

Punto 4.

Para Verlet se tiene:

$$X_{n+1} = X_n + V_n h + a_n \frac{h^2}{2}$$

$$V_{n+1} = V_n + (a_{n+1} + a_n) \frac{h}{2}$$

$$J = \begin{pmatrix} \frac{\partial X_{n+1}}{\partial X_n} & \frac{\partial X_{n+1}}{\partial V_n} \\ \frac{\partial V_{n+1}}{\partial X_n} & \frac{\partial V_{n+1}}{\partial V_n} \end{pmatrix} = \frac{\partial X_{n+1}}{\partial X_n} \frac{\partial V_{n+1}}{\partial V_n} - \frac{\partial X_{n+1}}{\partial V_n} \frac{\partial V_{n+1}}{\partial X_n}$$

$$= (1 \cdot 1) - (h \cdot 0) = 1 \Rightarrow \text{Simplectico}$$