IMO Stream Test 2

June Camp 2017

Time: $4\frac{1}{2}$ hours

- 1. Let ABC be a triangle with $AB = AC \neq BC$ and let I be its incentre. The line BI meets AC at D, and the line through D perpendicular to AC meets AI at E. Prove that the reflection of I in AC lies on the circumcircle of triangle BDE.
- 2. Let n, m, k and l be positive integers with $n \neq 1$ such that $n^k + mn^l + 1$ divides $n^{k+l} 1$. Prove that either
 - m = 1 and l = 2k; or
 - $l \mid k \text{ and } m = \frac{n^{k-l} 1}{n^l 1}$.

3.