# Problem 1 Warm-Up (3%)

Read an integer k and compute its factorial k!. The answer can be very large so output its value modulo  $10^9 + 7$ .

### Input

The first line contains an integer n,  $(1 \le n \le 100)$ , the number of test cases. Then n lines follow, each of which contains an integer k,  $(1 \le k \le 10^5)$ , to be tested.

### Output

For each input integer k output  $k! \mod 10^9 + 7$ .

## Example

Sample Input
4
3
6
30
100

Sample Output	
6	
720	
109361473	
437918130	

Due: March 1, 2019

### Note

In this example, we have

• 
$$3! \mod 10^9 + 7 = 1 \times 2 \times 3 \mod 10^9 + 7$$
  
=  $6$ 

• 6! 
$$\mod 10^9 + 7 = 1 \times 2 \times ... \times 6 \mod 10^9 + 7$$
  
= 720

• Note that, since

$$i \times j \times k \mod p = (i \times j \mod p) \times k \mod p,$$

you can take modulo along your computation to prevent overflow in this assignment.

# Problem 2 Gaussian Elimination (5%)

Deciding the dimension of a vector space is a fundamental problem in linear algebra. That is, to determine the number of bases (linearly independent vectors) from a given set of vectors.

Due: March 1, 2019

This can be done using Gaussian Elimination (高斯消去法).

To simplify the problem, we consider only  $\{0,1\}$ -vectors, and we take the value modulo 2 after every computation, i.e., 1+1 becomes 0, since  $1+1 \equiv 0 \mod 2$ . For example,

$$(1,0,1) + (1,0,0) \Rightarrow (0,0,1)$$
 and  $(0,0,1) + (0,0,1) \Rightarrow (0,0,0)$ .

Given a set of  $\{0,1\}$  vectors, please determine the dimension of the linear subspace it spans.

### Input

The first line contains two integers n and m,  $(1 \le n \le 20, 1 \le m \le 1000)$ , the length of the coordinates and the number of input vectors.

The next m lines contain n integers, i.e., at the  $i^th$  line are the coordinates  $a_{i,1}, a_{i,2}, \ldots, a_{i,n}, a_{i,j} \in \{0,1\}$ , of the  $i^th$  input vector.

### Output

Print the dimension of the subspace. (the number of linearly independent vectors)

### Example

$\mathbf{S}$	an	ıp.	le Input	
4	3			
1	0	0	1	
0	1	0	1	
1	1	0	0	

Sample Output

2

### Note

In this example, we can eliminate ("cancel out") the third vector (1, 1, 0, 0) using the first two vectors, and at most two vectors out of three can be linearly independent.