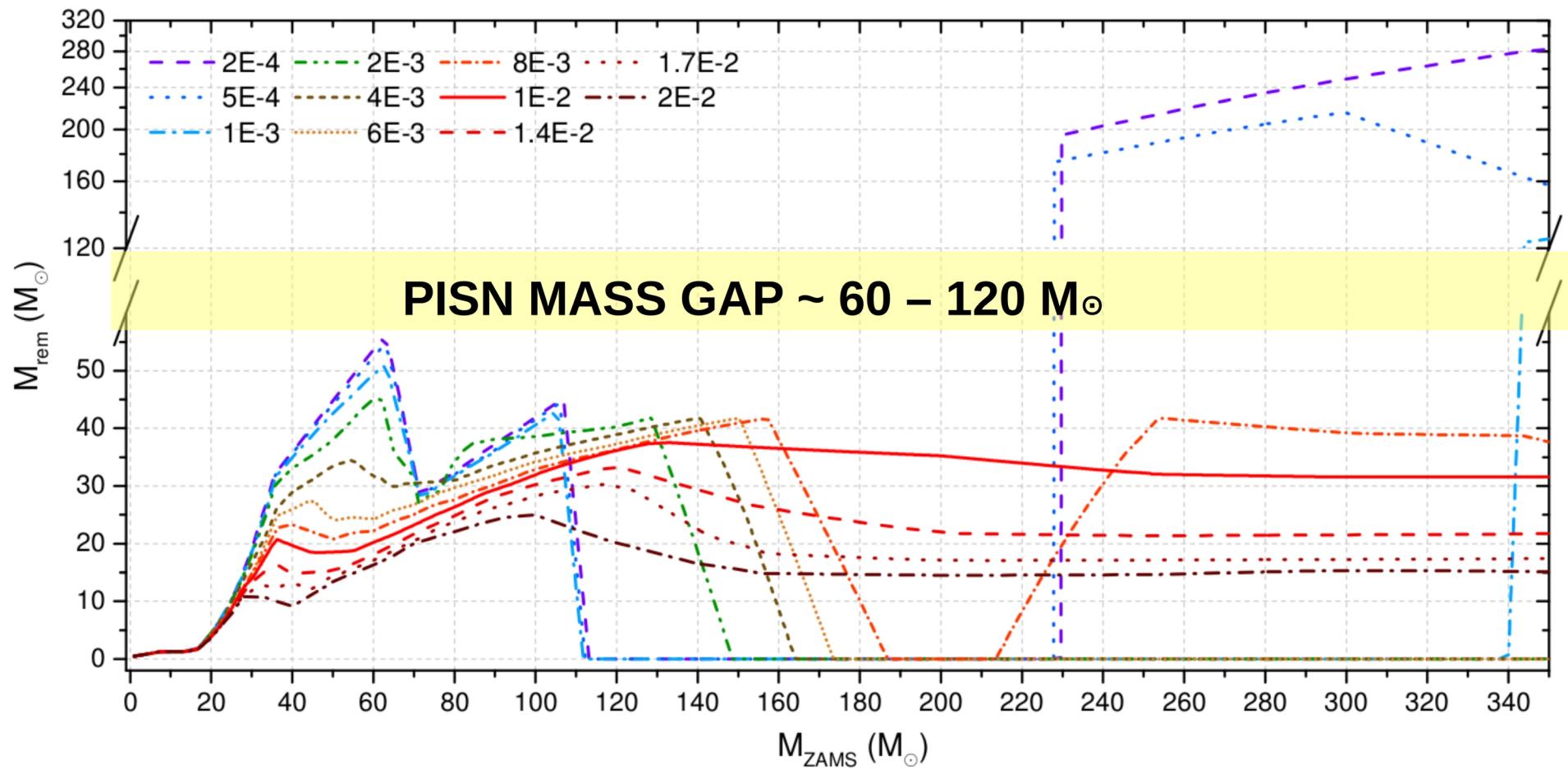
- enhancement of nuclear reactions restores pressure
- star gains equilibrium after one or more oscillations
- **oscillations enhance mass loss and final mass is lower**



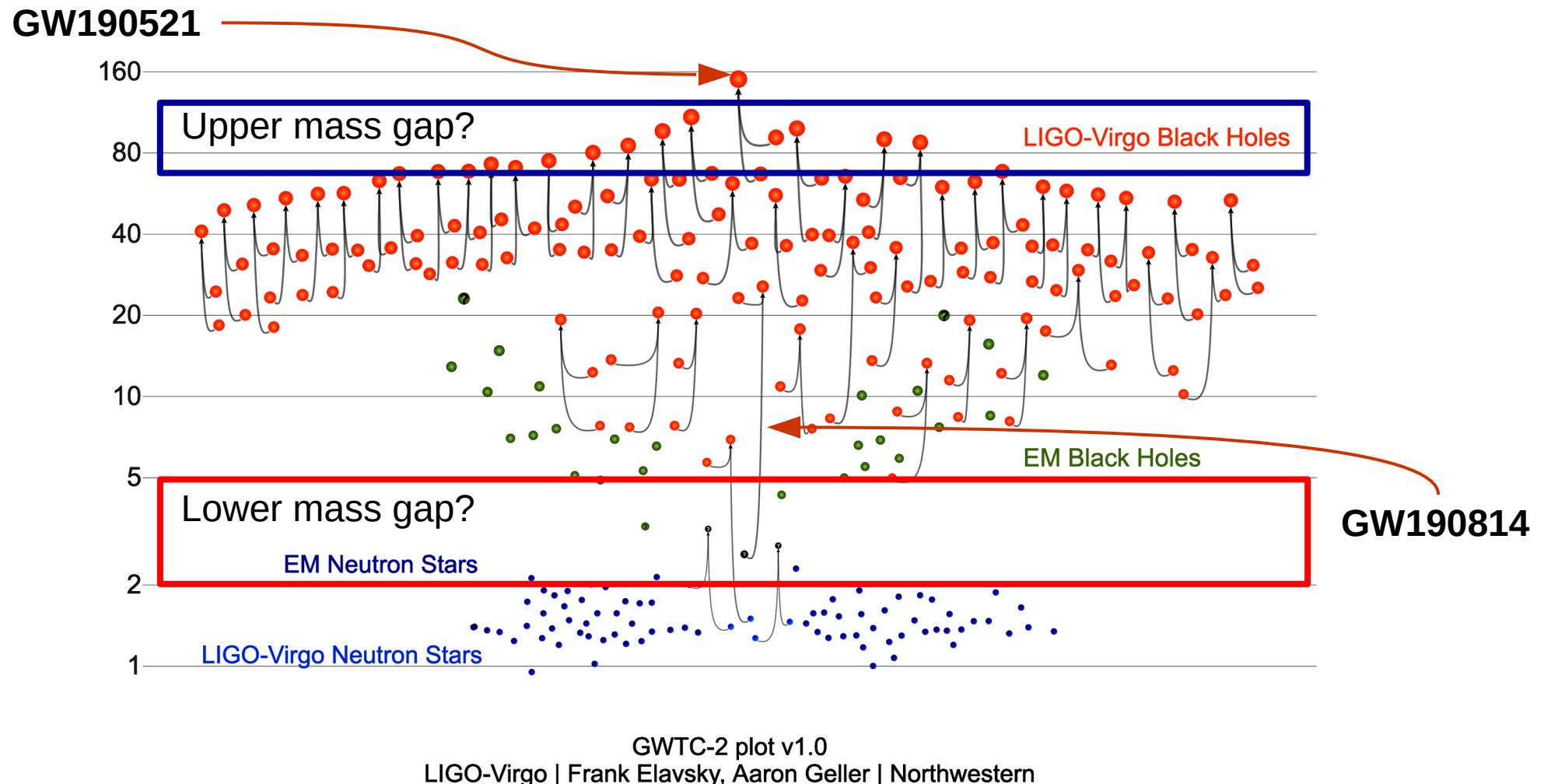
$$\Gamma = \frac{\partial \ln P}{\partial \ln \rho}$$

Costa et al. 2021

An upper mass gap because of (pulsational) pair instability?



A un upper mass gap in BH mass spectrum?



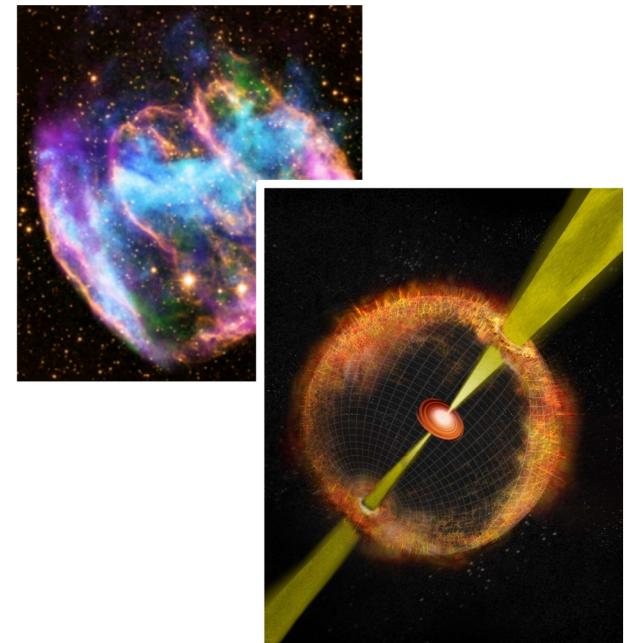
Abbott et al. 2020, GWTC-2, 2020, <https://arxiv.org/abs/2010.14527>

WHAT ABOUT THE SPIN? Spin magnitude is OPEN ISSUE

Spin of compact object should be related to spin of the core at the end of stellar evolution (if ang. mom. is conserved)

BUT:

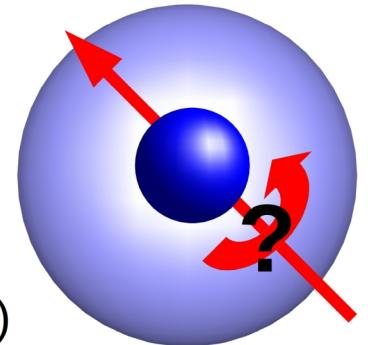
- if **supernova explosion**, part of spin is lost
- if **accretion disk or jet**, angular momentum is transported outward/away
- if star collapses to **black hole DIRECTLY**, angular momentum should be conserved



PROBLEM:

- large uncertainties on **angular momentum transport in the stellar interior**
 - **we do not know spin of the core at the end of stellar evolution**

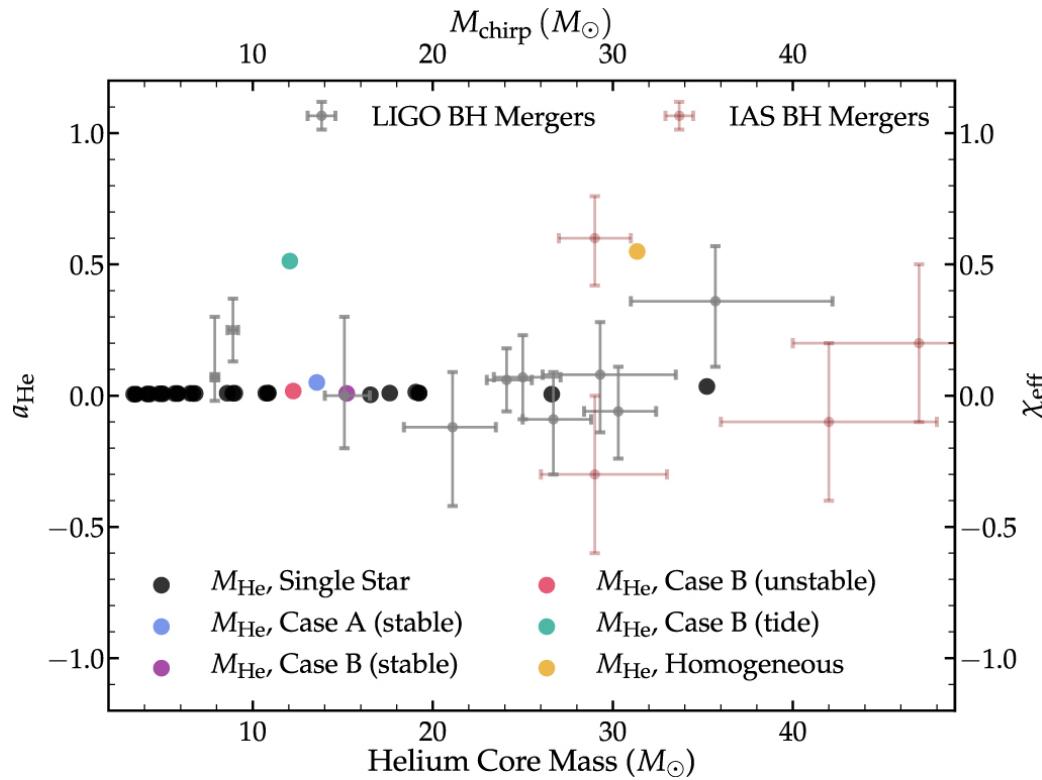
(e.g. Belczynski et al. 2020; Limongi & Chieffi 2018; MM et al. 2020)



WHAT ABOUT THE SPIN? Spin magnitude is OPEN ISSUE

Models of stellar evolution usually neglect or simplify MAGNETIC FIELD

→ Angular momentum from stellar core efficiently dissipated via magnetic effect - e.g. **Tayler-Spruit dynamo** (Spruit 2002)



**Final core spins
are close to zero
with Tayler-Spruit
dynamo**

Fuller & Ma 2019, ApJ, 881, L1

Does it work for some / all stars?

References:

* M. Mapelli, Formation channels of Single and Binary Stellar-Mass Black Holes, Chapter of the Book “Handbook of Gravitational Wave Astronomy”, 2021, Springer,
<https://ui.adsabs.harvard.edu/abs/2021hgwa.bookE...4M/abstract>

and MANY references therein