## Housing Price Analysis using Random Forest

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We see that linear regression model works well on predicting house price, the final model's  $R^2$  we get is approximately 0.874, which is very good in practice.

Next we try to move beyond linearity, one of the most important family of models in machine learning is tree models, includeing decision trees, bagging and random forest etc.

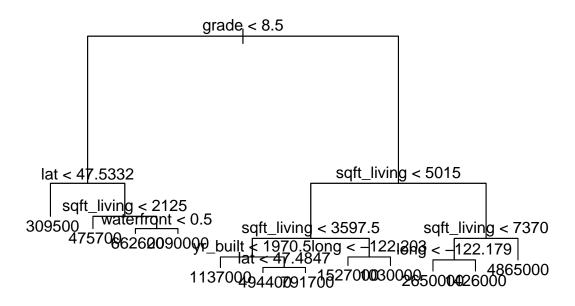
The predictors we used in the linear regression model includes:

sqftliving, bedrooms, bathrooms, grade, floors, waterfront, yrbuilt, lat, long, view, zipcode, condition.

#### 1. Decision Tree

First we start from single decision tree,

```
library(tree)
tree1 = tree(price ~. -date-zipcode, data = training)
summary(tree1)
##
## Regression tree:
## tree(formula = price ~ . - date - zipcode, data = training)
## Variables actually used in tree construction:
## [1] "grade"
                     "lat"
                                   "sqft_living" "waterfront" "yr_built"
## [6] "long"
## Number of terminal nodes: 12
## Residual mean deviance: 4.304e+10 = 3.046e+14 / 7076
## Distribution of residuals:
##
      Min. 1st Qu.
                                  Mean 3rd Qu.
                       Median
                                                    Max.
## -4065000
             -99520
                       -25680
                                     0
                                          68920 2195000
# Visualize the tree
plot(tree1)
text(tree1)
```



# # Text description of tree tree1

```
## node), split, n, deviance, yval
##
         * denotes terminal node
##
##
   1) root 7088 9.947e+14 537000
##
      2) grade < 8.5 5786 2.312e+14 437800
##
        4) lat < 47.5332 2442 3.164e+13 309500 *
##
        5) lat > 47.5332 3344 1.300e+14 531500
##
         10) sqft_living < 2125 2384 5.235e+13 475700 *
##
         11) sqft_living > 2125 960 5.185e+13 670000
##
           22) waterfront < 0.5 955 4.025e+13 662600 *
##
           23) waterfront > 0.5 5 1.466e+12 2090000 *
##
      3) grade > 8.5 1302 4.537e+14 977700
##
        6) sqft_living < 5015 1233 2.128e+14 907100
##
         12) sqft_living < 3597.5 920 9.172e+13 803100
##
           24) yr_built < 1970.5 163 2.071e+13 1137000 *
##
           25) yr_built > 1970.5 757 4.892e+13 731200
##
             50) lat < 47.4847 154 2.820e+12 494400 *
##
             51) lat > 47.4847 603 3.526e+13 791700 *
##
         13) sqft_living > 3597.5 313 8.197e+13 1213000
##
           26) long < -122.203 115 3.954e+13 1527000 *
##
           27) long > -122.203 198 2.447e+13 1030000 *
##
        7) sqft_living > 5015 69 1.248e+14 2239000
##
         14) sqft_living < 7370 63 5.722e+13 1989000
##
           28) long < -122.179 29 2.412e+13 2650000 *
```

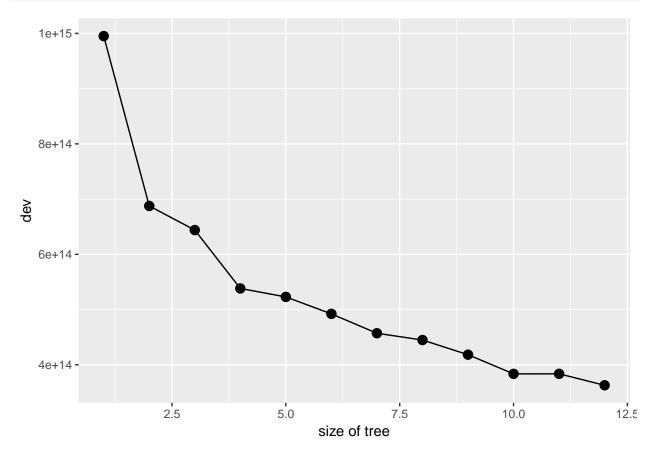
```
## 29) long > -122.179 34 9.649e+12 1426000 *
## 15) sqft_living > 7370 6 2.232e+13 4865000 *
```

Then we use cross validation to see whether pruning the tree will improve performance,

```
cv_tree1 = cv.tree(tree1)
library(ggplot2)
```

## Warning: package 'ggplot2' was built under R version 3.3.2

```
ggplot() +
  geom_line(mapping = aes(x = cv_tree1$size, y = cv_tree1$dev)) +
  geom_point(mapping = aes(x = cv_tree1$size, y = cv_tree1$dev), size = 3) +
  labs(x = "size of tree", y = "dev")
```



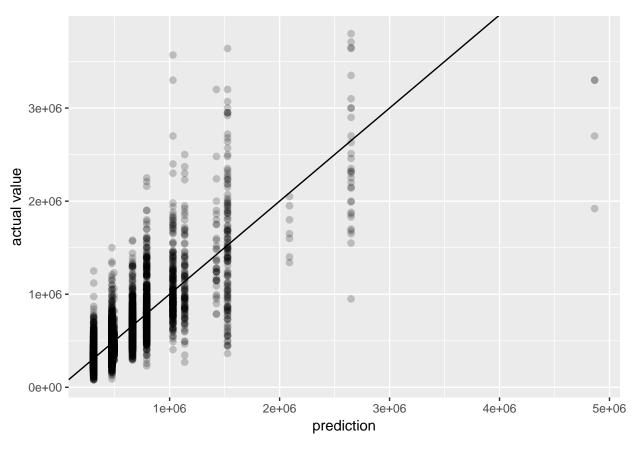
We can see that the dev of tree will get minimum when the tree size is 12. Therefore, the performance of tree doesn't improve much if we prune the tree.

Next we calculate the test error of this tree,

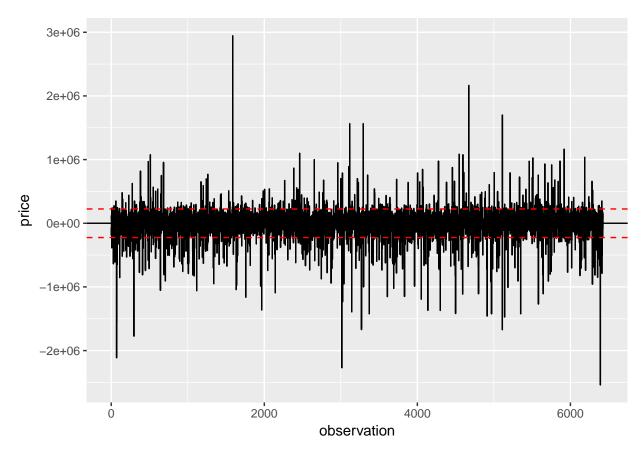
```
predOfTree1 = predict(tree1, newdata = testing)
rmse1 = sqrt(mean((predOfTree1 - testing*price)^2))
rmse1
```

```
## [1] 224316.3
```

```
ggplot() +
  geom_point(mapping = aes(x = predOfTree1, y = testing$price), alpha = .2, size = 2) +
  geom_abline(slope = 1, intercept = 0) +
  labs(x = "prediction", y = "actual value")
```



```
ggplot() +
  geom_line(mapping = aes(x = 1:length(predOfTree1), y = predOfTree1 - testing$price)) +
  geom_abline(slope = 0, intercept = 0) +
  geom_abline(slope = 0, intercept = rmse1, linetype = "dashed", color = "red") +
  geom_abline(slope = 0, intercept = -rmse1, linetype = "dashed", color = "red") +
  labs(x = "observation", y = "price")
```

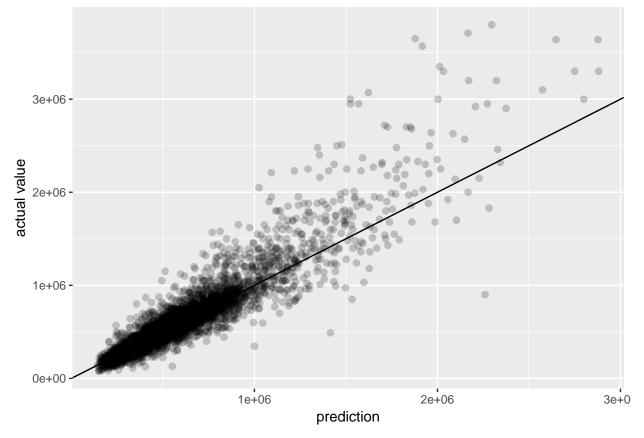


From this plot, we can see that many predictions are far away from their actual value. The error is still high. We need to seek models to predict more precisely.

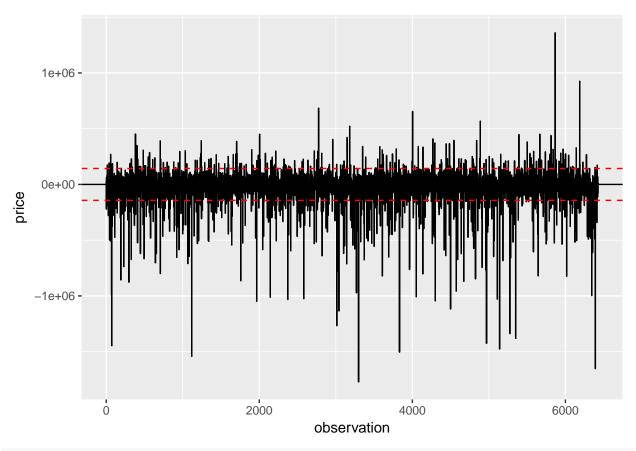
#### 2. Random Forest

We use ensemble methods to improve the performance of the tree model. One of the popular methods is random forest.

```
##
               Type of random forest: regression
                    Number of trees: 500
##
## No. of variables tried at each split: 5
##
##
           Mean of squared residuals: 0.03586097
                   % Var explained: 87.29
predOfrandForest = predict(randForest, newdata = testing)
rmse2 = sqrt(mean((testing$price - exp(predOfrandForest))^2))
rmse2
## [1] 142801.7
ggplot() +
 geom_point(mapping = aes(x = exp(predOfrandForest), y = testing$price), alpha = .2, size = 2) +
 geom_abline(slope = 1, intercept = 0) +
 labs(x = "prediction", y = "actual value")
```



```
ggplot() +
  geom_line(mapping = aes(x = 1:length(predOfrandForest), y = exp(predOfrandForest) - testing$price)) +
  geom_abline(slope = 0, intercept = 0) +
  geom_abline(slope = 0, intercept = rmse2, linetype = "dashed", color = "red") +
  geom_abline(slope = 0, intercept = -rmse2, linetype = "dashed", color = "red") +
  labs(x = "observation", y = "price")
```



## importance(randForest)

varImpPlot(randForest)

##		${\tt \%IncMSE}$	${\tt IncNodePurity}$
##	bedrooms	16.98279	17.682193
##	bathrooms	22.14704	71.858680
##	sqft_living	43.12953	325.628456
##	sqft_lot	48.61245	46.454551
##	floors	17.32741	14.573919
##	waterfront	25.23851	11.689565
##	view	34.66992	35.028867
##	condition	28.71623	14.200844
##	grade	33.68949	332.797907
##	sqft_above	26.46916	125.406629
##	${\tt sqft\_basement}$	22.85204	26.940917
##	<pre>yr_built</pre>	47.72134	62.636548
##	<pre>yr_renovated</pre>	11.61159	3.968069
##	lat	182.13863	579.685747
##	long	77.01030	76.154332
##	sqft_living15	43.72745	171.641281
##	sqft_lot15	43.87485	53.835669

## randForest

