

# Causal Reliable Broadcast

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## Motivation

- Assume we have a chat application
  - Whatever written is **reliably broadcast** to group
- If you get the following output, is it ok?

[ali] Are you sure? Not E?  
[MrsY] Auditorium D at Forum  
[MrX] Does anyone know where the lecture is today?
- MrX's message **caused** MrsY's message,
  - MrsY's message **caused** Ali's message

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## Motivation (2)

- Does uniform reliable broadcast remedy this? [d]
- Causal reliable broadcast solves this
  - Deliveries in **causal order**!
- Causality is same as happened-before relation by Lamport!

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## Causality Recalled

- Let  $m_1$  and  $m_2$  be any two messages:  
 $m_1 \rightarrow m_2$  ( $m_1$  **causally precedes**  $m_2$ ) if
  - **C1 (FIFO order)**.
    - Some process  $p_i$  broadcasts  $m_1$  before broadcasting  $m_2$
  - **C2 (Network order)**.
    - Some process  $p_i$  delivers  $m_1$  and later broadcasts  $m_2$
  - **C3 (Transitivity)**.
    - There is a message  $m'$  such that  $m_1 \rightarrow m'$  and  $m' \rightarrow m_2$

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## Causal Broadcast Interface

### ■ Module:

- Name: CausalOrder (co)

### ■ Events

- Request:  $\langle \text{coBroadcast} \mid m \rangle$
- Indication:  $\langle \text{coDeliver} \mid \text{src}, m \rangle$

### ■ Property:

- **CB:** If node  $p_i$  delivers  $m_1$ , then  $p_i$  must have delivered every message causally preceding ( $\rightarrow$ )  $m_1$  before  $m_1$

### ■ Is this useful? How can it be satisfied? [d]

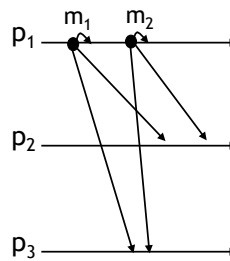
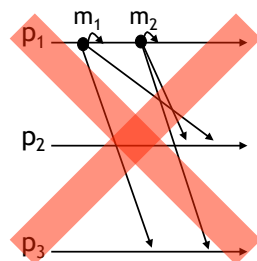
- It is only safety. Satisfy it by never delivering!

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## Causality

### □ C1 (FIFO order).

- Some process  $p_i$  broadcasts  $m_1$  before broadcasting  $m_2$

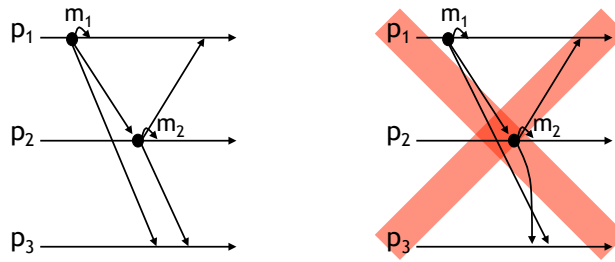


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## Causality (2)

### □ C2 (Network order).

- Some process  $p_i$  delivers  $m_1$  and later broadcasts  $m_2$

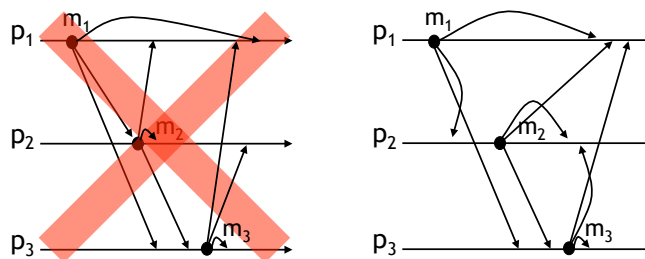


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## Causality (3)

### □ C3 (Transitivity).

- There is a message  $m'$  such that  $m_1 \rightarrow m'$  and  $m' \rightarrow m_2$



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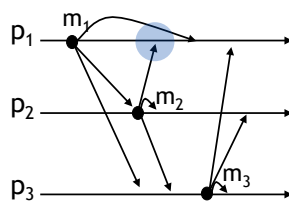
## Different Causalities

- **Property:**

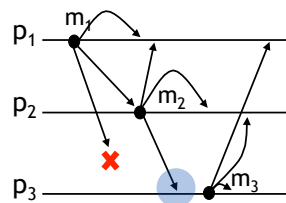
- **CB:** If node  $p_i$  delivers  $m_1$ , then  $p_i$  must deliver every message causally preceding ( $\rightarrow$ )  $m_1$  before  $m_1$
- **CB':** If  $p_i$  delivers  $m_1$  and  $m_2$ , and  $m_1 \rightarrow m_2$ , then  $p_i$  must deliver  $m_1$  before  $m_2$

- What is the difference? [d]

Violates CB and CB'



Violates CB, not CB'



- Indeed, CB implies CB'

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## Reliable Causal Broadcast Interface

- **Module:**

- Name: **ReliableCausalOrder (rco)**

- **Events**

- Request:  **$\langle \text{rcoBroadcast} \mid m \rangle$**
- Indication:  **$\langle \text{rcoDeliver} \mid \text{src}, m \rangle$**

- **Property:**

- **RB1-RB4** from regular reliable broadcast
- **CB:** If node  $p_i$  delivers  $m$ , then  $p_i$  must deliver every message causally preceding ( $\rightarrow$ )  $m$  before  $m$

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## Uniform Reliable Causal Broadcast

### ■ Module:

- Name: `UniformReliableCausalOrder` (urco)

### ■ Events

- Request: `<urcoBroadcast | m>`
- Indication: `<urcoDeliver | src, m>`

### ■ Property:

- **URB1-URB4** from uniform reliable broadcast
- **CB**: If node  $p_i$  delivers  $m$ , then  $p_i$  must deliver every message causally preceding ( $\rightarrow$ )  $m$  before  $m$

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## Idea Reuse...

### ■ Reuse RB for CB

- Use **reliable broadcast** abstraction to implement **reliable causal broadcast**
  - Use **uniform reliable broadcast** abstraction to implement **uniform causal broadcast**
- ### ■ This gives a layered architecture!
- CB component on top of RB component

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## Towards an Implementation

- Main idea
  - Each broadcasted message carries a **history**
  - Before delivery, ensure causality
- First algorithm
  - History is set of all **causally preceding** messages

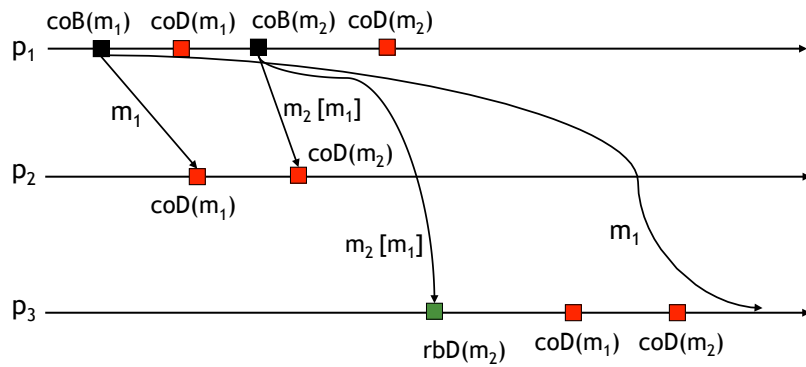
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## Fail-Silent No-Waiting Causal Bcast

- Each message **m** carries **ordered list** of causally preceding messages in **past<sub>m</sub>**
- Whenever a node **rbDelivers m**
  - coDeliver causally preceding messages in **past<sub>m</sub>**
  - coDelivers **m**
    - Avoid duplicates using **delivered** set

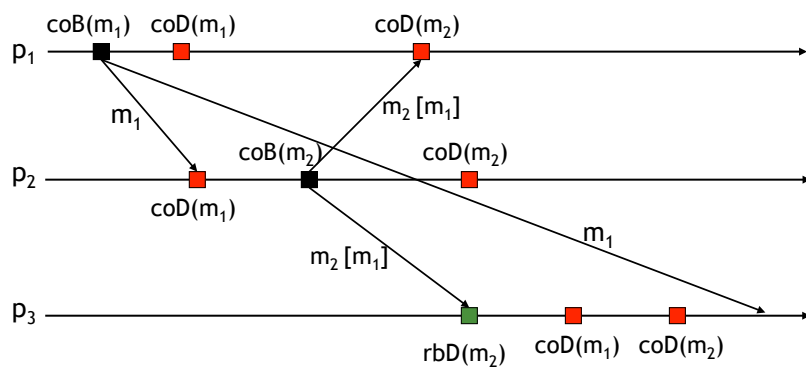
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## Execution (direct override)



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## Execution (indirect override)



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## Fail-Silent Causal Broadcast Impl

- **Implements:**

- ReliableCausalOrderBroadcast (rco).

- **Uses:** ReliableBroadcast (rb).

- **upon event  $\langle \text{Init} \rangle$  do**

- $\text{delivered} := \emptyset$ ;  $\text{past} := \text{nil}$

- **upon event  $\langle \text{rcoBroadcast} \mid m \rangle$  do**

- **trigger**  $\langle \text{rbBroadcast} \mid (\text{DATA}, \text{past}, m) \rangle$
- $\text{past} := \text{append}(\text{past}, \langle p_i, m \rangle)$

Append this message  
to past history

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## Fail-Silent Causal Broadcast Impl (2)

- **upon event  $\langle \text{rbDeliver} \mid p_i, (\text{DATA}, \text{past}_m, m) \rangle$  do**

- **if**  $m \notin \text{delivered}$  **then**

- **forall**  $(s_n, n) \in \text{past}_m$  **do**

in ascending order

- **if**  $n \notin \text{delivered}$  **then**

- **trigger**  $\langle \text{rcoDeliver} \mid s_n, n \rangle$

deliver preceding  
messages

- $\text{delivered} := \text{delivered} \cup \{n\}$

- $\text{past} := \text{append}(\text{past}, \langle s_n, n \rangle)$

append to history

- **trigger**  $\langle \text{rcoDeliver} \mid p_i, m \rangle$

deliver current  
message

- $\text{delivered} := \text{delivered} \cup \{m\}$

- $\text{past} := \text{append}(\text{past}, \langle p_i, m \rangle)$

append to history

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## Correctness

- RB1-RB4 follow from use of RB
  - No creation and no duplication still satisfied
  - Validity still satisfied
    - Some messages might be delivered earlier, never later
  - Agreement directly from RB
- CO by **induction** on prefixes of executions
  - It is vacuously true for empty executions
  - Assume it is true for all deliveries of a prefix
    - Then it is true for any extension with one event

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## Improving the Algorithm

- Disadvantage of algorithm is that the message size (bit complexity) grows
- Useful idea
  - **Garbage collect** old messages
- Implementation of GC
  - Ack receipt of every message  $m$  to all
  - Use perfect failure detector **P**
    - Determine with  $P$  when all correct nodes got message  $m$
    - Delete  $m$  from past when all correct nodes got  $m$

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## GC Implementation

- **Uses:** ReliableBroadcast (rb), PerfectFailureDetector (P)
- **upon event  $\langle \text{Init} \rangle$  do**
  - $\text{delivered} := \emptyset$ ;  $\text{past} := \text{nil}$
  - $\text{correct} := \Pi$
  - for all  $m$ :  $\text{ack}[m] := \emptyset$  ← **bookkeeping of acks**
- **upon event  $\langle \text{crash} \mid p_i \rangle$  do**
  - $\text{correct} := \text{correct} \setminus \{p_i\}$
- **upon event  $m \in \text{delivered}$  and  $\text{self} \notin \text{ack}[m]$  do** ← **called upon coDeliver**
  - $\text{ack} := \text{ack}[m] \cup \{\text{self}\}$
  - **trigger**  $\langle \text{rbBroadcast} \mid (\text{ACK}, m) \rangle$  ← **ack to all**
- **upon event  $\langle \text{rbDeliver} \mid p_i, [\text{ACK}, m] \rangle$  do**
  - $\text{ack} := \text{ack}[m] \cup \{p_i\}$
  - if  $\text{correct} \subseteq \text{ack}[m]$  do
  - $\text{past} := \text{remove}(\text{past}, \langle x, m \rangle)$  ← **When received ack from all, GC m from any x**

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## GC Questions

- What about the acks? **[d]**
  - The  $\text{ack}[m]$  array also grows with time
  - How do we garbage collect it?
- What happens if we use  $\Diamond P$ ? **[d]**
  - Does the garbage collector still work?

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## Towards Another Implementation

- Main idea
  - Each broadcasted message carries a **history**
  - Before delivery, ensure causality
- First algorithm
  - History is set of all **causally preceding** messages
- Second algorithm **[d]**
  - History is a **vector timestamp**

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## Fail-Silent Waiting Causal Broadcast

- Represent past history by **vector clock (VC)**
- Slightly modify the VC implementation
  - At node  $p_i$ 
    - **VC[i]**: number of messages  $p_i$  coBroadcasted
    - **VC[j],  $j \neq i$** : number of messages  $p_i$  coDelivered from  $p_j$
- Idea: vector clock only for **relevant events**

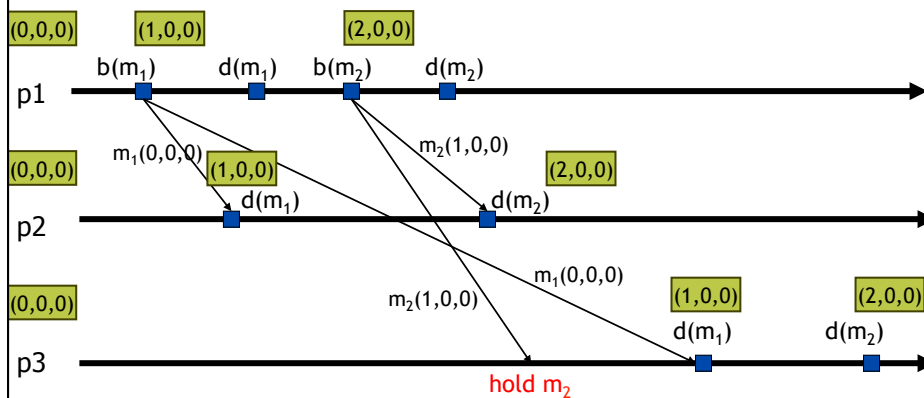
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## Fail-Silent Waiting Causal Broadcast

- Upon CO broadcast  $m$ 
  - Piggyback  $VC$  and RB broadcast  $m$
- Upon RB delivery of  $m$  with attached  $VC_m$ 
  - compare  $VC_m$  with local  $VC_i$
  - Only deliver  $m$  once  $VC_m$  precedes ( $\leq$ )  $VC_i$

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## Execution



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## Fail-Silent Waiting Causal Impl.

- **Implements:**

- ReliableCausalOrderBroadcast (rco)

- **Uses:** ReliableBroadcast (rb)

- **upon event  $\langle \text{Init} \rangle$  do**

- forall  $p_i \in \Pi$  do  $\text{VC}[i] := 0$

- **upon event  $\langle \text{rcoBroadcast} | m \rangle$  do**

- **trigger**  $\langle \text{rbBroadcast} | (\text{DATA}, \text{VC}, m) \rangle$
- $\text{VC}[\text{self}] := \text{VC}[\text{self}] + 1$
- **trigger**  $\langle \text{rcoDeliver} | \text{self}, m \rangle$

send m with VC

VC has only increased, so RCO deliver

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## Fail-Silent Waiting Causal Impl. (2)

- **upon event  $\langle \text{rbDeliver} | p_j, (\text{DATA}, \text{VC}_m, m) \rangle$  do**

- if  $p_j \neq \text{self}$  then

- $\text{pending} := \text{pending} \cup (p_j, (\text{DATA}, \text{VC}_m, m))$
- $\text{deliver-pending}()$

put on hold

- **procedure deliver-pending()**

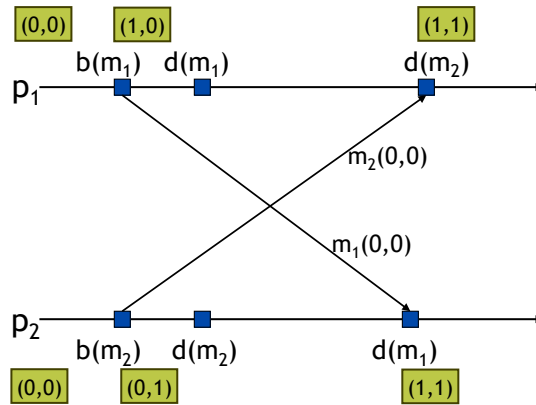
- **while exists**  $x = (s_m, (\text{DATA}, \text{VC}_m, m)) \in \text{pending}$  s.t.  $\text{VC} \geq \text{VC}_m$  **do**
- $\text{pending} := \text{pending} \setminus (s_m, (\text{DATA}, \text{VC}_m, m))$
- **trigger**  $\langle \text{rcoDeliver} | s_m, m \rangle$
- $\text{VC}[\text{rank}(s_m)] := \text{VC}[\text{rank}(s_m)] + 1$

for every message whose  $\text{VC}_m$  precedes local VC

Remove on hold deliver and increase local VC

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## Possible Execution?



- Delivery order isn't same!
  - What is wrong? **[d]** Nothing, there is no causality.

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## Different Possible Orderings

- Some common orderings
  - (Single-source) **FIFO order**
  - **Total order**
  - **Causal order**

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## Single-Source FIFO Order

- Intuitively
  - Msgs from **same node** delivered in **order sent**
- For all messages  $m_1$  and  $m_2$  and all  $p_i$  and  $p_j$ ,
  - if  $p_i$  broadcasts  $m_1$  before  $m_2$ , and if  $p_j$  delivers  $m_1$  and  $m_2$ , then  $p_j$  delivers  $m_1$  before  $m_2$
- Caveat
  - This formulation doesn't require delivery of both messages

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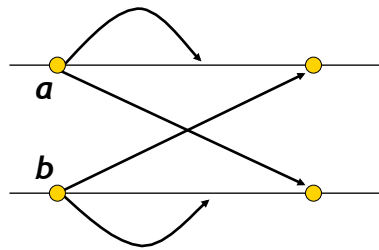
## Total Order

- Intuitively
  - **Everyone** delivers everything in exact **same order**
- For all messages  $m_1$  and  $m_2$  and all  $p_i$  and  $p_j$ ,
  - if both  $p_i$  and  $p_j$  deliver both messages, then they deliver them in the same order
- Caveats
  - This formulation doesn't require delivery of both messages
  - Everyone delivers in the *same order*, this might not be the *send order*!

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## Execution Example (1)



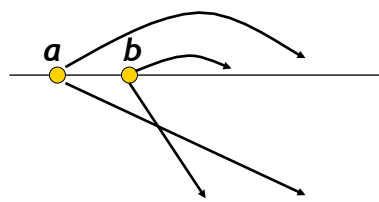
single-source FIFO? **yes**

totally ordered? **no**

causally ordered? **yes**

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## Execution Example (2)



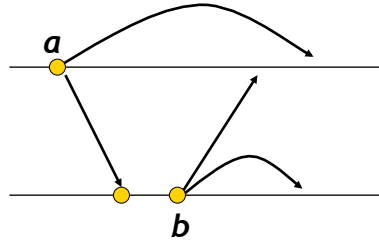
single-source FIFO? **no**

totally ordered? **yes**

causally ordered? **no**

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## Execution Example (3)



single-source FIFO? **yes**

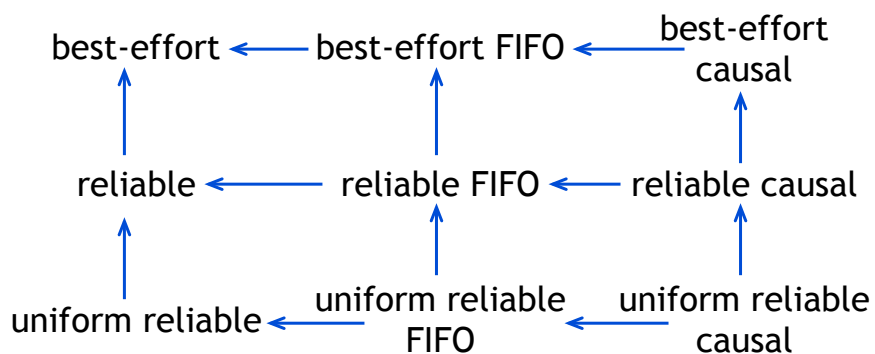
totally ordered? **no**

causally ordered? **no**

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## Hierarchy of Orderings

- Stronger **implies** weaker ordering ( $\rightarrow$ )



- Where does total order fit? **[d]**

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