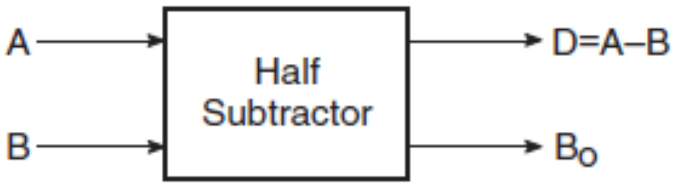
Half-Subtractor

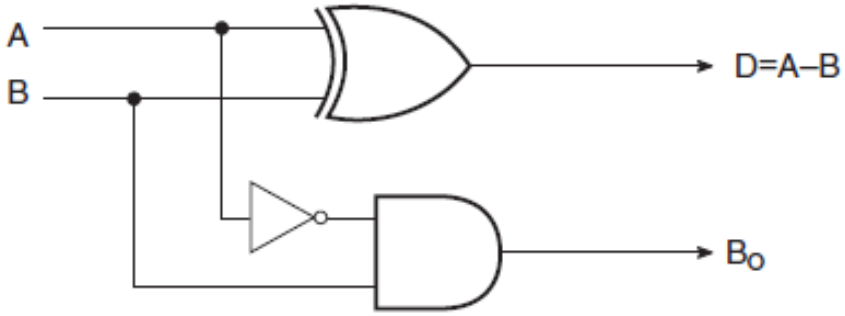
- A half-subtractor is a combinational circuit that can be used to subtract one binary digit from another to produce a **DIFFERENCE** output and a **BORROW** output



A	B	D	B_O
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

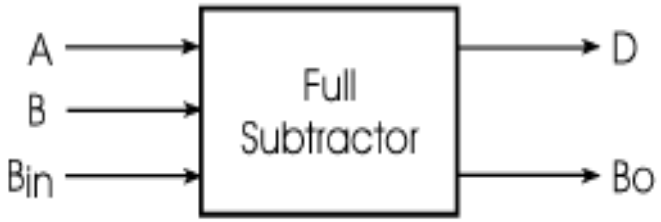
$$D = \overline{A}.B + A.\overline{B}$$

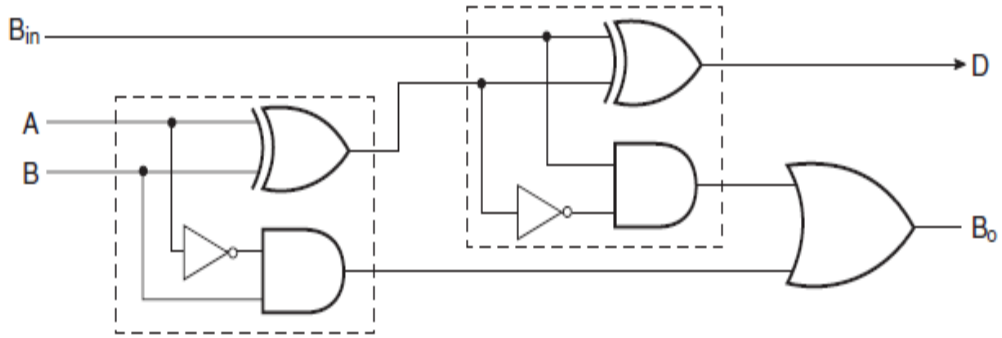
$$B_0 = \overline{A}.B$$

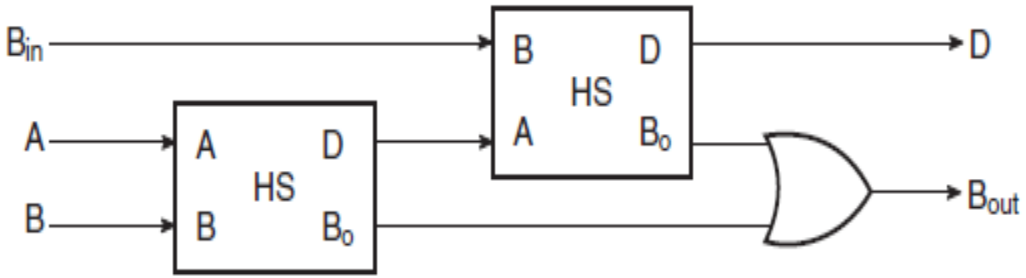


Full Subtractor

- A *full subtractor performs subtraction operation on two bits, a minuend and a subtrahend*







Minuend (A)	Subtrahend (B)	Borrow In (B_{in})	Difference (D)	Borrow Out (B_o)
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

- The Boolean expressions for the two output variables are given by the equations

$$D = \overline{A}.\overline{B}.B_{in} + \overline{A}.B.\overline{B}_{in} + A.\overline{B}.\overline{B}_{in} + A.B.B_{in}$$

$$B_o = \overline{A}.\overline{B}.B_{in} + \overline{A}.B.\overline{B}_{in} + \overline{A}.B.B_{in} + A.B.B_{in}$$

Minuend (A)	Subtrahend (B)	Borrow In (B_{in})	Difference (D)	Borrow Out (B_O)
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1