

1/7/25

Day 5 Aptitude

permutations & Combinations + Probability

1) ways 3 students seated in a row.

$$3! = 3 \times 2 \times 1 = \boxed{6 \text{ ways}}$$

2) Box - 5 diff coloured balls, ways pick 1 ball

$$1 \text{ ball choosing from 5 options} = \boxed{5 \text{ ways}}$$

3) "CAT" arrange the letters of word.

$$3 \text{ Letters} = 3! = 3 \times 2 \times 1 = \boxed{6 \text{ ways}}$$

4) 2 fruits in basket of 4 diff fruits
choose

$${}^4C_2 = \frac{4!}{(2! \times 2!)} = \boxed{6 \text{ ways}}$$

5) Probability of getting head flipping a fair coin.

outcomes \rightarrow head, tail.

$$\text{head} \rightarrow \boxed{\frac{1}{2} = 0.5}$$

6) die rolled once, probability of getting no. 4.

die \rightarrow 6 outcomes.

$$P(4) = \boxed{\frac{1}{6}}$$

7) 2 digit numbers formed using digits 1, 2, 3, 4 without repetition.

$$\text{Total} = 4 \times 3 = \boxed{12 \text{ numbers}}$$

$${}^4P_2 = \frac{4!}{(4-2)!} = \frac{4!}{2!} = \frac{4 \times 3 \times 2 \times 1}{2 \times 1} = 4 \times 3 = 12$$

8) 3 - Apples, 4 - Oranges. 1 fruit picked random the probability of picking an Apple.

$$\text{Total} = 3 + 4 = 7.$$

$$\text{Apples} - 3 \rightarrow P(3) = \boxed{\frac{3}{7}}$$

9) Ways can 4 people stand in a line

$$4! = 4 \times 3 \times 2 \times 1 = \boxed{24 \text{ ways}}$$

10) Bag \rightarrow 3 red, 2 green balls. probability of picking green.

$$\text{Total} = 3 + 2 = 5$$

$$P(\text{green}) = \boxed{\frac{2}{5}}$$

11) 3-digit number formed using digits 1 2 3 4

$$4 \text{ digits} = 4 \times 3 \times 2 = \boxed{24 \text{ numbers}}$$

1 2 3
1 3 4
1 4 2

12) ways can committee of 3 be chosen from 7

$${}^7C_3 = \frac{7 \times 6 \times 5}{3 \times 2 \times 1} = \boxed{35 \text{ ways}}$$

13) Probability of drawing a king from a standard deck of 52 cards.

$$4 \text{ king in } 52 \text{ cards} = \frac{4}{52} = \boxed{\frac{1}{13}}$$

14) Box - 6 white, 4 black balls. 1 ball drawn. probability it is black.

$$\text{Total balls} = 6 + 4 = 10$$

$$\text{Black ball} = \frac{4}{10} = \boxed{\frac{2}{5}}$$

15) ways 5 books arranged

$$5! = 5 \times 4 \times 3 \times 2 \times 1 = \boxed{120 \text{ ways}}$$

16) Diff passwords made with letters A, B, C, D taken at a time.

$${}_4P_3 = 4 \times 3 \times 2 = 24$$

17) probability of getting even no when die rolled
even no's in die = 2, 4, 6 \rightarrow 3 outcomes

$$P(\text{even}) = \frac{3}{6} = \boxed{\frac{1}{2}}$$

18) ways 2 letters chosen from word 'MATH'

$$4 \text{ letter} = {}^4C_2 = 6 \text{ ways}$$

19) probability drawing heart from deck of cards

$$13 \text{ hearts from } 52 \text{ cards} = \frac{{}^{13}C_1}{{}^{52}C_1} = \boxed{\frac{1}{4}}$$

20) ways can 4 people stand around circular table.

$$4(n-1) = (4-1)! = (3)! = \boxed{6 \text{ ways}}$$

21) 4-digit no can form using digits 1, 2, 3, 4, 5 without repetition such that even no.

Even digits - 2, 4.

Fix last digit as even.

Remaining 3 digits 4 options = ${}^4P_3 = 24$.

$$\text{Total} = 2 \times 24 = \boxed{48 \text{ numbers}}$$

22) Box - 3 red, 4 blue, 5 green ball. 2 balls drawn. probability both are green.

$$\text{Total} = 3 + 4 + 5 = 12$$

Green = 5.

$$P(\text{green both}) = \frac{{}^5C_2}{{}^{12}C_2} = \frac{10}{66} = \boxed{5/33}$$

23) ways 5 students arrange in row. student must not sit together.

$$5! = 120$$

$$2 \text{ sit together} = (4! \times 2) = (24 \times 2) = 48$$

$$120 - 48 = \boxed{72 \text{ ways}}$$

24) Group - 10 men & 8 women. committees of 4 people formed containing atleast 2 women.

$$2 \text{ women, } 2 \text{ men} = {}^8C_2 \times {}^{10}C_2 = 28 \times 45 = 1260$$

$$3 \text{ women, } 1 \text{ man} = {}^8C_3 \times {}^{10}C_1 = 56 \times 10 = 560$$

$$4 \text{ women} = {}^8C_4 = 70$$

$$\text{Total} = 1260 + 560 + 70 = \boxed{1890 \text{ ways}}$$



25) Die rolled twice. probability the sum is 7.

$$2 \text{ dice} = 6 \times 6 = 36.$$

ways to get (1,6) (2,5) (3,4) (4,3) (5,2) (6,1) \rightarrow 6 ways

$$\text{probability} = 6/36 = \boxed{1/6}$$