
Segmentation

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Machine Vision Technology							
Semantic information				Metric 3D information			
Pixels	Segments	Images	Videos	Camera		Multi-view Geometry	
Convolutions Edges & Fitting Local features Texture	Segmentation Clustering	Recognition Detection	Motion Tracking	Camera Model	Camera Calibration	Epipolar Geometry	SFM
10	4	4	2	2	2	2	2

Image segmentation



Source: S. Lazechnik

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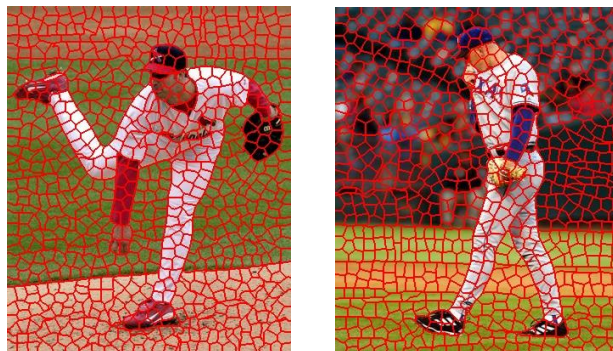
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The goals of segmentation

- Group together similar-looking pixels for efficiency of further processing
 - “Bottom-up” process
 - Unsupervised

“superpixels”



X. Ren and J. Malik. [Learning a classification model for segmentation](#). ICCV 2003.

Source: S. Lazechnik

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The goals of segmentation

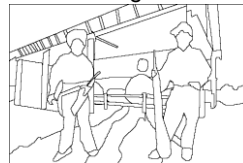
- Separate image into coherent “objects”
 - “Bottom-up” or “top-down” process?
 - Supervised or unsupervised?



image



human segmentation



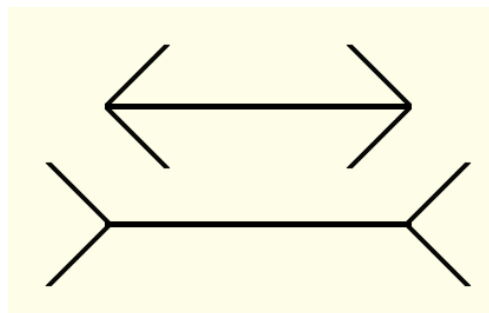
Berkeley segmentation database:

<http://www.eecs.berkeley.edu/Research/Projects/CS/vision/grouping/segbench/>

Inspiration from psychology

- The Gestalt school: Grouping is key to visual perception

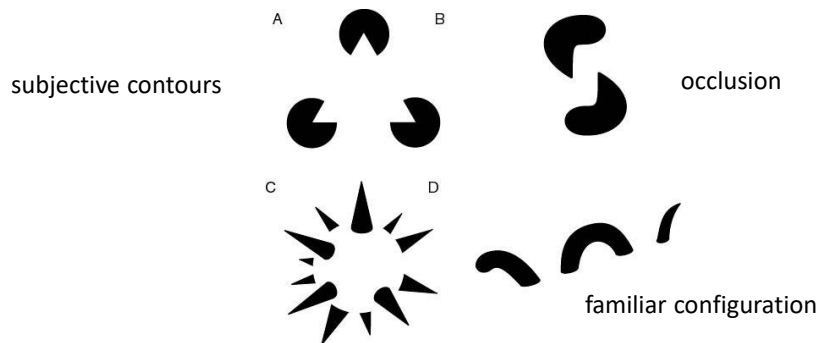
The Muller-Lyer illusion



http://en.wikipedia.org/wiki/Gestalt_psychology

The Gestalt school

- Elements in a collection can have properties that result from relationships
 - “The whole is greater than the sum of its parts”



http://en.wikipedia.org/wiki/Gestalt_psychology

Source: S. Lazebnik

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Emergence



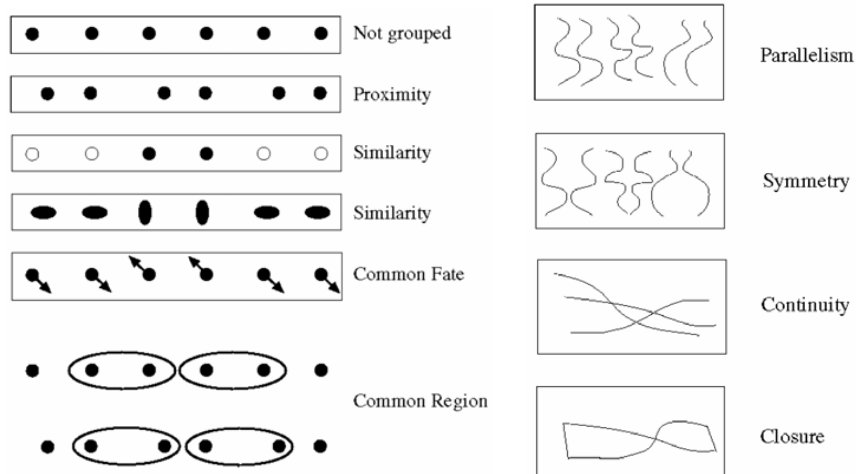
http://en.wikipedia.org/wiki/Gestalt_psychology

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Gestalt factors



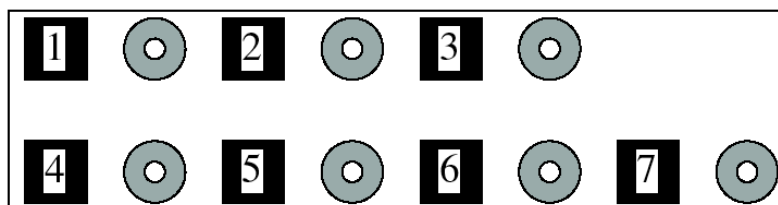
Source: S. Lazebnik

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Grouping phenomena in real life



Forsyth & Ponce, Figure 14.7

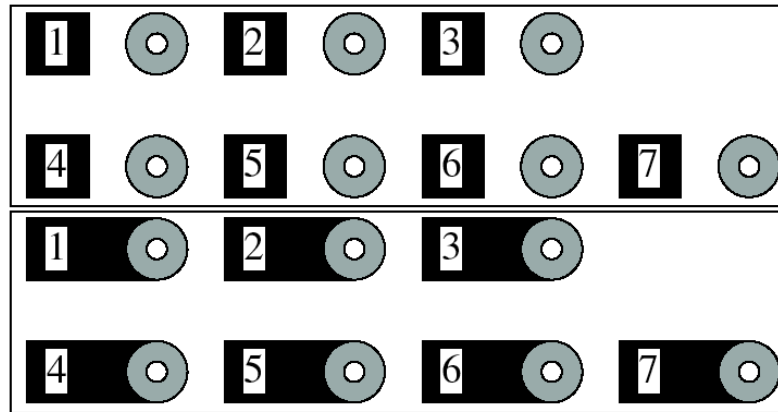
Source: S. Lazebnik

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Grouping phenomena in real life



Forsyth & Ponce, Figure 14.7

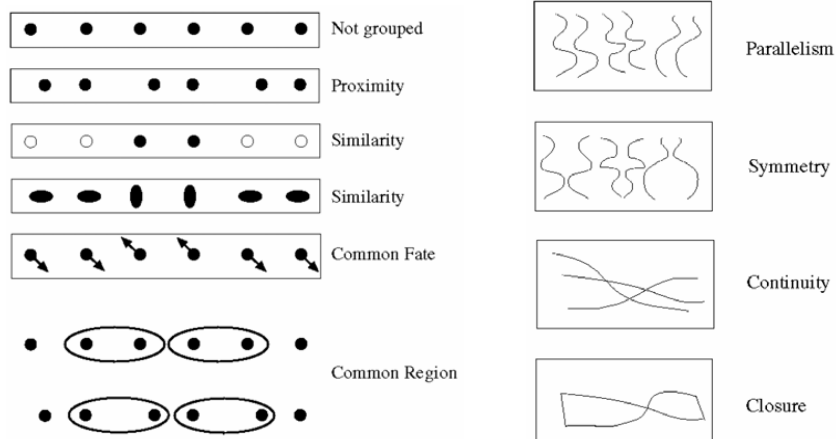
Source: S. Lazebnik

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Gestalt factors



These factors make intuitive sense, but are very difficult to translate into algorithms

Source: S. Lazebnik

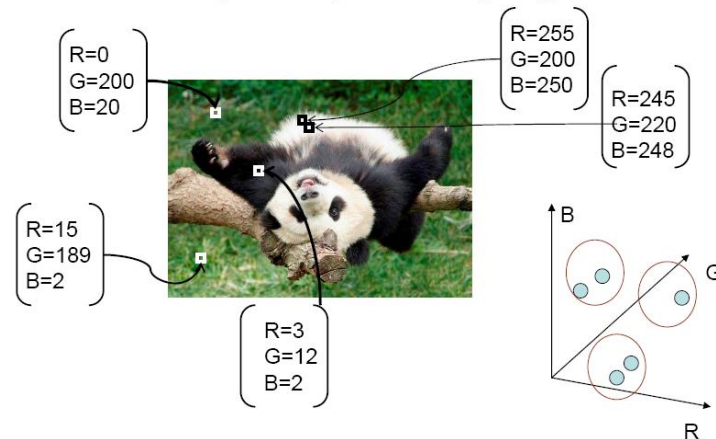
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Segmentation as clustering

- Cluster similar pixels (features) together



Source: K. Grauman

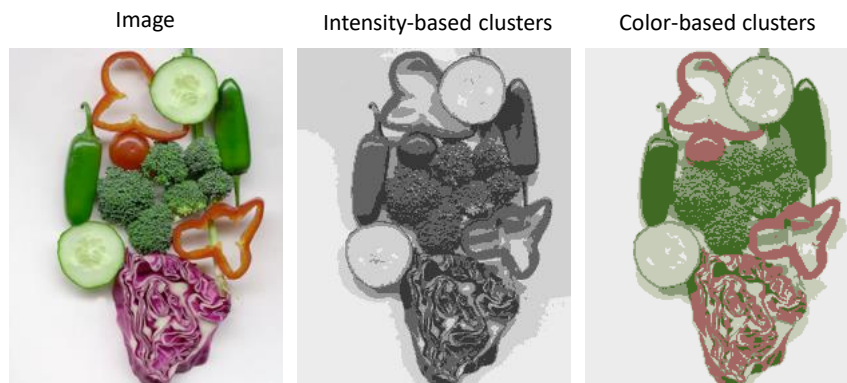
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Segmentation as clustering

- K-means clustering based on intensity or color is essentially vector quantization of the image attributes
 - Clusters don't have to be spatially coherent



Source: S. Lazebnik

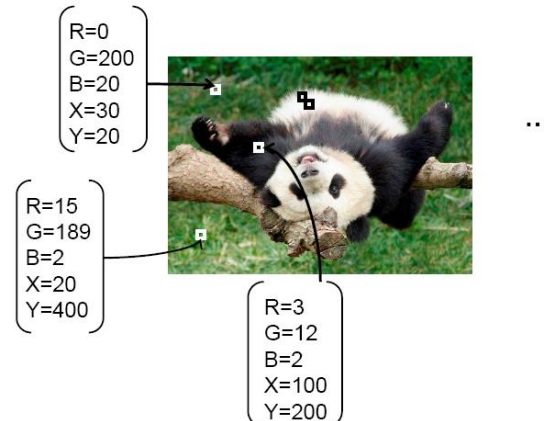
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Segmentation as clustering

- Cluster similar pixels (features) together



Source: K. Grauman

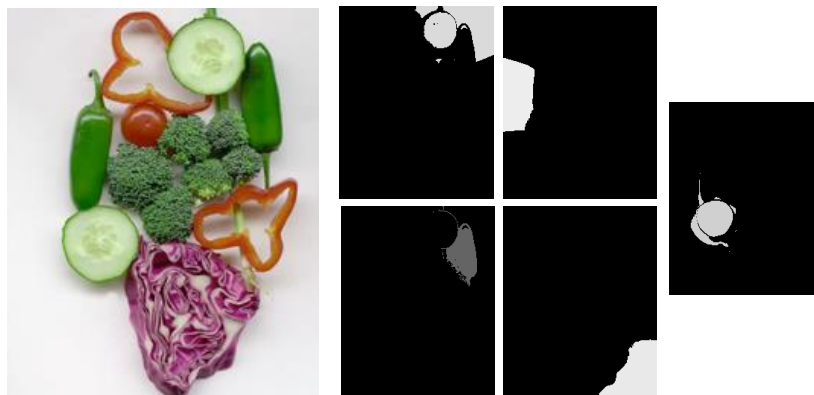
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Segmentation as clustering

- Clustering based on (r,g,b,x,y) values enforces more spatial coherence



Source: S. Lazebnik

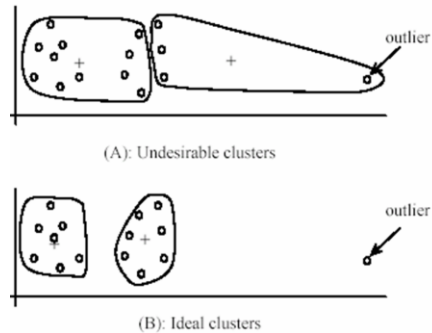
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K-Means for segmentation

- Pros
 - Very simple method
 - Converges to a local minimum of the error function
- Cons
 - Memory-intensive
 - Need to pick K
 - Sensitive to initialization
 - Sensitive to outliers
 - Only finds “spherical” clusters



Source: S. Lazebnik

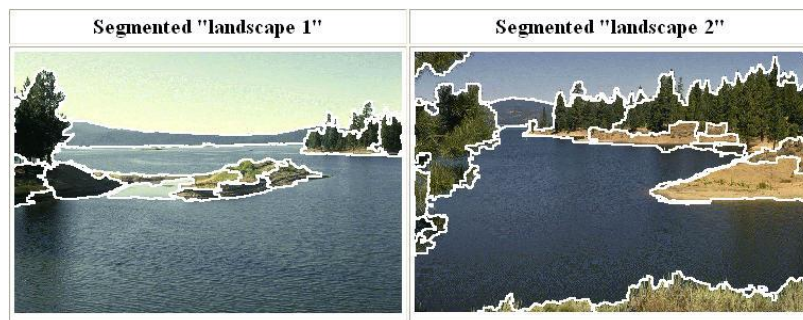
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Mean shift clustering and segmentation

- An advanced and versatile technique for clustering-based segmentation



<http://www.caip.rutgers.edu/~comanici/MSPAMI/msPamiResults.html>

D. Comaniciu and P. Meer, [Mean Shift: A Robust Approach toward Feature Space Analysis](#), PAMI 2002.

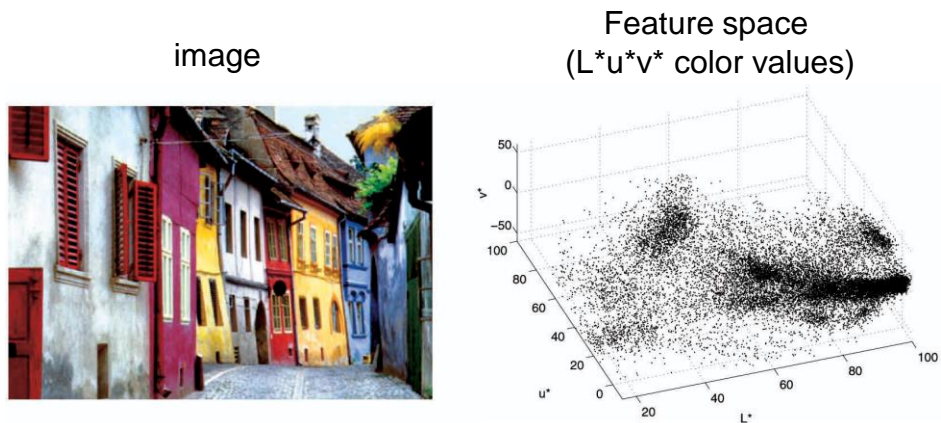
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Mean shift algorithm

- The mean shift algorithm seeks *modes* or local maxima of density in the feature space

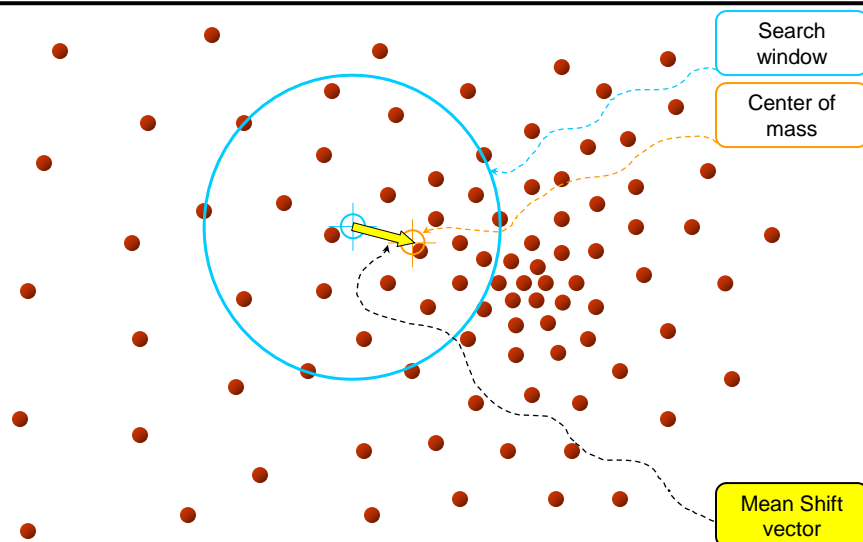


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Mean shift



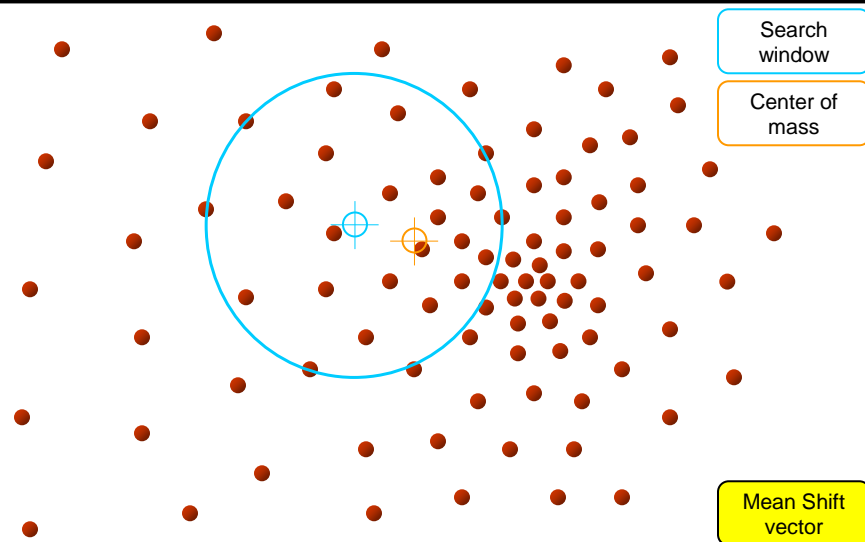
Source: Y. Ukrainitz & B. Sarel

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Mean shift



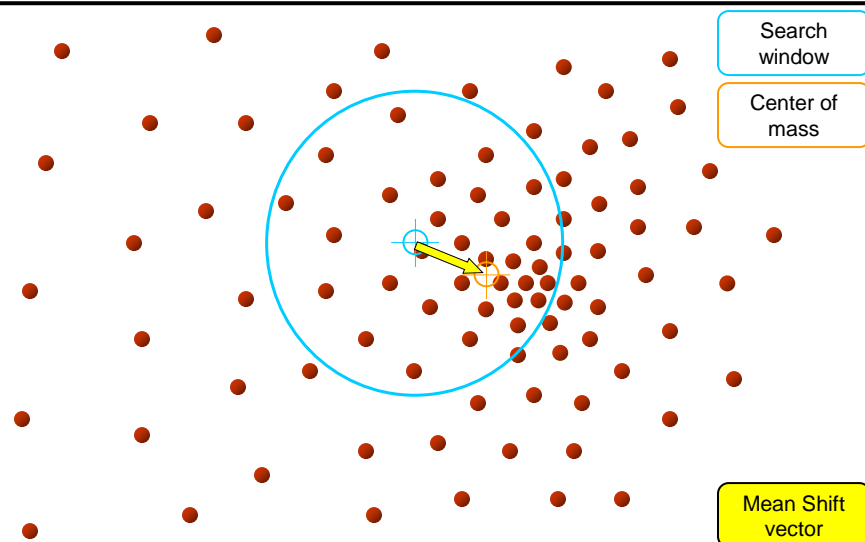
Source: Y. Ukrainitz & B. Sarel

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Mean shift



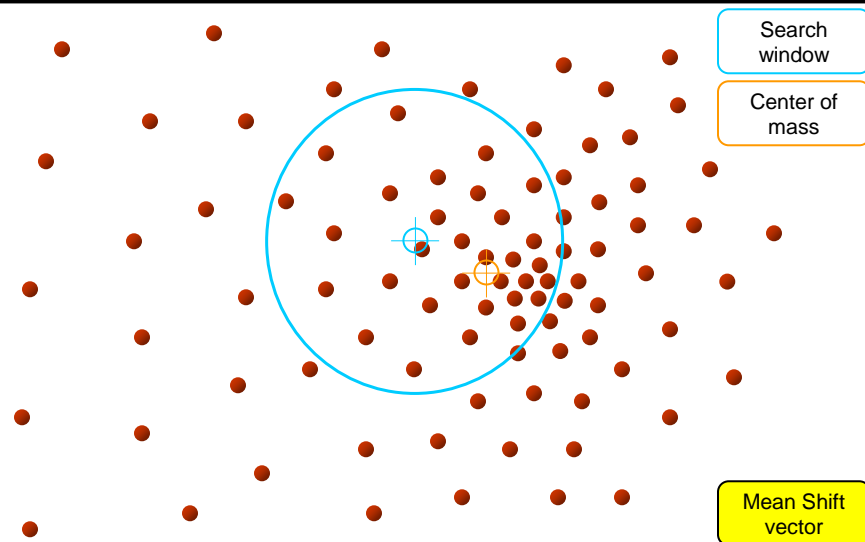
Source: Y. Ukrainitz & B. Sarel

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Mean shift



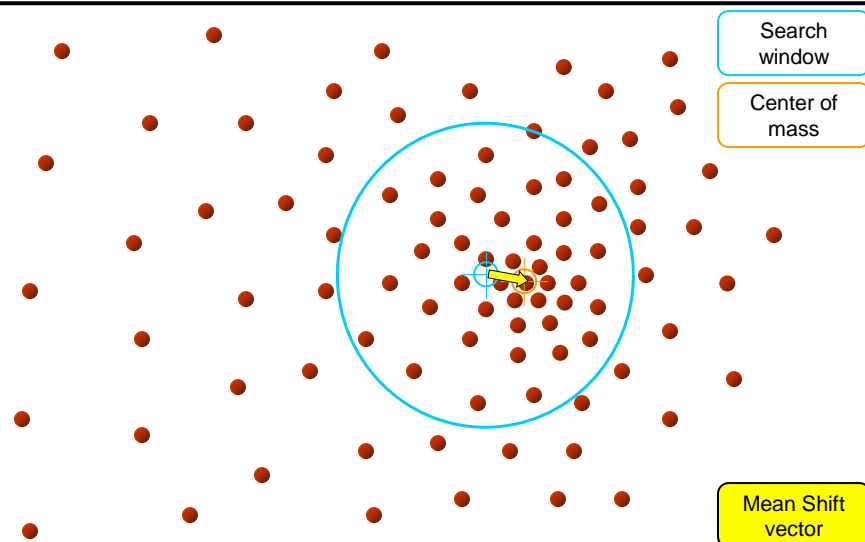
Source: Y. Ukrainitz & B. Sarel

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Mean shift



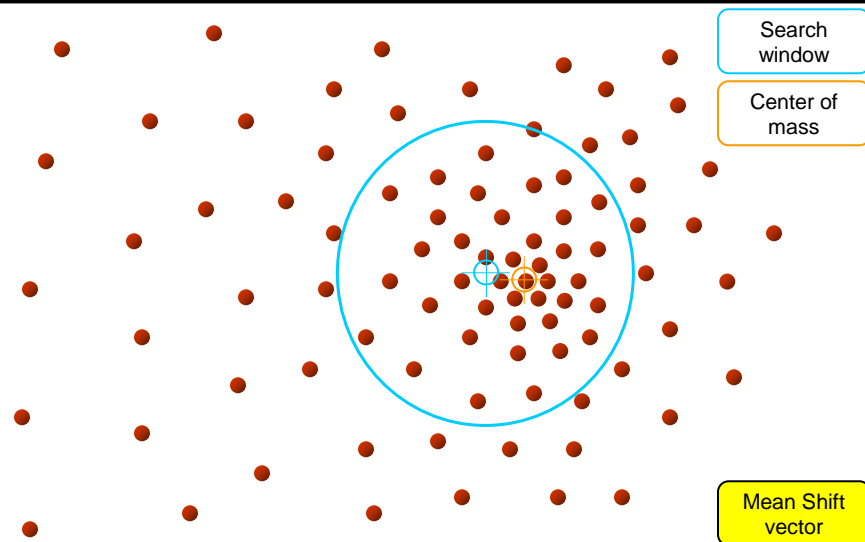
Source: Y. Ukrainitz & B. Sarel

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Mean shift



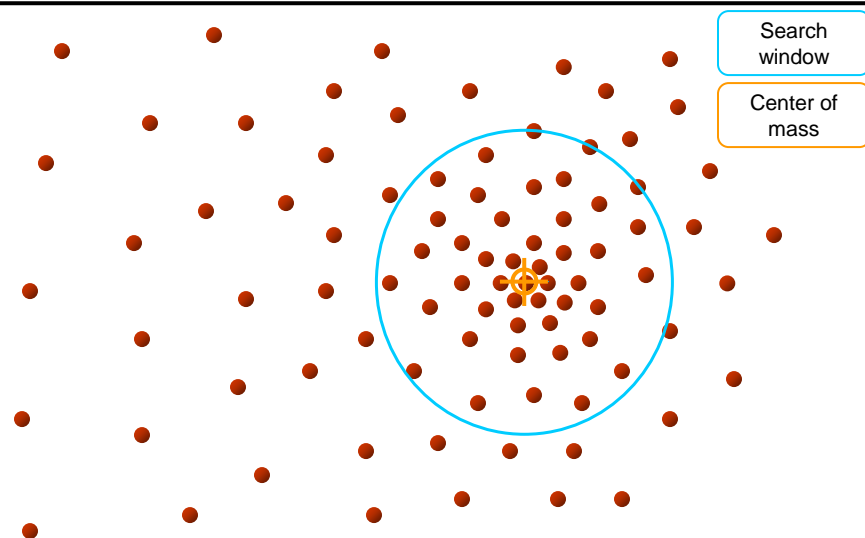
Source: Y. Ukrainitz & B. Sarel

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Mean shift



Source: Y. Ukrainitz & B. Sarel

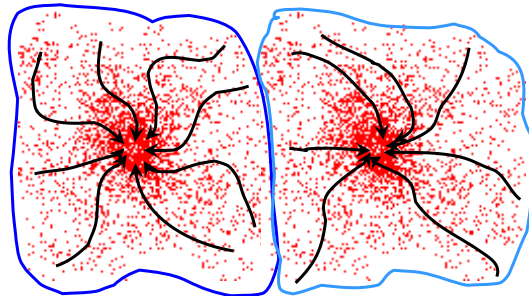
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Mean shift clustering

- Cluster: all data points in the attraction basin of a mode
- Attraction basin: the region for which all trajectories lead to the same mode



Source: Y. Ukrainitz & B. Sarel

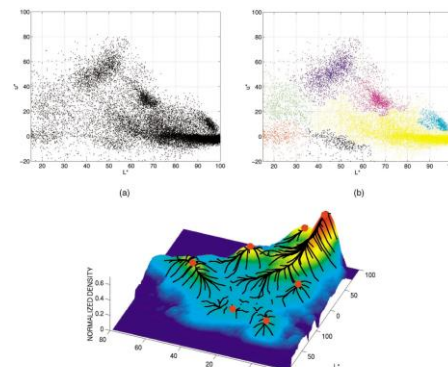
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Mean shift clustering/segmentation

- Find features (color, gradients, texture, etc)
- Initialize windows at individual feature points
- Perform mean shift for each window until convergence
- Merge windows that end up near the same “peak” or mode



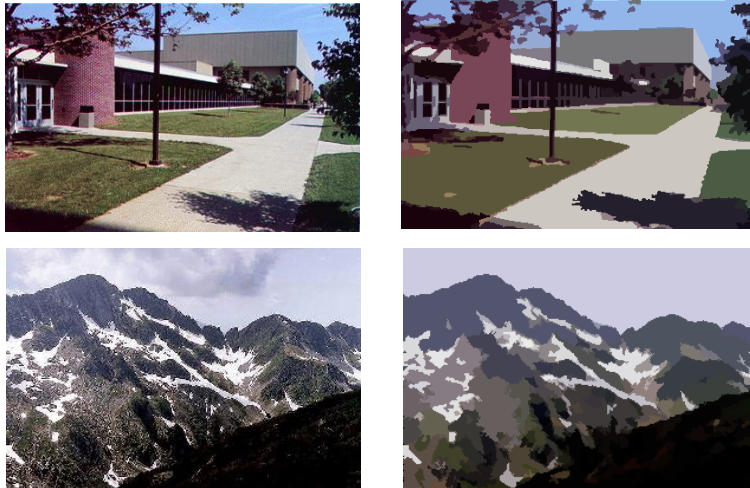
Source: S. Lazebnik

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Mean shift segmentation results



<http://www.caip.rutgers.edu/~comanici/MSPAMI/msPamiResults.html>

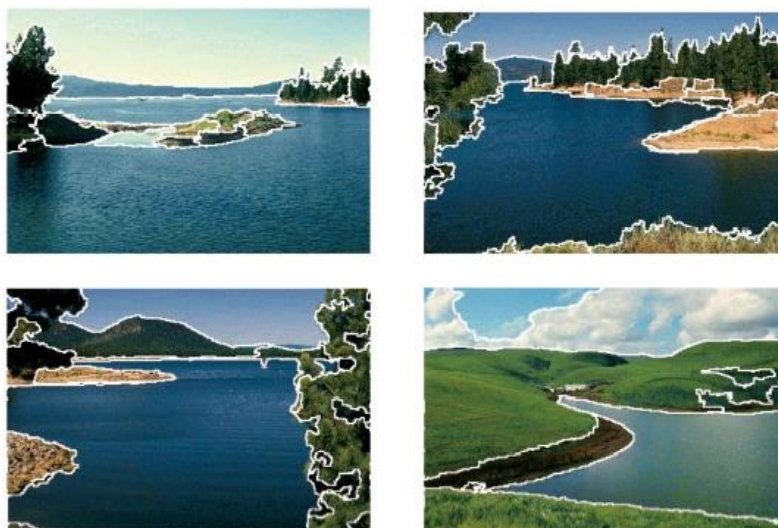
Source: S. Lazebnik

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More results



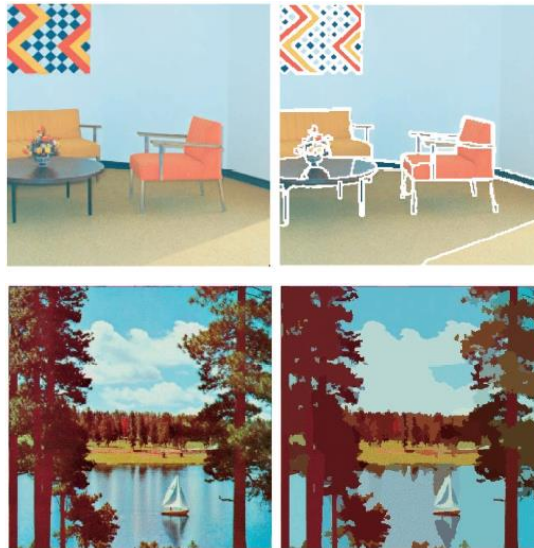
Source: S. Lazebnik

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More results



Source: S. Lazebnik

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Mean shift pros and cons

- Pros
 - Does not assume spherical clusters
 - Just a single parameter (window size)
 - Finds variable number of modes
 - Robust to outliers
- Cons
 - Output depends on window size
 - Computationally expensive
 - Does not scale well with dimension of feature space

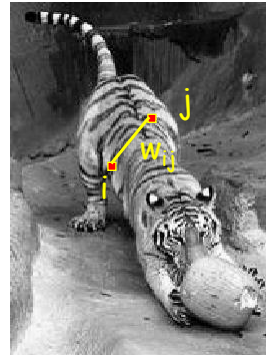
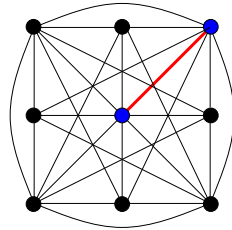
Source: S. Lazebnik

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Images as graphs



- Node for every pixel
- Edge between every pair of pixels (or every pair of “sufficiently close” pixels)
- Each edge is weighted by the *affinity* or similarity of the two nodes

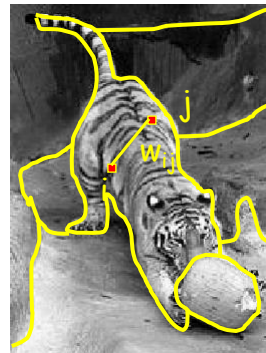
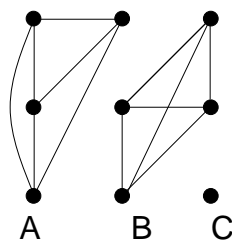
Source: S. Seitz

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Segmentation by graph partitioning



- Break Graph into Segments
 - Delete links that cross between segments
 - Easiest to break links that have low affinity
 - similar pixels should be in the same segments
 - dissimilar pixels should be in different segments

Source: S. Seitz

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Measuring affinity

- Suppose we represent each pixel by a feature vector \mathbf{x} , and define a distance function appropriate for this feature representation
- Then we can convert the distance between two feature vectors into an affinity with the help of a generalized Gaussian kernel:

$$\exp\left(-\frac{1}{2\sigma^2}\text{dist}(\mathbf{x}_i, \mathbf{x}_j)^2\right)$$

Source: S. Lazebnik

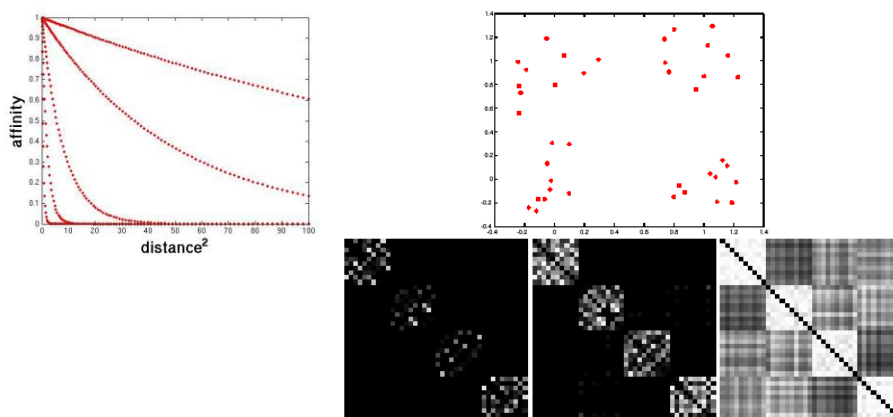
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Scale affects affinity

- Small σ : group only nearby points
- Large σ : group far-away points



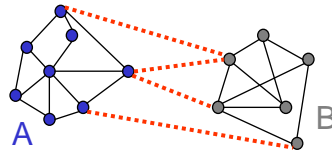
Source: S. Lazebnik

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Graph cut



- Set of edges whose removal makes a graph disconnected
- Cost of a cut: sum of weights of cut edges
- A graph cut gives us a segmentation
 - What is a “good” graph cut and how do we find one?

Source: S. Seitz

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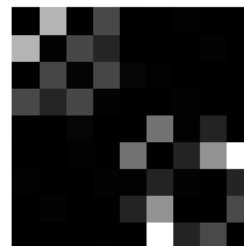
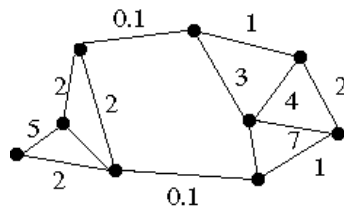
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Minimum cut

- We can do segmentation by finding the *minimum cut* in a graph
 - Efficient algorithms exist for doing this

Minimum cut example



Source: S. Lazebnik

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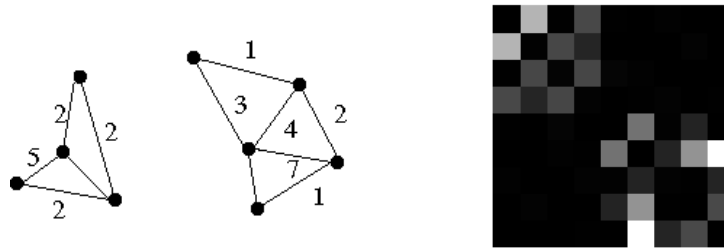
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Minimum cut

- We can do segmentation by finding the *minimum cut* in a graph
 - Efficient algorithms exist for doing this

Minimum cut example



Source: S. Lazebnik

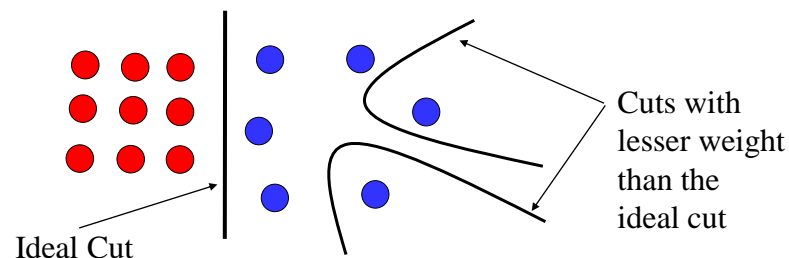
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Normalized cut

- Drawback: minimum cut tends to cut off very small, isolated components



Source: Khurram Hassan-Shafique

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Normalized cut

- Drawback: minimum cut tends to cut off very small, isolated components
- This can be fixed by normalizing the cut by the weight of all the edges incident to the segment
- The *normalized cut* cost is:

$$\frac{w(A, B)}{w(A, V)} + \frac{w(B, V)}{w(B, V)}$$

$w(A, B)$ = sum of weights of all edges between A and B

J. Shi and J. Malik. [Normalized cuts and image segmentation](#). PAMI 2000

Source: S. Lazebnik

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Normalized cut

- Let W be the adjacency matrix of the graph
- Let D be the diagonal matrix with diagonal entries $D(i, i) = \sum_j W(i, j)$
- Then the normalized cut cost can be written as

$$\frac{y^T (D - W) y}{y^T D y}$$

where y is an indicator vector whose value should be 1 in the i th position if the i th feature point belongs to A and a negative constant otherwise

J. Shi and J. Malik. [Normalized cuts and image segmentation](#). PAMI 2000

Source: S. Lazebnik

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Normalized cut

- Finding the exact minimum of the normalized cut cost is NP-complete, but if we *relax* y to take on arbitrary values, then we can minimize the relaxed cost by solving the *generalized eigenvalue problem* $(D - W)y = \lambda Dy$
- The solution y is given by the generalized eigenvector corresponding to the second smallest eigenvalue
- Intuitively, the i th entry of y can be viewed as a “soft” indication of the component membership of the i th feature
 - Can use 0 or median value of the entries as the splitting point (threshold), or find threshold that minimizes the Ncut cost

Source: S. Lazebnik

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Normalized cut algorithm

1. Represent the image as a weighted graph
 $G = (V, E)$, compute the weight of each edge, and summarize the information in D and W
2. Solve $(D - W)y = \lambda Dy$ for the eigenvector with the second smallest eigenvalue
3. Use the entries of the eigenvector to bipartition the graph

To find more than two clusters:

- Recursively bipartition the graph
- Run k-means clustering on values of several eigenvectors

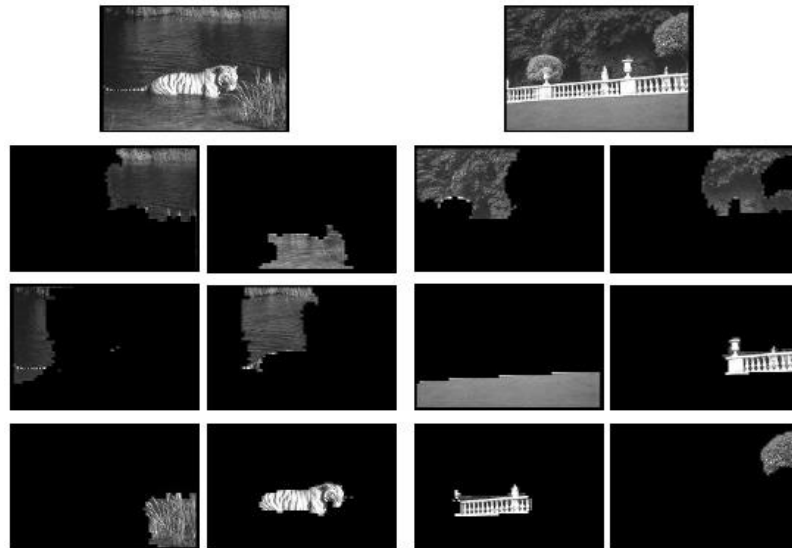
Source: S. Lazebnik

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Example result



Source: S. Lazebnik

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Challenge

- How to segment images that are a “mosaic of textures”?



Source: S. Lazebnik

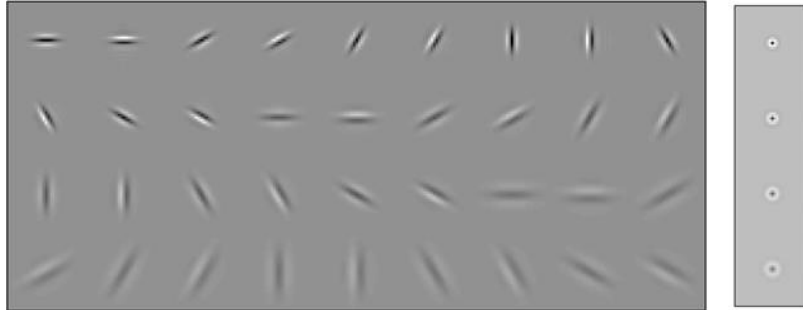
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Using texture features for segmentation

- Convolve image with a bank of filters



J. Malik, S. Belongie, T. Leung and J. Shi. "[Contour and Texture Analysis for Image Segmentation](#)". IJCV 43(1),7-27,2001.

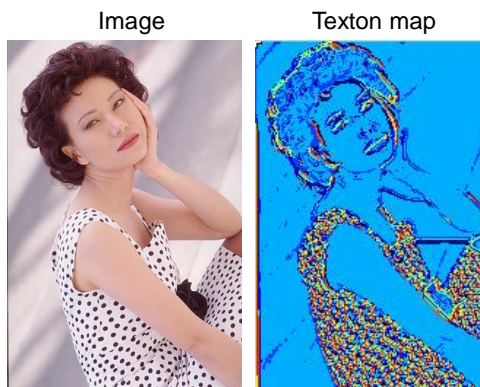
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Using texture features for segmentation

- Convolve image with a bank of filters
- Find *textons* by clustering vectors of filter bank outputs



J. Malik, S. Belongie, T. Leung and J. Shi. "[Contour and Texture Analysis for Image Segmentation](#)". IJCV 43(1),7-27,2001.

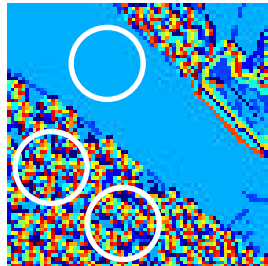
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Using texture features for segmentation

- Convolve image with a bank of filters
- Find *textons* by clustering vectors of filter bank outputs
- The final texture feature is a texton histogram computed over image windows at some “local scale”



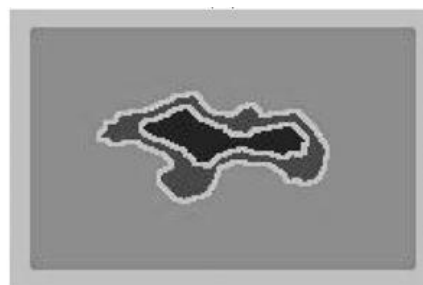
J. Malik, S. Belongie, T. Leung and J. Shi. "[Contour and Texture Analysis for Image Segmentation](#)". IJCV 43(1),7-27,2001.

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Pitfall of texture features



- Possible solution: check for “intervening contours” when computing connection weights

J. Malik, S. Belongie, T. Leung and J. Shi. "[Contour and Texture Analysis for Image Segmentation](#)". IJCV 43(1),7-27,2001.

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Example results



Source: S. Lazebnik

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Results: Berkeley Segmentation Engine



<http://www.cs.berkeley.edu/~fowlkes/BSE/>

Source: S. Lazebnik

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Normalized cuts: Pro and con

- Pros
 - Generic framework, can be used with many different features and affinity formulations
- Cons
 - High storage requirement and time complexity
 - Bias towards partitioning into equal segments

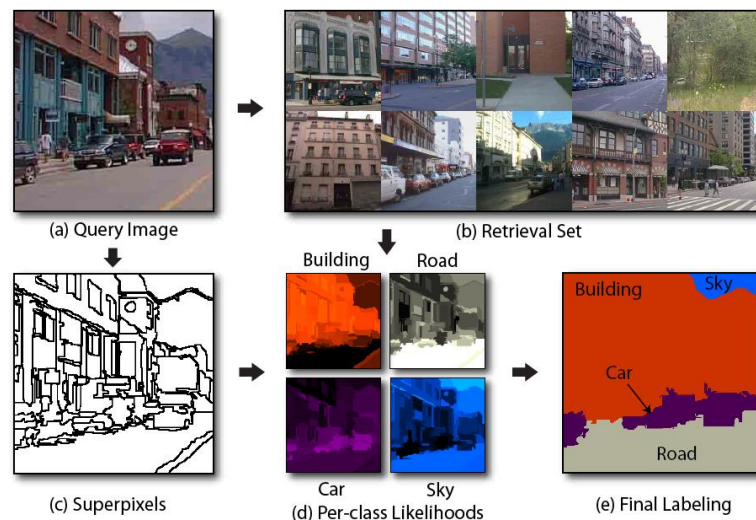
Source: S. Lazebnik

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Segments as primitives for recognition



J. Tighe and S. Lazebnik, ECCV 2010

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