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KAKATIYA INSTITUTE OF TECHNOLOGY & SCIENCE, WARANGAL

(An Autonomous Institute under Kakatiya University, Warangal)

FACULTY OF ENGINEERING AND TECHNOLOGY

B.Tech. (IT) V Semester Examination, January 2021

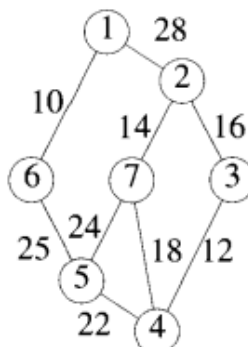
U18IT503: Design and Analysis of Algorithms

Time: 3 Hours]

[Max. Marks : 60

Note: Answer **all** the questions.

- | | | CDLL | CO's |
|----|---|--------|------|
| 1. | a. What is an Algorithm? What are the various criteria used to improve the characteristics of the algorithm? | [1] R | CO1 |
| | b. What are space and time complexities? | [1] R | CO1 |
| | c. What is the difference between a set and a disjoint set? | [1] U | CO1 |
| | d. Write the control abstraction of the greedy approach. | [1] R | CO2 |
| | e. What is meant by memoization? | [1] R | CO2 |
| | f. What is the difference between optimal solution and feasible solution? | [1] U | CO2 |
| | g. What is an optimal BST? | [1] R | CO3 |
| | h. What is a TSP? How dynamic programming is useful for solving it? | [1] U | CO3 |
| | i. Define sum of subsets problem. | [1] U | CO3 |
| | j. What are heuristics? Do they always guarantee solutions? | [1] R | CO4 |
| | k. Distinguish the branch-and-bound technique from the backtracking technique? | [1] U | CO4 |
| | l. Define NP-hard and NP-easy. | [1] U | CO4 |
| 2. | a. Write the following algorithms: | [6] R | CO1 |
| | i. Union algorithm with weighting rule | | |
| | ii. Find algorithm with collapsing rule | | |
| | b. Consider the behavior of WeightedUnion on the following sequence of unions starting from the initial configuration
$p[i] = -\text{count}[i] = -1, 1 \leq i \leq 8 = n$:
Union(1,2), Union(3,4), Union(5,6), Union(7,8), Union(1,3), union(5,7),
Union(1,5) | [6] U | CO1 |
| | (OR) | | |
| | c. Write the Merge sort algorithm and Merge algorithm for sorting n elements. | [6] R | CO1 |
| | d. Find an optimal solution to the knapsack instance $n=7, m=15, (p_1, \dots, p_7) = (10, 5, 15, 7, 6, 18, 3)$ and $(w_1, \dots, w_7) = (2, 3, 5, 7, 1, 4, 1)$. | [6] U | CO1 |
| 3. | a. Explain Strassen's matrix multiplication. | [6] U | CO2 |
| | b. Consider the array of ten elements $a[1:10] = (310, 285, 179, 652, 351, 423, 861, 254, 450, 520)$, sort these in ascending order using merge sort technique. | [6] Ap | CO2 |
| | (OR) | | |
| | c. Write the Prim's algorithm and explain the steps for finding MST for the below graph: | [6] U | CO2 |

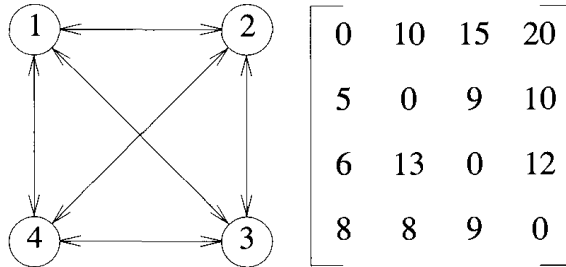


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|----|---|--------|-----|
| d. | Find an optimal binary merge pattern for 10 files whose lengths are 28,32,12,5,84,53,91,35,3,11 | [6] Ap | CO2 |
|----|---|--------|-----|

4. a. Use function OBST to compute $w(i,j)$, $r(i,j)$ and $c(i,j)$, $0 \leq i \leq j \leq 4$, for the identifier set $(a_1, a_2, a_3, a_4) = (\text{do}, \text{if}, \text{int}, \text{while})$ with $p(1:4) = (3, 3, 1, 1)$ and $q(0:4) = (2, 3, 1, 1, 1)$. Using the $r(i,j)$'s, construct the optimal binary search tree. [6] Ap CO3
- b. Generate the sets S^i , $0 \leq i \leq 3$, when $(w_1, w_2, w_3) = (2, 3, 4)$ and $(p_1, p_2, p_3) = (1, 2, 5)$. [6] An CO3

(OR)

- c. Design a three stage system with device type D1, D2, D3. The costs are ₹30, ₹15 and ₹20 respectively. The costs of the system are to be more than ₹105. The reliability of each device to be 0.9, 0.8 and 0.5 respectively. [6] Ap CO3
- d. Consider the directed graph with the edge lengths given by the adjacency matrix. Find the optimal tour of the graph. [6] An CO3



5. a. Solve the following instance of the TSP using LCBB. [6] Ap CO4

∞	20	30	10	11
15	∞	16	4	2
3	5	∞	2	4
19	6	18	∞	3
16	4	7	16	∞

- b. Draw the portion of the state space tree generated by LCBB for knapsack instance $n = 4$, $m = 15$, $(p_1, p_2, p_3, p_4) = (10, 10, 12, 18)$ and $(w_1, w_2, w_3, w_4) = (2, 4, 6, 9)$. [6] An CO4

(OR)

- c. Generate FIFO branch and bound solution for the given knapsack problem, $m=15$, $n=4$, $(p_1, p_2, p_3, p_4) = (10, 10, 12, 18)$ and $(w_1, w_2, w_3, w_4) = (2, 4, 6, 9)$. [6] Ap CO4
- d. Draw the portion of the state space tree generated by LCBB for knapsack instance $n = 5$, $m = 15$, $(p_1, p_2, p_3, p_4, p_5) = (10, 10, 12, 18, 20)$ and $(w_1, w_2, w_3, w_4, w_5) = (2, 4, 6, 9, 10)$. [6] An CO4

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