

Team Notebook

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1 BasicTemplate

1.1 Sagor

```
#include<bits/stdc++.h>
#define ll long long
#define yes cout << "YES" << endl
#define no cout << "NO" << endl
#define testing cout << "testing ";
#define mod 1000000007
#define optimize() ios_base::sync_with_stdio(0);cin.tie(0);
                           cout.tie(0);
using namespace std;

void do_the_honour(){

}

int main(){
    optimize();
    int t=1;
    cin>>t;
    for(int z=1;z<=t;z++){
        do_the_honour();
    }
    return 0;
}
```

2 Data Structures

2.1 2DBit

```
int bit[1001][1001];
int n;

void update(int x, int y, int val) {
    for (; x <= n; x += (x & (-x))) {
        for (int i = y; i <= n; i += (i & (-i))) { bit[x][i]
            += val; }
    }
}

int query(int x1, int y1, int x2, int y2) {
    int ans = 0;
    for (int i = x2; i; i -= (i & (-i))) {
```

```
        for (int j = y2; j; j -= (j & (-j))) { ans += bit[i][j]; }
    }
    for (int i = x2; i; i -= (i & (-i))) {
        for (int j = y1 - 1; j; j -= (j & (-j))) { ans -= bit[i][j]; }
    }
    for (int i = x1 - 1; i; i -= (i & (-i))) {
        for (int j = y2; j; j -= (j & (-j))) { ans -= bit[i][j]; }
    }
    for (int i = x1 - 1; i; i -= (i & (-i))) {
        for (int j = y1 - 1; j; j -= (j & (-j))) { ans += bit[i][j]; }
    }
    return ans;
}

int main() {
    iostream::sync_with_stdio(false);
    cin.tie(0);
    int q;
    cin >> n >> q;
    for (int i = 1; i <= n; i++) {
        for (int j = 1; j <= n; j++) {
            char c;
            cin >> c;
            if (c == '*') update(j, i, 1);
        }
    }
    while (q--) {
        int t;
        cin >> t;
        if (t == 1) {
            int x, y;
            cin >> y >> x;
            if (query(x, y, x, y)) update(x, y, -1);
            else update(x, y, 1);
        } else {
            int y1, x1, y2, x2;
            cin >> y1 >> x1 >> y2 >> x2;
            cout << query(x1, y1, x2, y2) << '\n';
        }
    }
    return 0;
}
```

2.2 Bit

```
int bit[100005];
```

```
void update(int i,int x){
    for(;i<=n;i+=(i&-i)){
        bit[i]+=x;
    }
}

int sum(int i){

    long ans=0;
    for(;i>0;i-=(i&-i)) ans+=bit[i];
    return ans;
}
```

2.3 kadane

```
sum = ans = ara[0];
int u = 0, v = 0;
for (int K = 1; K < n; K++) {
    if (sum + ara[K] >= ara[K]) {
        sum += ara[K];
        v++;
    } else {
        sum = ara[K];
        u = v = K;
    }
    if (sum > ans) {
        ans = sum;
        ans_l = u;
        ans_r = v;
    }
}
```

2.4 mergesortTree

```
vector<int> treee[800008];

int arr[200002];
//give call init(1,1,n);
```

```
void init(int node,int b,int e){

    if(b==e){
        int x=arr[b];
```

```

treee[node].push_back(x);
    return;
}
int left=node*2;
int right =node*2+1;
int mid=(b+e)/2;

init(left,b,mid);
init(right,mid+1,e);

int i=0;
int j=0;
while(i<treee[left].size() and j<treee[right].size()){
    int x=treee[left][i];
    int y=treee[right][j];
    if(x<=y){
        treee[node].push_back(x);
        i++;
    }
    else treee[node].push_back(y),j++;
}

while(i<treee[left].size()){
    int x=treee[left][i];
    treee[node].push_back(x);
    i++;
}

while(j<treee[right].size()){
    int x=treee[right][j];
    treee[node].push_back(x);
    j++;
}

int query(int node,int b,int e,int i, int j){
    if(i>e or j<b) return 0;
    if(b>=i and e<=j) {
        return treee[node].end()-(upper_bound(treee[node].begin()
            ,treee[node].end(),j));
    }

    int left=node*2;
    int right =node*2+1;
    int mid=(b+e)/2;
    int p1=query(left,b,mid,i,j);
    int p2=query(right,mid+1,e,i,j);
}

```

```

    return p1+p2;
}

void do_the_honour(){

    int n,k;cin >> n >> k;

    int a[n+1];
    for(int i=1;i<=n;i++) cin >> a[i];

    unordered_map<int,int>mp;
    for(int i=n;i>=1;i--){
        if(mp[a[i]]==0){
            arr[i]=n+1;
            mp[a[i]]=i;
        }
        else{
            arr[i]=mp[a[i]];
            mp[a[i]]=i;
        }
    }

    init(1,1,n);

    while(k--){
        int l,r;cin >> l >> r;
        cout << query(1,1,n,l,r) << endl;
    }
}

```

2.5 MO

```

//1-mo's algo

int blk=700;
int cnt[1000001];
int val=0;
int a[200001];

int lb=0,rb=-1;

bool cmp(tuple<int,int,int>&a,tuple<int,int,int>&b){

```

```

if(get<0>(a)/blk != get<0>(b)/blk)
    return get<0>(a)/blk <= get<0>(b)/blk;
else return get<1>(a) < get<1>(b);

}

void add(int i){

    val-=cnt[a[i]]*cnt[a[i]]*a[i];
    cnt[a[i]]++;
    val+=cnt[a[i]]*cnt[a[i]]*a[i];

}

void remove(int i){

    val-=cnt[a[i]]*cnt[a[i]]*a[i];
    cnt[a[i]]--;
    val+=cnt[a[i]]*cnt[a[i]]*a[i];
}

void do_the_honour(){

    int n;cin >> n;

    vector<tuple<int,int,int>>v;
    int q;cin >> q;

    for(int i=0;i<n;i++) cin >> a[i];

    for(int i=0;i<q;i++){
        int l,r;cin >> l >> r;
        l--,r--;
        v.push_back({l,r,i});
    }

    sort(v.begin(),v.end(),cmp);

    int ans[q];

    for(int i=0;i<q;i++){

```

```

auto [l,r,id]=v[i];
while(lb>l) lb--,add(lb);
while(rb<r) rb++,add(rb);

while(lb<l) remove(lb),lb++;
while(rb>r) remove(rb),rb--;
ans[id]=val;
}

for(auto u:ans) cout << u << endl;
}

```

2.6 OrderedSet

```

#include<ext/pb_ds/assoc_container.hpp>
#include<ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

template<class T> using oset=tree<T,null_type,less<T>,
          rb_tree_tag,tree_order_statistics_node_update>;
//oset<int>s;
//**s.find_by_order(x) //x-th largest element;
//s.order_of_key(x) //num of elements strictly less than x

```

2.7 polynomialqueries

```

#define MP make_pair
using ap = pair<int,int>;

struct node{
    ap lazy;
    int sum;
    node(){
        lazy ={0,0};
        sum=0;
    }
};

node merge(node a,node b){

    node ans;
    ans.sum=a.sum+b.sum;
    return ans;
}

```

```

node t[800033];
int arr[200004];

void push_down(ap cur, int child){

    t[child].lazy.first += cur.first;
    t[child].lazy.second += cur.second;
}

inline int getnth(ap cur,int n){

    return (cur.first+(n-1)*cur.second);
}

inline int getsum(ap cur,int n){

    return (n*(2*cur.first+(n-1)*cur.second))/2;
}

void push(int id,int l,int r){

    if(t[id].lazy==ap{0,0}) return;

    if(l!=r){
        push_down(t[id].lazy,id<<1);
        int mid=(l+r)/2;
        int n=mid+1-(l-1);
        int newa = getnth(t[id].lazy,n);
        push_down({newa,t[id].lazy.second},id<<1|1);
    }

    t[id].sum += getsum(t[id].lazy,r-l+1);
    t[id].lazy={0,0};
}

void update(int id,int l,int r,int lq,int rq,int a,int d){

    push(id,l,r);
    if(lq>r or rq<l) return;
    if(lq<=l and r<=rq){
        t[id].lazy={(l-lq+1),d};
        push(id,l,r);
        return;
    }
}

```

```

int mid=(l+r)/2;
update(2*id,l,mid,lq,rq,a,d);
update(2*id+1,mid+1,r,lq,rq,a,d);
t[id]=merge(t[id<<1],t[id<<1|1]);

}

int query(int id,int l,int r, int lq,int rq){

    push(id,l,r);
    if(lq>r or l>rq) return 0;
    if(lq<=l and r<=rq) return t[id].sum;

    int mid = (l + r) / 2;
    return (query(2*id,l,mid,lq,rq)+query(2*id+1,mid+1,r,lq,
        rq));
}

void build(int id,int l,int r){

    if(l==r){
        t[id].sum=arr[l];
        t[id].lazy={0,0};
        return;
    }
    int mid=(l+r)/2;
    build(2*id,l,mid);
    build(2*id+1,mid+1,r);
    t[id]=merge(t[2*id],t[2*id+1]);
}

void do_the_honour(){

    int n;cin >> n;
    int q;cin >> q;

    for(int i=1;i<=n;i++) cin >> arr[i];
    build(1,1,n);
    // cout << query(1,1,n,3,5) << endl;

    while(q--){
        int c,a,b,x; cin >> c;

```

```

if(c==1){
    cin >> a >> b;
    update(1,1,n,a,b,1,1);
}
else{
    cin >> a >> b;
    int ans=query(1,1,n,a,b);
    cout << ans << endl;
}
}

```

2.8 RangeUpdateSetSum

```

struct node{
    int lazy_add;
    int lazy_set;
    int sum;
    node(){
        lazy_add=0;
        lazy_set=0;
        sum=0;
    }
};

node merge(node a,node b){

    node ans;
    ans.sum=a.sum+b.sum;
    return ans;
}

node t[800033];
int arr[200004];

void push_down(int cur, int child){

    if(t[cur].lazy_set!=0){
        t[child].lazy_set=t[cur].lazy_set;
        t[child].lazy_add=0;
    }
    else{
        if(t[child].lazy_set!=0){
            t[child].lazy_set+=t[cur].lazy_add;
        }
        else{

```

```

            t[child].lazy_add+=t[cur].lazy_add;
        }
    }
}

void push(int id,int l,int r){

    if(t[id].lazy_add==0 and t[id].lazy_set==0) return;

    if(l!=r){
        push_down(id,id<<1);
        push_down(id,id<<1|1);
    }

    if(t[id].lazy_add!=0){
        t[id].sum += (r-l+1)*t[id].lazy_add;t[id].
            lazy_add=0;
    }
    else if(t[id].lazy_set!=0){
        t[id].sum = (r-l+1)*t[id].lazy_set; t[id].
            lazy_set=0;
    }
}

void update(int id,int l,int r,int lq,int rq,int val,int
utype){

    push(id,l,r);
    if(lq>r or rq<l) return;
    if(lq<=l and r<=rq){
        if(utype==0){
            t[id].lazy_set=val;
        }
        else{
            t[id].lazy_add+=val;
        }
        push(id,l,r);
        return;
    }

    int mid=(l+r)/2;
    update(2*id,l,mid,lq,rq,val,utype);
    update(2*id+1,mid+1,r,lq,rq,val,utype);
    t[id]=merge(t[id<<1],t[(id<<1)|1]);
}

```

```

int query(int id,int l,int r, int lq,int rq){

    push(id,l,r);
    if(lq>r or l>rq) return 0;
    if(lq<=l and r<=rq) return t[id].sum;

    int mid = (l + r) / 2;
    return (query(2*id,l,mid,lq,rq)+query(2*id+1,mid+1,r,lq,
rq));
}

void build(int id,int l,int r){

    if(l==r){
        t[id].sum=arr[l];
        t[id].lazy_add=0;
        t[id].lazy_set=0;
        return;
    }
    int mid=(l+r)/2;
    build(2*id,l,mid);
    build(2*id+1,mid+1,r);
    t[id]=merge(t[2*id],t[2*id+1]);
}

void do_the_honour(){

    int n;cin >> n;
    int q;cin >> q;

    for(int i=1;i<=n;i++) cin >> arr[i];

    build(1,1,n);
    // cout << query(1,1,n,3,5) << endl;

    while(q--){
        int c,a,b,x; cin >> c;
        if(c==1){
            cin >> a >> b >> x;
            update(1,1,n,a,b,x,1);
        }
        else if(c==2){
            cin >> a >> b >> x;

```

```

        update(1,1,n,a,b,x,0);
    }
    else{
        cin >> a >> b;
        int ans=query(1,1,n,a,b);
        cout << ans << endl;
    }
}

```
range update set and sum

```

## 2.9 Segmenttree

```

int tree[400004];
int arr[100001];
//give call init(1,1,n);
void init(int node,int b,int e){

 if(b==e){
 tree[node]=arr[b];
 return;
 }
 int left=node*2;
 int right =node*2+1;
 int mid=(b+e)/2;

 init(left,b,mid);
 init(right,mid+1,e);
 tree[node]=tree[left]+tree[right];

}

int query(int node,int b,int e,int i, int j){

 if(i>e or j<b) return 0;
 if(b>=i and e<=j) return tree[node];

 int left=node*2;
 int right =node*2+1;
 int mid=(b+e)/2;
 int p1=query(left,b,mid,i,j);
 int p2=query(right,mid+1,e,i,j);
 return p1+p2;
}

void update(int node,int b,int e,int i,int newvalue){

 if(i>e or i<b) return;

```

```

 if(b>=i and e<=i){
 tree[node]=newvalue;
 return;
 }
 int left=2*node;
 int right=node*2+1;
 int mid=(b+e)/2;
 update(left,b,mid,i,newvalue);
 update(right,mid+1,e,i,newvalue);
 tree[node]=tree[left]+tree[right];
 }

 //----lazy propagation----

 struct info{
 ll prop,sum;
 }tree[400001];

 int query(int node,int b, int e, int i, int j,int carry=0){
 if(i>e or j<b) return 0;
 if(b>=i and e<=j){
 return tree[node].sum+carry*(e-b+1);
 }

 int left=node*2;
 int right=node*2+1;
 int mid=(b+e)/2;

 int p1=query(left, b, mid, i, j,carry+tree[node].prop);
 int p2=query(right, mid+1, e, i,j,carry+tree[node].prop)
 ;
 return p1+p2;
 }

 void update(int node,int b,int e,int i,int j,ll x){
 if(i>e or j<b) return;
 if(b>=i and e<=j){

 tree[node].sum+=((e-b+1)*x);
 tree[node].prop+=x;
 return;
 }

 int left=node*2;
 int right =node*2+1;
 int mid=(b+e)/2;
 update(left,b,mid,i,j,x);
 update(right,mid+1,e,i,j,x);
 }
}

```

```

 tree[node].sum=tree[left].sum+tree[right].sum+(e-b+1)*
 tree[node].prop;
 }
}

```

## 2.10 SqrtDecomp

```

int n;
int a[500002];
int blk = 800;
int F[801];

// don't forget to call preprocess();
// static range min query

int getmin(int l, int r)
{
 int lb = l / blk;
 int rb = r / blk;

 int mn = 0;
 if (lb == rb)
 {
 for (int i = l; i <= r; i++)
 mn += a[i];
 return mn;
 }

 for (int i = l; i < min(r, (lb + 1) * blk); i++)
 mn += a[i];
 for (int i = lb + 1; i < rb; i++)
 mn += F[i];
 for (int i = blk * rb; i <= r; i++)
 mn += a[i];

 return mn;
}

void do_the_honour()
{
 for (int i = 0; i < 600; i++)
 F[i] = 0;
 cin >> n;
 int k;
 cin >> k;
 for (int i = 0; i < n; i++)
 {

 cin >> a[i];
 }
}

```

```

 F[i / blk] += a[i];
 }

 while (k--)
 {
 int l, r;
 cin >> l >> r;
 l--;
 r--;
 cout << getmin(l, r) << endl;
 }
}

```

## 3 DP

### 3.1 BitmaskDp

```

//bitmask DP: number of permutaton of length n such that no
//two adjacent elements diff are greater than k

ll int n,k;
vector<ll int>v;

ll dp[17][(1<<17)];
ll func(int id,int mask){

 if(mask==0) return 1;
 if(dp[id][mask]!=-1) return dp[id][mask];
 ll int ans=0;
 for(ll int i=0;i<=(n-1);i++){
 if(abs(i-id)>k) continue;
 if(mask&(1<<i)){
 ans+=func(i,mask^(1<<i));
 }
 }
 return dp[id][mask]=ans;
}

void do_the_honour(){

 cin >> n >> k;
 memset(dp,-1,sizeof dp);

 for(int i=0;i<n;i++) v.push_back(i);

 ll ans=0;
 for(int i=0;i<n;i++) ans+=func(i,((1<<n)-1)^(1<<i)) ;
 cout << ans << endl;
}

```

```

 }

3.2 DigitDp

```

//digit dp template: find number from a to b such that that
//number and sum of digits of that number are divisible
//by k
ll dp[10][82][2][1000];
int k;
ll func(string &s,int pos=0,int sum=0,int tight=1,int x=0){

    if(pos==s.size()){
        if(x%k==0 and sum%k==0) return 1;
        else return 0;
    }

    if(dp[pos][sum][tight][x]!=-1) return dp[pos][sum][tight]
        ][x];
    ll res=0;
    if(tight==1){

        for(int i=0;i<(s[pos]-'0');i++){
            res+=func(s,pos+1,sum+i,0,(x*10+i)%k);
        }
        res+=func(s,pos+1,sum+(s[pos]-'0'),1,(x*10+(s[pos]
            ]-'0'))%k);
    }
    else{
        for(int i=0;i<9;i++){
            res+=func(s,pos+1,sum+i,0,(x*10+i)%k);
        }
    }

    return dp[pos][sum][tight][x]=res;
}

void do_the_honour(int t){

    memset(dp,-1,sizeof(dp));
    int a,b;cin >> a >> b >>k;
    a--;
    string x=to_string(a);
    string y=to_string(b);

    ll cnt1=func(x);
    memset(dp,-1,sizeof(dp));
    ll cnt2=func(y);
    cout << "Case " << t << ":" << cnt2 - cnt1 << endl;
}

```


```

```

 }

```

## 4 GeoMetry

### 4.1 closestpair

```

// To find the closest pair of points
long long
closestPair(vector<pair<long long, long long> > coordinates,
 int n)

{
 // Sort points according to x-coordinates
 sort(coordinates.begin(), coordinates.end());

 // Set to store already processed points whose distance
 // from the current points is less than the smaller
 // distance so far
 set<pair<long long, long long> > s;

 long long squaredDistance = LLONG_MAX;
 long long j = 0;

 for (long long i = 0; i < n; ++i) {
 // Find the value of D
 long long D = ceil(sqrtl(squaredDistance));
 while (coordinates[i].first - coordinates[j].first >=
 D) {
 s.erase({ coordinates[j].second, coordinates[j].
 first });
 j += 1;
 }

 // Find the first point in the set whose y-
 // coordinate is less than D distance from ith
 // point
 auto start
 = s.lower_bound({ coordinates[i].second - D,
 coordinates[i].first });
 // Find the last point in the set whose y-
 // coordinate is less than D distance from ith
 // point
 auto end
 = s.upper_bound({ coordinates[i].second + D,
 coordinates[i].first });

 // Iterate over all such points and update the
 // minimum distance
 }
}

```

```

for (auto it = start; it != end; ++it) {
 long long dx = coordinates[i].first - it->second;
 long long dy = coordinates[i].second - it->first;
 squaredDistance = min(squaredDistance, 1LL * dx *
 dx + 1LL * dy * dy);
}

// Insert the point as {y-coordinate, x-coordinate}
s.insert({ coordinates[i].second,
 coordinates[i].first });

}

return squaredDistance;
}
closestPair(v,v.size());

```

## 4.2 convexhull

```

typedef pair<int, int> Point;

// Function to determine the orientation of the triplet (p, q, r).
int orientation(const Point& p, const Point& q, const Point& r) {
 int val = (q.second - p.second) * (r.first - q.first) - (
 q.first - p.first) * (r.second - q.second);
 if (val == 0) return -1; // Collinear
 return (val > 0) ? 1 : -1; // Clockwise or
 Counterclockwise
}

// Function to compute the convex hull using Andrew's
// monotone chain algorithm
vector<Point> convexHull(vector<Point>& points) {
 int n = points.size();
 if (n < 3) return points;

 // Sort points lexicographically (by x first, then by y)
 sort(points.begin(), points.end());

 vector<Point> hull;

 // Build the lower hull
 for (int i = 0; i < n; ++i) {
 while (hull.size() >= 2 && orientation(hull[hull.size() -
 () - 2], hull.back(), points[i]) != -1) {
 hull.pop_back();
 }
 hull.push_back(points[i]);
 }
}

```

```

}

// Build the upper hull, avoiding the last point of the
// lower hull
for (int i = n - 2, t = hull.size() + 1; i >= 0; --i) {
 while (hull.size() >= t && orientation(hull[hull.size() -
 () - 2], hull.back(), points[i]) != -1) {
 hull.pop_back();
 }
 hull.push_back(points[i]);
}

hull.pop_back(); // Remove the last point because it is
// the same as the first one

return hull;
}

```

## 4.3 Linesegment

```

// Function to find the orientation of the ordered triplet (p, q, r)
// The function returns:
// 0 -> p, q and r are collinear
// 1 -> Clockwise
// 2 -> Counterclockwise
int orientation(pair<int, int> p, pair<int, int> q, pair<int,
 int> r) {
 int val = (q.second - p.second) * (r.first - q.first) - (
 q.first - p.first) * (r.second - q.second);
 if (val == 0) return 0;
 return (val > 0) ? 1 : 2;
}

// Function to check if point q lies on segment pr
bool onSegment(pair<int, int> p, pair<int, int> q, pair<int,
 int> r) {
 if (q.first <= max(p.first, r.first) && q.first >= min(p.
 first, r.first) &&
 q.second <= max(p.second, r.second) && q.second >=
 min(p.second, r.second))
 return true;
 return false;
}

// Function to check if the line segments 'p1q1' and 'p2q2'
// intersect

```

```

bool doIntersect(pair<int, int> p1, pair<int, int> q1, pair<
 int, int> p2, pair<int, int> q2) {
 // Find the four orientations needed for general and
 // special cases
 int o1 = orientation(p1, q1, p2);
 int o2 = orientation(p1, q1, q2);
 int o3 = orientation(p2, q2, p1);
 int o4 = orientation(p2, q2, q1);

 // General case
 if (o1 != o2 && o3 != o4)
 return true;

 // Special Cases
 // p1, q1 and p2 are collinear and p2 lies on segment
 // p1q1
 if (o1 == 0 && onSegment(p1, p2, q1)) return true;

 // p1, q1 and q2 are collinear and q2 lies on segment
 // p1q1
 if (o2 == 0 && onSegment(p1, q2, q1)) return true;

 // p2, q2 and p1 are collinear and p1 lies on segment
 // p2q2
 if (o3 == 0 && onSegment(p2, p1, q2)) return true;

 // p2, q2 and q1 are collinear and q1 lies on segment
 // p2q2
 if (o4 == 0 && onSegment(p2, q1, q2)) return true;

 // Doesn't fall in any of the above cases
 return false;
}

void do_the_honour() {
 int x1, y1, x2, y2, x3, y3, x4, y4;
 cin >> x1 >> y1 >> x2 >> y2 >> x3 >> y3 >> x4 >> y4;

 pair<int, int> p1 = {x1, y1}, q1 = {x2, y2}, p2 = {x3, y3},
 q2 = {x4, y4};

 if (doIntersect(p1, q1, p2, q2)) yes;
 else no;
}

```

## 4.4 pointlocation

```

void do_the_honour() {
 int x1, y1, x2, y2, x3, y3;

```

```

cin >> x1 >> y1 >> x2 >> y2 >> x3 >> y3;

int cross_product = (x2 - x1) * (y3 - y2) - (y2 - y1) * (x3 - x2);

if (cross_product == 0) {
 cout << "TOUCH" << endl;
} else if (cross_product > 0) {
 cout << "LEFT" << endl;
} else {
 cout << "RIGHT" << endl;
}
}

```

## 4.5 polygonLatticepoints

```

int area(vector<pair<int, int>> vertices){

 int n=vertices.size();

 int area = 0;
 for (int i = 0; i < n; i++) {
 int j = (i + 1) % n;
 area += vertices[i].first * vertices[j].second;
 area -= vertices[i].second * vertices[j].first;
 }

 return abs(area);
}

int latticeonboundary(pair<int,int>p1,pair<int,int>p2){

 int a=abs(p1.first-p2.first);
 int b=abs(p1.second-p2.second);

 return (_gcd(a,b)-1);
}

//A=i+b/2-1
void do_the_honour(){

```

```

int n;cin >> n;
vector<pair<int,int>>vp;
for(int i=0;i<n;i++){
 int x,y; cin >> x >> y;
 vp.push_back({x,y});
}

int total=area(vp)/2;

int boundary=0;

for(int i=0;i<n;i++){
 boundary+= latticeonboundary(vp[i],vp[(i+1)%n]);
}

boundary+=n;

cout << total+1-(boundary/2) << " " << boundary << endl;
}

```

## 5 Graph

### 5.1 BeckedgeDetection

```

void Graph::dfs(int v, int parent) {
 visited[v] = true;
 tin[v] = low[v] = timer++;
 subtreeSize[v] = 1;

 for (int to : adj[v]) {
 if (to == parent) continue;
 if (visited[to]) {
 low[v] = min(low[v], tin[to]);
 } else {
 dfs(to, v);
 low[v] = min(low[v], low[to]);
 if (low[to] > tin[v]) {
 // Back edge detected between v and to
 int x = subtreeSize[to];
 int y = vertices - x;
 totalPairs = min(totalPairs, calculatePairs(x)
 + calculatePairs(y));
 }
 subtreeSize[v] += subtreeSize[to];
 }
 }
}

```

```

}

void Graph::countSubtreeSizes(int v, int parent) {
 visited[v] = true;
 subtreeSize[v] = 1;
 for (int to : adj[v]) {
 if (to != parent && !visited[to]) {
 countSubtreeSizes(to, v);
 subtreeSize[v] += subtreeSize[to];
 }
 }
}

```

## 5.2 BellMenFord

```

//bellmen_ford for negative cycle and printing suc a cycle
class triplet{
public:
 int first;
 int second;
 int third;
};

int n, m;
vector<triplet> edges;
vector<int> dist;
vector<int> relaxant;
void bellman_ford()
{
 int x;
 for(int i = 1; i <= n; ++i)
 {
 x = -1;
 for(auto e: edges)
 {

 int u = e.first;
 int v = e.second;
 int d = e.third;
 if(dist[u]+d < dist[v])
 {
 dist[v] = d+dist[u];
 relaxant[v] = u;
 x = v;
 }
 }
 }
 // n relaxations
}

if(x == -1)

```

```

cout << "NO" << endl;
else
{
 for(int i = 1; i <= n; ++i)
 {
 x = relaxant[x];
 }

 vector<int> cycle;
 for(int v = x; ; v = relaxant[v])
 {
 cycle.push_back(v);
 if(v == x and cycle.size() > 1)
 break;
 }

 reverse(cycle.begin(), cycle.end());
 cout << "YES" << endl;
 for(auto v: cycle)
 {
 cout << v << " ";
 }
 cout << endl;
}

int32_t main()
{
 cin >> n >> m;
 dist.resize(n+1);
 relaxant.resize(n+1);
 edges.resize(m);

 for(int i = 0; i < m; ++i)
 {
 struct triplet inp;
 cin >> inp.first >> inp.second >> inp.third;
 edges[i] = inp;
 }

 for(int i = 1; i <= n; ++i)
 {
 relaxant[i] = -1;
 }
}

```

```

 bellman_ford();
}

```

### 5.3 BipartiteMatching

```

int k;
int m; cin >> n >> m >>k;
int src=0,dest=n+m+1;
for (int i = 0; i < k; i++) {
 int x, y, w = 1; cin >> x >> y;
 capacity[x][y+n] = w;

 adj[x].push_back(y+n);
 adj[y+n].push_back(x);
 adj2[x][y+n] = 1;

}
for(int i=1;i<=n;i++)
{
 adj[src].push_back(i);
 adj[i].push_back(src);
 capacity[src][i]=1;
 adj2[0][i]=1;
}
for(int i=1;i<=m;i++)
{
 adj[i+n].push_back(dest);
 adj[dest].push_back(i+n);
 capacity[i+n][dest]=1;
 adj2[n+i][dest]=1;
}

cout << maxflow(src, dest) << endl;

fill(vis, vis + 10001, 0); // Reset the visited array
dfs(0);

for (int i = 1; i <= n; i++) {
 for (int j = n+1; j <= n+m; j++) {
 if ((capacity[i][j]==0) and (adj2[i][j]==1)) {
 ans.push_back({i, j-n});
 }
 }
}

```

```

for (auto u : ans) cout << u.first << " " << u.second << endl;

```

### 5.4 cycle in directed graph

```

vector<int>adj[200001];
vector<vector<int>>v;
int par[200001];
int color[200001];
bool f=0;
void dfs(int node,int pp){

if(color[node]==2) return;
if(f) return;
if(color[node]==1){
 vector<int>x;
 int p=pp;
 x.push_back(p);
 while(p!=node){ p=par[p];
 x.push_back(p);
 }
 reverse(x.begin(),x.end());
 v.push_back(x);
 if(x.size()>=2) f=1;
 x.clear();
 return ;
}
color[node]=1;
par[node]=pp;

for(auto u:adj[node]){
 if(u==pp) continue;
 dfs(u,node);
}
color[node]=2;
}

void do_the_honour(){

int n,m;cin >> n >> m;
map<pair<int,int>,bool>mp;

int b=-1,cc=-1;
for(int i=0;i<m;i++){
 int x,y; cin >> x >> y;
 adj[x].push_back(y);
 mp[{x,y}]=1;
}
}

```

```

 if(mp[{y,x}]){
 b=x,cc=y;
 }
 //adj[y].push_back(x);
 }
 if(b!=-1){
 cout << 3 << endl;
 cout << b << " " << cc << " " << b << endl;
 return;
 }

 for(int i=1;i<=n;i++){
 if(color[i]!=0) continue;
 dfs(i,0);
 }

 int sz=0;
 vector<int>ans;
 for(auto u:v){
 if(sz<u.size()){
 sz=u.size();
 ans=u;
 }
 }
 if(sz>=3){
 cout << ans.size()+1 << endl;
 for(auto u:ans) cout << u << " ";
 cout << ans[0] << endl;
 cout << endl;
 }
 else cout << "IMPOSSIBLE" << endl;
}

```

## 5.5 De Brujin

```

unordered_set<string> seen;
vector<int> edges;
void dfs(string node, int& k, string& A)
{
 for (int i = 0; i < k; ++i) {
 string str = node + A[i];
 if (seen.find(str) == seen.end()) {
 seen.insert(str);
 dfs(str.substr(1), k, A);
 edges.push_back(i);
 }
 }
}

```

```

 }
 }
 string deBruijn(int n, int k, string A)
 {

 seen.clear();
 edges.clear();

 string startingNode = string(n - 1, A[0]);
 dfs(startingNode, k, A);

 string S;

 // Number of edges
 int l = pow(k, n);
 for (int i = 0; i < l; ++i)
 S += A[edges[i]];
 S += startingNode;

 return S;
 }

 // Driver code
 int main()
 {
 int n = 3, k = 2;
 cin >> n;
 string A = "01";
 cout << deBruijn(n, k, A);
 return 0;
 }
}

```

## 5.6 Dijkstra with kth minimum path

```

const int N=2e5+3;
const int INF=1e15+10;
vector<pair<int,int>>g[N];
priority_queue<int>d[200001];
void dijkstra(int k){

 vector<int>dist(N,INF);
 vector<bool>vis(N,0);

 multiset<pair<int,int>>st;
 st.insert({0,1});

```

```

while(st.size()>0){
 auto node=*st.begin();
 st.erase(st.begin());
 int v=node.second;
 int v_dis=node.first;

 if(d[v].top()<v_dis) continue;

 for(auto child:g[v]){
 int child_v=child.first;
 int wt=child.second;
 if(v_dis+wt<d[child_v].top()){
 d[child_v].pop();
 d[child_v].push(v_dis+wt);
 st.insert({l,child_v});
 }
 }
}

void do_the_honour(){

 int n,m,k;cin >> n >> m >> k;

 for(int i=0;i<m;i++){
 int u,v,w; cin >> u >> v >> w;
 g[u].push_back({v,w});
 }

 for(int i=1;i<=n;i++){
 for(int j=1;j<=k;j++){
 d[i].push(INF);
 }
 }
 d[1].pop();
 d[1].push(0);
 dijkstra(k);
 vector<int>v;
 //cout << d[n].size() << endl;
 while(!d[n].empty()){
 v.push_back(d[n].top());
 d[n].pop();
 }
 while(!v.empty()){
 cout << v.back() << " ";
 v.pop_back();
 }
}

```

```
cout << endl;
}
```

## 5.7 DSU

```
const int N=2e5+10;
int parent[N];
int Size[N];

void make(int v) {parent[v]=v;Size[v]=1;}

int Find(int v){
 if(v==parent[v]) return v;
 return (parent[v]=Find(parent[v]));
}

void Union(int a,int b){
 a=Find(a);
 b=Find(b);
 if(Size[a]<Size[b]) swap(a,b);
 if(a!=b) parent[b]=a;
 Size[a]+=Size[b];
}
```

## 5.8 Euler Circuit in undirected graph

```
void dfs(int node){

set<int>&ev=adj[node];
while(!ev.empty()){
 int u=ev.begin();
 ev.erase(ev.begin());
 adj[u].erase(node);
 dfs(u);
}
path.push_back(node);

}

void do_the_honour(){

int n,m;cin >> n >> m;

int in[n+1]={0},out[n+1]={0};
for(int i=0;i<m;i++){
 int x,y;cin >> x >> y;
 vp.push_back({x,y});
 in[y]++,out[x]++;
 adj[x].push_back(y);
}
}
```

```
adj[y].insert(x);
}

for(int i=1;i<=n;i++){
 if(adj[i].size()&1){
 cout << "IMPOSSIBLE" << endl;//every node must
 have even degree;
 return;
 }

 dfs(i);
 if(path.size()!=m+1){
 cout << "IMPOSSIBLE" << endl;
 }
 else{
 for(auto u:path) cout << u << " ";
 }
}
```

## 5.9 Euler tour in directed graph

```
vector<pair<int,int>>vp;
vector<int>adj[200001];
set<int>seen;
vector<int>path;
void dfs(int node){

while(!adj[node].empty()){
 int x=adj[node].back();
 adj[node].pop_back();
 dfs(x);

}
path.push_back(node);

}

void do_the_honour(){

int n,m;cin >> n >> m;

int in[n+1]={0},out[n+1]={0};
for(int i=0;i<m;i++){
 int x,y;cin >> x >> y;
 vp.push_back({x,y});
 in[y]++,out[x]++;
 adj[x].push_back(y);
}
}
```

```
int c=0;
int s,e,ss=0,ee=0;
for(int i=1;i<=n;i++){
 if(in[i]-out[i]==0) c++;
 if(in[i]-out[i]==1) ee++,e=i;
 if(in[i]-out[i]==-1) ss++,s=i;
}

if(c!=n-2 or s!=1 or e!=n or ee!=1 or ss!=1) cout << "
IMPOSSIBLE";
else{
 dfs(1);
 if(path.size()!=m+1) cout << "IMPOSSIBLE";
 else{
 reverse(path.begin(),path.end());
 for(auto u:path) cout << u << " ";
 }
}
```

## 5.10 HamiltonTour

```
//visits each node exactly once
int n,m;
vector<int>adj[2000];
int dp[22][1<<22];
int dfs(int node,int mask){

if(mask==(1<<(n))-1) return 1;
else if(node==n-1) return 0;

if(~dp[node][mask]) return dp[node][mask];

int ans=0;
for(auto u:adj[node]){
 if(mask&(1<<u)) continue;
 ans+=dfs(u,mask|(1<<u));
 ans%=mod;
}

return dp[node][mask]=ans;
}
```

## 5.11 Hopcroft

```
const int mx=1e4+10;
```

```

vector<int>adj[mx];
map<pair<int,int>,int>cost;
int pairU[mx],pairV[mx],dist[mx],a,b;
bool bfs()
{
 queue<int> Q;
 for (int u=1; u<=a; u++)
 {
 if (pairU[u]==0)
 {
 dist[u] = 0;
 Q.push(u);
 }
 else dist[u] = inf;
 }
 dist[0] = inf;
 while (!Q.empty())
 {
 int u = Q.front();
 Q.pop();
 if (dist[u] < dist[0])
 {
 for (auto it : adj[u])
 {
 int v = it;
 if (dist[pairV[v]] == inf)
 {
 dist[pairV[v]] = dist[u] + 1;
 Q.push(pairV[v]);
 }
 }
 }
 }
 return (dist[0] != inf);
}
bool dfs(int u)
{
 if (u != 0)
 {
 for (auto it : adj[u])
 {
 int v = it;
 if (dist[pairV[v]] == dist[u]+1)
 {

 if (dfs(pairV[v]) == true)
 {
 pairV[v] = u;
 pairU[u] = v;
 return true;
 }
 }
 }
 }
 return false;
}
int hopcroftKarp()
{
 for (int u=0; u<=a; u++)
 pairU[u] = 0;
 for (int v=0; v<=a; v++)
 pairV[v] = 0;
 int result = 0;
 while (bfs())
 {
 for (int u=1; u<=a; u++)
 {
 if (pairU[u]==0 && dfs(u)){
 result++;
 }
 }
 return result;
 }
}
main()
{
 cin>>a>>b;
 int x,y;
 for(int i=0;i<b;i++){
 cin>>x>>y;
 adj[y].push_back(x);
 int cost;
 cin>>cost;
 cost[{y,x}]=cost;
 }
 int ans=hopcroftKarp();
}

```

```

 }
}
return false;
}
return true;
}

int hopcroftKarp()
{
 for (int u=0; u<=a; u++)
 pairU[u] = 0;
 for (int v=0; v<=a; v++)
 pairV[v] = 0;
 int result = 0;
 while (bfs())
 {
 for (int u=1; u<=a; u++)
 {
 if (pairU[u]==0 && dfs(u)){
 result++;
 }
 }
 return result;
 }
}
main()
{
 cin>>a>>b;
 int x,y;
 for(int i=0;i<b;i++){
 cin>>x>>y;
 adj[y].push_back(x);
 int cost;
 cin>>cost;
 cost[{y,x}]=cost;
 }
 int ans=hopcroftKarp();
}

```

## 5.12 kosaraju

```

#include<bits/stdc++.h>
#define ll long long
#define yes cout << "YES" << endl
#define no cout << "NO" << endl
#define testing cout << "testing ";
#define mod 1000000007
#define optimize() ios_base::sync_with_stdio(0);cin.tie(0);
cout.tie(0);

```

```

using namespace std;
vector<int>adj[200010];
vector<int>trans[200010];
vector<bool> vis(200010,false);
vector<int>v,x;
void dfs(int node){
 vis[node]=1;
 for(auto u:adj[node]){
 if(vis[u]) continue;
 dfs(u);
 }
 v.push_back(node);
}
void dfs2(int node){
 //cout << node << " ";
 vis[node]=1;
 for(auto u:trans[node]){
 if(vis[u]) continue;
 dfs2(u);
 }
 x.push_back(node);
}
void do_the_honour(){
 int n;cin >> n;
 int m;cin >> m;
 for(int i=0;i<m;i++){
 int x,y; cin >> x >> y;
 adj[x].push_back(y);
 trans[y].push_back(x);
 }
 v.clear();
 for(int i=1;i<=n;i++) if(vis[i]==0) dfs(i);
 for(int i=0;i<200010;i++) vis[i]=false;
 reverse(v.begin(),v.end());
 int cc=0;

```

```

vector<vector<int>>ans;
int xx=0,xy=0;
for(auto u:v){
 if(vis[u]) continue;
 if(ans.size()==0) xx=u;
 else xy=u;
 x.clear();
 dfs2(u);
 ans.push_back(x);
 cc++;
}
// cout << endl;
if(ans.size()>1){
 cout << "NO" << endl;
 cout << xy<< " " << xx << endl;
}
else{
 cout << "YES" << endl;
}

void reset(){
 for(int i=0;i<200010;i++){
 adj[i].clear();
 vis[i]=0;
 v.clear();
 trans[i].clear();
 }
}

int main(){
 optimize();
 int t=1;
 // cin>>t;
 for(int z=1;z<=t;z++){
 reset();
 do_the_honour();
 }
 return 0;
}

```

## 5.13 LCA and kth ancestor

```

const int MAXN = 200001;
const int LOG = 20;

```

```

int dp[LOG][MAXN];
int level[MAXN];
vector<int> adj[MAXN];
void dfs(int node, int par) {
 dp[0][node] = par;
 for (int i = 1; i < LOG; i++) { // Fixed boundary to LOG
 dp[i][node] = dp[i - 1][dp[i - 1][node]];
 }
 for (auto u : adj[node]) {
 if (u == par) continue;
 level[u] = level[node] + 1;
 dfs(u, node);
 }
}
adj[x].push_back(y);
adj[y].push_back(x);
level[1] = 0;
dfs(1, 0);
dp[0][1] = 0;

if (level[a] < level[b]) swap(a, b), swap(x, y);
int diff = level[a] - level[b];

for (int i = 0; i < LOG; i++) { // Fixed boundary to LOG
 if (diff & (1 << i)) {
 a = dp[i][a];
 }
 if (a == b) {
 node = a;
 } else {
 for (int ii = LOG - 1; ii >= 0; ii--) { // Fixed boundary to LOG
 if (dp[ii][a] != dp[ii][b]) {
 a = dp[ii][a];
 b = dp[ii][b];
 }
 }
 node = dp[0][a];
 }
}

```

## 5.14 MaxFlow

```

const int INF=1e18;
int n;
vector<vector<int>> capacity(1001,vector<int>(1001,0));
vector<vector<int>> adj(1001);
vector<vector<int>> adj3(1001);
int adj2[501][501];

```

```

int vis[10001];
int vis2[1001];
vector<pair<int,int>>ans;
void dfs(int node){

 vis[node]=1;
 for(auto u:adj[node]){
 if(vis[u] or capacity[node][u]<=0) continue;
 dfs(u);
 }
}
int bfs(int s, int t, vector<int>& parent) {
 fill(parent.begin(), parent.end(), -1);
 parent[s] = -2;
 queue<pair<int, int>> q;
 q.push({s, INF});

 while (!q.empty()) {
 int cur = q.front().first;
 int flow = q.front().second;
 q.pop();

 for (int next : adj[cur]) {
 if (parent[next] == -1 && capacity[cur][next]) {
 parent[next] = cur;
 int new_flow = min(flow, capacity[cur][next]);
 if (next == t)
 return new_flow;
 q.push({next, new_flow});
 }
 }
 }
 return 0;
}

int maxflow(int s, int t) {
 int flow = 0;
 vector<int> parent(n+1);
 int new_flow;

 while (new_flow = bfs(s, t, parent)) {
 flow += new_flow;
 int cur = t;
 while (cur != s) {
 int prev = parent[cur];
 capacity[prev][cur] -= new_flow;
 capacity[cur][prev] += new_flow;
 cur = prev;
 }
 }
}
```

```

}

return flow;
}

void do_the_honour(){

int m;cin >> n >> m;
for(int i=0;i<m;i++){
 int x,y,w=1; cin >> x >> y ;
 capacity[x][y]+=w;
 capacity[y][x]+=w;
 adj[x].push_back(y);
 adj[y].push_back(x);
 adj2[x][y]=1;
 adj2[y][x]=1;

 adj3[x].push_back(y);
}

cout << maxflow(1,n) << endl;
dfs(1);
for(int i=1;i<=n;i++) for(int j=1;j<=n;j++) if(adj2[i][j]
 and vis[i] and !vis[j]) ans.push_back({i,j});

//cout << ans.size() << endl;
for(auto u:ans) cout << u.first << " " << u.second <<
endl;
}

finding max flow and cut edges for undirected graph

```

## 5.15 num of path with minimum weight

```

if(dist[v]+wt<dist[child_v]){
 dist[child_v]=dist[v]+wt;
 route[child_v]=route[v];
 min_f[child_v]=min_f[v]+1;
 max_f[child_v]=max_f[v]+1;
 st.push({dist[child_v],child_v});
}
else if(dist[v]+wt==dist[child_v]){

```

```

 route[child_v]+=route[v];
 route[child_v]%=mod;
 min_f[child_v]=min(min_f[v]+1,min_f[child_v]);
 max_f[child_v]=max(max_f[v]+1,max_f[child_v]);

 }
}
```

## 6 Math

### 6.1 bineexp

```

ll binexp(ll int a,ll int b,ll int m){
 ll res=1;
 while(b>0){
 if(b&1){
 res=(res*1LL*a)%m;
 }
 a=(a*1LL*a)%m;
 b>>=1;
 }
 return res;
}

```

### 6.2 BitwiseSieve

```

// Bitwise - sieve :- prime number generator;
// 0 for prime, 1 for not prime; >> Not sure ... #define MX
 10000000
int marked[MX / 64 + 2];
vector<int> primes;
#define mark(x) marked[x >> 6] |= (1 << ((x & 63) >> 1))
#define check(x)(marked[x >> 6] & (1 << ((x & 63) >> 1)))
bool isPrime(int x) { return (x > 1) && ((x == 2) || ((x &
1) && !(check(x)))); }
void sieve(int n) {
 int i, j;
 primes.push_back(2);
 for (i = 3; i * i <= n; i += 2) {
 if (!check(i)) {
 primes.push_back(i);
 for (j = i * i; j <= n; j += i << 1) mark(j);
 }
 }
}

```

## 6.3 divisors

```

// Maximal number of divisors of any n-digit number:
// First 18 numbers: 4, 12, 32, 64, 128, 240, 448, 768,
 1344, 2304, 4032, 6720, 10752, 17280, 26880, 41472,
 64512, 103680
// Number of divisors...
// Euler's totient function
// first, run a sieve for value sqrt(n);
vector<pair<int, int> > divisors;
void divs(int n) {
 int cnt, tot = 1, i;
 for (i = 0; i < (int)primes.size() && (primes[i] * primes[i
]) <= n; i++) {
 if (n % primes[i] == 0) {
 cnt = 1;
 while (n % primes[i] == 0) {
 n /= primes[i];
 cnt++;
 }
 divisors.push_back(make_pair(primes[i], cnt - 1));
 tot *= cnt;
 }
 }
 if (n > 1) {
 tot *= 2;
 divisors.push_back(make_pair(n, 1));
 }
 printf("Number of divisors %d\n", tot);
 for (i = 0; i < (int)divisors.size(); i++) printf("%d %d\n"
 , divisors[i].first, divisors[i].second);
}
// Number of divisors...
ll NOD(int n) {
 ll ans = 1;
 for (int K = 0; K < sz(divisors); K++) {
 ans *= (ll)(divisors[K].se + 1);
 }
 return ans;
}
// Sum of divisors...
ll SOD(int n) {
 ll ans = 1, cnt;
 for (int K = 0; K < sz(divisors); K++) {
 cnt = divisors[K].fi;
 while (divisors[K].se--) cnt *= (ll)divisors[K].fi;
 ans *= (ll)(cnt - 1) / (divisors[K].fi - 1);
 }
 return ans;
}

```

## 6.4 FFT

```

const int N = 3e5 + 9;

const double PI = acos(-1);
struct base {
 double a, b;
 base(double a = 0, double b = 0) : a(a), b(b) {}
 const base operator + (const base &c) const
 { return base(a + c.a, b + c.b); }
 const base operator - (const base &c) const
 { return base(a - c.a, b - c.b); }
 const base operator * (const base &c) const
 { return base(a * c.a - b * c.b, a * c.b + b * c.a); }
};

void fft(vector<base> &p, bool inv = 0) {
 int n = p.size(), i = 0;
 for(int j = 1; j < n - 1; ++j) {
 for(int k = n >> 1; k > (i ^= k); k >>= 1);
 if(j < i) swap(p[i], p[j]);
 }
 for(int l = 1, m; (m = l << 1) <= n; l <= 1) {
 double ang = 2 * PI / m;
 base wn = base(cos(ang), (inv ? 1. : -1.) * sin(ang)), w;
 for(int i = 0, j, k; i < n; i += m) {
 for(w = base(1, 0), j = i, k = i + l; j < k; ++j, w = w *
 wn) {
 base t = w * p[j + 1];
 p[j + 1] = p[j] - t;
 p[j] = p[j] + t;
 }
 }
 if(inv) for(int i = 0; i < n; ++i) p[i].a /= n, p[i].b /= n;
 }
}

vector<long long> multiply(vector<int> &a, vector<int> &b) {
 int n = a.size(), m = b.size(), t = n + m - 1, sz = 1;
 while(sz < t) sz <= 1;
 vector<base> x(sz), y(sz), z(sz);
 for(int i = 0 ; i < sz; ++i) {
 x[i] = i < (int)a.size() ? base(a[i], 0) : base(0, 0);
 y[i] = i < (int)b.size() ? base(b[i], 0) : base(0, 0);
 }
 fft(x, fft(y));
 for(int i = 0; i < sz; ++i) z[i] = x[i] * y[i];
 fft(z, 1);
 vector<long long> ret(sz);

```

```

 for(int i = 0; i < sz; ++i) ret[i] = (long long) round(z[i].a);
 while((int)ret.size() > 1 && ret.back() == 0) ret.pop_back();
 }
 return ret;
}

```

## 6.5 LinearSieve

```

const int MX = 10000001;
int lp[MX];
vector<int> pr;
void linear_sieve() {
 for(int i = 2; i < MX; ++i) {
 if(lp[i] == 0) {lp[i] = i; pr.PB(i);}
 for(int j = 0; j < (int)pr.size() && pr[j] <= lp[i] && (i *
 pr[j]) < MX; ++j) lp[i * pr[j]] = pr[j];
 }
}

```

## 6.6 MatrixExp

```

array<ll,4> mul(array<ll,4>x, array<ll,4>y){
 ll a=x[0],b=x[1],c=x[2],d=x[3];
 ll e=y[0],f=y[1],g=y[2],h=y[3];

 ll m=((a*e)%mod+(b*g)%mod)%mod;
 ll n=((a*f)%mod+(b*h)%mod)%mod;
 ll o=((c*e)%mod+(d*g)%mod)%mod;
 ll p=((c*f)%mod+(d*h)%mod)%mod;
 return {m,n,o,p};
}

array<ll,4> Find(ll n){
 if(n==1) return {1,1,1,0};
 array<ll,4>x=Find(n/2);

 if(n&1) return mul(mul(x,x),Find(1));
 else return mul(x,x);
}

void do_the_honour(){

```

```

 ll int n;cin >> n;

 if(n==0) cout << 0;
 else if(n==1) cout << 1;
 else if(n==2) cout << 1;
 else if(n==3) cout << 2;
 else{
 cout << Find(n-1)[0];
 }
}

```

## 6.7 nCrWithArray

```

// Complexity O(n)
const int MX = 1e6;
ll fact[MX + 5], inv[MX + 5];
void factorial() {
 fact[0] = fact[1] = 1;
 for (ll K = 1; K <= MX; K++) fact[K] = fact[K - 1] * K %
 mod;
 inv[MX] = inverse(fact[MX], mod);
 for (ll K = MX - 1; K >= 1; K--) inv[K] = inv[K + 1] * (K +
 1) % mod;
 inv[0] = 1;
}
// function call ...
factorial();
cout << (fact[18] * inv[5] % mod) * inv[13] % mod << "\n";
// Combinatorics problems can be done using stars and bars.
 The number of ways to put n identical objects into k
 labeled boxes is (n+k-1)C(n)
// while counting nCr where n,r size is big to get rid of
 overflow we can do this :
// Code:
minnrcr(k,n-k);
ll ans=1;
for(ll i=1;i<=k;i++){
 ans = (ans*(n-i+1)) / i ;
}

```

## 6.8 SegmentedSieve

```

// Block/Segmented Sieve:
// Output: prime list in range {L, R}; (R-L+1) <= 1e7 && R
 <= 1e12;

```

```

vector<char> segmentedSieve(long long L, long long R) { // generate all primes up to sqrt(R)
 long long lim = sqrt(R);
 vector<char> mark(lim + 1, false);
 vector<long long> primes;
 for (long long i = 2; i <= lim; ++i) {
 if (!mark[i]) {
 primes.emplace_back(i);
 for (long long j = i * i; j <= lim; j += i) mark[j] = true;
 }
 }
 vector<char> isPrime(R - L + 1, true);
 for (long long i : primes)
 for (long long j = max(i * i, (L + i - 1) / i * i); j <= R; j += i) isPrime[j - L] = false;
 if (L == 1) isPrime[0] = false;
 return isPrime;
}

```

## 6.9 Sieve

```

// sieve :- prime number generator;
// 0 for prime, 1 for not prime;
vector<int> primes;
vector<bool> mark(1000002);
void sieve(int n) {
 int i, j, limit = sqrt(n*1.) + 2;
 mark[1] = 1;
 for(i = 4; i<=n; i+=2) mark[i] = 1;
 primes.push_back(2);
 for(i = 3; i <= n; i += 2){
 if(!mark[i]){
 primes.push_back(i);
 if(i<=limit){
 for(j = i*i; j <= n; j += i*2){
 mark[j] = 1;
 }
 }
 }
 }
}

```

## 6.10 TotientFunction

```

#define MX 1e5+6;
// phi pre-calculation function . . .

```

```

ll phi[MX];
void phi_function()
{
 memset(phi, 0, sizeof phi);
 phi[1] = 1;
 for(int i=2; i<=MAX; ++i){
 if(phi[i]==0){
 phi[i]=i-1;
 for(int j=i+i; j<=MAX; j+=i){
 if(phi[j]==0) phi[j] = j;
 phi[j]= phi[j]/i * (i-1);
 }
 }
 }
 // gcd sum calculation function . . .
 ll table[MAX];
 void div()
 {
 memset(table, 0, sizeof table);
 for(int i=1;i<MAX;i++){
 for(int j=i+i;j<MAX;j=j+i){
 table[j]+=(i*phi[j/i]);
 }
 }
 for(int i=2;i<MAX;i++)
 table[i]+=table[i-1];
 }
}

```

## 7 String

### 7.1 Manacher

```

vector<int> manacher_odd(string s) {
 // size of paliendrom at center s[i] = 2 * p[i] + 1
 int n = s.size();
 s = "$" + s + "^";
 vector<int> p(n + 2);
 int l = 1, r = 1;
 for(int i = 1; i <= n; i++) {
 p[i] = max(0, min(r - i, p[l + (r - i)]));
 while(s[i - p[i]] == s[i + p[i]]) {
 p[i]++;
 }
 if(i + p[i] > r) {
 l = i - p[i], r = i + p[i];
 }
 }
}

```

```

 }
 return vector<int>(begin(p) + 1, end(p) - 1);
}

vector<int> manacher(string s) {
 // size of odd paliendrom at center s[i] = p[2*i]
 // size of even paliendrom at center s[i]s[i+1] = p[2*i + 1]
 string t;
 for(auto c: s) t += string("#") + c;
 auto res = manacher_odd(t + "#");
 return vector<int>(begin(res) + 1, end(res) - 1);
}

```

### 7.2 prefixFunction

```

vector<int> prefix_function(string s) {
 int n = s.length();
 vector<int> pi(n);
 pi[0] = 0;
 for (int i = 1; i < n; i++) {
 int j = pi[i-1];
 while (j > 0 && s[i] != s[j]) {
 j = pi[j-1];
 }
 if (s[i] == s[j]) {
 j++;
 }
 pi[i] = j;
 }
 return pi;
}

```

### 7.3 StringHashing

```

const int N = 2e5 + 9;
const int mod1 = 1e9+21, mod2 = 1e9+9;
const int p1 = 37, p2 = 31;

pair<int,int> pw[N], invpw[N];
int bigMod(int a,int b,int mod) {
 int ans = 1;
 while(b) {
 if(b & 1) {
 ans = 1LL * ans * a % mod;
 }
 b = b / 2;
 a = a * a % mod;
 }
}

```

```

 a = 1LL * a * a % mod;
 b >>= 1;
 }
 return (ans % mod);
}

void preCalc() {
 pw[0] = {1, 1};
 for(int i = 1; i < N; i++) {
 pw[i].first = 1LL * pw[i-1].first * p1 % mod1;
 }
 for(int i = 1; i < N; i++) {
 pw[i].second = 1LL * pw[i-1].second * p2 % mod2;
 }
 int invpw1 = bigMod(p1, mod1 - 2, mod1);
 int invpw2 = bigMod(p2, mod2 - 2, mod2);
 invpw[0] = {1, 1};
 for(int i = 1; i < N; i++) {
 invpw[i].first = 1LL * invpw[i-1].first * invpw1 %
 mod1;
 invpw[i].second = 1LL * invpw[i-1].second * invpw2 %
 mod2;
 }
}

class Hash_node {
public:
 int n;
 string s;
 vector<pair<int,int>> hs, prehs;
 Hash_node(){}
 Hash_node(string _s) {
 s = _s;
 n = _s.size();
 hs.resize(n);
 for(int i = 0; i < n; i++) {
 hs[i].first += 1LL * s[i] * pw[i].first % mod1;
 hs[i].first %= mod1;
 }
 for(int i = 0; i < n; i++) {
 hs[i].second += 1LL * s[i] * pw[i].second % mod2;
 hs[i].second %= mod2;
 }
 prehs.resize(n);
 prehs[0].first = hs[0].first;
 for(int i = 1; i < n; i++) {
 prehs[i].first = prehs[i-1].first + hs[i].first;
 prehs[i].first %= mod1;
 }
 prehs[0].second = hs[0].second;
 for(int i = 1; i < n; i++) {

```

```

 prehs[i].second = prehs[i-1].second + hs[i].second;
 prehs[i].second %= mod2;
 }
 }
 pair<int,int> getHash(int i,int j) {
 assert(i <= j);
 pair<int,int> ans({0, 0});
 if(i == 0) {
 ans.first = prehs[j].first;
 ans.second = prehs[j].second;
 } else {
 ans.first = (prehs[j].first - prehs[i-1].first +
 mod1) % mod1;
 ans.first = 1LL * ans.first * invpw[i].first % mod1;
 ans.second = (prehs[j].second - prehs[i-1].second +
 mod2) % mod2;
 ans.second = 1LL * ans.second * invpw[i].second % mod2;
 }
 return ans;
 }
}

```

## 7.4 SuffixArray

```

vector<int> sort_cyclic_shifts(string const& s) {
 int n = s.size();
 const int alphabet = 256;
 vector<int> p(n), c(n), cnt(max(alphabet, n), 0);

 for (int i = 0; i < n; i++)
 cnt[s[i]]++;

 for (int i = 1; i < alphabet; i++)
 cnt[i] += cnt[i - 1];

 for (int i = 0; i < n; i++)
 p[--cnt[s[i]]] = i;

 c[p[0]] = 0;
 int classes = 1;

 for (int i = 1; i < n; i++) {
 if (s[p[i]] != s[p[i - 1]])

```

```

 classes++;
 c[p[i]] = classes - 1;
 }

 vector<int> pn(n), cn(n);

 for (int h = 0; (1 << h) < n; ++h) {
 for (int i = 0; i < n; i++) {
 pn[i] = p[i] - (1 << h);
 if (pn[i] < 0)
 pn[i] += n;
 }

 fill(cnt.begin(), cnt.begin() + classes, 0);

 for (int i = 0; i < n; i++) {
 cnt[c[pn[i]]]++;
 }

 for (int i = 1; i < classes; i++) {
 cnt[i] += cnt[i - 1];
 }

 for (int i = n - 1; i >= 0; i--) {
 p[--cnt[c[pn[i]]]] = pn[i];
 }

 cn[p[0]] = 0;
 classes = 1;

 for (int i = 1; i < n; i++) {
 pair<int, int> cur = {c[p[i]], c[(p[i] + (1 << h)) %
 n]};
 pair<int, int> prev = {c[p[i - 1]], c[(p[i - 1] +
 (1 << h)) % n]};
 if (cur != prev)
 ++classes;
 }

 cn[p[i]] = classes - 1;
 }

 c.swap(cn);
 if (classes == n)
 break;
 }

 return p;
}

vector<int> suffix_array_construction(string s) {
 s += "$";
 vector<int> sorted_shifts = sort_cyclic_shifts(s);
}
```

```

sorted_shifts.erase(sorted_shifts.begin());
return sorted_shifts;
}

vector<int> lcp_construction(string const& s, vector<int>
const& p) {
int n = s.size();
vector<int> rank(n, 0);

for (int i = 0; i < n; i++)
rank[p[i]] = i;

int k = 0;
vector<int> lcp(n - 1, 0);

for (int i = 0; i < n; i++) {
if (rank[i] == n - 1) {
k = 0;
continue;
}

int j = p[rank[i] + 1];
while (i + k < n && j + k < n && s[i + k] == s[j + k])
]
k++;

lcp[rank[i]] = k;

if (k)
k--;
}
}

return lcp;
}

//int main() {
// string s;
// cin >> s;
// vector<int> v = suffix_array_construction(s);
// for (int i = 0; i < v.size(); i++)
// cout << v[i] << " ";
// cout << endl;
// vector<int> lcp = lcp_construction(s, v);
// for (int i = 0; i < lcp.size(); i++)
// cout << lcp[i] << " ";
//}
```

```

// return 0;
//}

int check(int n,int mid, string& pattern,vector<int>&v,
vector<int>&lcp,string &s)
{
int flag = -1, patternSize = pattern.size(),
suffixStart = v[mid];

// Check if the suffix can contain the entire pattern
if (n - suffixStart >= patternSize)
flag = 0;

// Compare characters of the pattern and suffix
for (int i = 0; i < min(n - suffixStart, patternSize);
i++) {
if (s[suffixStart + i] < pattern[i])
return -1;
if (s[suffixStart + i] > pattern[i])
return 1;
}
return flag;
}

int countocc(string &pat,int n,vector<int>&v,vector<int>&lcp
,string &s){

int left=0,right=n-1;
int answer=-1;
int l=left,r=right;

while(l<=r){

int mid=(l+r)/2;
int num=check(n,mid,pat,v,lcp,s);

if(num==0){
answer=mid;
r=mid-1;
}
else if(num==1){
r=mid-1;
}
}
}

void do_the_honour(){

string s,t;cin >> s ;
string demo=s;

vector<int> v = suffix_array_construction(demo);
vector<int> lcp = lcp_construction(demo,v);

//for(auto u:v) cout << u << " ";
//cout << endl;
int k;cin >> k;
}
```

```

else{
l=mid+1;
}

}

if(answer==-1){
return 0;
}
left=answer;
l=left,r=right;
answer=left;

while(l<=r){

int mid=(l+r)/2;
int num=check(n,mid,pat,v,lcp,s);

if(num==0){
answer=mid;
l=mid+1;
}
else if(num==1){
l=mid+1;
}
else{
r=mid-1;
}
}

right=answer;
return right-left+1;
}

}
```

```

int n=s.size();

for(int i=0;i<v.size();i++){
 if(i==0){
 int sz=n-v[i];
 if(sz>=k){
 for(int i=v[i];i<=(v[i]+k-1);i++) cout << s[i]
];
 cout << endl;return;
 }
 else k-=sz;
 }
 else{
 int sz=n-v[i]-lcp[i-1];
 if(sz>=k){
 cout << s.substr(v[i],lcp[i-1]+k) << endl;
 return;
 }
 else k-=sz;
 }
}

```

## 7.5 Z-algo

```

vector<int> z_function(string s) {
 int n = s.size();
 vector<int> z(n);
 int l = 0, r = 0;
 for(int i = 1; i < n; i++) {
 if(i < r) z[i] = min(r - i, z[i - 1]);
 while(i + z[i] < n && s[z[i]] == s[i + z[i]]) z[i]++;
 if(i + z[i] > r) {
 l = i;
 r = i + z[i];
 }
 }
 return z;
}

```

# 8 Trees

## 8.1 Centroid

```

int sz;
void dfs(int node, int par){

 subtree[node]=1;
 sz++;
 for(auto u:adj[node]){
 if(u==par or vis[u]) continue;
 dfs(u,node);
 subtree[node]+=subtree[u];
 }
}

int centroid(int node,int par,int n){

 for(auto u:adj[node]){
 if(u==par) continue;
 if(!vis[u] and (subtree[u]*2)>n) return centroid(u,
 node,n);
 }
 return node;
}

void create_centroid_graph(int node,int par){

 sz=0;
 dfs(node,par);
 int c=centroid(node,0,sz);
 parent[c]=par;
 vis[c]=1;
 for(auto u:adj[c]){
 if(vis[u]) continue;

 create_centroid_graph(u,c);
 }
}
create_centroid_graph(1,0);

```

## 8.2 dynamicMST

```

#include "bits/stdc++.h"
using namespace std;

```

```

#define all(x) begin(x),end(x)
typedef long long ll;
typedef vector<int> vi;

const int oo = 1e9;

struct DSU{
 vector<int> sz,parent;
 int components;
 void reset(int n) {
 fill(sz.begin(),sz.begin()+n,1);
 iota(parent.begin(),parent.begin()+n,0);
 components=n;
 }
 DSU(int n) : sz(n),parent(n) {
 reset(n);
 }
 void link(int a, int b) {
 components--;
 if(sz[a]<sz[b]) swap(a,b);
 sz[a]+=sz[b];
 parent[b] = a;
 }
 bool unite(int a, int b) {
 int pa = find(a), pb = find(b);
 if(pa==pb) {
 link(pa,pb);
 return true;
 }
 return false;
 }
 int find(int a) {
 if(a==parent[a]) return a;
 return parent[a] = find(parent[a]);
 }
};

struct dynamicMST {
 struct edge {
 int l,r;
 int u,v,w;
 bool operator<(const edge& o) {
 return w<o.w;
 }
 };
 vector<edge> ives; // edges + time interval that they are
 // active.
 vector<array<int,3>> startes;
 vi touch; // last time this edge was touched
 int totaln;
};

```

```

DSU dsu,dsu2;
vi id;
dynamicMST(vector<array<int,3>> ES, int n) : startes(ES),
 touch(ES.size()), totaln(n), dsu(n),dsu2(n), id(n)
{
 // give all edges upfront.
}
int q=0;
void update(int i, int x) {
 // update edge weight of edge i to x
 // if you want to delete the edge, just set it to
 infinity
 q++;
 auto& [u,v,w] = startes[i];
 ives.push_back({touch[i],q,u,v,w});
 touch[i]=q;
 w = x;
}
vector<ll> ans;
void solve(int l, int r, vector<edge> es, int n, ll cost
=0) {
 // remove edges that don't belong to this interval
 es.erase(stable_partition(all(es),[&](const edge& e)
 {return !(e.r<=l || r<=e.l);}),es.end());
 dsu.reset(n),dsu2.reset(n);

 // compressing connected components
 for(auto& e : es) if(l<e.l || e.r<r) { // active
 edges
 dsu.unite(e.u,e.v);
 }

 for(auto& e : es) if(e.l<=l and r<=e.r) { // fully
 overlapping edges
 if(dsu.unite(e.u,e.v)) {
 cost+=e.w;
 dsu2.unite(e.u,e.v);
 }
 }

 if(l+1==r) { // base case, we found the MST.
 ans[l]=cost;
 return;
 }

 int cnt=0; // relabel all connected components to
 0...cnt-1
 for(int i=0;i<n;++i) if(dsu2.find(i)==i) id[i]=cnt++;
 dsu.reset(cnt);
}

```

```

for(auto& e : es) { // relabeling and marking useless
 edges
 e.u = id[dsu2.find(e.u)], e.v = id[dsu2.find(e.v)]
];
 if(e.l<=l and r<=e.r) {
 if(!dsu.unite(e.u,e.v)) e.l=-oo,e.r=-oo; // mark useless edge, will get deleted in next step
 }
 int m = (l+r)/2;
 solve(l,m,es,cnt,cost);
 solve(m,r,es,cnt,cost);
}

vector<ll> run() {
 int m = startes.size();
 q++;
 for(int i=0;i<m;++i) {
 auto& [u,v,w] = startes[i];
 ives.push_back({touch[i],q,u,v,w});
 }

 sort(all(ives)); // (q+m) log(q+m) time
 ans.resize(q);
 solve(0,q,ives,totaln); // (q+m) log(q) alpha(n) time
 return ans;
}

int main() {
 ios_base::sync_with_stdio(false);
 cin.tie(NULL);
 int n,m,q; cin >> n >> m >> q;
 vector<array<int,3>> es(m);

 for(auto& [u,v,w] : es) {
 cin >> u >> v >> w;
 --u,--v;
 }

 dynamicMST mst(es,n);

 for(int i=0;i<q;++i) {
 int k,d;
 cin >> k >> d, --k;
 mst.update(k,d);
 }
 auto ans = mst.run();
 for(int i=1;i<=q;++i) { // ans[0] gives the MST cost of the initial MST.

```

```

 cout << ans[i] << '\n';
 }
}

```

### 8.3 HLD

```

vector<int> parent, depth, heavy, head, pos;
int cur_pos;

int dfs(int v, vector<vector<int>> const& adj) {
 int size = 1;
 int max_c_size = 0;
 for (int c : adj[v]) {
 if (c != parent[v]) {
 parent[c] = v, depth[c] = depth[v] + 1;
 int c_size = dfs(c, adj);
 size += c_size;
 if (c_size > max_c_size)
 max_c_size = c_size, heavy[v] = c;
 }
 }
 return size;
}

void decompose(int v, int h, vector<vector<int>> const& adj)
{
 head[v] = h, pos[v] = cur_pos++;
 if (heavy[v] != -1)
 decompose(heavy[v], h, adj);
 for (int c : adj[v]) {
 if (c != parent[v] && c != heavy[v])
 decompose(c, c, adj);
 }
}

void initofHLD(vector<vector<int>> const& adj) {
 int n = adj.size();
 parent = vector<int>(n);
 depth = vector<int>(n);
 heavy = vector<int>(n, -1);
 head = vector<int>(n);
 pos = vector<int>(n);
 cur_pos = 0;

 dfs(0, adj);
 decompose(0, 0, adj);
}

vector<int> tree(400001), arr(100001);
int arrototree[300001];

```

```

void init(int n)
{
 for (int i = 0; i < n; i++)
 tree[n + i] = arr[i];

 for (int i = n - 1; i >= 1; i--)
 tree[i] = max(tree[2 * i], tree[2 * i + 1]);
}

void update(int pos, int value, int n)
{
 pos += n;
 tree[pos] = value;

 while (pos > 1) {
 pos >>= 1;
 tree[pos] = max(tree[2 * pos], tree[2 * pos + 1]);
 }
}

int segquery(int left, int right, int n)
{
 left += n;
 right += n + 1; // inclusive range
 int mi = (int)-1;

 while (left < right) {
 if (left & 1) {
 mi = max(mi, tree[left]);
 left++;
 }
 if (right & 1) {
 right--;
 mi = max(mi, tree[right]);
 }
 left >>= 1;
 right >>= 1;
 }
 return mi;
}

int query(int a, int b, int n) {
 int res = 0;
 while (head[a] != head[b]) {
 if (depth[head[a]] > depth[head[b]]) swap(a, b);
 res = max(res, segquery(pos[head[b]], pos[b], n));
 b = parent[head[b]];
 }
 if (depth[a] > depth[b]) swap(a, b);
 res = max(res, segquery(pos[a], pos[b], n));
}

```

```

 return res;
 }

 void do_the_honour() {
 int n, q;
 cin >> n >> q;
 vector<int> a(n);
 for (int i = 0; i < n; ++i) cin >> a[i];

 vector<vector<int>> adj(n);
 for (int i = 1; i < n; ++i) {
 int x, y;
 cin >> x >> y;
 --x; --y;
 adj[x].push_back(y);
 adj[y].push_back(x);
 }
 initofHLD(adj);

 arr.resize(n);
 tree.resize(4 * n);
 for (int i = 0; i < n; ++i) arr[pos[i]] = a[i];
 init(n);

 while (q--) {
 int type;
 cin >> type;
 if (type == 2) {
 int l, r;
 cin >> l >> r;
 cout << query(l - 1, r - 1, n) << '\n';
 } else {
 int s, x;
 cin >> s >> x;
 s--;
 update(pos[s], x, n);
 }
 cout << '\n';
 }
 }

```

## 8.4 NumOfPathsPassingThroughNodei

```

int dp[32][200001];
int level[200001];
vector<int>adj[200001];

void dfs(int node,int par){

```

```

 for(auto u:adj[node]){
 if(u==par) continue;
 level[u]=level[node]+1;
 dp[0][u]=node;
 dfs(u,node);
 }
}

int c[200001];

void dfs22(int node,int par){

 for(auto u:adj[node]){
 if(u==par) continue;
 dfs22(u,node);
 c[node]+=c[u];
 }
}

void do_the_honour(){

 int n,m;cin >> n >> m ;

 for(int i=2;i<=n;i++){
 int x,y;cin >> x >> y;
 adj[x].push_back(y);
 adj[y].push_back(x);
 }
 level[1]=0;
 dfs(1,0);
 dp[0][1]=0;

 for(int i=1;i<=24;i++){
 for(int j=1;j<=n;j++) dp[i][j]=dp[i-1][dp[i-1][j]];
 }

 for(int i=0;i<m;i++){
 int a,b;cin >> a >> b;
 int x=a,y=b;

 if(level[a]<level[b]) swap(a,b),swap(x,y);
 int diff=level[a]-level[b];

 for(int i=0;i<=24;i++){

```

```

 if(diff&(1<<i)){
 a=dp[i][a];
 }
}
int node=-1;
if(a==b){
 node=a;
}else{
 for(int ii=24;ii>=0;ii--){
 if(dp[ii][a]!=dp[ii][b]){
 a=dp[ii][a];
 b=dp[ii][b];
 }
 }
 node=dp[0][a];
}

c[x]++,c[y]++,c[node]--;
if(dp[0][node]>0) c[dp[0][node]]--;

}
dfs22(1,0);
for(int i=1;i<=n;i++) cout << c[i] << " ";
}

```

## 8.5 smallToLarge

---

```

//finding sum of most frequent values in the subtree of each
//node; small to large merging
vector<int>adj[200001];
map<int,int>s[200001];
int ans[200001];
int par[200001];

```

```

int max_freq_cnt[200001];
int max_freq[200001];
int merge(int a,int b){
 if(s[a].size()<s[b].size()) swap(a,b);
 for(auto u:s[b]){
 int color=u.first;
 int c=u.second;
 int new_cnt=c+s[a][color];
 s[a][color]+=c;

 if(new_cnt>max_freq[a]){
 max_freq[a]=new_cnt;
 max_freq_cnt[a]=color;
 }
 else if(new_cnt==max_freq[a]) max_freq_cnt[a]+=color;
 }
 return a;
}

int dfs(int node,int p){
 int i=par[node];
 for(auto u:adj[node]){
 if(p==u) continue;
 i=merge(i,dfs(u,node));
 }
 ans[node]=max_freq_cnt[i];
 return i;
}

void do_the_honour(){
 int n;cin >> n;
}

```

```

int color[n+1];
for(int i=1;i<=n;i++) cin >> color[i];

for(int i=1;i<=n;i++){
 s[i][color[i]]++;
 par[i]=i;
 max_freq[i]=1;
 max_freq_cnt[i]+=color[i];
}

for(int i=1;i<n;i++){
 int x,y; cin >> x >> y;
 adj[x].push_back(y);
 adj[y].push_back(x);
}

dfs(1,0);
for(int i=1;i<=n;i++) cout << ans[i] << " ";

}

```

---

## 8.6 Tree Flattening

---

```

void dfs(int node,int par){

 timer++;
 fa[timer]=node;
 for(auto u:adj[node]){
 if(u==par) continue;
 dfs(u,node);
 }
 timer++;
 fa[timer]=node;
}

```

---