

Wave Spectral Analysis Assessment

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The input data required for this code to run properly an excel data file; Containing the Significant wave height of the selected area and its frequency and the zero crossing periods and its frequency.

This markdown gives the code, process, visualization and report of qualities of the wave spectrum

This assessment:

1. Plots the histogram of significant wave height as well as zero crossing periods for the global wave statistics area in question.
2. Determines the ideal sea spectral for the most probable wave height and zero crossing period and plots it graphically
3. Calculates spectral moments m_0 , m_1 and m_2 .
4. Determine the 100 years wave height for the GWS area

This particular report uses North Atlantic Ocean Area 3 data

1. This is the section of the project that plots the histogram of the significant wave heights.

In [395...

```
import pandas as pd
import matplotlib.pyplot as plot
import numpy as np
from IPython.display import display, Markdown
from scipy.integrate import quad

# Custom styling function
def style_rows(row):
    if row.name == 0: # First row
        return ['background-color: darkblue; color: white' for _ in row]
    else: # Following rows
        return ['background-color: lightblue' for _ in row]

#Specify the Excel File Path
rawExcelData = 'Area 3.xlsx'
dataExcel = pd.read_excel(rawExcelData, header=None, keep_default_na=False)

#I want to plot for "ALL directions" of the wind first.
h_Range = [item[0] for item in dataExcel.iloc[1:15,0:1].values.tolist()]
h_Mean = [item[0] for item in dataExcel.iloc[1:15,1:2].values.tolist()]
h_Freq = [item[0] for item in dataExcel.iloc[1:15,2:3].values.tolist()]

t_Range = [item[0] for item in dataExcel.iloc[17:28,0:1].values.tolist()]
```

```

t_Mean = [item[0] for item in dataExcel.iloc[17:28,1:2].values.tolist()]
t_Freq = [item[0] for item in dataExcel.iloc[17:28,2:3].values.tolist()]

markdown_text4 = f'''
> 2. This is the section of the project that plots the Hs vs occurrences and Zero cr
\nThe table below shows the Wave Height(m), Mean Wave Height(m) and Occurances in t
'''

# Display the markdown
display(Markdown(markdown_text4))

df = pd.DataFrame({
    'Wave Height (m)': h_Range,
    'Mean Wave Height (m)': h_Mean,
    'Occurances': h_Freq
})
df = df.style.set_table_styles([{'selector': 'td, th', 'props': [('border', '2px so
display(df)

figg = plot.figure(figsize=(11, 5))
ay = figg.add_subplot(111)
ay.bar(h_Range,h_Freq, edgecolor='black')
ay.grid(True, axis='y');plot.xlabel("Significant Wave Height (m)");plot.ylabel("Occ

markdown_text5 = f'''

The table below shows the Zero Crossing Period(s), Mean Zero Crossing Period(m) and
'''

# Display the markdown
display(Markdown(markdown_text5))

df2 = pd.DataFrame({
    'Zero Crossing Period (s)': t_Range,
    'Mean Zero Crossing Period (m)': t_Mean,
    'Occurances': t_Freq
})

#df2 = df2.style.apply(style_rows, axis=1)
df2 = df2.style.set_table_styles([{'selector': 'td, th', 'props': [('border', '2px
display(df2)

fig = plot.figure(figsize=(9, 5))
ax = fig.add_subplot(111)
ax.bar(t_Range, t_Freq, edgecolor = 'Black')
ax.grid(True, axis='y');plot.xlabel("Zero Crossing Period (s)");plot.ylabel("Occura

```

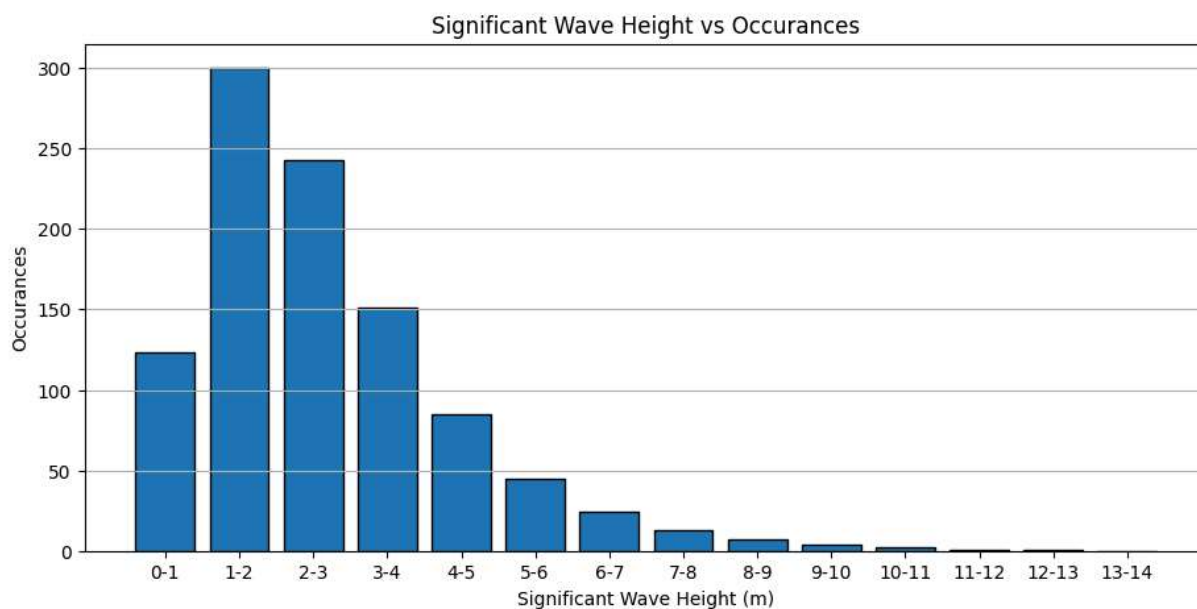
2. This is the section of the project that plots the Hs vs occurrences and Zero crossing period

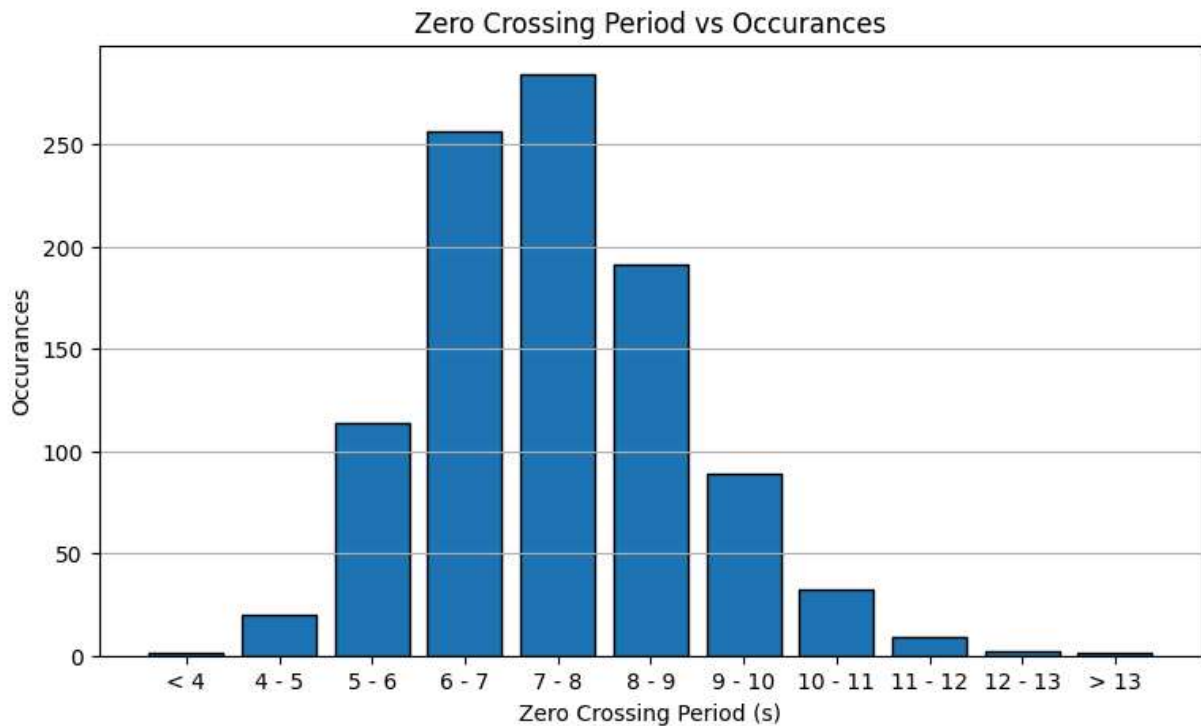
The table below shows the Wave Height(m), Mean Wave Height(m) and Occurances in the selected area.

	Wave Height (m)	Mean Wave Height (m)	Occurances
0	0-1	0.500000	123
1	1-2	1.500000	300
2	2-3	2.500000	243
3	3-4	3.500000	151
4	4-5	4.500000	85
5	5-6	5.500000	45
6	6-7	6.500000	24
7	7-8	7.500000	13
8	8-9	8.500000	7
9	9-10	9.500000	4
10	10-11	10.500000	2
11	11-12	11.500000	1
12	12-13	12.500000	1
13	13-14	13.500000	0

The table below shows the Zero Crossing Period(s), Mean Zero Crossing Period(m) and Occurances in the selected area.

	Zero Crossing Period (s)	Mean Zero Crossing Period (m)	Occurances
0	< 4		1
1	4 - 5	4.500000	20
2	5 - 6	5.500000	114
3	6 - 7	6.500000	256
4	7 - 8	7.500000	284
5	8 - 9	8.500000	191
6	9 - 10	9.500000	89
7	10 - 11	10.500000	32
8	11 - 12	11.500000	9
9	12 - 13	12.500000	2
10	> 13		1





In [396...

```
def S_w(w):
    return (A/w**5)*np.exp(-B/w**4)

def wS_w(w):
    return w*S_w(w)

def w2S_w(w):
    return w*wS_w(w)

def w4S_w(w):
    return w*w2S_w(w)

markdown_text6 = f'''

> 3. This section plots the Energy Density Spectrum, calculates A, B and Spectral m
...

# Display the markdown
display(Markdown(markdown_text6))

#Maximum Values
h_max = h_Mean[h_Freq.index(max(h_Freq))]
t_max = t_Mean[t_Freq.index(max(t_Freq))]
A = 123*((h_max**2)/(t_max**4))
B = 691/t_max**4
w = np.linspace(0, 4, 1000).tolist()
Sw = [S_w(item) if item!= 0 else 0 for item in w]
Mo, error = quad(S_w, 0, 4)
M1, error = quad(wS_w, 0, 4)
M2, error = quad(w2S_w, 0, 4)
M4, error = quad(w4S_w, 0, 4)
H1_3 = 4*np.sqrt(Mo)
```

```

plot.plot(w,Sw)
plot.ylim(bottom=0)
plot.xlim(left=0)
plot.xticks([0,1,2,3,4])
plot.title("Energy Density Spectrum")
plot.show()

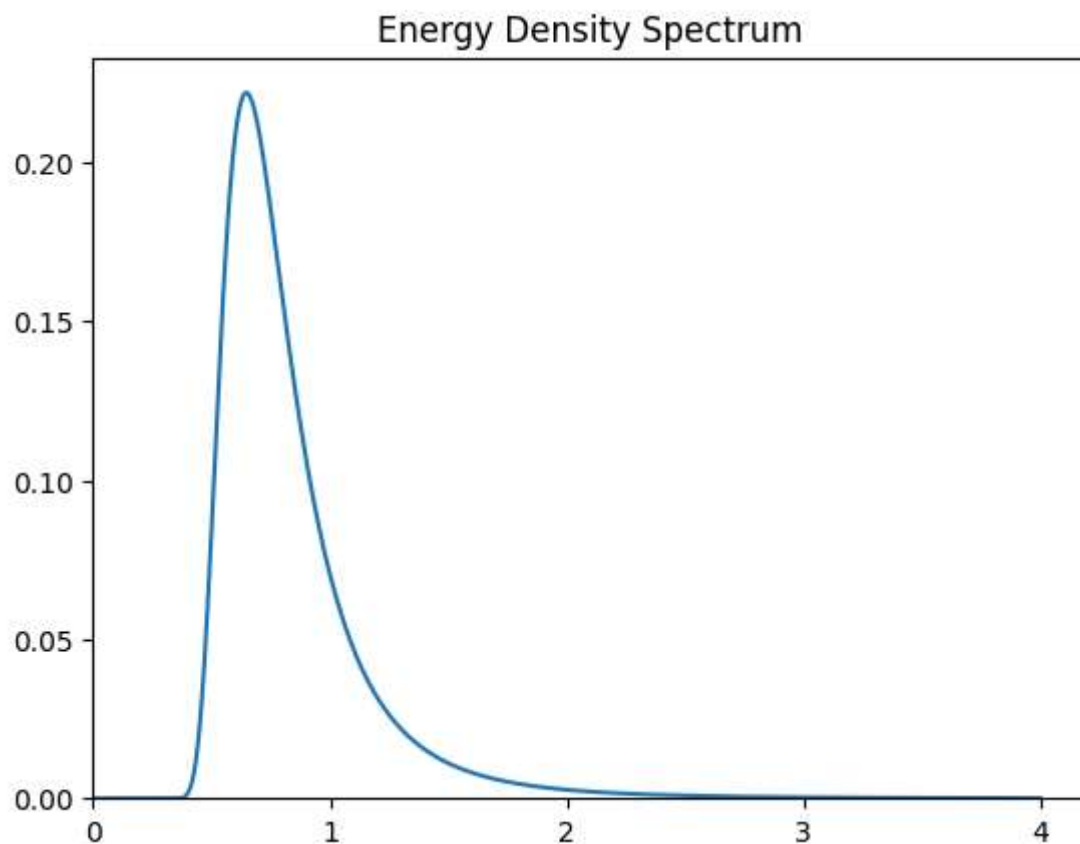
markdown_text = f"""

The Maximum Significant Height  $H_{1/3} = \{str(h\_max)\}$ 
\nThe Maximum Zero Crossing Period  $T_z (s) = \{str(t\_max)\}$ 
\n $A = \{round(123*((h\_max**2)/(t\_max**4)),4)\}$ 
\n $B = \{round(691/t\_max**4, 4)\}$ 
\n $H_{1/3} (4sqrt(Mo)) = \{H1\_3\}$ 
\n $Mo = \{Mo\}$ 
\n $M1 = \{round(M1,5)\}$ 
\n $M2 = \{round(M2,5)\}$ 
\n $M4 = \{round(M4,5)\}$ 

"""
# Display the markdown
display(Markdown(markdown_text))

```

3. This section plots the Energy Density Spectrum, calculates A, B and Spectral moments



The Maximum Significant Height $H_{1/3} = 1.5$

The Maximum Zero Crossing Period T_z (s) = 7.5

$A = 0.0875$

$B = 0.2184$

$H_{1/3}(4\sqrt{Mo}) = 1.2651719113677955$

$Mo = 0.10004124783212757$

$M1 = 0.08342$

$M2 = 0.0802$

$M4 = 0.09411$

```
In [397... from sklearn.linear_model import LinearRegression
from sklearn.metrics import r2_score

markdown_text7 = f'''

> 4. This section calculates and plots the Weibull Distribution, determines Form Fa
'''

# Display the markdown
display(Markdown(markdown_text7))

# Create a pandas DataFrame
df3 = pd.DataFrame({'H (m)': h_Mean, 'N': h_Freq})

# Filter out rows where frequency is 0
df3 = df3[df3['N'] > 0]

# Calculate cumulative frequency
df3['N_cum'] = df3['N'].cumsum()

N_sum = df3['N'].sum()

df3['F(H)'] = (df3['N_cum']/N_sum).round(4)
df3['z = ln(H)'] = np.log(df3['H (m)']).round(4)
df3['1/1-FH'] = (1/(1-df3['F(H)'])).round(4)
df3['y = ln(ln(1/1-FH))'] = (np.log(np.log(df3['1/1-FH']))).round(4)

display(df3)

df3 = df3[~np.isinf(df3['y = ln(ln(1/1-FH))'])] # This removes rows where 'z' is in
y = df3['y = ln(ln(1/1-FH))'].values.reshape(-1, 1)
z = df3['z = ln(H)'].values.reshape(-1, 1)
```

```

model = LinearRegression()
model.fit(z,y)

y_pred = model.predict(z)
r_squared = r2_score(y, y_pred)
slope = model.coef_[0][0]
intercept = model.intercept_[0]

plot.figure(figsize=(8, 6))
plot.scatter(z,y, color='blue', s=50, label = 'Graph of y against z')
plot.axhline(0, color='black', linewidth=1) # x-axis at y=0
plot.axvline(0, color='black', linewidth=1) # y-axis at x=0
plot.ylim([-3,3])
plot.xlim([-3,3])
plot.grid(True, which='both', linestyle='--', linewidth=0.5)

plot.plot(z, y_pred, color='red', label=f'Best fit line (y={slope:.4f}x+({intercept:.4f})')
plot.title("Weibull Distribution")
plot.legend(loc='best')
plot.show()

lnv= -(intercept/slope)
Scale_Factor = np.exp(lnv).round(4)
Hs = Scale_Factor*(np.log(100*365*8))**(1/slope)

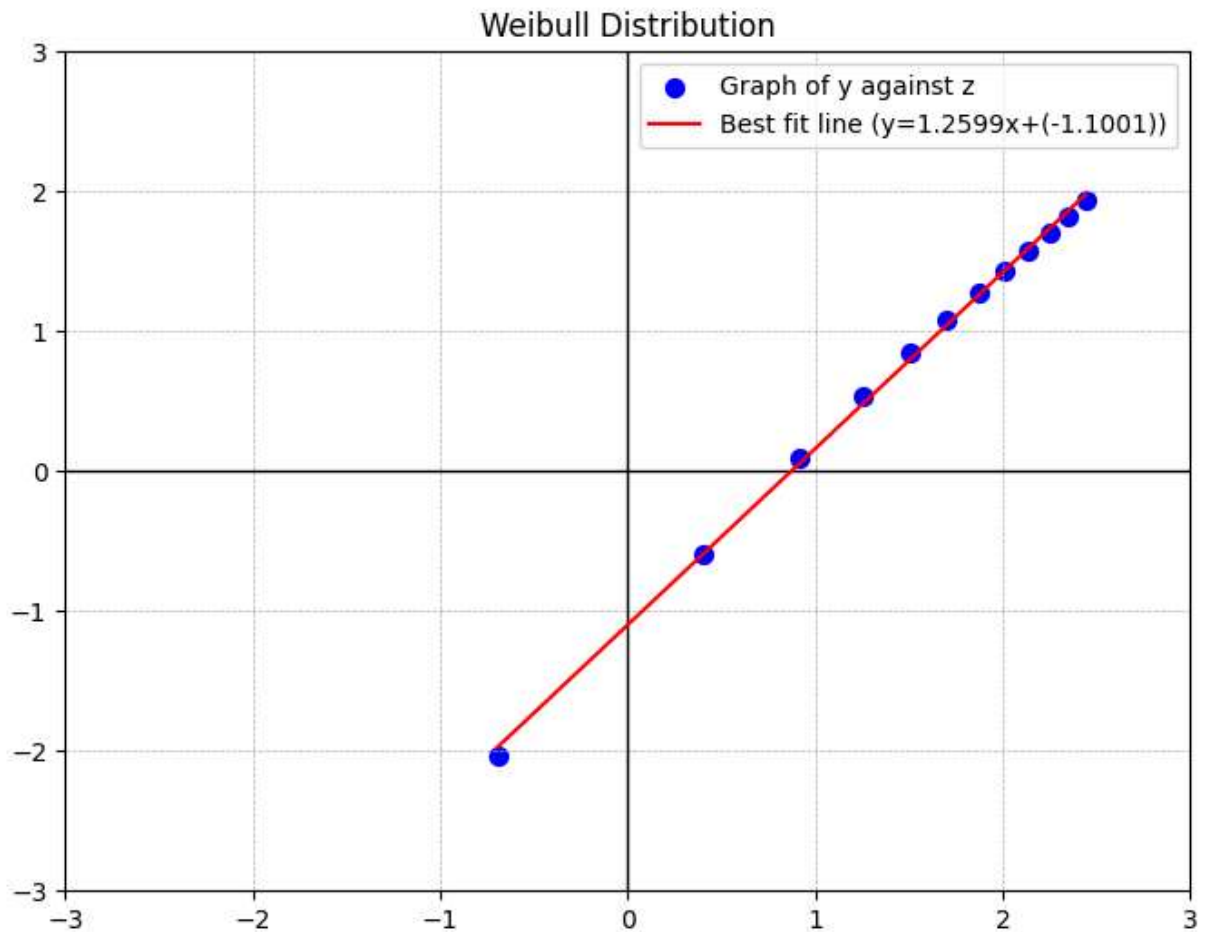
markdown_text2 = f"""
The equation of the Line of Best Fit is  $y = \{slope.round(4)\}x + \{intercept.round(4)\}$ 
\n R2 Value = {r_squared}
\n Form Factor  $k = \{slope.round(4)\}$ 
\n Scale Factor  $v = \{Scale\_Factor\}$ 
\n Predicted  $H_s$  after 100 years =  $\{Hs.round(1)\}m$ 
"""

# Display the markdown
display(Markdown(markdown_text2))

```

4. This section calculates and plots the Weibull Distribution, determines Form Factor k , Scale Factor v and Predicted H_s after 100 years.

	H (m)	N	N_cum	F(H)	$z = \ln(H)$	$1/1-FH$	$y = \ln(\ln(1/1-FH))$
0	0.5	123	123	0.1231	-0.6931	1.1404	-2.0297
1	1.5	300	423	0.4234	0.4055	1.7343	-0.5967
2	2.5	243	666	0.6667	0.9163	3.0003	0.0941
3	3.5	151	817	0.8178	1.2528	5.4885	0.5322
4	4.5	85	902	0.9029	1.5041	10.2987	0.8467
5	5.5	45	947	0.9479	1.7047	19.1939	1.0834
6	6.5	24	971	0.9720	1.8718	35.7143	1.2741
7	7.5	13	984	0.9850	2.0149	66.6667	1.4350
8	8.5	7	991	0.9920	2.1401	125.0000	1.5745
9	9.5	4	995	0.9960	2.2513	250.0000	1.7086
10	10.5	2	997	0.9980	2.3514	500.0000	1.8269
11	11.5	1	998	0.9990	2.4423	1000.0000	1.9326
12	12.5	1	999	1.0000	2.5257	inf	inf



The equation of the Line of Best Fit is $y = 1.2599x + [-1.1001]$

R2 Value = 0.9989059001600069

Form Factor $k = 1.2599$

Scale Factor $v = 2.3944$

Predicted H_s after 100 years = 17.9m

SPECTRAL PARAMETERS

In [398...

```
markdown_text8 = f'''

> 4. This section calculates other spectral parameters
'''

# Display the markdown
display(Markdown(markdown_text8))

w01 = M1/Mo
MeanPeriod_T1 = 2*np.pi*w01
T2 = 2*np.pi*np.sqrt(Mo/M2)
T4 = 2*np.pi*np.sqrt(M2/M4)
E = np.sqrt(1-((M2**2)/(Mo*M4)))

markdown_text3 = f"""

\n W_01 = {round(w01,4)}
\n Mean Period of the Zero Upcrossings T2 = {T2.round(4)}s
\n Peaks Mean Period T4 = {T4.round(4)}s
\n Band Width = {E.round(4)}m
"""

# Display the markdown
display(Markdown(markdown_text3))
```

4. This section calculates other spectral parameters

$W_{01} = 0.8339$

Mean Period of the Zero Upcrossings $T_2 = 7.0174s$

Peaks Mean Period $T_4 = 5.8004s$

Band Width = 0.5628m