EE24BTECH11010 - BALAJI B

Question:

The distance between the points $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$ and $\begin{pmatrix} a - b \\ a + b \end{pmatrix}$ is (10, 2022)

Answer:

Variable	Value	Description
P	$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$	First Endpoint
Q	$\begin{pmatrix} a-b\\a+b \end{pmatrix}$	Second Endpoint

TABLE 0: Variables Used

$$\therefore \mathbf{P} - \mathbf{Q} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} - \begin{pmatrix} a - b \\ a + b \end{pmatrix} = \begin{pmatrix} b - a \\ -a - b \end{pmatrix}$$
 (0.1)

$$(\mathbf{P} - \mathbf{Q})^{\mathsf{T}} (\mathbf{P} - \mathbf{Q}) = \begin{pmatrix} b - a & -a - b \end{pmatrix} \begin{pmatrix} b - a \\ -a - b \end{pmatrix}$$
(0.2)

$$(\mathbf{P} - \mathbf{Q})^{\mathsf{T}} (\mathbf{P} - \mathbf{Q}) = (b - a)^2 + (a + b)^2$$

$$(0.3)$$

Thus the desired distance is

$$d = ||P - Q|| = \sqrt{(b - a)^2 + (a + b)^2}$$
(0.4)

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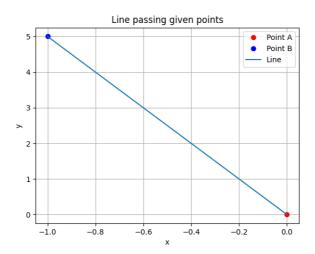


Fig. 0.1: Plot of the line passing through A and B