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In[1]:=  $\Lambda = \{\{1, 1, -1, 1\}, \{1, 1, 1, -1\}, \{1, -1, -1, -1\}, \{1, -1, 1, 1\}\}$ 
 $M = \frac{1}{\sqrt{2}} \{\{1, 0, 0, I\}, \{0, I, 1, 0\}, \{0, I, -1, 0\}, \{1, 0, 0, -I\}\}$ 
 $\theta_0 = (\text{Inverse}[\Lambda] \cdot \{\theta_0, \theta_1, \theta_2, \theta_3\})[[1]]$ 
 $\theta_1 = (\text{Inverse}[\Lambda] \cdot \{\theta_0, \theta_1, \theta_2, \theta_3\})[[2]]$ 
 $\theta_2 = (\text{Inverse}[\Lambda] \cdot \{\theta_0, \theta_1, \theta_2, \theta_3\})[[3]]$ 
 $\theta_3 = (\text{Inverse}[\Lambda] \cdot \{\theta_0, \theta_1, \theta_2, \theta_3\})[[4]]$ 
 $\sigma_x = \{\{0, 1\}, \{1, 0\}\}$ 
 $\sigma_y = \{\{0, -I\}, \{I, 0\}\}$ 
 $\sigma_z = \{\{1, 0\}, \{0, -1\}\}$ 
 $\phi_1 = \frac{1}{\sqrt{2}} * (\text{KroneckerProduct}[\{\{1, 0\}\}, \{\{1, 0\}\}] + \text{KroneckerProduct}[\{\{0, 1\}\}, \{\{0, 1\}\}])$ 
 $\phi_2 = \frac{-I}{\sqrt{2}} * (\text{KroneckerProduct}[\{\{1, 0\}\}, \{\{1, 0\}\}] - \text{KroneckerProduct}[\{\{0, 1\}\}, \{\{0, 1\}\}])$ 
 $\phi_3 = \frac{1}{\sqrt{2}} * (\text{KroneckerProduct}[\{\{1, 0\}\}, \{\{0, 1\}\}] - \text{KroneckerProduct}[\{\{0, 1\}\}, \{\{1, 0\}\}])$ 
 $\phi_4 = \frac{-I}{\sqrt{2}} * (\text{KroneckerProduct}[\{\{1, 0\}\}, \{\{0, 1\}\}] + \text{KroneckerProduct}[\{\{0, 1\}\}, \{\{1, 0\}\}])$ 
DMatrix =
  {Exp[I *  $\theta_0$ ], 0, 0, 0}, {0, Exp[I *  $\theta_1$ ], 0, 0}, {0, 0, Exp[I *  $\theta_2$ ], 0}, {0, 0, 0, Exp[I *  $\theta_3$ ]}
FullSimplify[M.DMatrix.ConjugateTranspose[M] -
  Exp[I *  $\theta_0$ ] * MatrixExp[I * ( $\theta_1$  * KroneckerProduct[ $\sigma_x$ ,  $\sigma_x$ ] +
     $\theta_2$  * KroneckerProduct[ $\sigma_y$ ,  $\sigma_y$ ] +  $\theta_3$  * KroneckerProduct[ $\sigma_z$ ,  $\sigma_z$ ])] ]

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Out[1]= $\{\{1, 1, -1, 1\}, \{1, 1, 1, -1\}, \{1, -1, -1, -1\}, \{1, -1, 1, 1\}\}$

Out[2]= $\{\{\frac{1}{\sqrt{2}}, 0, 0, \frac{i}{\sqrt{2}}\}, \{0, \frac{i}{\sqrt{2}}, \frac{1}{\sqrt{2}}, 0\}, \{0, \frac{i}{\sqrt{2}}, -\frac{1}{\sqrt{2}}, 0\}, \{\frac{1}{\sqrt{2}}, 0, 0, -\frac{i}{\sqrt{2}}\}\}$

Out[3]= $\frac{\theta_0}{4} + \frac{\theta_1}{4} + \frac{\theta_2}{4} + \frac{\theta_3}{4}$

Out[4]= $\frac{\theta_0}{4} + \frac{\theta_1}{4} - \frac{\theta_2}{4} - \frac{\theta_3}{4}$

Out[5]= $-\frac{\theta_0}{4} + \frac{\theta_1}{4} - \frac{\theta_2}{4} + \frac{\theta_3}{4}$

Out[6]= $\frac{\theta_0}{4} - \frac{\theta_1}{4} - \frac{\theta_2}{4} + \frac{\theta_3}{4}$

Out[7]= $\{\{0, 1\}, \{1, 0\}\}$

Out[8]= $\{\{0, -i\}, \{i, 0\}\}$

Out[9]= $\{\{1, 0\}, \{0, -1\}\}$

Out[10]= $\{\{\frac{1}{\sqrt{2}}, 0, 0, \frac{1}{\sqrt{2}}\}\}$

$$\text{Out}[11]= \left\{ \left\{ -\frac{i}{\sqrt{2}}, 0, 0, \frac{i}{\sqrt{2}} \right\} \right\}$$

$$\text{Out}[12]= \left\{ \left\{ 0, \frac{1}{\sqrt{2}}, -\frac{1}{\sqrt{2}}, 0 \right\} \right\}$$

$$\text{Out}[13]= \left\{ \left\{ 0, -\frac{i}{\sqrt{2}}, -\frac{i}{\sqrt{2}}, 0 \right\} \right\}$$

$$\text{Out}[14]= \left\{ \left\{ e^{i\Phi 0}, 0, 0, 0 \right\}, \left\{ 0, e^{i\Phi 1}, 0, 0 \right\}, \left\{ 0, 0, e^{i\Phi 2}, 0 \right\}, \left\{ 0, 0, 0, e^{i\Phi 3} \right\} \right\}$$

$$\text{Out}[15]= \left\{ \left\{ 0, 0, 0, 0 \right\}, \left\{ 0, 0, 0, 0 \right\}, \left\{ 0, 0, 0, 0 \right\}, \left\{ 0, 0, 0, 0 \right\} \right\}$$

(*OK, we miraculously exponentiated all this happiness*)

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In[16]:= FullSimplify[
  M.DMatrix.ConjugateTranspose[M] - Exp[I * \Theta 0] * MatrixExp[I * (\Theta 1 * KroneckerProduct[\sigma x, \sigma x] +
    \Theta 2 * KroneckerProduct[\sigma y, \sigma y] + \Theta 3 * KroneckerProduct[\sigma z, \sigma z])]]]
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$$\text{Out}[16]= \left\{ \left\{ 0, 0, 0, 0 \right\}, \left\{ 0, 0, 0, 0 \right\}, \left\{ 0, 0, 0, 0 \right\}, \left\{ 0, 0, 0, 0 \right\} \right\}$$

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