

PAMO Stream Test 2

June Camp 2017

Time: $4\frac{1}{2}$ hours

1. Does there exist a partition of the set of integers into three non-empty subsets A , B , C such that the sets $A + B$, $B + C$ and $C + A$ are disjoint?
2. Let ABC be a triangle with orthocentre H . Prove that the triangle formed by the perpendicular bisectors of AH , BH and CH is congruent to ABC .
3. Find all positive integers n, k_1, k_2, \dots, k_n such that

$$k_1 + k_2 + \dots + k_n = 5n - 4 \quad \text{and} \quad \frac{1}{k_1} + \frac{1}{k_2} + \dots + \frac{1}{k_n} = 1.$$