

12 SEPTEMBER 2024

ASE 367K: FLIGHT DYNAMICS

TTH 09:30-11:00 CMA 2.306

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Topics for Today

- Topic(s):
 - Longitudinal Static Stability Example Problems
 - Lateral Static Stability Example Problems

flight level charle mode

FLCM Spet put agre male

Sertical speed

(descent runk)

Thrush fixed on find Se

O: Other speed and J.

LI

I hast S to member agailibrium.

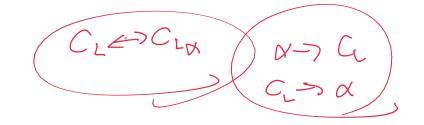
Maximum Climb octer = Max speck idle -> pisandown: max. decart falte.



LONGITUDINAL STABILITY EXAMPLES

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Question LONG 1

If the slope of the C_m versus C_L curve is -0.15 and the pitching moment at zero lift is equal to 0.08, determine the trim lift coefficient. If the center of gravity of the airplane is located at $X_{cg}/\bar{c}=0.3$, determine the stick fixed neutral point.

Question LONG 1 - Solution

Question LONG 1 - Solution

Stick-fixed neutral point? Static anyon

Cond = Cha (
$$\frac{x_{CQ}}{z_{C}} - \frac{x_{UP}}{z_{UP}}$$
) (as in equation $\frac{z_{C}}{z_{C}}$)

Thus $\frac{dCm}{dz} = \frac{dCm}{dz} =$

Question LONG 2

The C_m versus, α curve for a large jet transport can be seen in Figure P2.4. Use the figure and the following information to answer questions (a) to (c).

$$C_L = 0.03 + 0.08\alpha \text{ (deg.)}$$

 $-15^{\circ} \le \delta_e \le 20^{\circ}$

- (a) Estimate the stick fixed neutral point.
- (b) Estimate the control power $C_{m_{\delta_{\nu}}}$.
- (c) Find the forward center of gravity limit. Hint:

$$\frac{\mathrm{d}C_{m_{\mathrm{cg}}}}{\mathrm{d}C_{I}} = \frac{X_{\mathrm{cg}}}{\overline{c}} - \frac{X_{\mathrm{NF}}}{\overline{c}}$$

Stable town

Cm < 15°

Question LONG 2 (cont'd)

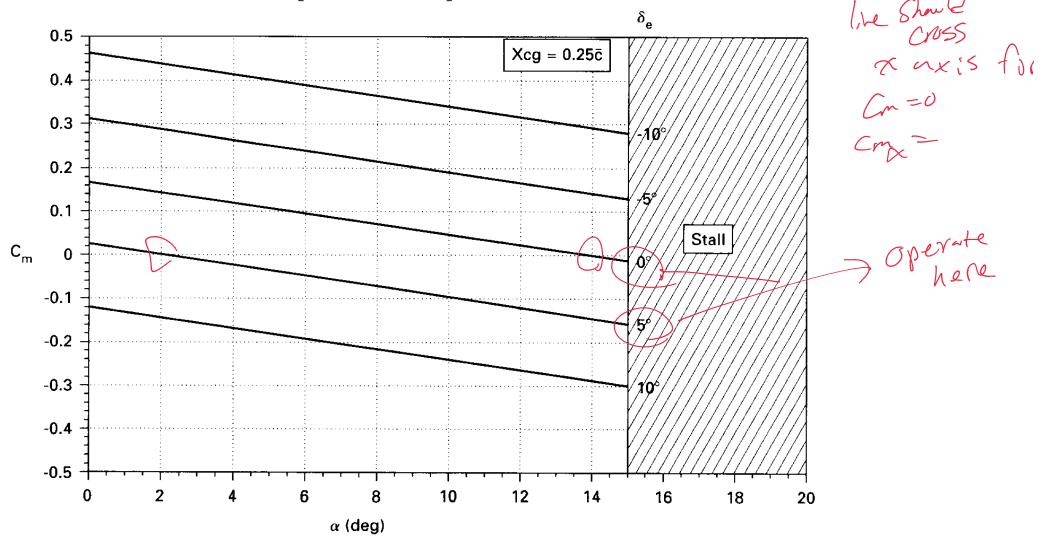


FIGURE P2.4

Question LONG 2 - Solution

Cma = dCex · (Stutic meng m)

From Figure P. 2.4
$$\frac{dCm}{da} = \frac{acm}{ba} = \frac{acm}{ba - oo} = -0.013 / deg$$

$$\frac{dCmcg}{dc_L} = \frac{dCmcg}{da} = \frac{dCm}{dc_L} \quad and \quad since \quad \frac{dc_L}{da} = 0.08 / deg$$

=> effection hiss of elevator on moment **Question LONG 2 - Solution**

(b) C_{mge} ? $C_{mge} = \frac{\partial C_{m}}{\partial G_{e}} = \frac{\Delta C_{m}}{\Delta G_{e}}$ From figure P2.4 at d=0 AGm = 0.17-0.46

AGe 00- (-10°)

run and of elevator seffection (c) Forward c-a limit? the forward co limit is determined by the requirement to trim the airplane at a high of (landing).

Here the Chmox occurs when I is max i.e. d=150

Question LONG 2 - Solution

Fai d=15° Crmay = 0.03+0.08x15° = 1.23 regetive Te Comve Chor Com is d becomes steeper-Form the control needs to be applied.

Question LONG 2 - Solution

$$\Delta Concentral = Conce demax = -0.029 (leg × (-150))$$

$$\Delta Concentral = 0.435$$

$$\Delta Concentral = Concentral - Con$$

Question LONG 3

An airplane has the following pitching moment characteristics at the center of gravity

position:

where

$$x_{\rm cg}/\overline{c} = 0.3.$$

$$C_{m_{\rm cg}} = C_{m_0} + \frac{\mathrm{d}C_{m_{\rm cg}}}{\mathrm{d}C_L}C_L + C_{m_{\delta_e}}\delta_e$$

$$C_{m_0} = 0.05 \qquad \frac{\mathrm{d}C_{m_{\rm cg}}}{\mathrm{d}C_L} = -0.1 \qquad C_{m_{\delta_e}} = -0.01/\mathrm{deg}$$

$$\frac{\mathrm{d}C_{m_{\rm cg}}}{\mathrm{d}C} = \left[\frac{X_{\rm cg}}{\overline{c}}\right] - \left[\frac{X_{\rm NP}}{\overline{c}}\right]$$

If the airplane is loaded so that the center of gravity position moves to $x_{cg}/\overline{c} = 0.10$, can the airplane be trimmed during landing, $C_L = 1.0$? Assume that C_{m_0} and $C_{m_{\delta_e}}$ are unaffected by the center of gravity travel and that $\delta_{e_{max}} = \pm 20^{\circ}$.

Question LONG 3 - Solution

· Find the bootin of the neutral point:

o For the new cod possition, what is the new value of day ?

$$\frac{10m0}{dq} = \frac{x_0 *}{c} - \frac{x_1}{c} = 0.1 - 0.4 = (-0.3)$$

Question LONG 3 - Solution

· Can the airplane toe trimmed? For Q=1.0

> if the airplane was trimmed, would the & required be within the At trim Cmg = 0 = 0.05 + (-0.3) 1.0 + (-0.01) Se Se = -0.05+0.3 = -25° → Se ≠ [-Semax, Semax] = [-20°, 20°] therefore the airplane comnot be trimmed at this c.g and lift coefficient



LATERAL STABILITY EXAMPLES

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Question LAT 1

For the twin engine airplane shown in Figure P2.16, determine the rudder size to control the airplane if one engine needs to be shut down. Use the flight information shown in the figure and

Wing:
$$S = 980 \text{ ft}^2$$
 $b = 93 \text{ ft}$

Vertical tail:
$$S_v = 330 \text{ ft}^2$$
 $AR_v = 4.3$ $l_v = 37 \text{ ft}$ $\eta_v = 1.0$

Rudder:
$$\delta_r = \pm 15^{\circ}$$

Propulsion:
$$T = 14,000 \text{ lb each}$$
 $y_T = 16 \text{ ft}$

Flight condition:
$$V = 250 \text{ ft/s}$$
 $\rho = 0.002378 \text{ slug/ft}^3$

Question LAT 1 (cont'd)

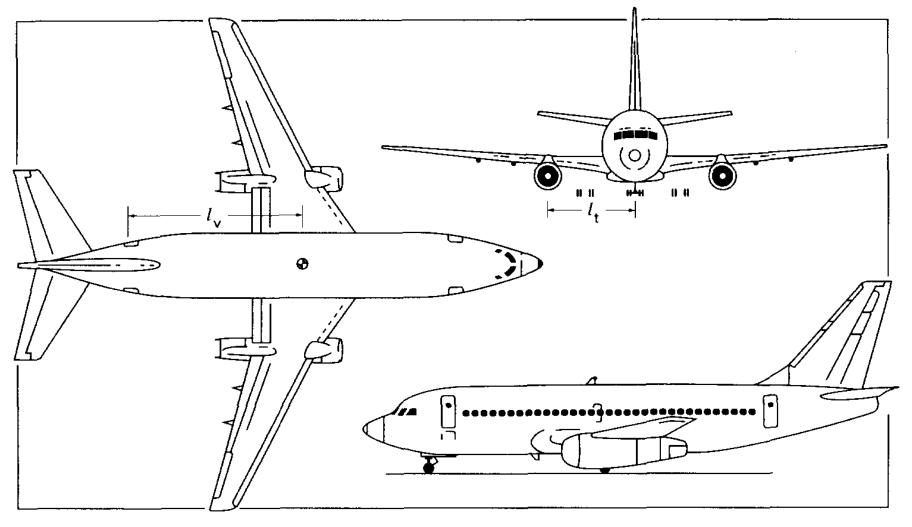


FIGURE P2.16

Question LAT 1 - Solution

went to control the extratore with one engine shut down is the total youing moment should be zero:

Naero + Wengine = 0

From rudda)

Nongine = $-Ty_T$ \Rightarrow None = $-Very re = Ty_T = 14,600 \times 16$ None = 224,000 16. ft

= By definition Cn = Namo = 724000 = 20002378 x 2502 x 980 x 93

Cn = 0.0331

Question LAT 1 - Solution

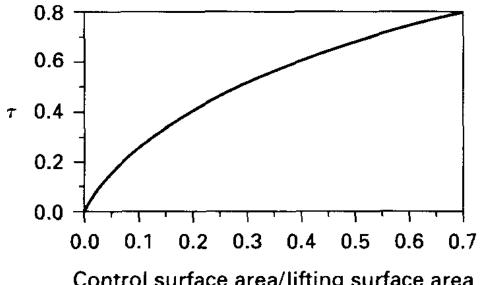
Question LAT 1 - Solution

Flap effectiveness parameter versus control surface area

$$8=0.23 = 5 = 50.08 = 380 \times 0.08$$

$$S_r = 50.08 = 380 \times 0.08$$

$$S_r = 26.4 9 = 380 \times 0.08$$



· Kems

Control surface area/lifting surface area

Question LAT 2

Develop an expression for the wing dihedral effect $C_{l_{\beta}}$ for a wing planform that uses dihedral only for the outboard portion of the wing (see Figure P2.18). Clearly state all of your assumptions.

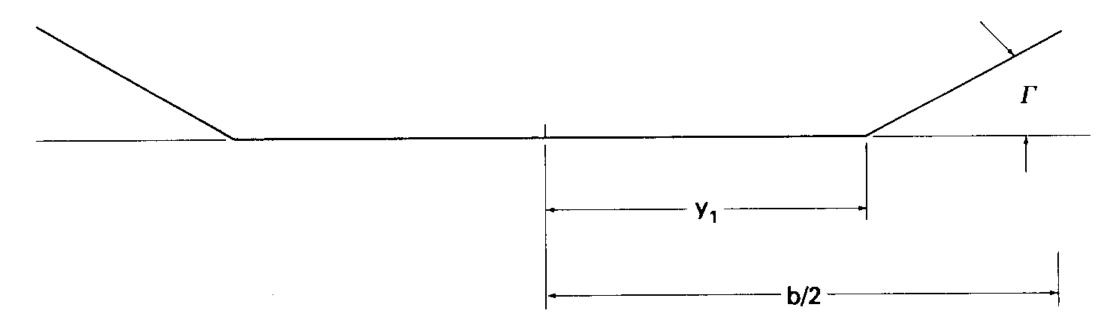


FIGURE P2.18

Question LAT 2 - Solution

Question LAT 2 - Solution

the non-dimensional coefficient is:

$$dCe = \frac{dL}{dSb} = -\frac{C_{Ld}}{dSb} \frac{\Delta d}{dS} \frac{dS}{dS} \frac{$$

