EE24BTECH11010 - BALAJI B

Question:

In what ratio does the point $\binom{\frac{24}{11}}{y}$ divide the line segment joining he points $\mathbf{P} = \begin{pmatrix} 2 \\ -2 \end{pmatrix}$ and $\mathbf{Q} = \begin{pmatrix} 3 \\ 7 \end{pmatrix}$? Also find the value of y. (10,2017)

Answer:

Let the point $\begin{pmatrix} \frac{24}{11} \\ y \end{pmatrix}$ be equals to **R**.

Point	Description
P (2, -2)	First endpoint
Q (3, 7)	Second end-point
$\mathbf{R}\left(\frac{24}{11},y\right)$	Point divides P and Q in the ratio $k:1$

TABLE 0: Variables Used

The point $\mathbf{R} \begin{pmatrix} \frac{24}{11} \\ y \end{pmatrix}$ divides the points $\mathbf{P} \begin{pmatrix} 2 \\ -2 \end{pmatrix}$ and $\mathbf{Q} \begin{pmatrix} 3 \\ 7 \end{pmatrix}$ in the ratio k:1.

Section formula:-

$$\mathbf{C} = \frac{k\mathbf{B} + \mathbf{A}}{k + 1} \tag{0.1}$$

Here,

$$(k+1)\begin{pmatrix} \frac{24}{11} \\ y \end{pmatrix} = k \begin{pmatrix} 3 \\ 7 \end{pmatrix} + \begin{pmatrix} 2 \\ -2 \end{pmatrix} \tag{0.3}$$

$$\implies k = \frac{2}{9} \tag{0.4}$$

Substituting the value of k in the equation (0.2) we get value of y as

$$y = \frac{-4}{11} \tag{0.5}$$

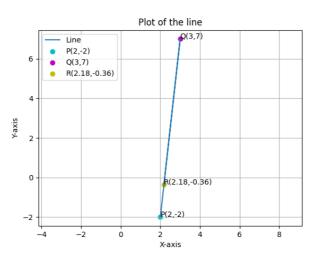


Fig. 0.1: Plot of the line