# **Convolutional Neural Networks: Step by Step**

Welcome to Course 4's first assignment! In this assignment, you will implement convolutional (CONV) and pooling (POOL) layers in numpy, including both forward propagation and (optionally) backward propagation.

### Notation:

- Superscript [l] denotes an object of the  $l^{th}$  layer.
  - Example:  $a^{[4]}$  is the  $4^{th}$  layer activation.  $W^{[5]}$  and  $b^{[5]}$  are the  $5^{th}$  layer parameters.
- Superscript (i) denotes an object from the  $i^{th}$  example.
  - Example:  $\chi^{(i)}$  is the  $i^{th}$  training example input.
- Lowerscript i denotes the  $i^{th}$  entry of a vector.
  - **Example:**  $a_i^{[l]}$  denotes the  $i^{th}$  entry of the activations in layer l, assuming this is a fully connected (FC) layer.
- $n_H$ ,  $n_W$  and  $n_C$  denote respectively the height, width and number of channels of a given layer. If you want to reference a specific layer l, you can also write  $n_H^{[l]}$ ,  $n_W^{[l]}$ ,  $n_C^{[l]}$ .
- $n_{H_{prev}}$ ,  $n_{W_{prev}}$  and  $n_{C_{prev}}$  denote respectively the height, width and number of channels of the previous layer. If referencing a specific layer l, this could also be denoted  $n_H^{[l-1]}$ ,  $n_W^{[l-1]}$ ,  $n_C^{[l-1]}$ .

We assume that you are already familiar with numpy and/or have completed the previous courses of the specialization. Let's get started!

# 1 - Packages

Let's first import all the packages that you will need during this assignment.

- numpy (www.numpy.org) is the fundamental package for scientific computing with Python.
- matplotlib (http://matplotlib.org) is a library to plot graphs in Python.
- np.random.seed(1) is used to keep all the random function calls consistent. It will help us grade your work.

```
In [1]: import numpy as np
import h5py
import matplotlib.pyplot as plt

%matplotlib inline
plt.rcParams['figure.figsize'] = (5.0, 4.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

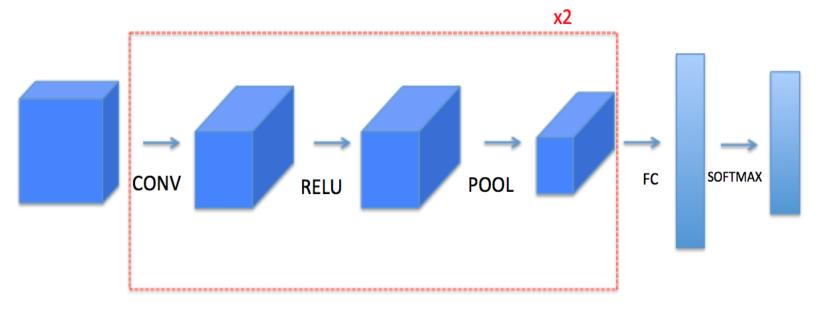
%load_ext autoreload
%autoreload 2
np.random.seed(1)
```

# 2 - Outline of the Assignment

You will be implementing the building blocks of a convolutional neural network! Each function you will implement will have detailed instructions that will walk you through the steps needed:

- · Convolution functions, including:
  - Zero Padding
  - Convolve window
  - Convolution forward
  - Convolution backward (optional)
- Pooling functions, including:
  - Pooling forward
  - Create mask
  - Distribute value
  - Pooling backward (optional)

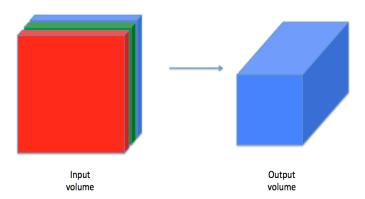
This notebook will ask you to implement these functions from scratch in numpy. In the next notebook, you will use the TensorFlow equivalents of these functions to build the following model:



**Note** that for every forward function, there is its corresponding backward equivalent. Hence, at every step of your forward module you will store some parameters in a cache. These parameters are used to compute gradients during backpropagation.

# 3 - Convolutional Neural Networks

Although programming frameworks make convolutions easy to use, they remain one of the hardest concepts to understand in Deep Learning. A convolution layer transforms an input volume into an output volume of different size, as shown below.



In this part, you will build every step of the convolution layer. You will first implement two helper functions: one for zero padding and the other for computing the convolution function itself.

# 3.1 - Zero-Padding

Zero-padding adds zeros around the border of an image:

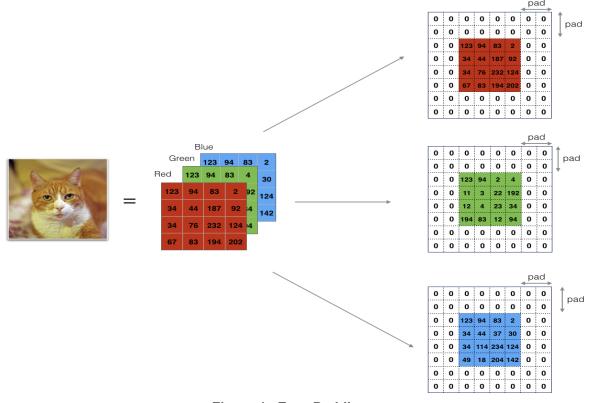


Figure 1 : Zero-Padding Image (3 channels, RGB) with a padding of 2.

The main benefits of padding are the following:

- It allows you to use a CONV layer without necessarily shrinking the height and width of the volumes. This is important for building deeper networks, since otherwise the height/width would shrink as you go to deeper layers. An important special case is the "same" convolution, in which the height/width is exactly preserved after one layer.
- It helps us keep more of the information at the border of an image. Without padding, very few values at the next layer would be affected by pixels as the edges of an image.

**Exercise**: Implement the following function, which pads all the images of a batch of examples X with zeros. <u>Use np.pad</u> (<a href="https://docs.scipy.org/doc/numpy/reference/generated/numpy.pad.html">https://docs.scipy.org/doc/numpy/reference/generated/numpy.pad.html</a>). Note if you want to pad the array "a" of shape (5, 5, 5, 5) with pad = 1 for the 2nd dimension, pad = 3 for the 4th dimension and pad = 0 for the rest, you would do:

```
a = np.pad(a, ((0,0), (1,1), (0,0), (3,3), (0,0)), 'constant', constant values = (..,..))
```

```
In []: # GRADED FUNCTION: zero_pad

def zero_pad(X, pad):
    """
    Pad with zeros all images of the dataset X. The padding is applied to the height and width of an image, as illustrated in Figure 1.

Argument:
    X -- python numpy array of shape (m, n_H, n_W, n_C) representing a batch of m images pad -- integer, amount of padding around each image on vertical and horizontal dimensions

Returns:
    X_pad -- padded image of shape (m, n_H + 2*pad, n_W + 2*pad, n_C)
    """

### START CODE HERE ### (≈ 1 Line)
    X_pad = None
    ### END CODE HERE ###
    return X_pad
```

```
      x.shape:
      (4, 3, 3, 2)

      x_pad.shape:
      (4, 7, 7, 2)

      x[1,1]:
      [[ 0.90085595 -0.68372786] [-0.12289023 -0.93576943] [-0.26788808 0.53035547]]

      x_pad[1,1]:
      [[ 0. 0.] [ 0. 0.] [ 0. 0.] [ 0. 0.] [ 0. 0.] [ 0. 0.] [ 0. 0.] [ 0. 0.]
```

# 3.2 - Single step of convolution

In this part, implement a single step of convolution, in which you apply the filter to a single position of the input. This will be used to build a convolutional unit, which:

- · Takes an input volume
- · Applies a filter at every position of the input
- Outputs another volume (usually of different size)

<b>1</b> <sub>×1</sub>	1,0	<b>1</b> <sub>×1</sub>	0	0					
0,0	<b>1</b> <sub>×1</sub>	<b>1</b> <sub>×0</sub>	1	0		4			
<b>0</b> <sub>×1</sub>	0,×0	<b>1</b> <sub>×1</sub>	1	1					
0	0	1	1	0					
0	1	1	0	0					
Image						Convolved Feature			

Figure 2: Convolution operation

with a filter of 2x2 and a stride of 1 (stride = amount you move the window each time you slide)

In a computer vision application, each value in the matrix on the left corresponds to a single pixel value, and we convolve a 3x3 filter with the image by multiplying its values element-wise with the original matrix, then summing them up and adding a bias. In this first step of the exercise, you will implement a single step of convolution, corresponding to applying a filter to just one of the positions to get a single real-valued output.

Later in this notebook, you'll apply this function to multiple positions of the input to implement the full convolutional operation.

Exercise: Implement conv single step(). Hint (https://docs.scipy.org/doc/numpy-1.13.0/reference/generated/numpy.sum.html).

```
In [ ]: # GRADED FUNCTION: conv single step
        def conv_single_step(a_slice_prev, W, b):
            Apply one filter defined by parameters W on a single slice (a slice prev) of the output activation
            of the previous layer.
            Arguments:
            a slice prev -- slice of input data of shape (f, f, n C prev)
            W -- Weight parameters contained in a window - matrix of shape (f, f, n C prev)
            b -- Bias parameters contained in a window - matrix of shape (1, 1, 1)
            Returns:
            Z -- a scalar value, result of convolving the sliding window (W, b) on a slice x of the input data
            ### START CODE HERE ### (≈ 2 lines of code)
            # Element-wise product between a slice and W. Do not add the bias yet.
            s = None
            # Sum over all entries of the volume s.
            Z = None
            # Add bias b to Z. Cast b to a float() so that Z results in a scalar value.
            Z = None
            ### END CODE HERE ###
            return Z
```

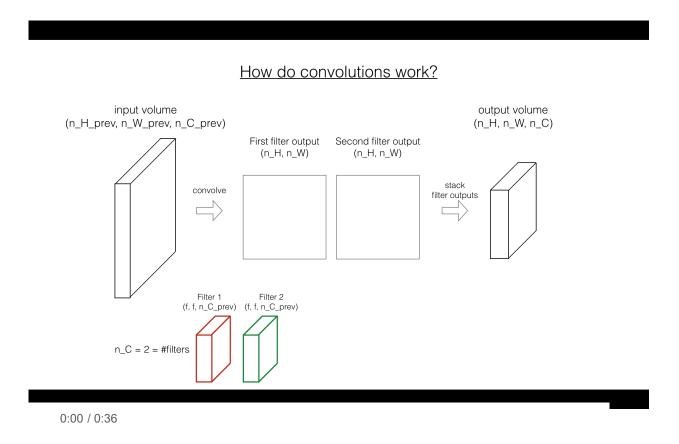
```
In [ ]: np.random.seed(1)
    a_slice_prev = np.random.randn(4, 4, 3)
    W = np.random.randn(4, 4, 3)
    b = np.random.randn(1, 1, 1)

Z = conv_single_step(a_slice_prev, W, b)
    print("Z =", Z)
```

**Z** -6.99908945068

## 3.3 - Convolutional Neural Networks - Forward pass

In the forward pass, you will take many filters and convolve them on the input. Each 'convolution' gives you a 2D matrix output. You will then stack these outputs to get a 3D volume:



**Exercise**: Implement the function below to convolve the filters W on an input activation A\_prev. This function takes as input A\_prev, the activations output by the previous layer (for a batch of m inputs), F filters/weights denoted by W, and a bias vector denoted by b, where each filter has its own (single) bias. Finally you also have access to the hyperparameters dictionary which contains the stride and the padding.

### Hint:

1. To select a 2x2 slice at the upper left corner of a matrix "a\_prev" (shape (5,5,3)), you would do:

This will be useful when you will define a slice prev below, using the start/end indexes you will define.

2. To define a\_slice you will need to first define its corners vert\_start, vert\_end, horiz\_start and horiz\_end. This figure may be helpful for you to find how each of the corner can be defined using h, w, f and s in the code below.

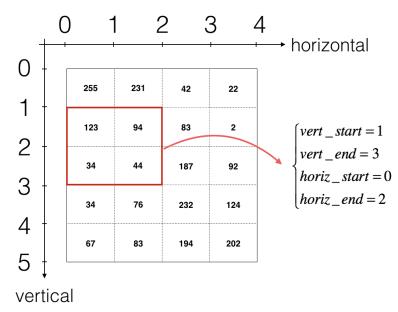


Figure 3: Definition of a slice using vertical and horizontal start/end (with a 2x2 filter)

This figure shows only a single channel.

Reminder: The formulas relating the output shape of the convolution to the input shape is:

$$n_{H} = \lfloor \frac{n_{H_{prev}} - f + 2 \times pad}{stride} \rfloor + 1$$

$$n_{W} = \lfloor \frac{n_{W_{prev}} - f + 2 \times pad}{stride} \rfloor + 1$$

 $n_C$  = number of filters used in the convolution

For this exercise, we won't worry about vectorization, and will just implement everything with for-loops.

```
In [ ]: # GRADED FUNCTION: conv forward
        def conv_forward(A_prev, W, b, hparameters):
            Implements the forward propagation for a convolution function
            Arguments:
            A_prev -- output activations of the previous layer, numpy array of shape (m, n_H_prev, n_W_prev, n_C_prev)
            W -- Weights, numpy array of shape (f, f, n C prev, n C)
            b -- Biases, numpy array of shape (1, 1, 1, n C)
            hparameters -- python dictionary containing "stride" and "pad"
            Returns:
            Z -- conv output, numpy array of shape (m, n H, n W, n C)
            cache -- cache of values needed for the conv backward() function
            ### START CODE HERE ###
            # Retrieve dimensions from A prev's shape (≈1 line)
            (m, n H prev, n W prev, n C prev) = None
            # Retrieve dimensions from W's shape (≈1 line)
            (f, f, n C prev, n C) = None
            # Retrieve information from "hparameters" (≈2 lines)
            stride = None
            pad = None
            # Compute the dimensions of the CONV output volume using the formula given above. Hint: use int() to floor.
            n H = None
            n W = None
            # Initialize the output volume Z with zeros. (≈1 line)
            Z = None
            # Create A prev pad by padding A prev
            A prev pad = None
            for i in range(None):
                                                                 # loop over the batch of training examples
                                                                 # Select ith training example's padded activation
                a prev pad = None
                for h in range(None):
                                                                 # loop over vertical axis of the output volume
                                                                 # loop over horizontal axis of the output volume
                    for w in range(None):
```

```
for c in range(None):
                                                    # loop over channels (= #filters) of the output volume
                # Find the corners of the current "slice" (≈4 lines)
                vert start = None
                vert end = None
                horiz start = None
                horiz end = None
                # Use the corners to define the (3D) slice of a prev pad (See Hint above the cell). (≈1 line)
                a slice prev = None
                # Convolve the (3D) slice with the correct filter W and bias b, to get back one output neuron
                Z[i, h, w, c] = None
### END CODE HERE ###
# Making sure your output shape is correct
assert(Z.shape == (m, n_H, n_W, n_C))
# Save information in "cache" for the backprop
cache = (A prev, W, b, hparameters)
return Z, cache
```

**Z's mean** 0.0489952035289

**Z[3,2,1]** [-0.61490741 -6.7439236 -2.55153897 1.75698377 3.56208902 0.53036437 5.18531798 8.75898442]

[-0.20075807 0.18656139 0.41005165]

Finally, CONV layer should also contain an activation, in which case we would add the following line of code:

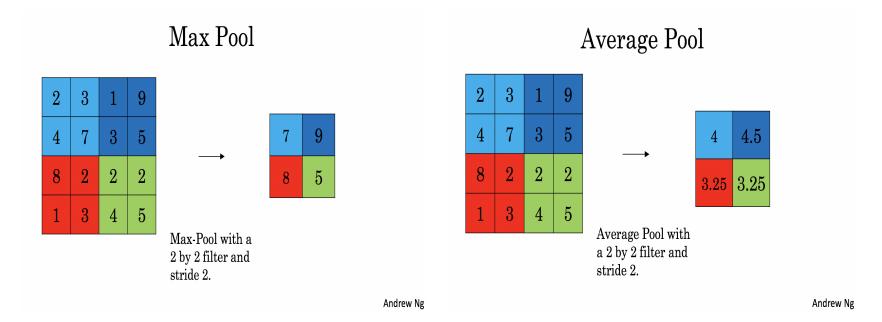
```
# Convolve the window to get back one output neuron
Z[i, h, w, c] = ...
# Apply activation
A[i, h, w, c] = activation(Z[i, h, w, c])
```

You don't need to do it here.

# 4 - Pooling layer

The pooling (POOL) layer reduces the height and width of the input. It helps reduce computation, as well as helps make feature detectors more invariant to its position in the input. The two types of pooling layers are:

- Max-pooling layer: slides an (f, f) window over the input and stores the max value of the window in the output.
- Average-pooling layer: slides an (f, f) window over the input and stores the average value of the window in the output.



These pooling layers have no parameters for backpropagation to train. However, they have hyperparameters such as the window size f. This specifies the height and width of the fxf window you would compute a max or average over.

# 4.1 - Forward Pooling

Now, you are going to implement MAX-POOL and AVG-POOL, in the same function.

**Exercise**: Implement the forward pass of the pooling layer. Follow the hints in the comments below.

**Reminder**: As there's no padding, the formulas binding the output shape of the pooling to the input shape is:

$$n_{H} = \lfloor \frac{n_{H_{prev}} - f}{stride} \rfloor + 1$$

$$n_{W} = \lfloor \frac{n_{W_{prev}} - f}{stride} \rfloor + 1$$

$$n_{C} = n_{C_{prev}}$$

```
In [1]: # GRADED FUNCTION: pool forward
        def pool_forward(A_prev, hparameters, mode = "max"):
            Implements the forward pass of the pooling layer
            Arguments:
            A prev -- Input data, numpy array of shape (m, n H prev, n W prev, n C prev)
            hparameters -- python dictionary containing "f" and "stride"
            mode -- the pooling mode you would like to use, defined as a string ("max" or "average")
            Returns:
            A -- output of the pool layer, a numpy array of shape (m, n H, n W, n C)
            cache -- cache used in the backward pass of the pooling layer, contains the input and hparameters
            # Retrieve dimensions from the input shape
            (m, n H prev, n W prev, n C prev) = A prev.shape
            # Retrieve hyperparameters from "hparameters"
            f = hparameters["f"]
            stride = hparameters["stride"]
            # Define the dimensions of the output
            n H = int(1 + (n H prev - f) / stride)
            n W = int(1 + (n W prev - f) / stride)
            n C = n C prev
            # Initialize output matrix A
            A = np.zeros((m, n H, n W, n C))
            ### START CODE HERE ###
            for i in range(None):
                                                          # loop over the training examples
                for h in range(None):
                                                          # loop on the vertical axis of the output volume
                    for w in range(None):
                                                          # loop on the horizontal axis of the output volume
                                                          # loop over the channels of the output volume
                        for c in range (None):
                            # Find the corners of the current "slice" (≈4 lines)
                            vert start = None
                            vert end = None
                            horiz start = None
                            horiz end = None
```

```
In [ ]: np.random.seed(1)
    A_prev = np.random.randn(2, 4, 4, 3)
    hparameters = {"stride" : 2, "f": 3}

A, cache = pool_forward(A_prev, hparameters)
    print("mode = max")
    print("A =", A)
    print()
    A, cache = pool_forward(A_prev, hparameters, mode = "average")
    print("mode = average")
    print("A =", A)
```

```
A = [[[[ 1.74481176 0.86540763 1.13376944]]] [[[ 1.13162939 1.51981682 2.18557541]]]]

A = [[[[ 0.02105773 -0.20328806 -0.40389855]]] [[[-0.22154621 0.51716526 0.48155844]]]]
```

Congratulations! You have now implemented the forward passes of all the layers of a convolutional network.

The remainer of this notebook is optional, and will not be graded.

# 5 - Backpropagation in convolutional neural networks (OPTIONAL / UNGRADED)

In modern deep learning frameworks, you only have to implement the forward pass, and the framework takes care of the backward pass, so most deep learning engineers don't need to bother with the details of the backward pass. The backward pass for convolutional networks is complicated. If you wish however, you can work through this optional portion of the notebook to get a sense of what backprop in a convolutional network looks like.

When in an earlier course you implemented a simple (fully connected) neural network, you used backpropagation to compute the derivatives with respect to the cost to update the parameters. Similarly, in convolutional neural networks you can to calculate the derivatives with respect to the cost in order to update the parameters. The backprop equations are not trivial and we did not derive them in lecture, but we briefly presented them below.

## 5.1 - Convolutional layer backward pass

Let's start by implementing the backward pass for a CONV layer.

### 5.1.1 - Computing dA:

This is the formula for computing dA with respect to the cost for a certain filter  $W_c$  and a given training example:

$$dA + = \sum_{h=0}^{n_H} \sum_{w=0}^{n_W} W_c \times dZ_{hw}$$
 (1)

Where  $W_c$  is a filter and  $dZ_{hw}$  is a scalar corresponding to the gradient of the cost with respect to the output of the conv layer Z at the hth row and wth column (corresponding to the dot product taken at the ith stride left and jth stride down). Note that at each time, we multiply the the same filter  $W_c$  by a different dZ when updating dA. We do so mainly because when computing the forward propagation, each filter is dotted and summed by a different a\_slice. Therefore when computing the backprop for dA, we are just adding the gradients of all the a\_slices.

In code, inside the appropriate for-loops, this formula translates into:

### 5.1.2 - Computing dW:

This is the formula for computing  $dW_c$  ( $dW_c$  is the derivative of one filter) with respect to the loss:

$$dW_c + = \sum_{h=0}^{n_H} \sum_{w=0}^{n_W} a_{slice} \times dZ_{hw}$$
 (2)

Where  $a_{slice}$  corresponds to the slice which was used to generate the acitivation  $Z_{ij}$ . Hence, this ends up giving us the gradient for W with respect to that slice. Since it is the same W, we will just add up all such gradients to get dW.

In code, inside the appropriate for-loops, this formula translates into:

### 5.1.3 - Computing db:

This is the formula for computing db with respect to the cost for a certain filter  $W_c$ :

$$db = \sum_{h} \sum_{w} dZ_{hw} \tag{3}$$

As you have previously seen in basic neural networks, db is computed by summing dZ. In this case, you are just summing over all the gradients of the conv output (Z) with respect to the cost.

In code, inside the appropriate for-loops, this formula translates into:

**Exercise**: Implement the conv\_backward function below. You should sum over all the training examples, filters, heights, and widths. You should then compute the derivatives using formulas 1, 2 and 3 above.

```
In [ ]: def conv_backward(dZ, cache):
            Implement the backward propagation for a convolution function
            Arguments:
            dZ -- gradient of the cost with respect to the output of the conv layer (Z), numpy array of shape (m, n H, n
            cache -- cache of values needed for the conv backward(), output of conv forward()
            Returns:
            dA prev -- gradient of the cost with respect to the input of the conv layer (A prev),
                       numpy array of shape (m, n_H_prev, n_W_prev, n_C_prev)
            dW -- gradient of the cost with respect to the weights of the conv layer (W)
                  numpy array of shape (f, f, n_C_prev, n_C)
            db -- gradient of the cost with respect to the biases of the conv layer (b)
                  numpy array of shape (1, 1, 1, n C)
             .....
            ### START CODE HERE ###
            # Retrieve information from "cache"
            (A prev, W, b, hparameters) = None
            # Retrieve dimensions from A prev's shape
            (m, n_H_prev, n_W_prev, n_C_prev) = None
            # Retrieve dimensions from W's shape
            (f, f, n C prev, n C) = None
            # Retrieve information from "hparameters"
            stride = None
            pad = None
            # Retrieve dimensions from dZ's shape
            (m, n H, n W, n C) = None
            # Initialize dA prev, dW, db with the correct shapes
            dA prev = None
            dW = None
            db = None
            # Pad A prev and dA prev
            A prev pad = None
            dA prev pad = None
```

```
for i in range(None):
                                                  # loop over the training examples
        # select ith training example from A prev pad and dA prev pad
        a prev pad = None
        da prev pad = None
        for h in range(None):
            h in range(None): # loop over vertical axis of the output volume
for w in range(None): # loop over horizontal axis of the output volume
                for c in range(None):
                                                 # loop over the channels of the output volume
                     # Find the corners of the current "slice"
                    vert start = None
                    vert end = None
                    horiz start = None
                    horiz end = None
                    # Use the corners to define the slice from a prev pad
                     a slice = None
                     # Update gradients for the window and the filter's parameters using the code formulas given d
                    da prev pad[vert start:vert end, horiz start:horiz end, :] += None
                    dW[:,:,:,c] += None
                    db[:,:,:,c] += None
        # Set the ith training example's dA prev to the unpaded da prev pad (Hint: use X[pad:-pad, pad:-pad, :])
        dA prev[i, :, :, :] = None
    ### END CODE HERE ###
    # Making sure your output shape is correct
    assert(dA prev.shape == (m, n H prev, n W prev, n C prev))
    return dA prev, dW, db
dA, dW, db = conv backward(Z, cache conv)
```

```
In [ ]: np.random.seed(1)
    dA, dW, db = conv_backward(Z, cache_conv)
    print("dA_mean =", np.mean(dA))
    print("dW_mean =", np.mean(dW))
    print("db_mean =", np.mean(db))
```

dA mean 1.45243777754

dW mean 1.72699145831

db\_mean 7.83923256462

# 5.2 Pooling layer - backward pass

Next, let's implement the backward pass for the pooling layer, starting with the MAX-POOL layer. Even though a pooling layer has no parameters for backprop to update, you still need to backpropagation the gradient through the pooling layer in order to compute gradients for layers that came before the pooling layer.

# 5.2.1 Max pooling - backward pass

Before jumping into the backpropagation of the pooling layer, you are going to build a helper function called create\_mask\_from\_window() which does the following:

$$X = \begin{bmatrix} 1 & 3 \\ 4 & 2 \end{bmatrix} \quad \rightarrow \quad M = \begin{bmatrix} 0 & 0 \\ 1 & 0 \end{bmatrix} \tag{4}$$

As you can see, this function creates a "mask" matrix which keeps track of where the maximum of the matrix is. True (1) indicates the position of the maximum in X, the other entries are False (0). You'll see later that the backward pass for average pooling will be similar to this but using a different mask.

**Exercise**: Implement create mask from window(). This function will be helpful for pooling backward. Hints:

- <u>np.max() ()</u> may be helpful. It computes the maximum of an array.
- If you have a matrix X and a scalar x: A = (X == x) will return a matrix A of the same size as X such that:

$$A[i,j] = True if X[i,j] = x$$
  
 $A[i,j] = False if X[i,j] != x$ 

• Here, you don't need to consider cases where there are several maxima in a matrix.

```
In []: def create_mask_from_window(x):
    """
    Creates a mask from an input matrix x, to identify the max entry of x.

Arguments:
    x -- Array of shape (f, f)

Returns:
    mask -- Array of the same shape as window, contains a True at the position corresponding to the max entry of
    """

### START CODE HERE ### (≈1 Line)
    mask = None
    ### END CODE HERE ###
    return mask
```

```
In [ ]: np.random.seed(1)
    x = np.random.randn(2,3)
    mask = create_mask_from_window(x)
    print('x = ', x)
    print("mask = ", mask)
```

```
x = [[ 1.62434536 -0.61175641 -0.52817175]

[-1.07296862 0.86540763 -2.3015387 ]]

mask = [[ True False False]

[False False False]
```

Why do we keep track of the position of the max? It's because this is the input value that ultimately influenced the output, and therefore the cost. Backprop is computing gradients with respect to the cost, so anything that influences the ultimate cost should have a non-zero gradient. So, backprop will "propagate" the gradient back to this particular input value that had influenced the cost.

## 5.2.2 - Average pooling - backward pass

In max pooling, for each input window, all the "influence" on the output came from a single input value--the max. In average pooling, every element of the input window has equal influence on the output. So to implement backprop, you will now implement a helper function that reflects this.

For example if we did average pooling in the forward pass using a 2x2 filter, then the mask you'll use for the backward pass will look like:

$$dZ = 1 \quad \rightarrow \quad dZ = \begin{bmatrix} 1/4 & 1/4 \\ 1/4 & 1/4 \end{bmatrix} \tag{5}$$

This implies that each position in the dZ matrix contributes equally to output because in the forward pass, we took an average.

**Exercise**: Implement the function below to equally distribute a value dz through a matrix of dimension shape. <u>Hint (https://docs.scipy.org/doc/numpy-1.13.0/reference/generated/numpy.ones.html)</u>

```
In [ ]: def distribute value(dz, shape):
            Distributes the input value in the matrix of dimension shape
            Arguments:
            dz -- input scalar
            shape -- the shape (n H, n W) of the output matrix for which we want to distribute the value of dz
            Returns:
            a -- Array of size (n H, n W) for which we distributed the value of dz
            ### START CODE HERE ###
            # Retrieve dimensions from shape (≈1 line)
            (n H, n W) = None
            # Compute the value to distribute on the matrix (≈1 line)
            average = None
            # Create a matrix where every entry is the "average" value (≈1 line)
            a = None
            ### END CODE HERE ###
            return a
```

```
In [ ]: a = distribute_value(2, (2,2))
print('distributed value =', a)
```

# 5.2.3 Putting it together: Pooling backward

You now have everything you need to compute backward propagation on a pooling layer.

**Exercise**: Implement the pool\_backward function in both modes ("max" and "average"). You will once again use 4 for-loops (iterating over training examples, height, width, and channels). You should use an if/elif statement to see if the mode is equal to 'max' or 'average'. If it is equal to 'average' you should use the distribute\_value() function you implemented above to create a matrix of the same shape as a\_slice. Otherwise, the mode is equal to 'max', and you will create a mask with create\_mask\_from\_window() and multiply it by the corresponding value of dZ.

```
In [ ]: | def pool backward(dA, cache, mode = "max"):
            Implements the backward pass of the pooling layer
            Arguments:
            dA -- gradient of cost with respect to the output of the pooling layer, same shape as A
            cache -- cache output from the forward pass of the pooling layer, contains the layer's input and hparameters
            mode -- the pooling mode you would like to use, defined as a string ("max" or "average")
            Returns:
            dA prev -- gradient of cost with respect to the input of the pooling layer, same shape as A prev
            ### START CODE HERE ###
            # Retrieve information from cache (≈1 line)
            (A prev, hparameters) = None
            # Retrieve hyperparameters from "hparameters" (≈2 lines)
            stride = None
            f = None
            # Retrieve dimensions from A prev's shape and dA's shape (≈2 lines)
            m, n H prev, n W prev, n C prev = None
            m, n H, n W, n C = None
            # Initialize dA prev with zeros (≈1 line)
            dA_prev = None
            for i in range(None):
                                                       # loop over the training examples
                # select training example from A prev (≈1 line)
                a prev = None
                                        # loop on the vertical axis
                for h in range(None):
                    for w in range(None):
                                                     # loop on the horizontal axis
                        for c in range(None):
                                                       # loop over the channels (depth)
                            # Find the corners of the current "slice" (≈4 lines)
                            vert start = None
                            vert end = None
                            horiz start = None
```

```
horiz end = None
                # Compute the backward propagation in both modes.
                if mode == "max":
                    # Use the corners and "c" to define the current slice from a prev (≈1 line)
                    a prev slice = None
                    # Create the mask from a prev slice (≈1 line)
                    mask = None
                    # Set dA prev to be dA prev + (the mask multiplied by the correct entry of dA) (≈1 line)
                    dA prev[i, vert start: vert end, horiz start: horiz end, c] += None
                elif mode == "average":
                    # Get the value a from dA (≈1 line)
                    da = None
                    # Define the shape of the filter as fxf (≈1 line)
                    shape = None
                    # Distribute it to get the correct slice of dA prev. i.e. Add the distributed value of do
                    dA prev[i, vert start: vert end, horiz start: horiz end, c] += None
### END CODE ###
# Making sure your output shape is correct
assert(dA prev.shape == A prev.shape)
return dA prev
```

```
In [ ]: np.random.seed(1)
        A prev = np.random.randn(5, 5, 3, 2)
        hparameters = {"stride" : 1, "f": 2}
        A, cache = pool forward(A prev, hparameters)
         dA = np.random.randn(5, 4, 2, 2)
        dA_prev = pool_backward(dA, cache, mode = "max")
        print("mode = max")
        print('mean of dA = ', np.mean(dA))
        print('dA prev[1,1] = ', dA prev[1,1])
         print()
        dA prev = pool backward(dA, cache, mode = "average")
        print("mode = average")
        print('mean of dA = ', np.mean(dA))
        print('dA prev[1,1] = ', dA prev[1,1])
```

mode = max:

# **Congratulations!**

Congratulation on completing this assignment. You now understand how convolutional neural networks work. You have implemented all the building blocks of a neural network. In the next assignment you will implement a ConvNet using TensorFlow.