

# A Control Researchers' Guide to the Reinforcement Learning Galaxy: A Survey

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**Abstract**—This paper is aimed at providing researchers in the field of control a bridge for incorporating deep reinforcement learning into their work. We are not talking about adding newly developed visual recognition capacity into end-to-end control loops, but technical details on how to take advantage of the progresses brought about by deep learning and its computational infrastructures. Reinforcement Learning is an inference based "Blackbox" approach while traditional optimization is the "Whitebox" approach where phase portrait of a dynamic system is carefully manipulated. Clearly, neither is perfect. "Blackbox" approach is data hungry and there would always be dynamics that elude the "Whitebox" description. Some of the techniques developed in the reinforcement learning community should be readily adaptable by control researchers, yet there are four barriers that prevent them to do so: different notation conventions; lack of theoretical proof; obfuscating acronyms; fast evolving best practices. In this paper, we present the taxonomy of reinforcement learning from the perspective of control and optimization. We tease out the most important concepts and hope to provide control researchers ideas and clues as of how to further their research by riding the wave of reinforcement learning.

**Index Terms**—Reinforcement Learning, Control Theory, Optimal Control, Optimization

## I. INTRODUCTION

**R**EINFORCEMENT learning is the process of methodically extracting information from experiments to gradually bound the policy distribution, maximizing the expected reward along a path. Trajectory Optimization, on the other hand, tries to capture the dynamics of a system with differential or recursive equations, and reshape the phase portrait with actions at each step. When the first batch of reasonable RL results were introduced, they were met with coldness. The preface of Bertsekas's book *Neuro Dynamic Programming* provides a good sample on how reinforcement learning is perceived by the control community back in 1996: ...These methods (Reinforcement Learning) were aiming to provide effective suboptimal solutions to complex problems of planning and sequential decision making under uncertainty, that for a long time were thought to be intractable. Our first impression was that the new methods were ambitious, overly optimistic, and lacked firm foundation....Three years later, after a lot of study, analysis, and experimentation, we believe that our initial impressions were largely correct. [?]

Things are certainly different today. Reinforcement Learning community routinely generates results that seem unattainable to the control community. What has changed is not the theoretical

foundation of RL, which is as leaky as it was in 1996, but its computational infrastructure. Before 2010, the predominant tools for function approximation are kernel methods, where feature spaces are used to transform nonlinear functions into linear space such that regression can be performed. Today, the default function approximator are neural networks. Another major change in computation is that of GPU based acceleration. Before the advent of CUDA, GPU programming requires PhD in computer graphics. Today, anyone who is proficient in C/C++ can programme GPU to parallelize their computation. Software packages such as PyTorch and Tensorflow made this even easier.

However, reinforcement learning methods are not perfect. RL community has been trying to make it more broadly applicable and more efficient: Imitation learning and reverse reinforcement learning [1] aims at derive constraints from observed best solution; Sergey Levine utilizes unsupervised learning to build an agent with intuitions of the physical world [2]; Chelsea Finn introduced Meta-Learning [3] to extract overarching invariant structures from similar tasks with different setting. This line of research require firm grasp of statistical learning theory, information theory to design efficient schemes for exploration and minimize sampling collection.

Model of a dynamic system and its control strategies can be learned statistically or they can be written down mathematically, and there is no reason why these two perspectives can't merge together. Unfortunately, these two subjects are studied by two communities of researchers who use different notations to describe the same processes and they publish their research only in journals of their own disciplines. In this paper, we hope to provide a bridge for researchers in the field of control who would like to incorporate reinforcement learning into their works. We are not the first ones to take up this challenge. Recently, there are interdisciplinary conferences held specifically for the purpose of bridging the gaps between these groups of people, for instance the L4DC (Learning for Dynamic Control) conference and Intersections between Control, Learning and Optimization Workshop.

In this paper, we build on the work of Benjamin Recht [4] to formulate reinforcement learning in the language of optimization. The first barrier facing control researchers is consolidating the notation between control and reinforcement learning communities. Control communities use the notation system introduced by Lev Pontryagin. State is denoted  $\mathcal{X}$ , Action is denoted  $\mathcal{U}$  (the first letter of Russian for "Action"), the dynamics and stochasticity is captured by physical model constraints  $x_{t+1} = f(x_t, u_t, e_t)$  where  $e$  denote the noise of a system. The objective is usually to minimize the cost function

$\mathcal{J}(\cdot)$ . Reinforcement Learning communities use the notation system introduced by Richard Bellman who studied dynamic programming. State is denoted  $\mathcal{S}$ , Action is denoted  $\mathcal{A}$ . The dynamics and stochasticity is captured via transition matrix  $\mathcal{P}$  of a Markov Decision Process. The objective of RL is the maximize the reward function  $\mathcal{R}(\cdot)$ . Yet, if we set the transition matrix to be identical to the noise, then it is clear that the underlying process behind these two notation system are exactly the same. The differences are nothing but style. Since the audience of our paper is the control community, we would cast reinforcement learning in the control notation system.

The second barrier facing the control researchings is the sense of standing on shifting sand. For instance, while the convergence of dynamic programming method is proven, no guarantee can be found in the approximated version of the same algorithm; The asynchronous actor critic method obviously updates the parameters in a haphazard manner yet it works well empirically; the DQN method replace system function with the a specific form of Q function without theoretical proof, etc. For classically trained control researchers who is used to rigorous mathematical formalism, and they may have a broader set of mathematical tools available to them, which might turns out to be a hinderance. For instance, a control researcher might ask why KL divergence is used instead of all the other measurements the guages how different two fucntions are. Turns out, it is emperically easier to implement, yet you need to go to a senimar to find the reasoning behind it. they may find the lack of theoretical support hard to palade. The idea of reinforcement learning is rather straight forward, what is hard is its implementation details.

The third barrier facing control researchers is the jagons and speed of change. If you try to pick up RL from text book today, most likely you would be overwholed by acronyms such XXXXXXXXXX. Some of them might already be proven ineffective implementation of the underlying ideas and the best practice has converged to something else.

This wave of innovation brought about by the reinforcement learning community is not just the implementation techniques, but also the computational infrastructure, notabally the GPU enabled parallelization. There are classical control algorithms that such as Differential Dynamic Programming can now be computed in a paralleled fashion. We would also like to list the papers who adapt well known control algorithms for the newly available computational platforms.

We first provide a taxotomy of reinforcement learning, then we elaborate on the enumerated path in section II and list all the important papers in this area of research. Finally, in section VII, we introduce how the computational capacity unleashed for reinforcement learning algorithms can be better merged with well-known control algorithms.

## II. INTUITION BEHIND NEURAL NETWORK

By now, neural network is widely accepted that as the universal function approximator [5] and the grandfathers of this field such as Andrew Ng and Geoffrey Hinton are also its most proficient proselytizer. Yet not that many materials goes into the intuition behind neural network. Here we provide

control researchers with minimal exposure to deep learning the graphical reasonings behind neural network. For people who are interested in tracing the development of this subject, we list the following seminal papers: [6] [7].....

### A. Basic Network

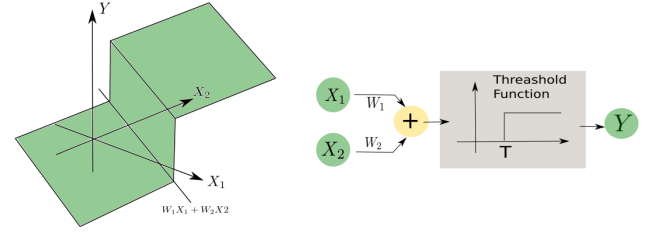


Fig. 1: Graphical Representation of Network Unit

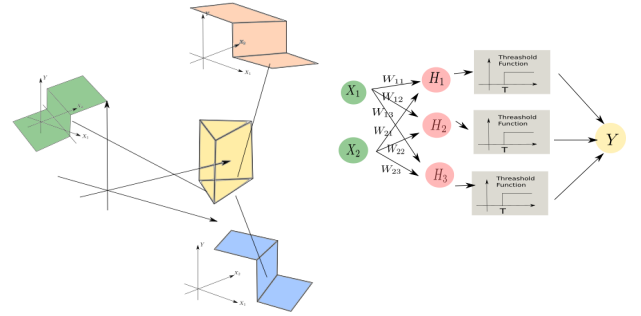


Fig. 2: jljlkjljljkj

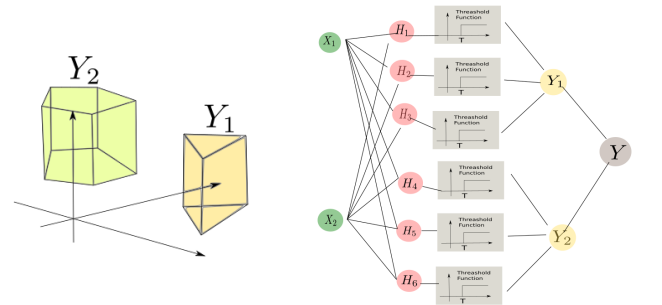


Fig. 3: lkjlkljlkjljkj

### B. Recurrent Network and Variational Inference

Pratially Observable Markov Decision Process (POMDP) is treated with recurrent neural network to contextualize the

## III. WHERE TO APPROXIMATE

The constraints imposed in the Trajectory Optimization formulation manifest themselves directly in policy  $\pi(x)$  and resulting in either a narrow band of trajectories or a single optimal solution. However, adjustments in the reinforcement learning formulation is not the policy per se but its distribution.

Eventually, what we hope to achieve via learning is a policy distribution, either through policy gradient method or cost to go method, which would maximize the expected reward of a trajectory.

Reinforcement Learning is not a new subject, control researchers probably know it by the name Approximate Dynamic Programming. Yet the major progress in recent years is the enhanced computation power which brought about the potential of neuronetworks as a to fruition. Most notably the series of wins reinforcement agents such as AlphaGo, AlphaStar forged against the best human players in the respective disciplines.

Broadly speaking, there are three revenues where neuronetwork based approximation can find its way into optimization as shown in 4. One is learning a dynamics model from samle; Second is policy gradient based learning; Third is approximation of cost to go functions such as value funtion and Q function. The details of the implementation would be specified in the subsequent sections.

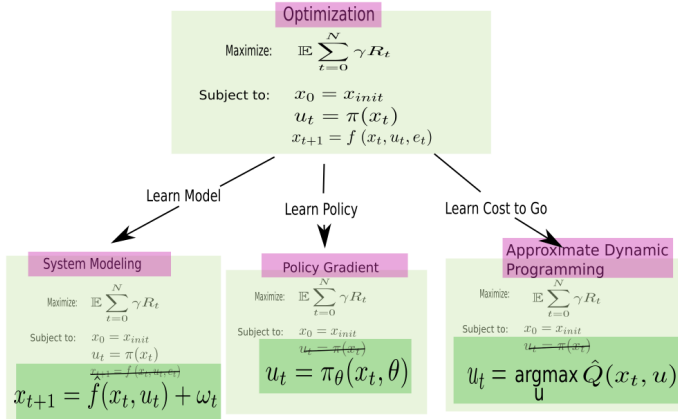


Fig. 4: From Optimization to Learning

Before we dive into the detailed researches in each category, we'd like to introduce additional mathematical tools and measurements that has been proven useful in merging reinforcement learning with optimization. One of the most important change of perspectives when control researchers ventures into the land of reinforcement learning is to formulate optimization as an inference problem [8]. Traditional optimization would translate constraints imposed on the struture into definitive trajectories, subject to disturbance and correction. Yet inference view of optimization is an ever narrowing band od distribution as information trickles in via experiments.

There are two things control researchers should be aware of. One, if you simply apply reinforcement learning as it is written in Richard Sutton's book, it probably won't work for you. Additional statistical learning techniques are required. Two, Statistical learning is booming with ideas at this point. Every newly invented measurement and methods could be pretzeled into a self-sustainly structure if you know how to make such arguments, that does not mean it would be a useful tool for your research.

Here we point out two concepts: Mutual Information and Baysian NeuroNet, which have proven to be integral for converting optimization into an inference.

The go to text book for reinforcement learning community is that of Richard Sutton [9]. In the system constructed by Richard, the objective of an agent is to maximize discounted reward. This formulation is proven a sound goal in the context of video games. However, for optimizations with a physics underpinning, reward maximization is not adequate for noise and disturbances.

Exploration and Exploitation trade off is something studied exhaustively in the reinforcement learning community. A common strategy is  $\epsilon$  greedy policy where the value of epsilon decays as the learning progresses. Yet, the decaying rate is a hyperparater that need to be tuned. Is there are more sysmtmatical way to balance the exploration and exploitation trade-off? This is particularly important for control related training since this application has considerable amount of disturbance and noise. If the policy converges too soon, any subsequent disturce can deviate the trajectory to the extend that it is no longer controllable.

The intuition behind maximum entropy reinforcenement learning is the heuristic that when we don't know all the circumstance, we should prioritize options that could give us more choices regardless of how the system dynamics turns out to be. Statitically speaking, this means we should maximize the entropy of a distribution, which measures how uncertain or how broad the distributionb is.

The mathematical measurement used is mutual information [10]. It measures how much information regarding the random variable X is contained in the distribution of random variable Y. A reasonable question to ask is that out of all those measurements which captures "distance" in measurement theory, why a divergence is chosen? Turns out, this choice is made because of its computational convenience, much like exponentials are chosen in integral transform because its nice features.

#### IV. SYSTEM MODELLING

There are two ways for collecting data of the system. One is offline. Just collecting as much trajectories as possible about this system and then build the model later. Second is online data collection where a sample is collected and then incorporated into the model building process right away.

Strictly speaking, offline data collection based model building belongs to the domain of System Identification rather than reinforcement learning. But since it is tangentially related to our paper, we still list it here. After the data is collected and a system model is trained from offline data, an appropriate controllers can be computed based on that model. There are numerous applications in this line of research, supposedly the first successfully implemented non-linear controller based on this method is that of Caltech's Neural Lander. [11]

Model building in the reinforcement context really refers to the only data collection and model refinement process. This model training process doesn't have to start from scratch, although that is certainly an option. Most likely there already exist a model that partially describes the system. It would be more efficient if we can somehow combine that partial model with a neural network, which would capture the unmodelled dynamics via online training.

## ONLINE MIRROR DESCENT. BRYAN BOON'S WORK ON PATH PLANNING AND REINFORCEMENT LERAN-ING

A existing model can be additively combined [12] with a neural network, or it can be embedded into a neural network [13] as shown by Fig. 5. Optimization solver can also be embedded in the neural network as a laywer to encourage faster convergence. [14] [15] [16].

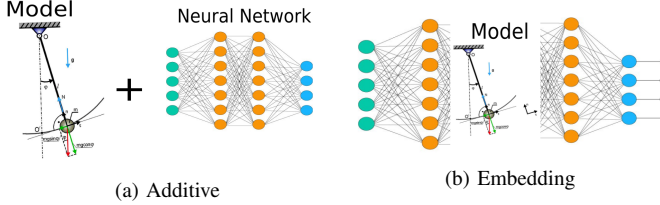


Fig. 5: Combine Model and Neural Net

While in theory the aforementioned modelling method should work, in practice it is proven to be far from optimal. [17]. One possible explanation is that any overfitting of the model along the way would be difficult to overcome by subsequent training, resulting in suboptimal performance. One solution is to measure uncertainly of the model with Bayesian Neural Network.

The venena formulation of neuronetwork is one where the weight of each neuron  $w_i$  is a single number, which is adjusted based on the backward propogation process. Baysian Neural Network(BNN) is a network where the weigh is subject to a parameterized distribution as shown in Fig. 6

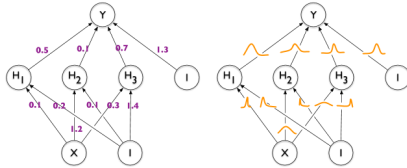


Fig. 6: Neural Network and BNN

BNN is used to measure the uncertainly of the model and better choices can be made when uncertainly of the model is part of the decision making process. [18]

## THIS IS THE PART ABOUT BAYSIAN REINFORCE- MENT LEARNING

The collected data can be used to train a model which informs which actions should be chosen. It can also be used to train the policy distribution either directly or through policy gradient. The direct policy training method is a theoretical possibility, but due since the number of actions along a trajectory is usually rather large, the valishing gradient problem facing this methods makes it had to implement. In this paper,we focus our discussion on the Policy Gradient Method.

When control researchers are first exposed to the proof of policy gradient method provided in Richard Sutton's book, they would find it difficult to swallow. The notations are tidious and the logic non-rigirous. A better proof was only recently presented. Please refer to this paper for policy gradient derivation. [19]

## V. POLICY GRADIENT

### VI. APPROXIMATE DYNAMIC PROGRAMMING

1. MAX entropy 2. the formulation of cost to go without a system model

### VII. OTHER WAYS TO UTILIZE INCREASED COMPUTATIONAL POWER

A. Multiagent Formulation

B. Monte Carlo Tree Search

C. Random Shoot

One of the corrilary of the development of reinforcement leraning is improvement in computational infrastructure, which is something the control community can take advantage of. Before this wave of hype in machine learning, GPU enabled computation was a specialty knowledge that is only accessible to large corporations. But now, with CUDA and related software, such computational power is as easy

Random shoot is the idea if rolling out trajectory at random and wht the fuck is random shoot?

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