Deep Reinforcement Learning Based Intelligent Reflecting Surface for Secure Wireless Communications

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Abstract

In this paper, we study an intelligent reflecting surface (IRS)-aided wireless secure communication system for physical layer security, where an IRS is deployed to adjust its reflecting elements to secure the communication of multiple legitimate users in the presence of multiple eavesdroppers. Aiming to improve the system secrecy rate, a design problem for jointly optimizing the base station (BS)'s beamforming and the IRS's reflecting beamforming is formulated considering different quality of service (QoS) requirements and time-varying channel conditions. As the system is highly dynamic and complex, and it is challenging to address the non-convex optimization problem, a novel deep reinforcement learning (DRL)-based secure beamforming approach is firstly proposed to achieve the optimal beamforming policy against eavesdroppers in dynamic environments. Furthermore, post-decision state (PDS) and prioritized experience replay (PER) schemes are utilized to enhance the learning efficiency and secrecy performance. Specifically, PDS is capable of tracing the environment dynamic characteristics and adjust the beamforming policy accordingly. Simulation results demonstrate that the proposed deep PDS-PER learning based secure beamforming approach can significantly improve the system secrecy rate and QoS satisfaction probability in IRS-aided secure communication systems.

Index Terms—Physical layer security, intelligent reflecting surface, beamforming, secrecy rate, deep reinforcement learning.

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I. INTRODUCTION

Physical layer security (PLS) has attracted increasing attention as an alternative of cryptography-based techniques for wireless communications [1], where PLS exploits the wireless channel characteristics by using signal processing designs and channel coding to support secure communication services without relying on a shared secret key [1], [2]. So far, a variety of approaches have been reported to improve PLS in wireless communication systems, e.g., cooperative relaying strategies [3], [4], artificial noise-assisted beamforming [5], [6], and cooperative jamming [7], [8]. However, employing a large number of active antennas and relays in PLS systems incurs an excessive hardware cost and the system complexity. Moreover, cooperative jamming and transmitting artificial noise require extra transmit power for security guarantees.

To tackle these shortcomings of the existing approaches [3]-[8], a new paradigm, called intelligent reflecting surface (IRS) [9]-[13], has been proposed as a promising technique to achieve high spectrum efficiency and energy efficiency, and enhance secrecy rate in the fifth generation (5G) and beyond wireless communication systems. In particular, IRS is a uniform planar array which is comprised of a number of low-cost passive reflecting elements, where each of elements adaptively adjusts its reflection amplitude and/or phase to control the strength and direction of the electromagnetic wave, hence IRS is capable of enhancing and/or weakening the reflected signals at different users [9]. As a result, the reflected signal by IRS can increase the received signal at legitimate users while suppressing the signal at the eavesdroppers [9]-[13]. Hence, from the PLS perspective, some innovative studies have been recently devoted to performance optimization for IRS-aided secure communications [14]-[25].

A. Related Works

Initial studies on IRS-aided secure communication systems have reported in [14]-[17], where a simple system model with only a single-antenna legitimate user and a single-antenna eavesdropper was considered in these works. The authors in [14] and [15] applied the alternative optimization (AO) algorithm to jointly optimize the transmit beamforming vector at the base station (BS) and the phase elements at the IRS for the maximization of the secrecy rate, but they did not extend their models to multi-user IRS-assisted secure communication systems. To minimize the transmit power at the BS subject to the secrecy rate constraint, the authors in [18]

utilized AO solution and semidefinite programming (SDP) relaxation to address the optimization problem with the objective to jointly optimize the power allocation and the IRS reflecting beamforming. In addition, Feng, et al. [19] also studied the secure transmission framework with an IRS to minimize the system transmit power in cases of rank-one and full-rank BS-IRS links, and derived a closed-form expression of beamforming matrix. Different from these studies [14]-[19] which considered only a single eavesdropper, secure communication systems comprising multiple eavesdroppers were investigated in [20]-[22]. Chen, $et\ al.$ [20] presented a minimum-secrecy-rate maximization design to provide secure communication services for multiple legitimate users while keeping them secret from multiple eavesdroppers in an IRS-aided multi-user multiple-input single-output (MISO) system, but the simplification of the optimization problem may cause a performance loss. The authors in [23] and [24] studied an IRS-aided multiple-input multiple-output (MIMO) channel, where a multi-antenna BS trasnmits data stream to a multi-antenna legitimate user in the presence of an eavesdropper configured with multiple antennas, and a suboptimal secrecy rate maximization approach was presented to optimize the beamforming policy. In addition to the use of AO or SDP in the system performance optimization, the minorization-maximization (MM) algorithm was recently utilized to optimize the joint transmit beamforming at the BS and phase shift coefficient at the IRS [16], [23].

Moreover, the authors in [22] and [25] employed the artificial noise-aided beamforming for IRS-aided MISO secure communication systems to improve the system secrecy rate, and an AO based solution was applied to jointly optimize the BSs beamforming, artificial noise interference vector and IRSs reflecting beamforming with the goal to maximize the secrecy rate. All these existing studies [14]-[20], [22]-[25] assumed that perfect channel state information (CSI) of legitimate users or eavesdroppers is available at the BS, which is not a practical assumption. The reason is that acquiring perfect CSI at the BS is challenging since the corresponding CSI may be outdated when the channel is time-varying due to the transmission delay, processing delay, and high mobility of users. Hence, Yu, $et\ al.$ [21] investigated a optimization problem with considering the effectt of outdated CSI of the eavesdropping channels in an IRS-aided secure communication system, and a robust algorithm was proposed to address the optimization problem in the presence of multiple eavesdroppers.

The above mentioned studies [14]-[25] mainly applied the traditional optimization techniques

e.g., AO, SDP or MM algorithms to jointly optimize the BSs beamforming and the IRSs reflecting beamforming in IRS-aided secure communication systems, which are less efficient for large-scale systems. Inspired by the recent advances of artificial intelligence (AI), several works attempted to utilize AI algorithms to optimize IRSs reflecting beamforming [26]-[29]. Deep learning (DL) was exploited to search the optimal IRS reflection matrices that maximize the achievable system rate in an IRS-aided communication system, and the simulation demonstrated that DL significantly outperforms conventional algorithms. Moreover, the authors in [31] and [32] proposed deep reinforcement learning (DRL) based approach to address the non-convex optimization problem, and the phase shifts at the IRS are optimized effectively. However, the works [26]-[29] merely considered to maximize the system achievable rate of a single user without considering the scenario of multiple users, secure communication and imperfect CSI in their models. The authors in [30] and [31] applied reinforcement learning (RL) to achieve smart beamforming at the BS against an eavesdropper in complex environments, but the IRS-aided secure communication system needs to optimize the IRS's reflect beamforming in addition to the BS's transmit beamforming. To the best of our knowledge, RL or DRL has not been explored yet in prior works to optimize both the BS's transmit beamforming and the IRS's reflect beamforming in dynamic IRS-aided secure communication systems, under the condition of multiple eavesdroppers and imperfect CSI, which thus motivates this work.

B. Contributions

In this paper, we investigate an IRS-aided secure communication system with the objective to maximize the system secrecy rate of multiple legitimate users in the presence of multiple eavesdroppers under realistic time-varying channels, while guaranteeing quality of service (QoS) requirements of legitimate users. A novel DRL-based secure beamforming approach is firstly proposed to jointly optimize the beamforming matrix at the BS and the reflecting beamforming matrix (reflection phases) at the IRS in dynamic environments. The major contributions of this paper are summarized as follows:

- The physical secure communication based on IRS with multiple eavesdroppers is investigated under the condition of time-varying channel coefficients in this paper. In addition, we formulate a joint BS's transmit beamforming and IRS's reflect beamforming optimization

problem with the goal of maximizing the system secrecy rate while considering the QoS requirements of legitimate users.

- An RL-based intelligent beamforming framework is presented to achieve the optimal BSs beamforming and the IRS's reflecting beamforming, where the central controller intelligently optimizes the beamforming policy by using a Markov decision process (MDP) according to the instantaneous observations from dynamic environment. Specifically, a QoS-aware reward function is constructed by covering both the secrecy rate and users QoS requirements into the learning process.
- A DRL-based secure beamforming approach is proposed to improve the learning efficiency and secrecy performance by fully exploiting the information of complex structure of the beamforming policy domain, where post-decision state (PDS) is utilized to improve the learning efficiency and rate, and prioritized experience replay (PER) is applied to enhance the sampling efficiency.
- Extensive simulation results are provided to demonstrate the effectiveness of the proposed deep PDSPER leaning based secure beamforming approach in terms of improving the secrecy rate and the QoS satisfaction probability, compared with other existing approaches. For instance, the proposed learning approach achieves the secrecy rate and QoS satisfaction level improvements of 17.21% and 8.67%, compared with the approach [14] in time-varying channel condition.

The rest of this paper is organized as follows. Section II presents the system model and problem formulation. The optimization problem is formulated as an RL problem in Section III. Section IV proposes a deep PDS-PER based secure beamforming approach. Section V provides simulation results and Section VI concludes the paper.

Notations: In this paper, vectors and matrices are represented by Boldface lowercase and uppercase letters, respectively. $\mathrm{Tr}(\cdot)$, $(\cdot)^*$ and $(\cdot)^H$ denote the trace, the conjugate and the conjugate transpose operations, respectively. $|\cdot|$ and $||\cdot||$ stand for the absolute value of a scalar and the Euclidean norm of a vector or matrix, respectively. $\mathbb{E}[\cdot]$ denotes the expectation operation. $\mathbb{C}^{M\times N}$ represents the space of complex-valued matrices.

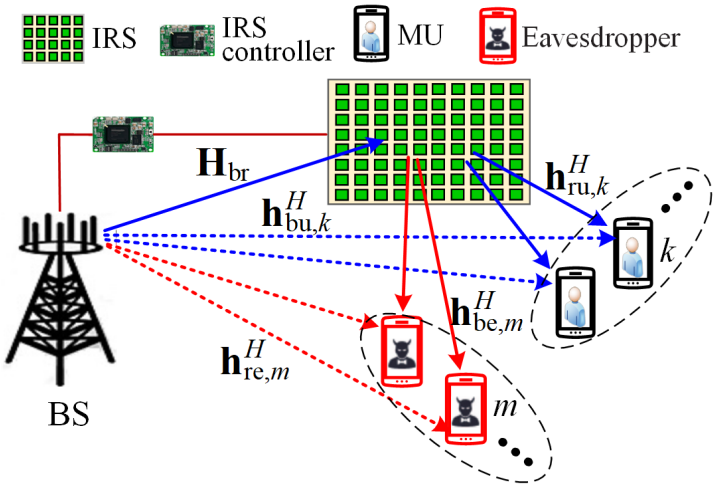

Fig. 1. IRS-aided secure communication under multiple eavesdroppers.

II. System Model and Problem Formulation

A. System Model

We consider an IRS-aided secure communication system, as shown in Fig. 1, where the BS is equipped with N antennas to serve K single-antenna legitimate mobile users (MUs) in the presence of M single-antenna eavesdroppers. An IRS with L reflecting elements is deployed in the system to assist secure wireless communications from the BS to the MUs. The IRS is equipped with a controller to coordinate the BS. For the ease of practical implementation, the maximal reflection without power loss at the IRS is considered since the reflecting elements are designed to maximize the reflected desired signal power to the MUs [13]-[23]. In addition, unauthorized eavesdroppers aim to eavesdrop any of the data streams of the MUs. Hence, the use of reflecting beamforming at IRS is also investigated to improve the achievable secrecy rate at the MUs while suppressing the wiretapped data rate at the eavesdroppers.

Let $\mathcal{K} = \{1, 2, \ldots, K\}$, $\mathcal{M} = \{1, 2, \ldots, M\}$ and $\mathcal{L} = \{1, 2, \ldots, L\}$ denote the MU set, the eavesdropper set and the IRS reflecting element set, respectively. Let $\mathbf{H}_{\rm br} \in \mathbb{C}^{L\times N}$, $\mathbf{h}_{{\rm bu},k}^H \in \mathbb{C}^{1\times N}$, $\mathbf{h}_{{\rm ru},k}^H \in \mathbb{C}^{1\times L}$, $\mathbf{h}_{{\rm be},m}^H \in \mathbb{C}^{1\times N}$, and $\mathbf{h}_{{\rm re},m}^H \in \mathbb{C}^{1\times L}$ denote the channel coefficients from the BS to the IRS, from the BS to the k-th MU, from the IRS to the k-th MU, from the BS to the m-th eavesdropper, and from the IRS to the m-th eavesdropper, respectively. All the above mentioned channel coefficients in the system are assumed to be small-scale fading with path loss which

follows the Rayleigh fading model [11]-[14], [21]. Let $\mathbf{\Psi} = \text{diag}(\chi_1 e^{j\theta_1}, \chi_2 e^{j\theta_2}, \ldots, \chi_L e^{j\theta_L})$ denote the reflection coefficient matrix associated with effective phase shifts at the IRS, where $\chi_l \in [0, 1]$ and $\theta_l \in [0, 2\pi]$ denote the amplitude reflection factor and the phase shift coefficient on the combined transmitted signal, respectively. As each phase shift is desired to be design to achieve full reflection, we consider that $\chi_l = 1$, $\forall l \in \mathcal{L}$ in the sequel of the paper. .

At the BS side, the beamforming vector for the k-th MU is denoted as $\mathbf{v}_k \in \mathbb{C}^{N\times 1}$, which is the continuous linear precoding [11]-[16], [23]. Thus, the transmitted signal for all MUs at the BS is written as $\mathbf{x} = \sum_{k=1}^{K} \mathbf{v}_k s_k$, where s_k is the transmitted symbol for the k-th MU which can be modelled as independent and identically distributed (i.i.d.) random variables with zero mean and unit variance [11]-[16], [23]. The total transmit power at the BS is subject to the maximum power constraint:

$$\mathbb{E}[||\mathbf{x}||^2] = \text{Tr}(\mathbf{V}\mathbf{V}^H) \leq P_{\max} \tag{1}$$

where $\mathbf{V} \triangleq [\mathbf{v}_1, \mathbf{v}_2, \ldots, \mathbf{v}_K] \in \mathbb{C}^{M\times K}$, and $P_{\max}$ is the maximum transmit power at the BS.

When the BS transmits a secret message to the k-th MU, the MU will receive the signal from the BS and the reflected signal from the IRS. Accordingly, the received signal at MU k can be given by

$$y_k = \underbrace{\left(\mathbf{h}_{\text{ru},k}^H \mathbf{\Psi} \mathbf{H}_{\text{br}} + \mathbf{h}_{\text{bu},k}^H\right) \mathbf{v}_k s_k}_{\text{desired signal}} + \underbrace{\sum_{i\in\mathcal{K}, i\neq k} \left(\mathbf{h}_{\text{ru},k}^H \mathbf{\Psi} \mathbf{H}_{\text{br}} + \mathbf{h}_{\text{bu},k}^H\right) \mathbf{v}_i s_i}_{\text{inter-userinterference}} + n_k \tag{2}$$

where n_k denotes the additive complex Gaussian noise (AWGN) with the with zero mean and variance δ_k^2 at the k-th MU. In (2), we observe that in addition to the received desired signal, each MU also suffers inter-user interference (IUI) in the system. In addition, the received signal at eavesdropper m is expressed by

$$y_k = \underbrace{\left(\mathbf{h}_{\text{ru},k}^H \mathbf{\Psi} \mathbf{H}_{\text{br}} + \mathbf{h}_{\text{bu},k}^H\right) \mathbf{v}_k s_k}_{\text{desired signal}} + \underbrace{\sum_{i\in\mathcal{K}, i\neq k} \left(\mathbf{h}_{\text{ru},k}^H \mathbf{\Psi} H_{\text{br}} + \mathbf{h}_{\text{bu},k}^H\right) \mathbf{v}_i s_i}_{\text{inter-userinterference}} + n_k \tag{3}$$

where n_k is the AWGN of eavesdropper m with the variance δ_m^2 .

Based on (2), the data rate of the k-th MU in (bits/s/Hz) is given by

$$R_k^{\mathrm{u}} = \log_2 \left(1 + \frac{\left| (\mathbf{h}_{\mathrm{ru},k}^H \mathbf{\Psi} \mathbf{H}_{\mathrm{br}} + \mathbf{h}_{\mathrm{bu},k}^H) \mathbf{v}_k \right|^2}{\left| \sum_{i \in \mathcal{K}, i \neq k} (\mathbf{h}_{\mathrm{ru},k}^H \mathbf{\Psi} \mathbf{H}_{\mathrm{br}} + \mathbf{h}_{\mathrm{bu},k}^H) \mathbf{v}_i \right|^2 + \delta_k^2} \right). \tag{4}$$

If the m-th eavesdropper attempts to eavesdrop the signal of the k-th MU, its achievable wiretapped data rate can be expressed by

$$R_{m,k}^{\mathrm{e}} = \log_2 \left(1 + \frac{\left| (\mathbf{h}_{\mathrm{re},m}^H \mathbf{\Psi} \mathbf{H}_{\mathrm{br}} + \mathbf{h}_{\mathrm{be},m}^H) \mathbf{v}_k \right|^2}{\left| \sum_{i \in \mathcal{K}, i \neq k} (\mathbf{h}_{\mathrm{re},m}^H \mathbf{\Psi} \mathbf{H}_{\mathrm{br}} + \mathbf{h}_{\mathrm{be},m}^H) \mathbf{v}_i \right|^2 + \delta_m^2} \right). \tag{5}$$

Since each eavesdropper can eavesdrop any of the K MUs' signal, according to [14]-[25], the achievable individual minimum-secrecy rate from the BS to the k-th MU can be expressed by

$$R_k^{\mathrm{sec}} = \left[R_k^{\mathrm{u}} - \max_{\forall m} R_{m,k}^{\mathrm{e}} \right]^+ \tag{6}$$

where $[z]^+ = \max(0, z)$.

In practical systems, it is not easy for the BS and the IRS to obtain perfect CSI [9], [21]. This is due to the fact that both the transmission delay and processing delay exist, as well as the mobility of the users. Therefore, CSI may be outdated at the time when the BS and the IRS transmits the data stream to the MUs [21]. Once this outdated CSI is employed for beamforming, it will lead to a negative effect on the demodulation at the MUs, thereby leading to substantial performance loss [21]. Therefore, it is necessary to consider outdated CSI in the IRS-aided secure communication system.

Let T_{delay} denote the delay between the outdated CSI and the real-time CSI. In other words, when the BS receives the pilot sequences sent from the MUs at the time slot t, it will complete the channel estimation process and begin to transmit data stream to the MUs at the time slot $t+T_{\mathrm{delay}}$. Hence, the relation between the outdated channel vector $\mathbf{h}(t)$ and the real-time channel

vector $\mathbf{h}(t+T_{\text{delay}})$ can be expressed by

$$\mathbf{h}(t+T_{\text{delay}}) = \rho\mathbf{h}(t) + \sqrt{1-\rho^2}\hat{\mathbf{h}}(t+T_{\text{delay}}). \tag{7}$$

In (7), $\hat{\mathbf{h}}(t+T_{\text{delay}})$ is independent identically distributed with $\mathbf{h}(t)$ and $\mathbf{h}(t+T_{\text{delay}})$, and it is with zero-mean and unit-variance complex Gaussian entries. ρ is the autocorrelation function (outdated CSI coefficient) of the channel gain $\mathbf{h}(t)$ and $0 \leq \rho \leq 1$, which is given by

$$\rho = J_0(2\pi_{\text{pi}} f_D T_{\text{delay}}) \tag{8}$$

where $J_0(\cdot)$ is the zeroth-order Bessel function of the first kind, f_D is the Doppler spread which is generally a function of the velocity (υ) of the transceivers, the carrier frequency (f_c) and the speed of light (c), i.e., $f_D = \upsilon f_c/c$. Note that $\rho = 1$ indicates the outdated CSI effect is eliminated, whereas $\rho = 0$ represents no CSI.

B. Problem Formulation

To improve the security of the above mentioned IRS-aided communication system in the physical layer, we need to jointly optimize the BS's transmit beamforming matrix $\mathbf{V}$ and the IRS' reflecting beamforming matrix $\mathbf{\Psi}$ to maximize the achievable secrecy rate among all the MUs, subject to the QoS requirements and total transmit power constraint in the system. As such, the optimization problem is formulated as

$$\begin{aligned}
&\max_{\mathbf{V},\mathbf{\Psi}} \sum_{k\in\mathcal{K}} R_k^{\text{sec}} \\
&s.t.\ (\text{a}):\ R_k^{\text{sec}} \geq R_k^{\text{sec},\min}, \forall k \in \mathcal{K}, \\
&\quad\ (\text{b}):\ R_k^{\text{u}} \geq R_k^{\min},\ \forall k \in \mathcal{K}, \\
&\quad\ (\text{c}):\ \text{Tr}(\mathbf{V}) \leq P_{\max}, \\
&\quad\ (\text{d}):\ |\chi_l e^{j\theta_l}| = 1,\ 0 \leq \theta_l \leq 2\pi,\ \forall l \in \mathcal{L}
\end{aligned} \tag{9}$$

where $R_k^{\text{sec},\min}$ is the target secrecy rate of the k-th MU, and $R_k^{\min}$ denotes its target data rate. The constraints in (9a) and (9b) are imposed to satisfy the secure communication and the minimum data rate requirements, respectively. The constraint in (9c) is set to satisfy the

BS's maximum power constraint. The constraint in (9d) is the constraint of the IRS reflecting elements. Obviously, it is challenging to obtain an optimal solution to the optimization (9), since the objective function in (9) is non-concave with respect to either $\mathbf{V}$ or $\mathbf{\Psi}$, and the coupling of the optimization variables ($\mathbf{V}$ and $\mathbf{\Psi}$) and the unit-norm constraints in (9d) are non-convex.

III. Problem Transformation Based on RL

The optimization problem given in (9) is difficult to address as it is a non-convex problem. In addition, in realistic IRS-aided secure communication systems, the capabilities of MUs, the channel quality, and the service applications will change dynamically. Moreover, the problem in (9) is just a single time slot optimization problem, which may converge to a suboptimal solution and obtain the greedy-search like performance due to the ignorance of the historical system state and the long term benefit. Hence, it is generally infeasible to apply the traditional optimization techniques (AO, SDP, and MM) to achieve an effective secure beamforming policy in uncertain dynamic environments.

Model-free RL is a dynamic programming tool which can be adopted to solve the decision-making problem by learning the optimal solution in dynamic environments [32]. Hence, we model the secure beamforming optimization problem as an RL problem. In RL, the IRS-aided secure communication system is treated as an environment, the central controller at the BS is regarded as a learning agent. The key elements of RL are defined as follows

State space: Let $\mathcal{S}$ denote the system state space. The current system state $s \in \mathcal{S}$ includes the channel information of all users, the predicted secrecy rate, the transmission data rate of the last time slot and the QoS satisfaction level, which is defined as

$$s = \left\{ \{\mathbf{h}_k\}_{k\in K}, \{\mathbf{h}_m\}_{m\in\mathcal{M}}, \{R_k^{\text{sec}}\}_{k\in\mathcal{K}}, \{R_k\}_{k\in\mathcal{K}}, \{\text{QoS}_k\}_{k\in\mathcal{K}} \right\} \tag{10}$$

where $\mathbf{h}_k$ and $\mathbf{h}_m$ are the channel coefficients of the k-th MU and m-th eavesdropper, respectively. QoS_k is the feedback QoS satisfaction level of the k-th MU. Other parameters in (10) are already defined in Section II.

Action space: Let $\mathcal{A}$ denote the system action space. According to the observed system state s, the central controller chooses the beamforming vector $\{\mathbf{v}_k\}_{k\in\mathcal{K}}$ at the BS and the IRS reflecting

beamforming coefficient (phase shift) $\{\theta_l\}_{l\in\mathcal{L}}$ at the IRS. Hence, the action $a \in \mathcal{A}$ can be defined by

$$a = \left\{ \{\mathbf{v}_k\}_{k\in\mathcal{K}}, \{\theta_l\}_{l\in\mathcal{L}} \right\}. \tag{11}$$

Transition probability: Let $\mathcal{T}(s'|s,a)$ represent the transition probability, which is the probability of transitioning to a new state $s' \in \mathcal{S}$, given the action a executed in the sate s.

Reward function: In RL, the reward acts as a signal to evaluate how good the secure beamforming policy is when the agent executes an action at a current state. The system performance will be enhanced when the reward function at each learning step correlates with the desired objective. Thus, it is important to design an efficient reward function to improve the MUs' QoS satisfaction levels.

In this paper, the reward function represents the optimization objective, and our objective is to maximize the system secrecy rate of all MUs while guaranteeing their QoS requirements. Thus, the presented QoS-aware reward function is expressed as

$$r = \underbrace{\sum_{k\in\mathcal{K}} R_k^{\text{sec}}}_{\text{part 1}} - \underbrace{\sum_{k\in\mathcal{K}} \mu_1 p_k^{\text{sec}}}_{\text{part 2}} - \underbrace{\sum_{k\in\mathcal{K}} \mu_2 p_k^{\text{u}}}_{\text{part 3}} \tag{12}$$

where

$$p_k^{\text{sec}} = \begin{cases} 1, \text{ if } R_k^{\text{sec}} < R_k^{\text{sec},\min}, \forall k \in \mathcal{K}, \\ 0, \text{ otherwise}, \end{cases} \tag{13}$$

$$p_k^{\text{u}} = \begin{cases} 1, \text{ if } R_k < R_k^{\min}, \forall k \in \mathcal{K}, \\ 0, \text{ otherwise}. \end{cases} \tag{14}$$

In (12), the part 1 represents the immediate utility (system secrecy rate), the part 2 and the part 3 are the cost functions which are defined as the unsatisfied secrecy rate requirement and the unsatisfied minimum rate requirement, respectively. The coefficients μ_1 and μ_2 are the positive constants of the part 2 and the part 3 in (12) , respectively, and they are used to balance the

utility and cost [33]-[35].

The goals of (13) and (14) are to impose the QoS satisfaction levels of both the secrecy rate and the minimum data rate requirements, respectively. If the QoS requirement is satisfied in the current time slot, then $p_k^{\text{sec}} = 0$ or $p_k^{\text{u}} = 0$, indicating that there is no punishment of the reward function due to the successful QoS guarantees.

The goal of the learning agent is to search for an optimal policy π^* (π is a mapping from states in $\mathcal{S}$ to the probabilities of choosing an action in $\mathcal{A}$: $\pi(s) : \mathcal{S} \rightarrow \mathcal{A}$) that maximizes the long-term expected discounted reward, and the cumulative discounted reward function can be defined as

$$U_t = \sum_{\tau=0}^{\infty} \gamma_\tau r_{t+\tau+1} \tag{15}$$

where $\gamma \in (0, 1]$ denotes the discount factor. Under a certain policy π, the state-action function of the agent with a state-action pair (s, a) is given by

$$Q^\pi(s_t, a_t) = \mathbb{E}_\pi \left[U_t | s_t = s, a_t = a \right]. \tag{16}$$

The conventional Q-Learning algorithm can be adopted to learn the optimal policy. The key objective of Q-Learning is to update Q-table by using the Bellman's equation as follows:

$$Q^\pi(s_t, a_t) = \mathbb{E}_\pi \left[r_t + \gamma \sum_{s_{t+1} \in \mathcal{S}} T(s_{t+1}|s_t, a_t) \sum_{a_{t+1} \in \mathcal{A}} \pi(s_{t+1}, a_{t+1}) Q^\pi(s_{t+1}, a_{t+1}) \right]. \tag{17}$$

The optimal action-value function in (17) is equivalent to the Bellman optimality equation, which is expressed by

$$Q^*(s_t, a_t) = r_t + \gamma \max_{a_{t+1}} Q^*(s_{t+1}, a_{t+1}) \tag{18}$$

and the state-value function is achieved as follows:

$$V(s_t) = \max_{a_t \in \mathcal{A}} Q(s_t, a_t). \tag{19}$$

In addition, the Q-value is updated as follows:

$$Q_{t+1}(s_t, a_t) = (1 - \alpha_t)Q_t(s_t, a_t) + \alpha_t \left(r_t + \gamma V_t(s_{t+1})\right) \tag{20}$$

where $\alpha_t \in (0, 1]$ is the learning rate. Q-Learning generally constructs a lookup Q-table $Q(s, a)$, and the agent selects actions based on the greedy policy for each learning step [32]. In the $\varepsilon-$greedy policy, the agent chooses the action with the maximum Q-table value with probability $1 - \varepsilon$, whereas a random action is picked with probability ε to avoid achieving stuck at non-optimal policies [32]. Once the optimal Q-function $Q^*(s, a)$ is achieved, the optimal policy is determined by

$$\pi^*(s, a) = \arg\max_{a \in \mathcal{A}} Q^*(s, a). \tag{21}$$

IV. Deep PDS-PER Learning Based Secure Beamforming

The secure beamforming policy discussed in Section III can be numerically achieved by using Q-Learning, policy gradient, and deep Q-Network (DQN) algorithms [32]. However, Q-Learning is not an efficient learning algorithm because it cannot deal with continuous state space and it has slow learning convergence speed. The policy gradient algorithm has the ability to handle continuous state-action spaces, but it may converge to a suboptimal solution. In addition, it is intractable for Q-learning and policy gradient algorithms to solve the optimization problem under high-dimensional input state space. Although DQN performs well in policy learning problem with continuous and high-dimensional state space, its non-linear Q-function estimator may lead to unstable or even diverge.

Considering the fact that the IRS-aided secure communication system has high-dimensional and high-dynamical characteristics according to the system state that is defined in (10) and uncertain CSI that is shown in (7), we propose a deep PDS-PER learning based secure beamforming approach, as shown in Fig. 2, where PDS-learning and PER mechanisms are utilized to enable the learning agent to learn and adapt faster in dynamic environments. In detail, the agent utilizes the observed state (i.e, CSI, previous secrecy rate, QoS satisfaction level), the feedback reward from environment as well as the historical experience from the replay buffer to train its learning

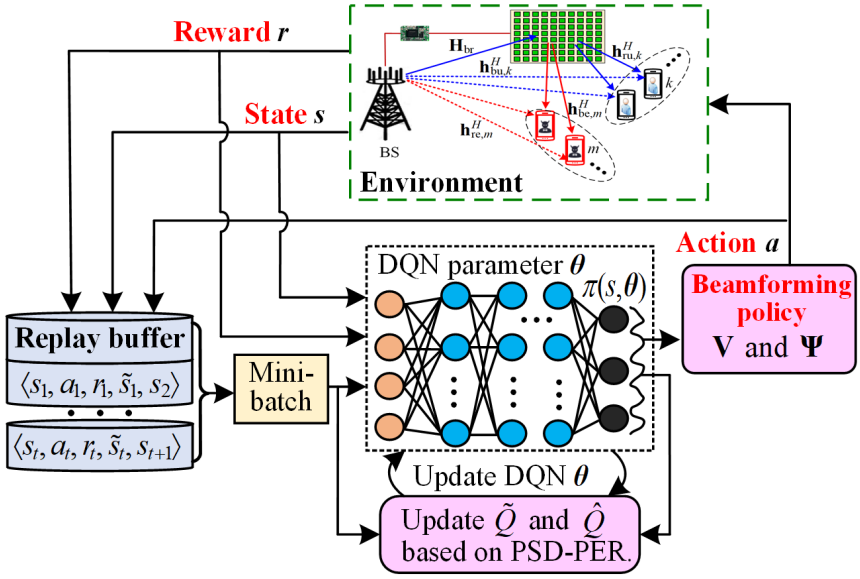

Fig. 2. Deep PDS-PER learning based beamforming for IRS-aided secure communications.

model. After that, the agent employs the trained model to make decision (beamforming matrices $\mathbf{V}$ and $\mathbf{\Psi}$) based on its learned policy. The procedures of the proposed learning based secure beamforming are provided in the following subsections.

Note that the policy optimization (in terms of the BS's beamforming matrix $\mathbf{V}$ and the RIS's reflecting beamforming matrix $\mathbf{\Psi}$) in the IRS-aided secure communication system can be performed at the BS and that the optimized reflecting beamforming matrix can be transferred in an offline manner to the IRS by the controller to adjust the corresponding reflecting elements accordingly.

A. Proposed Deep PDS-PER Learning

As discussed in Section II, CSI is unlikely to be known accurately due to the transmission delay, processing delay, and mobility of users. At the same time, beamforming with outdated CSI will decrease the secrecy capacity, and therefore, a fast optimization solution needs to be designed to reduce processing delay. PDS-learning as a well-known algorithm has been used to improve the learning speed by exploiting extra partial information (e.g., the previous location information and the mobility velocity of MUs or eavesdroppers that affect the channel coefficients)) and search for an optimal policy in dynamic environments [33]-[35]. Motivated by this, we devise a modified deep PDS-learning to trace the environment dynamic characteristics, and then adjust

the transmit beamforming at the BS and the reflecting elements at the IRS accordingly, which can speed up the learning efficiency in dynamic environments.

PDS-learning can be defined as an immediate system state $\tilde{s}_t \in \mathcal{S}$ happens after executing an action a_t at the current state s_t and before the next time state s_{t+1} . In detail, the PDS-learning agent takes an action a_t at state s_t, and then will receive known reward $r^{\mathrm{k}}(s_t, a_t)$ from the environment before transitioning the current state s_t to the PDS state $\tilde{s}_t$ with a known transition probability $\mathcal{T}^{\mathrm{k}}(\tilde{s}_t|s_t, a_t)$. After that, the PDS state further transform to the next state s_{t+1} with an unknown transition probability $\mathcal{T}^{\mathrm{u}}(s_{t+1}|\tilde{s}_t, a_t)$ and an unknown reward $r^{\mathrm{u}}(s_t, a_t)$, where corresponds to the wireless CSI dynamics. In PDS-learning, s_{t+1} is independent of s_t given the PDS state $\tilde{s}_t$, and the reward $r(s_t, a_t)$ is decomposed into the sum of $r^{\mathrm{k}}(s_t, a_t)$ and $r^{\mathrm{u}}(s_t, a_t)$ at $\tilde{s}_t$ and s_{t+1}, respectively. Mathematically, the state transition probability in PDS-learning from s_t to s_{t+1} admits

$$\mathcal{T}(s_{t+1}|s_t, a_t) = \sum\nolimits_{\tilde{s}_t} \mathcal{T}^{\mathrm{u}}(s_{t+1}|\tilde{s}_t, a_t)\mathcal{T}^{\mathrm{k}}(\tilde{s}_t|s_t, a_t). \tag{22}$$

Moreover, it can be verified that the reward of the current state-action pair (s_t, a_t) is expressed by

$$r(s_t, a_t) = r^{\mathrm{k}}(s_t, a_t) + \sum\nolimits_{\tilde{s}_t} \mathcal{T}^{\mathrm{k}}(\tilde{s}_t|s_t, a_t)r^{\mathrm{u}}(\tilde{s}_t, a_t). \tag{23}$$

At the time slot t, the PDS action-value function $\tilde{Q}(\tilde{s}_t, a_t)$ of the current PDS state-action pair $(\tilde{s}_t, a_t)$ is defined as

$$\tilde{Q}(\tilde{s}_t, a_t) = r^{\mathrm{u}}(\tilde{s}_t, a_t) + \gamma \sum_{s_{t+1}} \mathcal{T}^{\mathrm{u}}(s_{t+1}|\tilde{s}_t, a_t)V(s_{t+1}). \tag{24}$$

By employing the extra information (the known transition probability $\mathcal{T}^{\mathrm{k}}(\tilde{s}_t|s_t, a_t)$ and known reward $r^{\mathrm{k}}(s_t, a_t)$), the Q-function $\hat{Q}(s_t, a_t)$ in PDS-learning can be further expanded under all state-action pairs (s, a), which is expressed by

$$\hat{Q}(s_t, a_t) = r^{\mathrm{k}}(s_t, a_t) + \sum\nolimits_{\tilde{s}_t} \mathcal{T}^{\mathrm{k}}(\tilde{s}_t|s_t, a_t)\tilde{Q}(\tilde{s}_t, a_t). \tag{25}$$

The state-value function in PDS-learning is defined by

$$\hat{V}_t(s_t) = \sum\nolimits_{s_{t+1}} \mathcal{T}^{\mathrm{k}}(s_{t+1}|s_t, a_t)\tilde{V}(s_{t+1}) \tag{26}$$

where $\tilde{V}_t(s_{t+1}) = \max\limits_{a_t \in \mathcal{A}} \tilde{Q}_t(\tilde{s}_{t+1}, a_t)$. At each time slot, the PDS action-value function $\tilde{Q}(\tilde{s}_t, a_t)$ is updated by

$$\tilde{Q}_{_{t+1}}(\tilde{s}_t, a_t) = (1-\alpha_t)\tilde{Q}_t(\tilde{s}_t, a_t) + \alpha_t \left(r^{\mathrm{u}}(\tilde{s}_t, a_t) + \gamma \hat{V}_t(s_{t+1})\right). \tag{27}$$

After updating $\tilde{Q}_{_{t+1}}(\tilde{s}_t, a_t)$, the action-value function $\hat{Q}_{_{t+1}}(s_t, a_t)$ can be updated by plugging $\tilde{Q}_{_{t+1}}(\tilde{s}_t, a_t)$ into (25).

After presenting in the above modified PDS-learning, a deep PDS learning algorithm is presented. In the presented learning algorithm, the traditional DQN is adopted to estimatete the action-value Q-function $Q(s, a)$ by using $Q(s, a; \boldsymbol{\theta})$, where $\boldsymbol{\theta}$ denote the DNN parameter. The objective of DQN is to minimize the following loss function at each time slot

$$\begin{aligned} \mathcal{L}(\boldsymbol{\theta}_t) &= \left[\{\hat{V}_t(s_t; \boldsymbol{\theta}_t) - \hat{Q}(s_t, a_t; \boldsymbol{\theta}_t)\}^2\right] \\ &= \left[\{r(s_t, a_t) + \gamma \max_{a_{t+1} \in \mathcal{A}} \hat{Q}_t(s_{t+1}, a_{t+1}; \boldsymbol{\theta}_t) - \hat{Q}(s_t, a_t; \boldsymbol{\theta}_t)\}^2\right] \end{aligned} \tag{28}$$

where $\hat{V}_t(s_t; \boldsymbol{\theta}_t) = r(s_t, a_t) + \gamma \max\limits_{a_{t+1} \in \mathcal{A}} \hat{Q}_t(s_{t+1}, a_{t+1}; \boldsymbol{\theta}_t)$ is the target value. The error between $\hat{V}_t(s_t; \boldsymbol{\theta}_t)$ and the estimated value $\hat{Q}(s_t, a_t; \boldsymbol{\theta}_t)$ is usually called temporal-difference (TD) error, which is expressed by

$$\delta_t = \hat{V}_t(s_t; \boldsymbol{\theta}_t) - \hat{Q}(s_t, a_t; \boldsymbol{\theta}_t). \tag{29}$$

The DNN parameter $\boldsymbol{\theta}$ is achieved by taking the partial differentiation of the objective function (28) with respect to $\boldsymbol{\theta}$, which is given by

$$\boldsymbol{\theta}_{t+1} = \boldsymbol{\theta}_t + \beta \nabla L(\boldsymbol{\theta}_t). \tag{30}$$

where β is the learning rate of $\boldsymbol{\theta}$, and $\nabla(\cdot)$ denotes the first-order partial derivative.

Accordingly, the policy $\hat{\pi}_t(s)$ of the modified deep PDS-learning algorithm is given by

$$\hat{\pi}_t(s) = \arg\max_{a_t \in \mathcal{A}} \hat{Q}(s_t, a_t; \boldsymbol{\theta}_t). \tag{31}$$

Although DQN is capable of performing well in policy learning with continuous and high-dimensional state space, DNN may learn ineffectively and cause divergence owing to the non-stationary targets and correlations between samples. Experience replay is utilized to avoid the divergence of the RL algorithm. However, classical DQN uniformly samples each transition $e_t = \langle s_t, a_t, r_t, \tilde{s}_t, s_{t+1} \rangle$ from the experience replay, which may lead to an uncertain or negative effect on learning a better policy. The reason is that different transitions (experience information) in the replay buffer have different importance for the learning policy, and sampling every transition equally may unavoidably result in inefficient usage of meaningful transitions. Therefore, a prioritized experience replay (PER) scheme has been presented to address this issue and enhance the sampling efficiency [36], [37], where the priority of transition is determined by the values of TD error. In PER, a transition with higher absolute TD error has higher priority in the sense that is has more aggressive correction for the action-value function.

In the deep PDS-PER learning algorithm, similar to classical DQN, the agent collects and stores each experience $e_t = \langle s_t, a_t, r_t, \tilde{s}_t, s_{t+1} \rangle$ into its experience replay buffer, and DNN updates the parameter by sampling a mini-batch of tuples from the replay buffer. So far, PER was adopted only for DRL and Q-learning, and has never been employed with the PDS-learning algorithm to learn the dynamic information. In this paper, we further extend this PER scheme to enable prioritized experience replay in the proposed deep PDS-PER learning framework, in order to improve the learning convergence rate.

The probability of sampling transition i (experience i) based on the absolute TD-error is defined by

$$p(i) = |\delta(i)|^{\eta_1} \Big/ \sum\nolimits_{j'} |\delta(j')|^{\eta_1} \tag{32}$$

where the exponent η_1 weights how much prioritization is used, with $\eta_1 = 0$ corresponding to being uniform sampling. The transition with higher $p(i)$ will be more likely to be replayed from

the replay buffer, which is associated with very successful attempts by preventing the DNN from being over-fitting. With the help of PER, the proposed deep PDS-PER learning algorithm tends to replay valuable experience and hence learns more effectively to find the best policy.

It is worth noting that experiences with high absolute TD-error are more frequently replayed, which alters the visitation frequency of some experiences and hence causes the training process of the DNN prone to diverge. To address this problem, importance-sampling (IS) weights are adopted in the calculation of weight changes

$$W(i) = (D \cdot p(i))^{-\eta_2} \tag{33}$$

where D is the size of the experience replay buffer, and the parameter η_2 is used to adjust the amount of correction used.

Accordingly, by using the PER scheme into the deep PDS-PER learning, the DNN loss function (28) and parameter are rewritten respectively as follows:

$$\mathcal{L}\left(\boldsymbol{\theta}_t\right) = \frac{1}{H}\sum_{i=1}^{H}\left(W_i \mathcal{L}_i(\boldsymbol{\theta}_t)\right) \tag{34}$$

$$\boldsymbol{\theta}_{t+1} = \boldsymbol{\theta}_t + \beta\delta_t \nabla_{\boldsymbol{\theta}} \mathcal{L}(\boldsymbol{\theta}_t)) \tag{35}$$

Theorem 1: The presented deep PDS-PER learning can converge to the optimal $\hat{Q}(s_t, a_t)$ of the MDP with probability 1 when the learning rate sequence α_t meets the following conditions $\alpha_t \in [0, 1)$, $\sum_{t=0}^{\infty} \alpha_t = \infty$ and $\sum_{t=0}^{\infty} \alpha_t^2 < \infty$, where the above mentioned requirements on appear in most of the RL algorithms [32] and they are not specific to the proposed deep PDS-PER learning algorithm [32].

Proof: If each action can be executed with an infinite number of learning steps at each system state, or in other words, the learning policy is greedy with the infinite explorations, the Q-function $\hat{Q}(s_t, a_t)$ in PDS-learning and its corresponding policy strategy $\pi(s)$ will converge to the optimal points, respectively, with the probability of 1 [33]-[35]. The existing references [34] and [35] have provided the proof.

B. Secure Beamforming Based on Proposed Deep PDS-PER Learning

Similar to most DRL algorithms, our proposed deep PDS-PER learning based secure beamforming approach consists of two stages, i.e., the training stage and implement stage. The training process of the proposed approach is shown in **Algorithm 1**. A central controller at the BS is responsible for collecting environment information and making decision for secure beamforming.

In the training stage, similar to RL-based policy control, the control controller initializes network parameters and observes the current system state including CSI of all users, the previous predicted secrecy rate and the transmission data rate. Then, the state vector is input into DQN to train the learning model. The ε-greedy scheme is leveraged to balance both the exploration and exploitation, i.e., the action with the maximum reward is selected probability 1- ε according to the known knowledge, while a random action is chosen with probability ε based on the unknown knowledge. After executing the selected action, the agent receives a reward from the environment and observes the sate transition from s_t to PDS state $\tilde{s}_t$ and then to the next state s_{t+1}. Then, PDS-learning is used to update the PDS action-value function $\tilde{Q}(\tilde{s}_t, a_t; \theta_t)$ and Q-function $\hat{Q}(s_t, a_t; \theta_t)$, before collecting and storing the transition tuple (also called experience) $e_t = \langle s_t, a_t, r_t, \tilde{s}_t, s_{t+1} \rangle$ into the experience replay memory buffer $\mathcal{D}$, which includes the current system state, selected action, instantaneous reward and PDS state along with the next state. The experience in the replay buffer is selected by the PER scheme to generate mini-batches and they are used to train DQN. In detail, the priority of each transition $p(i)$ is calculated by using (32) and then get its IS weight $W(i)$ in (33), where the priorities ensure that high-TD-value ($\delta(i)$) transitions are replayed more frequently. The weight $W(i)$ is integrated into deep PDS learning to update both the loss function $\mathcal{L}(\theta)$ and DNN parameter $\boldsymbol{\theta}$. Once DQN converges, the deep PDS-PER learning model is achieved.

After adequate training in **Algorithm 1**, the learning model is loaded for the implement stage. During the implement stage, the controller uses the trained learning model to output its selected action a by going through the DNN parameter $\boldsymbol{\theta}$, with the observed state s from the IRS-aided secure communication system. Specifically, it chooses an action a, with the maximum value based on the trained deep PDS-PER learning model. Afterwards, the environment feeds back an instantaneous reward and a new system state to the agent. Finally, the beamforming matrix $\mathbf{V}^*$ at the BS and the phase shift matrix $\boldsymbol{\Psi}^*$ (reflecting beamforming) at the IRS are achieved

according to the selected action.

We would like to point out that the training stage needs a powerful computation server which can be performed offline at the BS while the implement stage can be completed online. The trained learning model requires to be updated only when the environment (IRS-aided secure communication system) has experienced greatly changes, mainly depending on the environment dynamics and service requirements.

C. Computational Complexity Analysis

For the training stage, in DNN, let L, Z_0 and Z_l denote the training layers, the size of the input layer (which is proportional to the number of states) and the number of neurons in the l-th layer, respectively. The computational complexity in each time step for the agent is $O(Z_0 Z_l + \sum_{l=1}^{L-1} Z_l Z_{l+1})$. In the training phase, each mini-batch has N^{epi} episodes with each episode being T time steps, each trained model is completed over I iterations until convergence. Hence, the total computational complexity in DNN is $O\left(IN^{\text{epi}}T(Z_0 Z_l + \sum_{l=1}^{L-1} Z_l Z_{l+1})\right)$. The high computational complexity of the DNN training phase can be performed offline for a finite number of episodes at a centralized powerful unit (such as the BS).

In our proposed deep PDS-PER learning algorithm, PDS-learning and PER schemes are utilized to improve the learning efficiency and enhance the convergence speed, which requires extra computational complexity. In PDS-learning leaning, since the set of PDS states is the same as the set of MDP states $\mathcal{S}$ [30]-[32], the computational complexity of the classical DQN algorithm and the deep PDS-learning algorithm are $O(|\mathcal{S}|^2 \times |\mathcal{A}|)$ and $O(2|\mathcal{S}|^2 \times |\mathcal{A}|)$, respectively. In PER, since the relay buffer size is D, the system requires to make both updating and sampling $O\left(\log_2 D\right)$ operations, so the computational complexity of the PER scheme is $O\left(\log_2 D\right)$.

According the above analysis, the complexity of the classical DQN algorithm and the proposed deep PDS-PER learning algorithm are respectively $O\left(IN^{\text{epi}}T(Z_0 Z_l + \sum_{l=1}^{L-1} Z_l Z_{l+1}) + |\mathcal{S}|^2 \times |\mathcal{A}|\right)$ and $O\left(IN^{\text{epi}}T(Z_0 Z_l + \sum_{l=1}^{L-1} Z_l Z_{l+1}) + 2|\mathcal{S}|^2 \times |\mathcal{A}| + \log_2 D\right)$, indicating that the complexity of the proposed algorithm is slightly higher than the classical DQN learning algorithm. However, our proposed algorithm achieves better performance than that of the classical DQN algorithm, which will be shown in the next section.

Algorithm 1 Deep PDS-PER Learning Based Secure Beamforming

Input: IRS-aided secure communication simulator and QoS requirements of all MUs (e.g., minimum secrecy rate and transmission rate).

Initialize: DQN with initial Q-function $Q(s, a; \boldsymbol{\theta})$, parameters $\boldsymbol{\theta}$, learning rate α and β.

Initialize: experience replay buffer $\mathcal{D}$ with size D, and mini-batch size H.

for each episode =1, 2, ..., N^{epi} **do**

  Observe an initial system state s;

  for each time step t=0, 1, 2, ..., T **do**

    Select action based on the ε-greedy policy at current state s_t: choose a random action a_t with probability ε;

    Otherwise, $a_t = \arg\max_{a_t \in \mathcal{A}} Q(s_t, a_t; \theta_t)$;

    Execute action a_t, receive an immediate reward $r^{\text{k}}(s_t, a_t)$ and observe the sate transition from s_t to PDS state $\tilde{s}_t$ and then to the next state s_{t+1};

    Update the reward function $r(s_t, a_t)$ under PDS-learning using (23);

    Update the PDS action-value function $\tilde{Q}(\tilde{s}_t, a_t; \boldsymbol{\theta}_t)$ using (27);

    Update the Q-function $\hat{Q}(s_t, a_t; \boldsymbol{\theta}_t)$ using (25);

    Store PDS experience $e_t = \langle s_t, a_t, r_t, \tilde{s}_t, s_{t+1} \rangle$ in experience replay buffer $\mathcal{D}$, if $\mathcal{D}$ is full, remove least used experience from $\mathcal{D}$;

    for i= 1, 2, ..., H **do**

      Sample transition i with the probability $p(i)$ using (32);

      Calculate the absolute TD-error $|\delta(i)|$ in (29);

      Update the corresponding IS weight W_i using (33);

      Update the priority of transition i based on $|\delta(i)|$;

    end for

    Update the loss function $\mathcal{L}(\boldsymbol{\theta})$ and parameter $\boldsymbol{\theta}$ of DQN using (34) and (35), respectively;

  end for

end for

Output: Return the deep PDS-PER learning model.

V. Simulation Results and Analysis

This section evaluates the performance of the IRS-aided secure communication system. As illustrated in Fig. 3, K single-antenna MUs and M single-antenna eavesdroppers are randomly

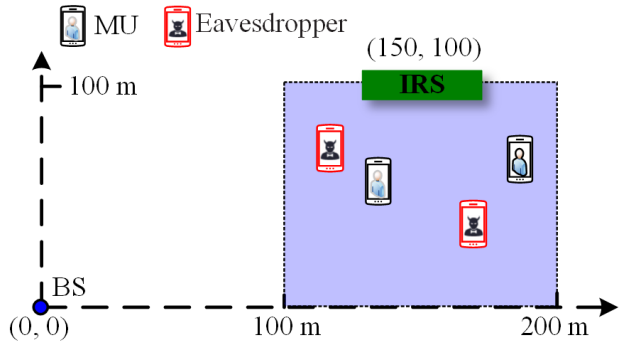

Fig. 3. Simulation setup.

located in the $100m \times 100m$ half right-hand side rectangular of Fig. 3 (light blue area) in a two-dimensional plane. The BS and the IRS are located at (0, 0) and (150, 100) in meter (m), respectively. The background noise power of MUs and eavesdroppers is equal to -90 dBm. We set the number of antennas at the BS is $N = 4$, the number of MUs is $K = 2$ and the number of eavesdroppers is $M = 2$. The transmit power $P_{\max}$ at the BS varies between 15 dBm and 40 dBm, the number of IRS elements L varies between 10 and 60, and the outdated CSI coefficient ρ varies from 0.5 to 1 for different simulation settings. The minimum secrecy rate and the minimum transmission data rate are 3 bits/s/Hz and 5 bits/s/Hz, respectively. The path loss model is defined by $PL = (PL_0 - 10\varsigma \log 10(d/d_0))$ dB, where $PL_0 = 30$ dB is the path loss at the reference distance $d_0 = 1$ m [9], $\varsigma = 3$ is the path loss exponent, and d is the distance from the transmitter to the receiver. The learning model consists of three connected hidden layers, containing 500, 250, and 200 neurons [38], respectively. The learning rate is set to $\alpha = 0.02$, the discount factor is set to $\gamma = 0.95$ and the exploration rate is set to $\varepsilon = 0.1$. The parameters μ_1 and μ_2 in (12) are set to $\mu_1 = \mu_2 = 2$ to balance the utility and cost [33]-[35]. Other parameters can be seen in references [9], [13] and [17]. The following simulation results are averaged over 500 independent realizations.

In addition, simulation results are provided to evaluate the performance of the proposed deep PDS-PER learning based secure beamforming approach (denoted as deep PDS-PER beamforming) in the IRS-aided secure communication system, and compare the proposed approach with the following exiting approaches:

- The classical DQN based secure beamforming approach (denoted as DQN-based beamform-

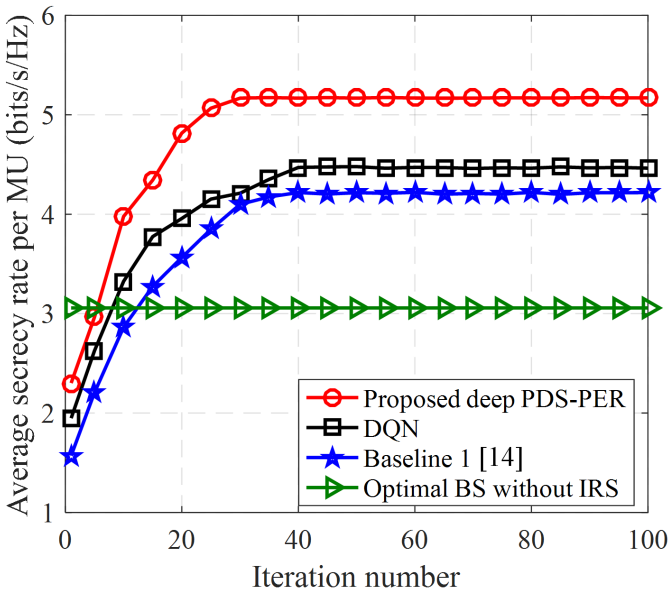

Fig. 4. Convergence comparisons of various approaches.

ing), where DNN is employed to estimate the Q-value function, when acting and choosing the secure beamforming policy corresponding to the highest Q-value.

- The existing secrecy rate maximization approach which optimizes the BS's transmit beamforming and the IRS's reflect beamforming by fixing other parameters as the constants (denoted as Baseline 1 [14]).
- The optimal BS's transmit beamforming approach without IRS assistance (denoted as optimal BS without IRS).

In Fig. 4, we first investigate the convergence performances of all secure beamforming approaches in terms of the average secrecy rate per MU, when $P_{\max} = 30$ dBm, $L = 40$, and $\rho = 0.95$. It is observed that the secrecy rate of all approaches first enhances and then converges to a constant level. In addition, it is worth noting that the proposed learning approach has the faster convergence speed and higher secrecy rate than that of the DQN approach by adopting by PDS-learning and PER schemes to enhance the learning efficiency, in order to improve convergence speed and provide the global optimal solution for joint beamforming optimization problem. Even through the Baseline1 approach needs the smaller number of iterations to achieve convergence than that of the DQN approach, it has lower secrecy rate. Moreover, the optimal

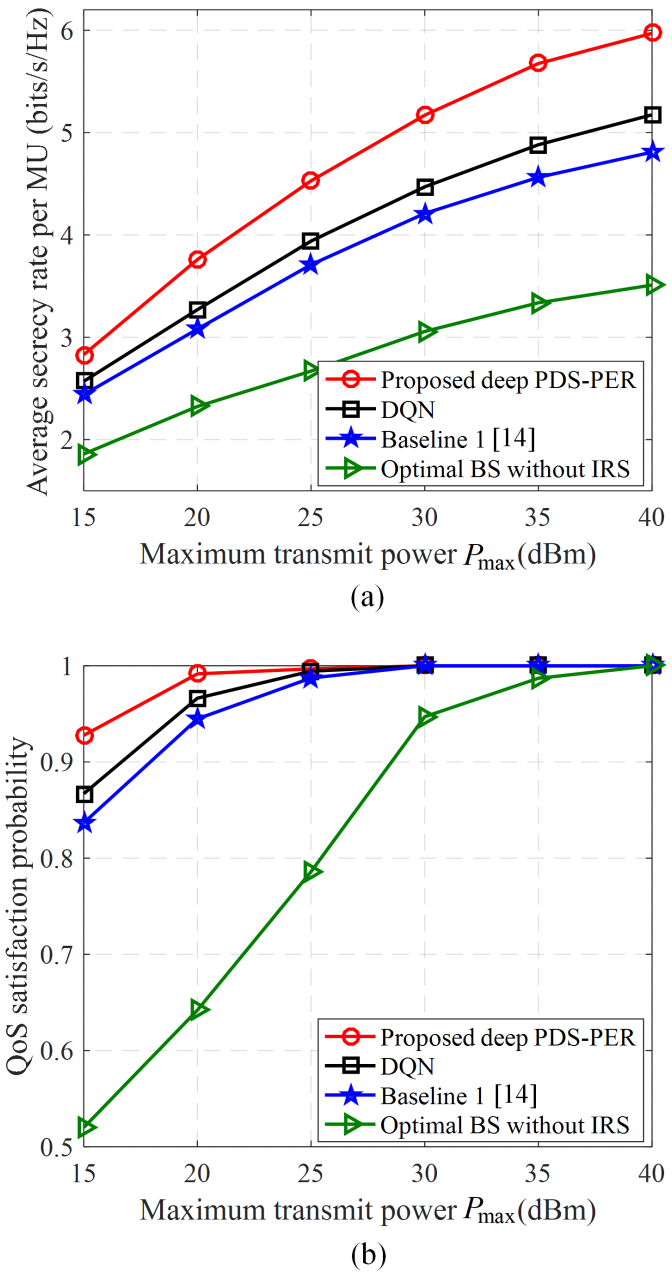

Fig. 5. Performance comparisons versus the maximum transmit power at the BS.

BS beamforming approach without IRS has the fastest convergent speed, but its performance is worst among the four approaches, because it does not employ the IRS for security provisioning.

Fig. 5 shows the average secrecy rate and QoS satisfaction level versus the maximum transmit power $P_{\max}$, when $L = 40$ and $\rho = 0.95$. As expected, both the secrecy rate and QoS satisfaction level of all the approaches enhance monotonically with increasing $P_{\max}$. The reason

is that when $P_{\max}$ increases, the received SINR at MUs improves, leading to the performance improvement. In addition, we find that our proposed learning approach outperforms the Baseline1 approach. In fact, our approach jointly optimizes the beamforming matrixes $\mathbf{V}$ and $\mathbf{\Psi}$, which can simultaneously facilitates more favorable channel propagation benefit for MUs and impair eavesdroppers, while the Baseline1 approach optimizes the beamforming matrixes in an iterative way. Moreover, our proposed approach has higher performance than DQN in terms of both secrecy rate and QoS satisfaction level, due to its efficient learning capacity by utilizing PDS-learning and PER schemes in the dynamic environment. From Fig. 5, we also find that the three IRS assisted secure beamforming approaches provide significant higher secrecy rate and QoS satisfaction level than the traditional system without IRS. This indicates that the IRS can effectively guarantee secure communication and QoS requirements via reflecting beamforming, where reflecting elements (IRS-induced phases) at the IRS can be adjusted to maximize the received SINR at MUs and suppress the wiretapped rate at eavesdroppers.

In Fig. 6, the achievable secrecy rate and QoS satisfaction level performance of all approaches are evaluated through changing the IRS elements, i.e., from $L = 10$ to 60, when $P_{\max} = 30$ dBm and $\rho = 0.95$. For the secure beamforming approaches assisted by the IRS, their achievable secrecy rates and QoS satisfaction levels are obvious increment with the number of the IRS elements. The improvement results from the fact that more IRS elements, more signal paths and signal power can be reflected by the IRS to improve the received SINR at the MUs but to decrease the received SINR at the eavesdroppers. In addition, the performance of the approach without IRS remains constant under the different numbers of the IRS elements.

From Fig. 6(a), it is found that the secrecy rate of the proposed learning approach is higher than those of the Baseline 1 and DQN approaches, especially, their performance gap also obviously increases with L, this is because that with more reflecting elements at the IRS, the proposed deep PDS-PER learning based secure communication approach becomes more flexible for optimal phase shift (reflecting beamforming) design and hence achieves higher gains. In addition, from Fig. 6(b) compared with the Baseline 1 and DQN approaches, as the reflecting elements at the IRS increases, we observe that the proposed learning approach is the first one who attains 100% QoS satisfaction level. This superior achievements are based on the particular design of the QoS-aware reward function shown in (12) for secure communication.

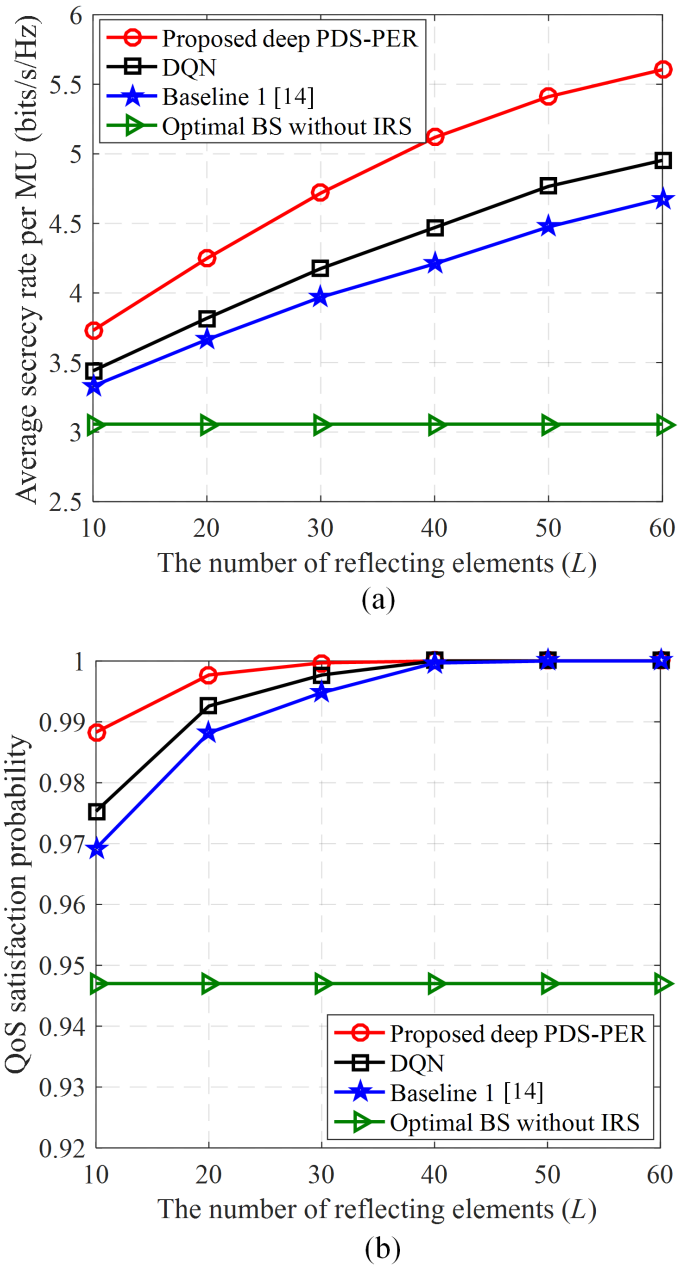

Fig. 6. Performance comparisons versus the number of IRS elements.

In Fig. 7, we further analyze how the system secrecy rate and QoS satisfaction level performances are affected by the outdated CSI coefficient in the system, i.e., from $\rho = 0.5$ to 1, when $P_{\max} = 30$ dBm and $L = 40$. Note that as decreases, the CSI becomes more outdated as shown in (7) and (8), and $\rho = 1$ means non-outdated CSI. It can be observed from all beamforming approaches, when CSI becomes more outdated (as ρ decreases), the average secrecy rate and

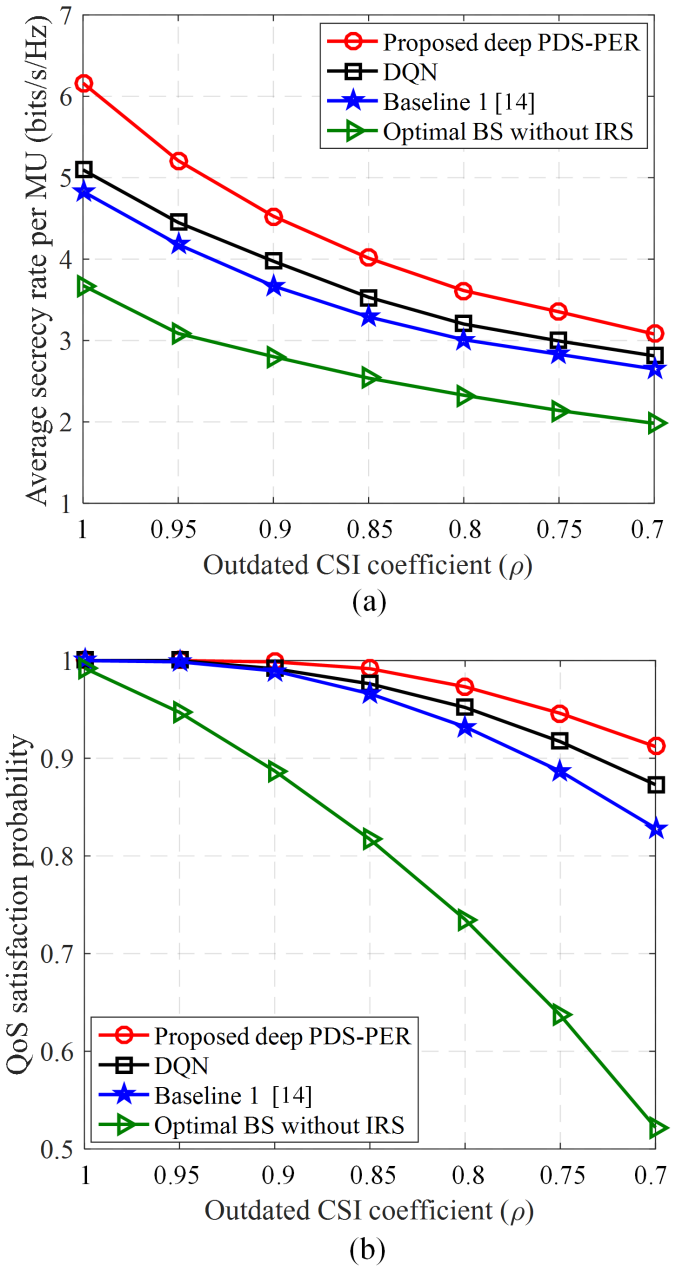

Fig. 7. Performance comparisons versus outdated CSI coefficient ρ.

QoS satisfaction level decrease. The reason is that a higher value of ρ indicates more accurate CSI, which will enable all the approaches to optimize secure beamforming policy to achieve higher average secrecy rate and QoS satisfaction level in the system.

It can be observed that reducing ρ has more effects on the performance of the other three approaches while our proposed learning approach still maintains the performance at a favor-

able level, indicating that the other three approaches are more sensitive to the uncertainty of CSI and the robust of the proposed learning approach. For instance, the proposed learning approach achieves the secrecy rate and QoS satisfaction level improvements of 17.21% and 8.67%, compared with the Baseline 1 approach when $\rho = 0.7$. Moreover, in comparison, the proposed learning approach has the best performance among all approaches. The reason is that the proposed learning approach considers the time-varying channels and takes advantage of PDS-learning to effectively learn the dynamic environment.

VI. Conclusion

In this work, we have investigated the joint BS's beamforming and IRS's reflect beamforming optimization problem under the time-varying channel conditions. As the system is highly dynamic and complex, we have exploited the recent advances of machine learning, and formulated the secure beamforming optimization problem as an RL problem. A deep PDS-PER learning based secure beamforming approach has been proposed to jointly optimize both the BS's beamforming and the IRS's reflect beamforming in the dynamic IRS-aided secure communication system, where PDS and PER schemes have been utilized to improve the learning convergence rate and efficiency. Simulation results have verified that the proposed learning approach outperforms other existing approaches in terms of enhancing the system secrecy rate and the QoS satisfaction probability.

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