# 3 - Data Project – Team Winrate - Descriptive Regression - Summer 2019

May 31, 2020

```
[1]: import numpy as np
  import pandas as pd
  pd.options.display.max_columns=100
  from sklearn.model_selection import train_test_split, cross_val_score
  from sklearn.preprocessing import StandardScaler as SSc
  from sklearn.decomposition import PCA
  import matplotlib.pyplot as plt
  from mpl_toolkits.mplot3d import Axes3D
  import graphviz as gviz
  %matplotlib inline

#set width of window to preference
  from IPython.core.display import display, HTML
  display(HTML("<style>.container { width:90% !important; }</style>"))
```

<IPython.core.display.HTML object>

```
[2]: #year = "2019"
                                                                            #choose year
      \rightarrowto get data from
     #split = "summer"
                                                                            #choose split_
      →to get data from(spring, summer, worlds)
     \#infile = r"C: \Users \Triplea657 \000 \MSCS-335 \2020 \Datasets \League\_"\#path
     #inf = "-Wrangled.csv"
                                                                            #file to read
     #filein = infile+year+"\\"+year+'-'+split+'-'+inf
     #data = pd.read_csv(filein,low_memory=False)
     #data.head(10)
     #changed for submission version
     data = pd.read_csv("Datasets/League_2019/2019-summer-Wrangled.csv", index_col=0,_
      →low_memory=False)
     data.head()
```

```
[2]:
       league_CBLoL league_LCK league_LCS league_LEC
                                                         league_LMS gamelength
     0
                0.0
                            0.0
                                        1.0
                                                    0.0
                                                                0.0
                                                                      35.500000
     1
                0.0
                            0.0
                                        1.0
                                                    0.0
                                                                0.0
                                                                      35.500000
```

```
0.0
                                                   0.0
                                                                0.0
                                                                      29.700000
2
                         0.0
                                      1.0
3
            0.0
                         0.0
                                      1.0
                                                   0.0
                                                                0.0
                                                                      29.700000
                                                                0.0
                                                                      31.983333
4
            0.0
                         0.0
                                      1.0
                                                   0.0
   result
                                fb
                                                                     fd
              k
                     d
                            a
                                         kpm
                                                   okpm
                                                              ckpm
                        52.0 0.0
                                    0.591549
0
      1.0
           21.0
                  14.0
                                              0.394366
                                                         0.985915
                                                                    0.0
                                    0.394366
      0.0
           14.0
                  21.0
                        32.0
                               1.0
                                               0.591549
                                                         0.985915
                                                                    1.0
1
2
           11.0
                        25.0
                               1.0
                                    0.370370
                                               0.134680
                                                         0.505051
      1.0
                   4.0
                                                                    1.0
3
            4.0
                        10.0 0.0
                                   0.134680
                                              0.370370
                                                         0.505051
                                                                    0.0
      0.0
                 11.0
      1.0
           12.0
                   3.0
                        26.0
                              1.0
                                    0.375195
                                              0.093799
                                                         0.468994
                                                                    0.0
                               oppdragkills
      fdtime
               teamdragkills
                                              elementals
                                                           oppelementals
   12.556633
0
                         2.0
                                        2.0
                                                     2.0
                         2.0
                                                     2.0
                                                                     2.0
1
   12.556633
                                        2.0
   12.306967
                         2.0
                                                     2.0
                                                                     1.0
                                        1.0
  12.306967
                         1.0
                                        2.0
                                                     1.0
                                                                     2.0
 10.158933
                                                                     1.0
                         3.0
                                        1.0
                                                     3.0
               waterdrakes
                             earthdrakes
                                                       elders
                                                                oppelders
   firedrakes
                                           airdrakes
                                                                           herald
0
          2.0
                        0.0
                                      0.0
                                                  0.0
                                                           0.0
                                                                      0.0
                                                                               1.0
          1.0
                        0.0
                                      0.0
                                                  1.0
                                                           0.0
                                                                      0.0
                                                                               0.0
1
2
          0.0
                        0.0
                                      1.0
                                                  1.0
                                                          0.0
                                                                               0.0
                                                                      0.0
3
          0.0
                        1.0
                                      0.0
                                                  0.0
                                                          0.0
                                                                      0.0
                                                                               1.0
          1.0
                        0.0
                                      0.0
                                                  2.0
                                                           0.0
                                                                      0.0
                                                                               0.0
   heraldtime
                 ft
                        fttime firstmidouter firsttothreetowers
    13.369417
                     15.162683
                                            1.0
0
               1.0
1
    13.369417
               0.0
                     15.162683
                                           0.0
                                                                 1.0
                     12.791600
2
    12.377433
                1.0
                                            1.0
                                                                 1.0
    12.377433
               0.0
                    12.791600
                                           0.0
                                                                 0.0
3
    12.242783 0.0
                    14.386333
                                            1.0
                                                                 1.0
   teambaronkills
                    oppbaronkills
                                    dmgtochamps
                                                  dmgtochampsperminute
                                                                         wards
0
               1.0
                               0.0
                                        70545.0
                                                            1987.183099
                                                                         109.0
              0.0
                               1.0
                                                                          108.0
1
                                        71736.0
                                                            2020.732394
2
               1.0
                               0.0
                                        51538.0
                                                            1735.286195
                                                                          96.0
3
              0.0
                               1.0
                                        38185.0
                                                            1285.690236
                                                                          93.0
               1.0
                               0.0
                                        49421.0
                                                            1545.211047
                                                                         143.0
                                   totalgold
                                                  earnedgpm goldspent
        wpm
             wardkills
                             wcpm
                                                                              gspd
   3.070423
                         1.436620
                                      69022.0
                                                1293.464789
                                                                65108.0
                                                                         0.110966
                   51.0
                                                1082.732394
   3.042254
                   37.0
                         1.042254
                                      61541.0
                                                                58263.0 -0.110966
   3.232323
                   44.0
                         1.481481
                                      59081.0
                                                1330.861953
                                                                50910.0 0.135867
3 3.131313
                   41.0
                         1.380471
                                      45794.0
                                                 883.488215
                                                               44433.0 -0.135867
4 4.471079
                   44.0
                        1.375717
                                      61326.0
                                               1262.351225
                                                               54340.0 0.158169
```

cspm goldat10 \

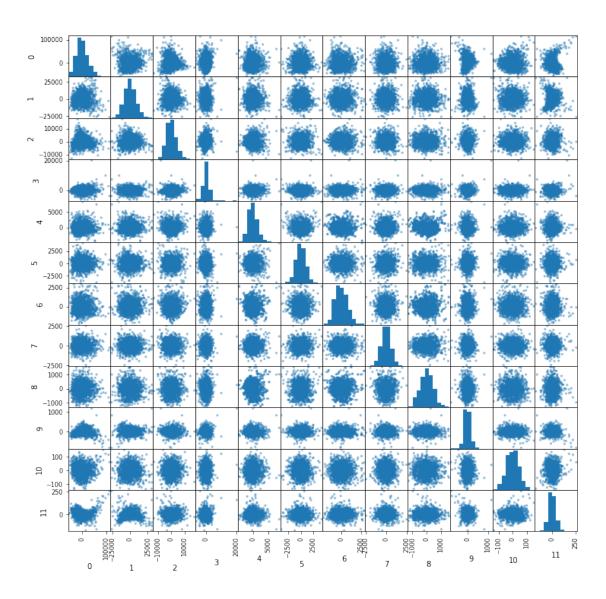
monsterkillsownjungle monsterkillsenemyjungle

```
0
                        151.0
                                                  24.0 31.802817
                                                                     16118.0
     1
                        155.0
                                                   4.0 32.985915
                                                                     15436.0
     2
                        102.0
                                                  56.0 35.656566
                                                                     16270.0
     3
                                                        33.265993
                         82.0
                                                   0.0
                                                                     14985.0
     4
                        128.0
                                                  18.0 34.299114
                                                                     16157.0
        oppgoldat10 gdat10 goldat15 oppgoldat15 gdat15
                                                             xpat10 oppxpat10 \
     0
                      682.0
                              24287.0
                                                     671.0 19260.0
            15436.0
                                           23616.0
                                                                        18621.0
     1
            16118.0 -682.0
                              23616.0
                                           24287.0 -671.0 18621.0
                                                                        19260.0
     2
            14985.0 1285.0
                              27399.0
                                           23026.0 4373.0 19015.0
                                                                        18226.0
     3
            16270.0 -1285.0
                              23026.0
                                           27399.0 -4373.0 18226.0
                                                                        19015.0
     4
            14365.0 1792.0
                              26339.0
                                           22782.0 3557.0 19284.0
                                                                        18656.0
        xpdat10
                 csat10
                         oppcsat10 csdat10 csat15
                                                    oppcsat15
                                                                csdat15
          639.0
                  334.0
                                       18.0
                                              548.0
                                                          535.0
     0
                             316.0
                                                                    13.0
       -639.0
                  316.0
                                                                   -13.0
     1
                             334.0
                                      -18.0
                                              535.0
                                                          548.0
     2
         789.0
                  316.0
                                      -19.0
                                                          506.0
                                                                     3.0
                             335.0
                                              509.0
     3
         -789.0
                  335.0
                             316.0
                                       19.0
                                              506.0
                                                          509.0
                                                                    -3.0
          628.0
                                       17.0
                                                                    42.0
     4
                  322.0
                             305.0
                                              512.0
                                                          470.0
[3]: mean = data.mean()
     print(mean)
    league_CBLoL
                      0.132964
    league_LCK
                      0.337950
    league_LCS
                      0.182825
    league_LEC
                      0.173130
    league_LMS
                      0.173130
    oppcsat10
                    318.845568
    csdat10
                      0.000000
    csat15
                    503.474377
    oppcsat15
                    503.474377
    csdat15
                      0.000000
    Length: 62, dtype: float64
    PCA without data standardization
[4]: pca = PCA(n_components=12)
     pca.fit(data)
     #print("PCA components:
                                            "+str(pca.components_))
     print("\nPCA explained variance ratio: "+str(pca.explained_variance_ratio_))
     print("\nPCA singular values:
                                            "+str(pca.singular_values_))
     X = pd.DataFrame(pca.transform(data))
     pd.plotting.scatter_matrix(X,figsize=(12,12));
```

PCA explained variance ratio: [8.67627130e-01 1.01407391e-01 1.95668660e-02 4.99782276e-03 3.15962230e-03 1.48517238e-03 9.23823613e-04 4.94639370e-04 2.96124762e-04 3.27582717e-05 2.77884748e-06 2.47570114e-06] PCA singular values: [937142.1768778 320386.14434339 140734.17063465 71126.15758824 56553.11189101 38772.81689976 30579.71627688 22376.04168278 17313.15770017 5758.36795488 1677.14757112 1583.0259366 ] C:\Users\Triplea657\anaconda3\lib\sitepackages\pandas\plotting\\_matplotlib\tools.py:298: MatplotlibDeprecationWarning: The rowNum attribute was deprecated in Matplotlib 3.2 and will be removed two minor releases later. Use ax.get\_subplotspec().rowspan.start instead. layout[ax.rowNum, ax.colNum] = ax.get\_visible() C:\Users\Triplea657\anaconda3\lib\sitepackages\pandas\plotting\\_matplotlib\tools.py:298: MatplotlibDeprecationWarning: The colNum attribute was deprecated in Matplotlib 3.2 and will be removed two minor releases later. Use ax.get\_subplotspec().colspan.start instead. layout[ax.rowNum, ax.colNum] = ax.get\_visible() C:\Users\Triplea657\anaconda3\lib\sitepackages\pandas\plotting\\_matplotlib\tools.py:304: MatplotlibDeprecationWarning: The rowNum attribute was deprecated in Matplotlib 3.2 and will be removed two minor releases later. Use ax.get\_subplotspec().rowspan.start instead. if not layout[ax.rowNum + 1, ax.colNum]: C:\Users\Triplea657\anaconda3\lib\sitepackages\pandas\plotting\\_matplotlib\tools.py:304: MatplotlibDeprecationWarning:

packages\pandas\plotting\\_matplotlib\tools.py:304: MatplotlibDeprecationWarning The colNum attribute was deprecated in Matplotlib 3.2 and will be removed two minor releases later. Use ax.get\_subplotspec().colspan.start instead.

if not layout[ax.rowNum + 1, ax.colNum]:



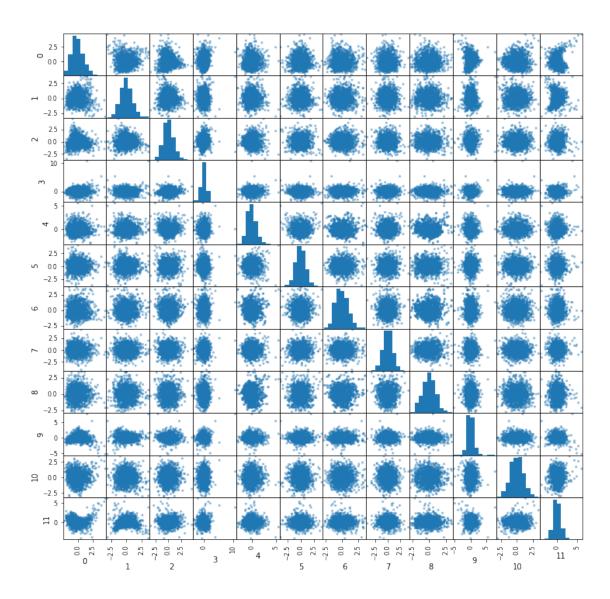
#### PCA with data standardization

```
[5]: pca = PCA(n_components=12)
    pca.fit(X)
    #print("PCA components: "+str(pca.components_))
    print("\nPCA explained variance ratio: "+str(pca.explained_variance_ratio_))
    print("\nPCA singular values: "+str(pca.singular_values_))

ssc = SSc()
    X = pd.DataFrame(ssc.fit_transform(X))

X = pd.DataFrame(pca.transform(X))
    pd.plotting.scatter_matrix(X,figsize=(12,12));
```

```
PCA explained variance ratio: [8.67630076e-01 1.01407735e-01 1.95669325e-02
4.99783973e-03
3.15963303e-03 1.48517742e-03 9.23826750e-04 4.94641049e-04
 2.96125768e-04 3.27583829e-05 2.77885691e-06 2.47570954e-06]
PCA singular values:
                              [937142.1768778 320386.14434339 140734.17063465
71126.15758824
  56553.11189101 38772.81689976 30579.71627688 22376.04168278
                  5758.36795488
  17313.15770017
                                   1677.14757112
                                                   1583.0259366 ]
C:\Users\Triplea657\anaconda3\lib\site-
packages\pandas\plotting\_matplotlib\tools.py:298: MatplotlibDeprecationWarning:
The rowNum attribute was deprecated in Matplotlib 3.2 and will be removed two
minor releases later. Use ax.get_subplotspec().rowspan.start instead.
  layout[ax.rowNum, ax.colNum] = ax.get_visible()
C:\Users\Triplea657\anaconda3\lib\site-
packages\pandas\plotting\_matplotlib\tools.py:298: MatplotlibDeprecationWarning:
The colNum attribute was deprecated in Matplotlib 3.2 and will be removed two
minor releases later. Use ax.get_subplotspec().colspan.start instead.
  layout[ax.rowNum, ax.colNum] = ax.get_visible()
C:\Users\Triplea657\anaconda3\lib\site-
packages\pandas\plotting\_matplotlib\tools.py:304: MatplotlibDeprecationWarning:
The rowNum attribute was deprecated in Matplotlib 3.2 and will be removed two
minor releases later. Use ax.get_subplotspec().rowspan.start instead.
  if not layout[ax.rowNum + 1, ax.colNum]:
C:\Users\Triplea657\anaconda3\lib\site-
packages\pandas\plotting\_matplotlib\tools.py:304: MatplotlibDeprecationWarning:
The colNum attribute was deprecated in Matplotlib 3.2 and will be removed two
minor releases later. Use ax.get_subplotspec().colspan.start instead.
```



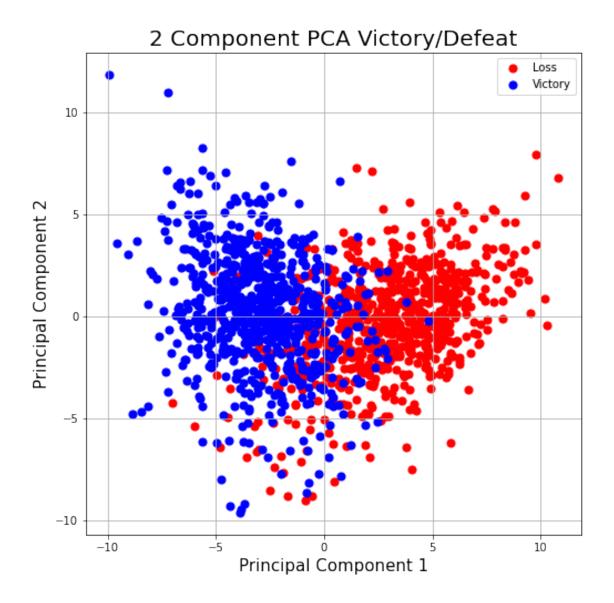
## PCA analysis of victory/defeat (2 components)

```
[6]: def pcaout(pca, n_ftrs, col_nms):
    print("Principal components:")
    idx = ['PC-1','PC-2','PC-3','PC-4','PC-5','PC-6']
    return pd.DataFrame(pca.components_, columns=col_nms, index = idx[:n_ftrs])
```

```
[7]: X = data.iloc[:,data.columns != 'result']
    Xcol = X.columns
    Y = data.iloc[:,data.columns == 'result']
    #transform input data (normalize)
    ssc = SSc()
    Xft = ssc.fit_transform(X)
    X = pd.DataFrame(Xft)
```

```
pca = PCA(n_components=2)
components = pca.fit_transform(X)
componentDf = pd.DataFrame(data=components, columns=['principal component 1', __
→'principal component 2'])
pltDF = pd.concat([componentDf, Y], axis = 1)
print("PCA explained variance ratio: {}".format(pca.explained_variance_ratio_))
print("Portion of variance explained: {}".format(pca.explained_variance_ratio_/
⇒sum(pca.explained_variance_ratio_)))
#plot
fig = plt.figure(figsize = (8,8))
ax = fig.add_subplot(1,1,1)
ax.set_xlabel('Principal Component 1', fontsize = 15)
ax.set_ylabel('Principal Component 2', fontsize = 15)
ax.set_title('2 Component PCA Victory/Defeat', fontsize = 20)
results = [0.0, 1.0]
colors = ['r', 'b']
for result, color in zip(results,colors):
    indicesToKeep = (pltDF['result'] == result)
    ax.scatter(pltDF.loc[indicesToKeep, 'principal component 1']
               , pltDF.loc[indicesToKeep, 'principal component 2']
               , c = color
               , s = 50)
ax.legend(['Loss','Victory'])
ax.grid()
```

PCA explained variance ratio: [0.25647711 0.12592736] Portion of variance explained: [0.67069589 0.32930411]



```
[8]: df = pcaout(pca, 2, Xcol) df
```

## Principal components:

```
[8]:
          league_CBLoL league_LCK league_LCS league_LEC league_LMS \
              0.003958
    PC-1
                         -0.008343
                                     0.000866
                                                0.005484
                                                            0.000509
    PC-2
              0.046823
                        -0.115762
                                     0.012782
                                                0.101831
                                                           -0.012185
          gamelength
                                                                         okpm \
                            k
                                      d
                                                        fb
                                                                 kpm
                                               a
    PC-1 -0.050080 -0.166795 0.139952 -0.158998 -0.086159 -0.156447 0.161371
    PC-2
           -0.298563 0.064694 0.004309 0.031856 0.033971 0.155790 0.089599
```

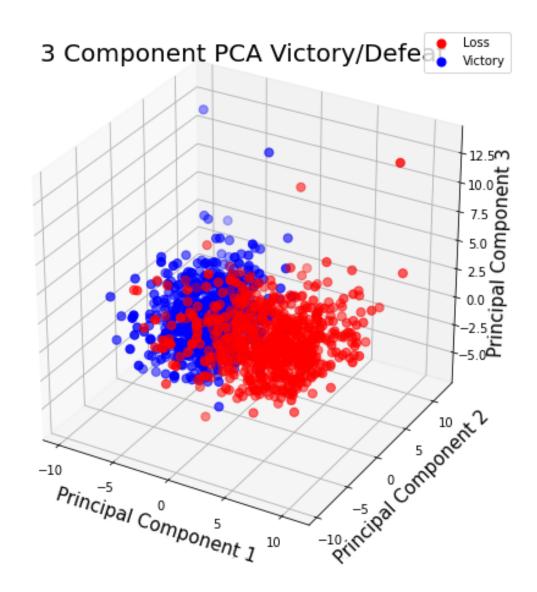
```
fd fdtime teamdragkills oppdragkills elementals \
PC-1 0.003948 -0.115469 0.003115
                                -0.202534
                                           0.167631
                                                      -0.202371
PC-2 0.196758 0.035238 0.022261
                                             -0.151020
                                 -0.063025
                                                      -0.030192
     oppelementals firedrakes waterdrakes earthdrakes airdrakes \
         0.177836 -0.108573
                           -0.092821
PC-1
                                       -0.085696 -0.097351
PC-2
        -0.121844 -0.004087 -0.023802 -0.007486 -0.021806
                      herald heraldtime
      elders oppelders
                                             ft
                                                   fttime \
PC-1 -0.047086 -0.008447 -0.074291 0.000345 -0.143544 -0.006874
PC-2 -0.164998 -0.168354 0.026337
                              0.003719 0.046607 -0.084438
     firstmidouter firsttothreetowers teambaronkills oppbaronkills \
PC-1
       -0.170376 -0.187454 -0.156228
                                                   0.121386
PC-2
        0.044149
                         0.047430
                                     -0.067670
                                                   -0.115831
     dmgtochamps dmgtochampsperminute wards
                                              wpm wardkills \
PC-1
      -0.110854
                        -0.123607 -0.056646 -0.047123 -0.082411
PC-2
      -0.141347
                         0.021892 -0.304310 -0.206338 -0.290090
        wcpm totalgold earnedgpm goldspent
                                            gspd \
PC-1 -0.089111 -0.147279 -0.217007 -0.116267 -0.218768
PC-2 -0.216231 -0.233344 0.048704 -0.254233 0.046821
     monsterkillsownjungle monsterkillsenemyjungle cspm goldat10 \
PC-1
              -0.054776
                                   -0.170127 -0.111433 -0.146216
PC-2
               -0.287850
                                   -0.016775 -0.083955 0.092978
    oppgoldat10
               gdat10 goldat15 oppgoldat15
                                            gdat15
                                                     xpat10 \
PC-1
      PC-2
      -0.013079 0.067696 0.125517
                                   0.018078 0.066082 -0.058053
     oppxpat10 xpdat10 csat10 oppcsat10 csdat10 csat15 oppcsat15 \
     PC-1
                                                         0.079592
PC-2 -0.136850 0.061247 -0.124232 -0.185095 0.052517 -0.140902 -0.197828
    csdat15
PC-1 -0.16317
PC-2 0.05022
```

#### PCA analysis of victory/defeat (3 components)

```
[9]: X = data.iloc[:,data.columns != 'result']
Y = data.iloc[:,data.columns == 'result']
#transform input data (normalize)
ssc = SSc()
Xft = ssc.fit_transform(X)
```

```
X = pd.DataFrame(Xft)
pca = PCA(n_components=3)
components = pca.fit_transform(X)
componentDf = pd.DataFrame(data=components, columns=['principal component 1', u
pltDF = pd.concat([componentDf, Y], axis = 1)
print("PCA explained variance ratio: {}".format(pca.explained_variance_ratio_))
print("Portion of variance explained: {}".format(pca.explained_variance_ratio_/
→sum(pca.explained_variance_ratio_)))
#plot
fig = plt.figure(figsize = (8,8))
ax = fig.add_subplot(1,1,1,projection='3d')
ax.set_xlabel('Principal Component 1', fontsize = 15)
ax.set_ylabel('Principal Component 2', fontsize = 15)
ax.set_zlabel('Principal Component 3', fontsize = 15)
ax.set_title('3 Component PCA Victory/Defeat', fontsize = 20)
results = [0.0, 1.0]
colors = ['r', 'b']
for result, color in zip(results,colors):
   indicesToKeep = (pltDF['result'] == result)
   ax.scatter(pltDF.loc[indicesToKeep, 'principal component 1']
              , pltDF.loc[indicesToKeep, 'principal component 2']
              , pltDF.loc[indicesToKeep, 'principal component 3']
              , c = color
              , s = 50)
ax.legend(['Loss','Victory'])
ax.grid()
```

PCA explained variance ratio: [0.25647711 0.12592736 0.08840393] Portion of variance explained: [0.54475899 0.26747051 0.1877705 ]



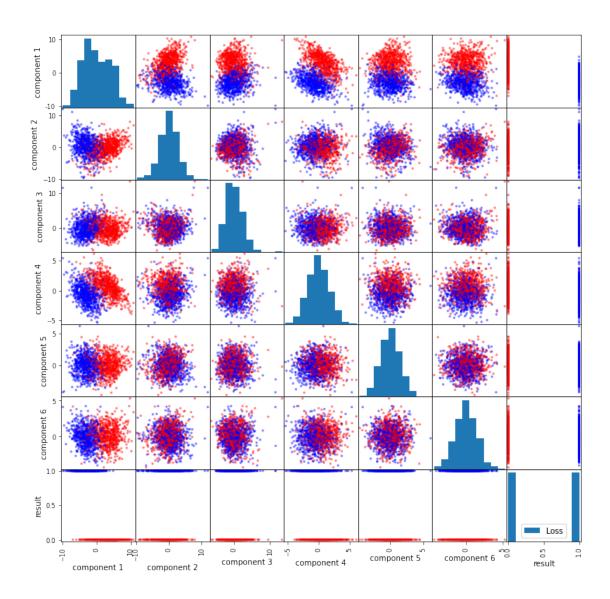
## PCA analysis of victory/defeat (6 components)

```
[10]: X = data.iloc[:,data.columns != 'result']
Y = data.iloc[:,data.columns == 'result']
#transform input data (normalize)
ssc = SSc()
Xft = ssc.fit_transform(X)
X = pd.DataFrame(Xft)

pca = PCA(n_components=6)
components = pca.fit_transform(X)
componentDf = pd.DataFrame(data=components, columns=['component 1', 'component_\textsup \frac{1}{2}', 'component 3',
```

```
'component 4', 'component
 \rightarrow5', 'component 6'])
pltDF = pd.concat([componentDf, Y], axis = 1)
print("PCA explained variance ratio: {}".format(pca.explained_variance_ratio_))
print("Portion of variance explained: {}".format(pca.explained_variance_ratio_/
 →sum(pca.explained_variance_ratio_)))
colors = ['r', 'b']
pd.plotting.scatter_matrix(pltDF,figsize=(12,12),c=pltDF.result.apply(lambda x:
 \rightarrowcolors[int(x)]))
print("\n\n\t6-component PCA")
plt.legend(['Loss','Victory'])
plt.show()
PCA explained variance ratio: [0.25647711 0.12592736 0.08840393 0.05106679
0.03655437 0.03350323]
Portion of variance explained: [0.43328755 0.21273929 0.14934791 0.08627126
0.06175427 0.05659972]
C:\Users\Triplea657\anaconda3\lib\site-
packages\pandas\plotting\_matplotlib\tools.py:298: MatplotlibDeprecationWarning:
The rowNum attribute was deprecated in Matplotlib 3.2 and will be removed two
minor releases later. Use ax.get_subplotspec().rowspan.start instead.
  layout[ax.rowNum, ax.colNum] = ax.get_visible()
C:\Users\Triplea657\anaconda3\lib\site-
packages\pandas\plotting\_matplotlib\tools.py:298: MatplotlibDeprecationWarning:
The colNum attribute was deprecated in Matplotlib 3.2 and will be removed two
minor releases later. Use ax.get_subplotspec().colspan.start instead.
  layout[ax.rowNum, ax.colNum] = ax.get_visible()
C:\Users\Triplea657\anaconda3\lib\site-
packages\pandas\plotting\_matplotlib\tools.py:304: MatplotlibDeprecationWarning:
The rowNum attribute was deprecated in Matplotlib 3.2 and will be removed two
minor releases later. Use ax.get_subplotspec().rowspan.start instead.
  if not layout[ax.rowNum + 1, ax.colNum]:
C:\Users\Triplea657\anaconda3\lib\site-
packages\pandas\plotting\_matplotlib\tools.py:304: MatplotlibDeprecationWarning:
The colNum attribute was deprecated in Matplotlib 3.2 and will be removed two
minor releases later. Use ax.get_subplotspec().colspan.start instead.
  if not layout[ax.rowNum + 1, ax.colNum]:
```

6-component PCA



# PCA analysis of region played

```
[11]: #filein = inpath+year+"\\"+year+'-'+split+"-"+"WrangledNotHot.csv"
#changed for submission version
filein = "Datasets/League_2019/2019-summer-WrangledNotHot.csv"
data2 = pd.read_csv(filein,low_memory=False,index_col=0)

X = data2.iloc[:,1:]
Y = data2.iloc[:,:1]
#transform input data (normalize)
ssc = SSc()
Xft = ssc.fit_transform(X)
X = pd.DataFrame(Xft)
```

```
pca = PCA(n_components=3)
components = pca.fit_transform(X)
componentDf = pd.DataFrame(data=components, columns=['principal component 1', |
→'principal component 2', 'principal component 3'])
pltDF = pd.concat([componentDf, Y], axis = 1)
print("PCA of regions")
print("PCA explained variance ratio: {}".format(pca.explained_variance_ratio_))
print("Portion of variance explained: {}".format(pca.explained_variance_ratio_/
⇒sum(pca.explained_variance_ratio_)))
#plot
fig = plt.figure(figsize = (8,8))
ax = fig.add_subplot(1,1,1,projection='3d')
ax.set_xlabel('Principal Component 1', fontsize = 15)
ax.set_ylabel('Principal Component 2', fontsize = 15)
ax.set_zlabel('Principal Component 3', fontsize = 15)
ax.set_title('3 Component PCA game region', fontsize = 20)
regions = ['CBLoL', 'LCK', 'LCS', 'LEC']
colors = ['m', 'r', 'b', 'y']
for region, color in zip(regions, colors):
    indicesToKeep = (pltDF['league'] == region)
    ax.scatter(pltDF.loc[indicesToKeep, 'principal component 1']
               , pltDF.loc[indicesToKeep, 'principal component 2']
               , pltDF.loc[indicesToKeep, 'principal component 3']
               , c = color
               , s = 50)
ax.legend(regions)
ax.grid()
```

PCA of regions
PCA explained variance ratio: [0.28470343 0.13203852 0.09198295]
Portion of variance explained: [0.55964123 0.25954798 0.18081079]

