

Heat transfer, thermal stress and failure analyses in a TiB₂ gas turbine stator blade



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ABSTRACT

Gas turbine stator blades do not experience centrifugal force contrary to the rotor blades; but they are exposed to high-temperature combustion gases causing thermal stresses. In the present work, a series of numerical simulations were carried out to clarify the feasibility of TiB₂ utilization as an appropriate material for gas turbine stator blades. The governing equations of heat transfer and solid mechanics were discretized by the finite element method and solved using Comsol Multiphysics software. The boundary conditions were applied, and temperature, displacement and maximum principle stress were obtained. The results showed that using ceramics such as TiB₂ instead of conventional alloys can enhance the maximum displacement. Temperature distribution in the blade is more uniform than that of alloys, and consequently, the thermal stresses are reduced. The TiB₂ can withstand the applied stresses according to the Coulomb–Mohr theory with a safety factor of 2.4.

1. Introduction

Turbines have broad application in thermal power generation units such as power plants (steam turbines and gas turbines), manufacturing and transportation systems. Gas turbines are common power generation plants and their flexibility to the fuels is one of the reasons for their extensive application in particular, renewable fuels e.g. biogas [1,2]. The turbine efficiency is in direct relation with working temperature and pressure ratio. Increasing the inlet gas temperature enhances the turbine efficiency considerably [3,4]. However, metallurgical limitations of the applied materials confine the turbine working temperatures. For eliminating these problems, two strategies are generally suggested: cooling of the blades, and selecting appropriate materials for manufacturing turbine parts, especially the blades [5]. The use of cooling ducts inside the blades are one of the common ways of protecting them against high temperatures. Nevertheless, cooling the blades, decreases the turbine efficiency. Therefore, new types of materials are needed to work at higher temperatures without any metallurgical problems [5]. It is also necessary to investigate the temperature distribution and consequent thermal stresses to evaluate the feasibility of the applied materials and cooling methods.

The previously conducted studies demonstrated significance of

thermal stresses and temperature distribution in the turbine blades. Sadowski et al. [6] presented analytical methods for estimation of stresses in the turbine blade together with the solution to the problem. By using the Extended Finite Element Method (XFEM), the advanced damage was modeled numerically. They concluded that the critical threshold of the rotor speed with the turbine blade at the thin thermal barrier coating layer does not undergo damage by using the mentioned technique.

Mezur et al. [7] investigated the failure analysis in the first stage of blades of a 70 MW-gas turbine which made of Inconel 738LC (nickel-based alloy) after 24000 h of operation at high temperatures. They found out that high temperatures result in the transformation of MC to M₂₃C₆ carbide type at airfoil part of the blade. This transformation and carbide formation reduced the ductility of the alloy as its toughness and the lifetime consequently.

The study of the blade failures in gas turbine engines has been conducted by Hou et al. [8]. They pursued mechanical analyses and non-linear finite element method studies to determine the steady dynamic characteristics and stresses of blades. By evaluating these characteristics and stresses, they identified the reasons of blade failure. They reported that the thermal expansion, gas pressure, and centrifugal load at the stationary condition do not have a remarkable effect on crack

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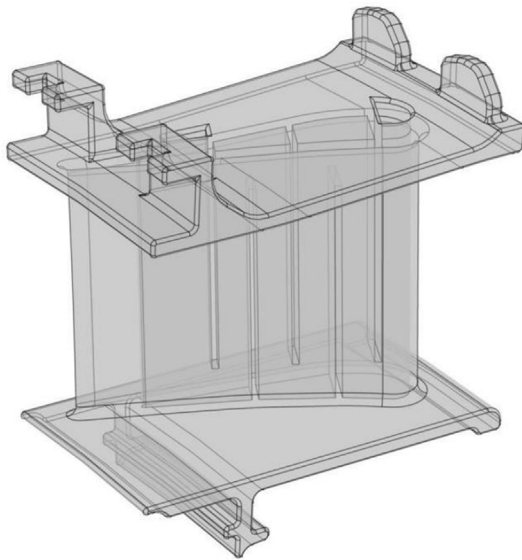


Fig. 1. The whole geometry of the turbine stator blade together with mounting details and cooling ducts.

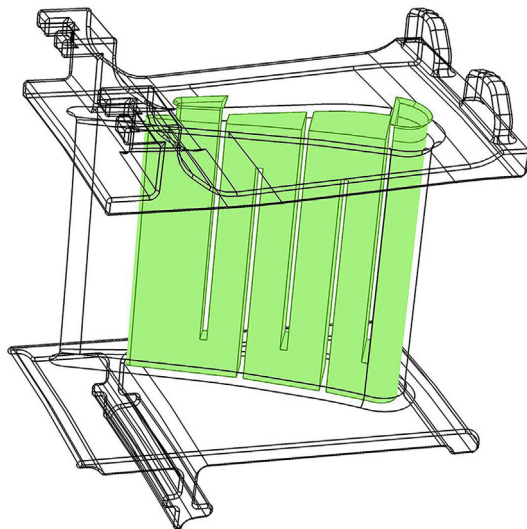


Fig. 2. Internal cooling ducts of blades.

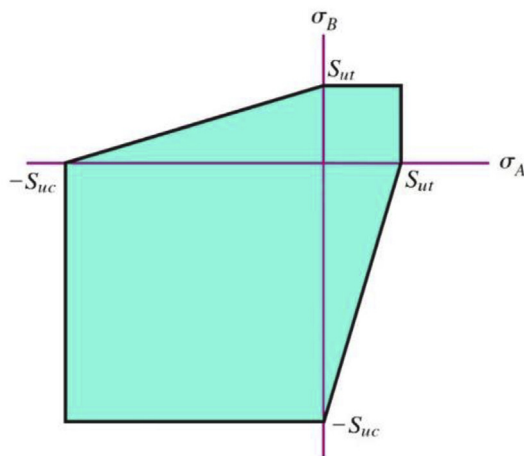


Fig. 3. The safety regions in Coulomb-Mohr theory.

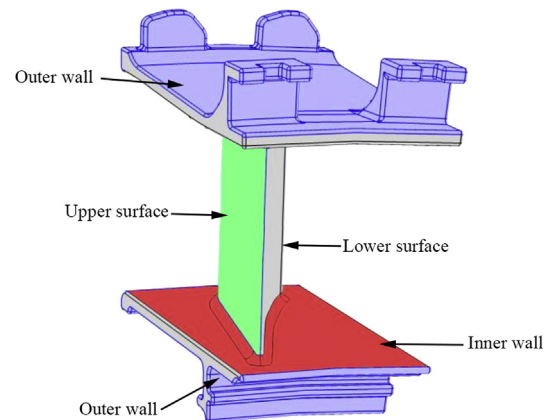


Fig. 4. The surfaces for applied thermal boundary conditions.

formation at the sharp leading corners.

Among the researches concentrating on the heat transfer of gas turbines studies, Kim et al. [9] rigorously examined the conjugation of convection and conduction heat transfer in the gas turbine as well as the weak points of hot parts of the turbine by obtaining the temperature distributions in a combustion liner. They reported that the heat transfer coefficients enhance sharply in the forward section.

Chyu et al. [10] investigated the heat transfer at the rectangular tip of the turbine blades. They stated that the influence of blade rotation on heat transfer is negligible. It should be noted that the study of heat transfer using several tip models, including flat and rectangular models, have been conducted in several papers [10–12]. They all concluded insignificant effect of relative motion on the tip heat transfer.

Nickel-based alloys, which have acceptable mechanical properties, are the common materials in producing turbine blades; however, at high temperatures, they encounter problems such as oxidation and creep caused deformations. In recent years, ceramic materials have been proposed for ultra-high temperature applications such as heat exchangers [13], and gas turbine blades [3]. The proposed ceramics can withstand higher temperatures with lower oxidation such as ZrB_2 -SiC and HfB_2 -SiC [14].

Ultra-high temperature ceramics (UHTC) are a group of materials with considerably high strength and melting point which offer good chemical and physical stabilities at high temperatures [15–24] which can be a proper candidate in the manufacturing of different parts of turbines.

ZrB_2 , as a UHTC, has been proposed as a candidate for the manufacturing of gas turbine stator blade by our group [3,25–41]. They investigated a stator blade of gas turbine made of zirconium diboride and showed that ZrB_2 has a lower displacement in comparison with common metal-based blades. The more uniform temperature distribution was also reported [3]. Another diboride which has been used in many industrial applications is TiB_2 . Titanium diboride as one of the UHTCs has very good mechanical and thermal properties such as high hardness (~ 32 GPa), high melting point (3225°C), great elastic modulus (529 GPa) and excellent electrical and thermal conductivity ($\sim 10^5$ S/cm and 60–120 W/m-k, respectively) [28,42–62], which makes it a promising candidate to adapt with harsh working environments like impact, corrosion, wear and high temperatures. TiB_2 has been used in various industries including manufacturing gas turbine blade materials, machine tools, engine valves, and ball bearings [52,55,62–64].

The main objective of the present research is to investigate the feasibility of using TiB_2 as turbine stator blade. TiB_2 can work at high operational temperatures, resulting in better power cycle efficiencies. In addition, the problems associated with metallurgical problems of commonly used alloys may be avoided. In this regard, a series of numerical simulations were carried out by the finite element method to

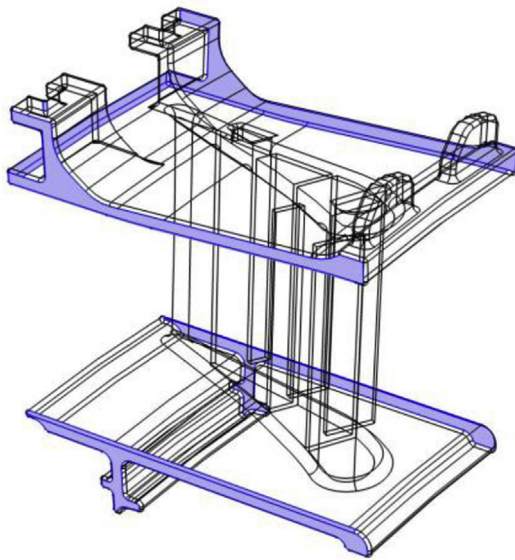


Fig. 5. Thermally insulated boundaries.

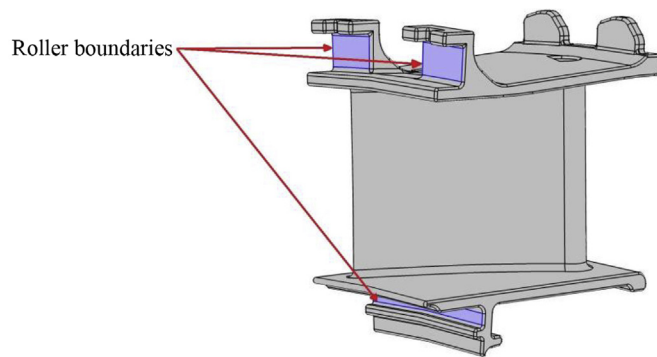


Fig. 6. The surfaces with roller boundary condition.

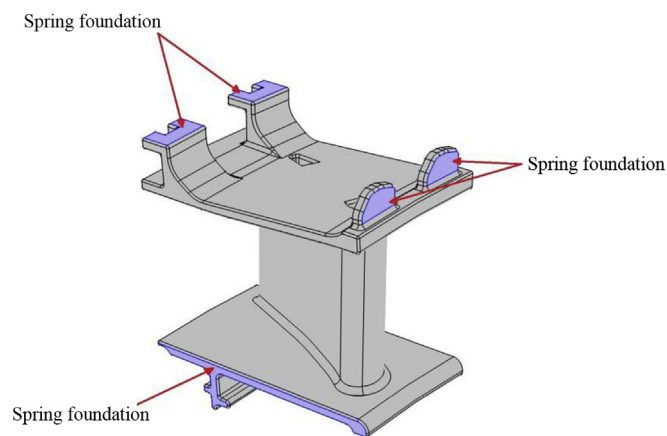


Fig. 7. The top view of spring foundations.

obtain the temperature distribution and resulted thermal stresses.

2. Methodology

2.1. Geometry

The geometry applied in the present work is a modified version of the selected geometry in Ref. [65]. The whole geometry of the turbine

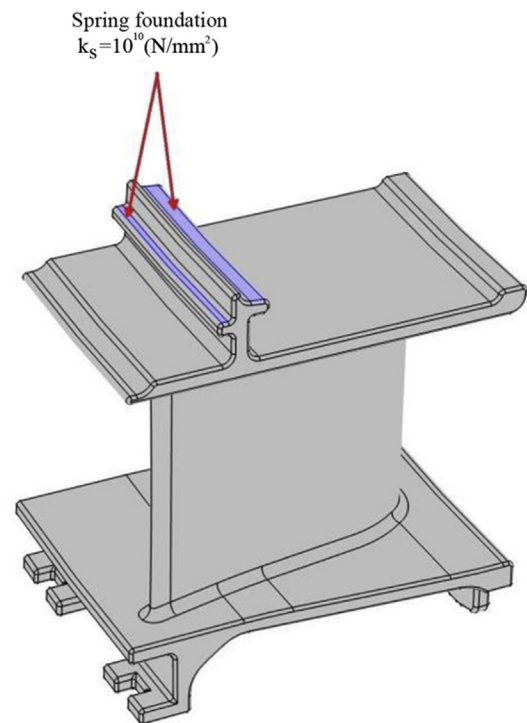


Fig. 8. The bottom view of boundary condition for spring foundation.

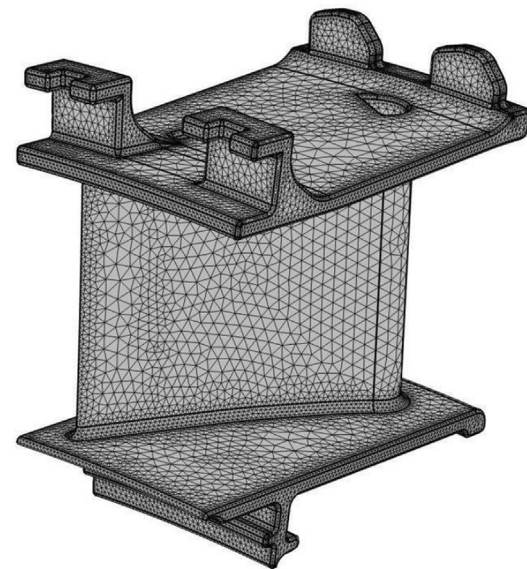


Fig. 9. The generated mesh on turbine stator blade.

stator blade together with mounting details and cooling ducts are presented in Fig. 1. At very high operating temperatures, the metallurgical problems such as corrosion, oxidation, and sulphidation are possible. Thus, for preventing these problems, the cooling of blades is essential. The air coming from the compressor passes among the internal ducts and cools the blades. Fig. 2 shows the internal cooling ducts of blades which have been used in the present work, however, for the convenience of calculation, the details of ribs geometry inside the ducts are neglected, and instead the average Nusselt number correlation is calculated for obtaining the heat transfer coefficient [3]. The air, as a cooling fluid, is considered at the pressure of 30 bar and the temperature of 600 K.

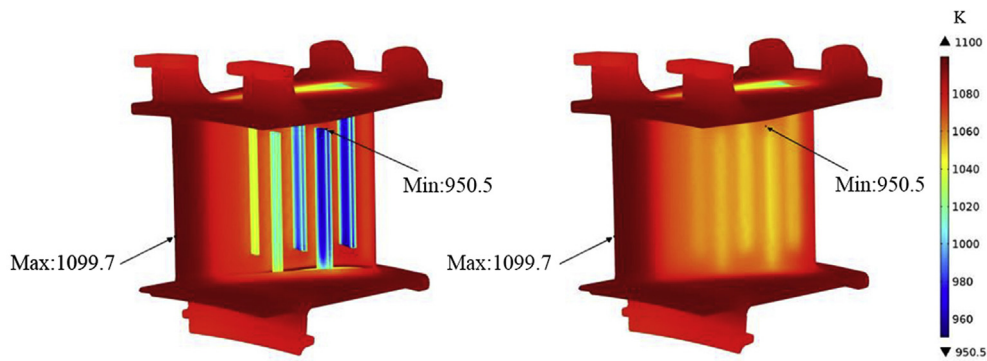


Fig. 10. The temperature distribution in the blade made of TiB₂ and cooling duct.

Table 1
The different temperatures of TiB₂, ZrB₂ ceramics and M152 alloy.

Average temperature (K)	Minimum temperature (K)	Maximum temperature (K)	Blade material
1070.1	867.8	1100.0	M152 alloy [3]
1079.1	953.9	1100.0	Zirconium diboride [3]
1078.9	950.5	1099.7	Titanium diboride

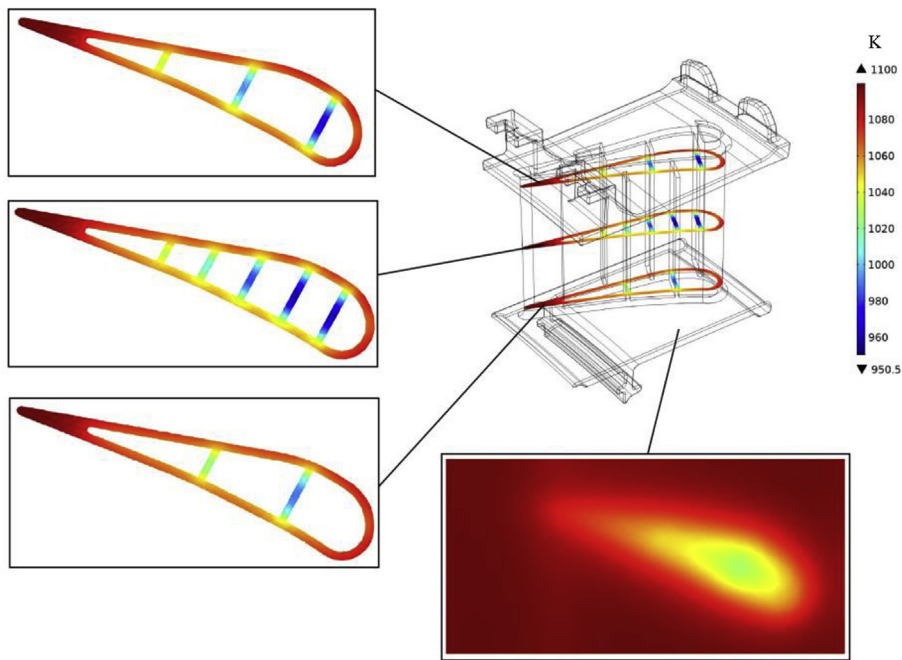


Fig. 11. 2D temperature contours in different sections of turbine blade.

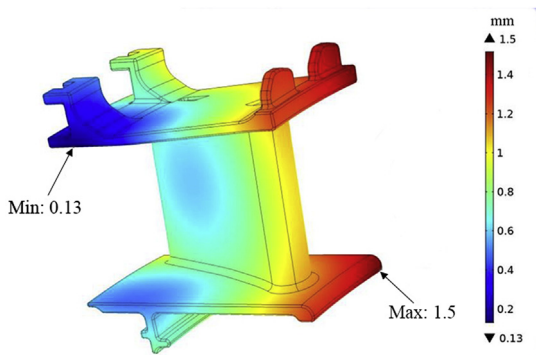


Fig. 12. The contours of displacement at various parts of the turbine blade.

2.2. Governing equations

The hot gases transfer the heat to the blade by convection mechanism while the transferred heat diffuses in the blade material by conduction. Temperature distribution through the blade results in thermal stresses due to the fixed supports. Therefore, two sets of governing equations are needed to cover both thermal behavior and mechanical characteristics of blades. The governing equations consist of heat diffusion and linear elastic equations. The heat diffusion equation is presented as Eq. (1) [3]:

$$\rho C \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) \tag{1}$$

where ρ , c and k are allocated to density, heat capacity and thermal conductivity of the blade material, respectively. The transferred heat

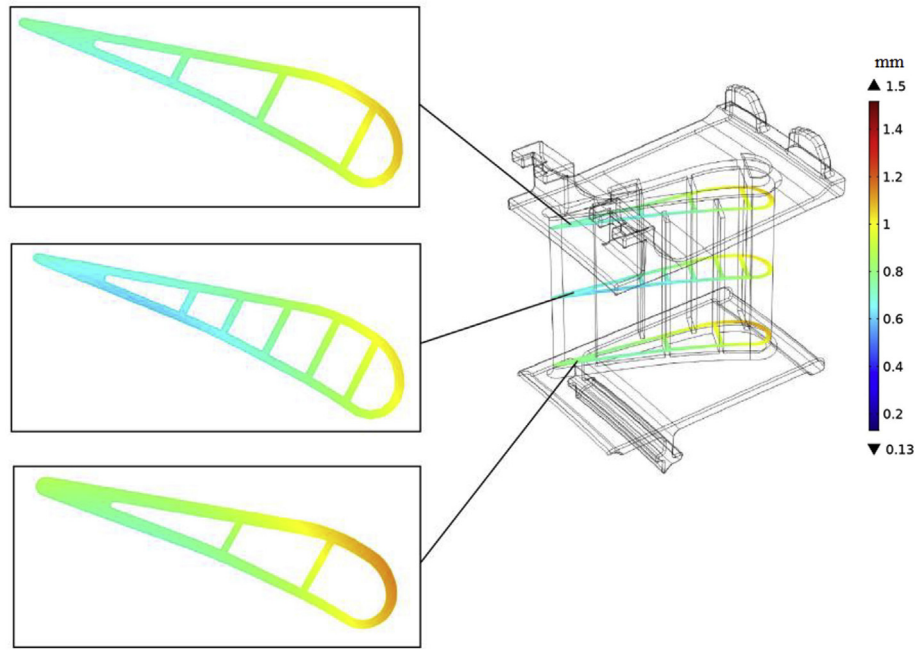


Fig. 13. The displacement of the blade at three different cross-sections.

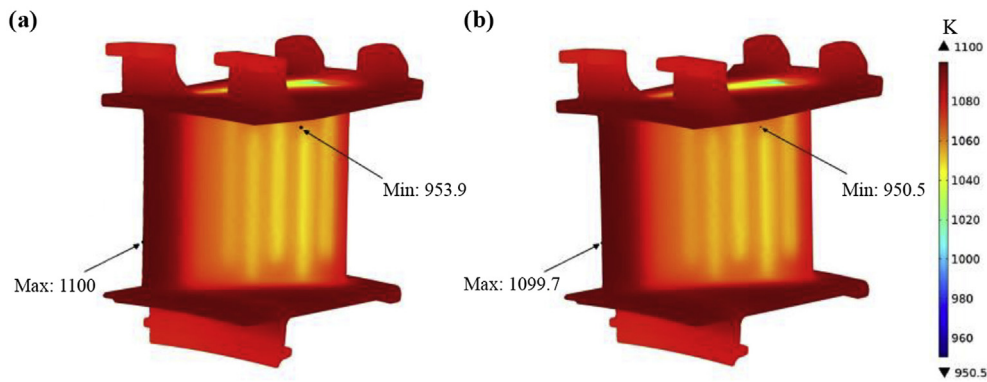


Fig. 14. The temperature distribution in the turbine blade made of (a) ZrB_2 [3] and (b) TiB_2 .

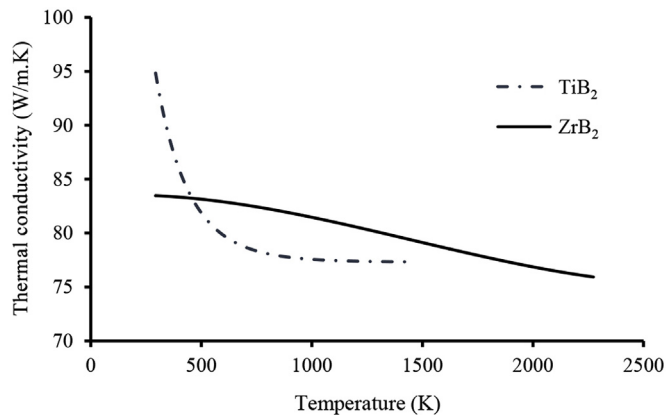


Fig. 15. Thermal conductivities of TiB_2 [42] and ZrB_2 [73].

from the surfaces in contact with the hot and cold fluid is obeying the Newton cooling law which is as:

$$q_0 = h(T_{ext} - T) \quad (2)$$

In which q_0 represent the heat flux and h is the convective heat

transfer coefficient, T_{ext} and T represent the external fluid and the solid surface temperatures, respectively.

The general form of strain tensor for solid domain can be written as Eq. (3) [3]:

$$\varepsilon = \frac{\nabla \vec{u} + \nabla \vec{u}^T}{2} \quad (3)$$

where u shows the displacement vector. The relation between strain tensor, stress tensor and temperature is stated by Duhamel-Hook's law according to Eq. (4), in which D is elasticity tensor. In this relation, thermal expansion and other material properties are assumed to be isotropic and initial stresses and strains are neglected [3].

$$\sigma = D(\varepsilon - \alpha(T - T_0)) \quad (4)$$

In fact, D shows the stiffness matrix of materials and due to the symmetric condition it has, a 3×3 matrix indicates the three stress components [3].

$$\begin{bmatrix} \sigma_x \\ \sigma_y \\ \sigma_z \end{bmatrix} = \frac{E}{(1+\nu)(1-2\nu)} \begin{bmatrix} 1-\nu & \nu & \nu \\ \nu & 1-\nu & \nu \\ \nu & \nu & 1-\nu \end{bmatrix} \begin{bmatrix} \varepsilon_x \\ \varepsilon_y \\ \varepsilon_z \end{bmatrix} \quad (5)$$

where σ , ε and ν are the stress, strain and the Poisson's ratio, respectively. E shows the Young's modulus. The linear relationship between

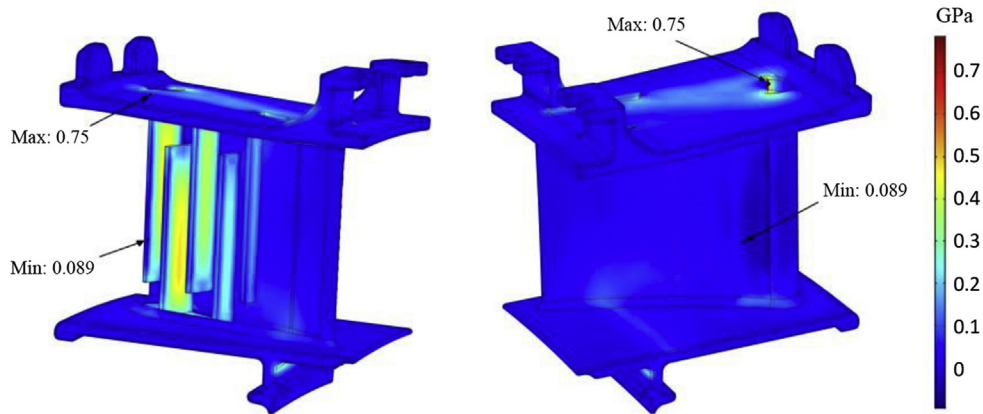


Fig. 16. The contour of principle compressive stresses.

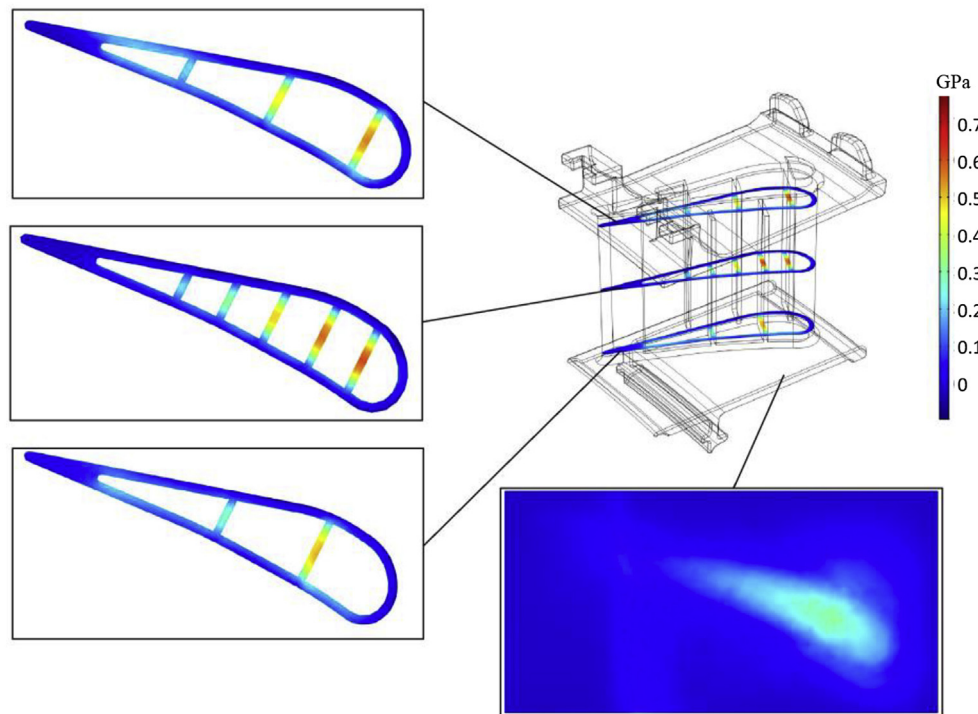


Fig. 17. The contour of principle compressive stresses in various cross sections.

strain and shear components is presented by Eq. (6). This relation is a function of Young's modulus and Poisson's ratio.

$$\tau_{ij} = \frac{E\varepsilon_{ij}}{(1 - 2\nu)} \quad (6)$$

The effective factors on rate of deformation are the properties of material, the applied load and the exposure temperature. In a number of cases such as ceramics, concretes, and other brittle materials the Coulomb-Mohr theory is a suitable criterion for investigating the probability of failure. If a component fails in a high speed gas turbine, the high rotational speed can lead to a full rupture of the whole turbine. The brittle materials have compressive strength more than their corresponding tensile values and TiB_2 as a ceramic material has brittle manner. The obtained stresses under the support forces and temperature gradients are the thermal stresses. Presence of the utilized supports as well as no possibility of movements for blade cause formation of compressive stresses when the body is heated and expanded [3]. Thermal stresses are dominant in this study which are compressive [3], so the third case of the Coulomb-Mohr theory is used for failure

estimation of the blade made of TiB_2 . The coulomb-Mohr theory can be formulated as Eq. (7):

$$\begin{aligned} \sigma_A &= \frac{S_{ut}}{n} & \sigma_A &\geq \sigma_B \geq 0 \\ \frac{\sigma_A}{S_{ut}} - \frac{\sigma_B}{S_{uc}} &= \frac{1}{n} & \sigma_A &\geq 0 \geq \sigma_B \\ \sigma_B &= -\frac{S_{uc}}{n} & 0 &\geq \sigma_A \geq \sigma_B \end{aligned} \quad (7)$$

where n represents the factor of safety, σ_A and σ_B are the principle stresses, S_{ut} and S_{uc} are allocated to ultimate strength in tension and compression, respectively. The plot of Coulomb-Mohr failure theory is shown in Fig. 3. Any point in the colored area represents no failure condition.

2.3. Material properties

Despite rotor blades of the gas turbine, stator blades are stationary and no centrifugal force acts on them. So tensile stresses due to centrifugal force are neglected and most of the stresses generated in the

stator blades are due to fluid flow forces (drag and lift forces) and thermal stresses. The thermal stresses are dominant ones in the stator blades and are compressive. So ceramics are a good candidate because of their compressive strength. ZrB₂ with excellent mechanical properties [14,66–68] have been proposed and tested in the authors' previous paper [3] and the verification of the proposed numerical solution has been achieved. In this paper, monolithic TiB₂ as an UHTC with excellent mechanical and thermal properties is also chosen as the stator blade material and investigated numerically. The governing equations are solved by means of Comsol Multiphysics software. Comsol needs the mechanical and thermal properties of monolithic TiB₂ to solve the governing equations. The properties are obtained from the references [42,43] and presented as:

Elastic modulus (GPa):

$$E = E_0 + (dE/dT)(T - T_0) \quad (8)$$

where E_0 and T_0 are considered as 565 GPa and 296 K, respectively, for the temperature lower than 1000 °C, $dE/dT = -(0.032 \pm 0.015)$ GPa/K should be used.

Thermal conductivity (W/m.K):

$$k = 77.3 + \frac{8270 \times 10^{[-0.002 \times (T-273)]}}{410 + (T - 273)} \quad (9)$$

Thermal diffusivity (m²/s):

$$\alpha = 0.0000145 + \frac{0.00917 \times 10^{[-0.00279 \times (T-273)]}}{530 + (T - 273)} \quad (10)$$

Specific heat capacity (J/kg.K):

$$C_p = 976 + 0.21 \times (T - 273) - 426 \times 10^{[-0.008 \times (T-273)]} \quad (11)$$

The Poisson's ratio is considered as 0.111 based on Refs. [42,69].

2.4. Boundary conditions

The surfaces which were used as places of thermal boundaries are demonstrated in Fig. 4. The heat flux on the blade surfaces is determined using the convective heat transfer coefficient. In this regard, the pressure and suction sides are approximated as two flat plates employing the local heat transfer coefficient for external forced convection. The coefficient of convective heat transfer is given by Eq. (12), in which x is distance from the starting point of the plate and the parameter of U , which is used in the Reynolds number relation, is the fluid flow velocity. The allocated values of velocity for upper surface (suction side), the lower surface (stator pressure side) and the alongside platform walls are 300, 450 and 350 m/s, respectively [3,70]. The temperature of air (combustion gases) is 1100 K as well as a pressure of 30 bar, and the evaluated temperature of materials data is $(T_{\text{surface}} + T_{\text{gas}})/2$. The working temperature of turbine is considered at 900 K and the coefficient of heat transfer is 25 W/m².K. It is worth noting that the sound speed is about 650 m/s, and following that the Mach number is approximately 0.7 for concave side and 0.45 for convex sides which means that the flow is subsonic and the convective heat transfer coefficients can be calculated by Eq. (12) [71].

$$h = \frac{k}{x} Pr^{\frac{1}{3}} \times \begin{cases} 0.332 Re_x^{\frac{1}{2}} & Re_x \leq 5 \times 10^5 \\ 0.0296 Re_x^{\frac{4}{5}} & Re_x \geq 5 \times 10^5 \end{cases} \quad (12)$$

In the present work, for simplifying the simulation of flow in ducts, the average Nusselt number of 400 was considered for cooling ducts and the related heat flux was calculated by Ref. [3]:

$$q'' = \frac{Nu_{\text{cool}} \mu_{\text{cool}} C_{\text{cool}}}{2Pr_{\text{cool}} H_{\text{cool}}} (T_{\text{cool}} - T) \quad (13)$$

where μ , C and H represented the viscosity of cooling air, specific heat capacity and the characteristic length of cooling ducts, respectively.

The rest boundary conditions, shown in Fig. 5, are considered thermally insulated.

The roller and spring foundation was used as coupling of the stator parts to the supports. The rest of the boundaries are free to deform because of thermal expansion. The roller boundary conditions is indicated in Fig. 6, in which the body only allowed to move in parallel direction to specified surface which obeys the following relation:

$$u \cdot n = 0 \quad (14)$$

where n is surface normal vector. The movement of top and bottom surfaces of stator blade is controlled by spring foundation which its boundary condition is given by Eq. (15) and shown in Figs. 7 and 8. K_s is allocated to the stiffness of spring foundation while F and u are the applied forces and displacement, respectively.

$$F = -K_s(u - u_0) \quad (15)$$

The meshed geometry is displayed in Fig. 9. In order to obtain results independent of mesh, different size of unstructured tetrahedral elements were generated and mesh independency was obtained by 147481 elements.

3. Results and discussion

A numerical heat transfer and thermal stress analysis were carried out to investigate the feasibility of using Titanium diboride as turbine stator blade material. At first, the described numerical method verified by the authors' previous paper [3] with the same geometry, material and boundary conditions. Then, the simulations were developed for TiB₂. The temperature distribution in blades and the cooling ducts is presented in Fig. 10 which helps better understanding of cooling effect. As it can be seen, the minimum temperature of 950.5 K arises at the cooling duct. On the other hand, the maximum temperature of 1099.7 K arises at the trailing edge and after that at the mounting parts which are located at the farthest distance from the internal cooling duct. It can be concluded that internal cooling has a significant influence on cooling process of blades. The maximum and minimum temperatures of blades made of different materials are presented in Table 1. Comparing to Ref. [3] the maximum temperature is almost the same, because the thermal resistance in the blade to blade passage is the same and is not a function of the blade material, while the minimum temperature is reduced in comparison with a blade ZrB₂ but increased comparing to the M152 alloy.

As a result of internal cooling, the temperature distribution is not uniform. The differences in temperature distribution are the main reason for the formation of thermal stresses. The trailing edge reaches a very high temperature approximately close to the temperature of combustion gases which may be because of insufficient cooling or higher convection coefficient of the high-speed combustion gases. The higher temperature gradient may lead to cracks formation and propagation near the internal cooling ducts and may result in blade failure. Fig. 11 shows the two-dimensional contours of temperature in different sections of the turbine blade.

Fig. 12 demonstrates the contours of displacement at various parts of the turbine blade made of TiB₂. The minimum displacement of 0.13 mm occur in thermal insulation wall, and the maximum displacement of 1.5 mm occur in the upper wall. As shown in Fig. 12, the displacement is reduced from the leading edge of the blade to the trailing edge due to the roller and spring supports, respectively. The leading edge is near the internal cooling duct that causes higher temperature difference, and because of this thermal gradient, the leading edge has more displacement than trailing edge [72]. Compared to ZrB₂, the maximum displacement is more than that of TiB₂, which is a result of higher thermal expansion of TiB₂. The displacement of different cross-sections of the blade is also shown in Fig. 13.

For comparing the results of temperature distribution in ZrB₂ ceramic and TiB₂ as the alternative material, Fig. 14 is presented. Based

on obtained contours, TiB_2 possesses the more temperature difference in the surface of the blade while temperature distribution in a blade made of ZrB_2 is more uniform. Referring to Table 1, the difference between maximum and minimum temperatures is higher for TiB_2 compared to ZrB_2 , and it is worth noting that the higher temperature difference in the blade made of TiB_2 causes higher thermal gradient and results in higher thermal stresses in turbine blades. The changes in thermal conductivities versus temperature for TiB_2 and ZrB_2 materials are given in Fig. 15. The thermal conductivity of TiB_2 drops sharply at temperatures lower than about 800 K, and in the temperature range between 800–1400 K, the TiB_2 ceramic has the thermal conductivity coefficient lower than ZrB_2 and this is the reason of more non-uniform distribution of temperature in turbine blade made of TiB_2 .

Since TiB_2 is classified as a brittle material, Coulomb–Mohr theory is the most appropriate one to estimate the probability of the blade failure. In this regard, maximum compressive principle stress is used along with the third case of the Coulomb–Mohr theory. In Fig. 16, the maximum compressive principle stress in the turbine blade is shown. The maximum compressive stress of 0.75 GPa is obtained at the internal cooling duct, which is not more than the reported value of 1.8 GPa for ultimate compression strength S_{uc} [42]. It seems that the gas turbine blade made of TiB_2 can withstand the compressive stresses and does not fail with the safety factor of 2.4. Besides, the minimum stress 0.089 GPa is observed near the tip of the turbine blade and indicates that the minimum possibility of failure occurs in these regions. Fig. 17 demonstrates the details of principle stresses in different cross sections of the turbine.

4. Conclusions

In the present study, TiB_2 is selected as an alternative material in manufacturing gas turbine stator blades, and the thermal stresses and temperature distribution is calculated. The paper has presented a numerical solution to investigate heat transfer in turbine stator blades and obtain the thermal stresses via Comsol Multiphysics software. The authors have also considered the consequences of deformation and the possibility of failure as a result of thermal compression stresses. The obtained results were broadly consistent with the reported data of ZrB_2 with the same geometry and applied boundary conditions. The results show that the high thermal conductivity of TiB_2 leads to a faster heat transfer in this ceramic as well as a reduction in thermal stresses. On the other hand, according to Coulomb–Mohr theory, the calculated safety factor ($n = 2.4$) is more than unity and states that the turbine can withstand the applied compressive loads due to high temperatures does not fail. Compared to the ZrB_2 , TiB_2 experiences more maximum displacement.

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