Evaluation of the Virtual Crystal Approximation for Predicting Alloy Vibrational Mode Properties and Thermal Conductivity

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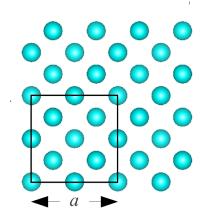
http://ntpl.me.cmu.edu/

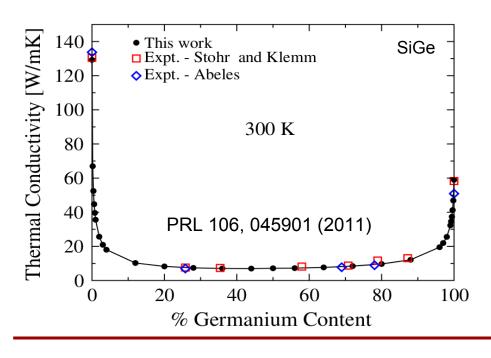
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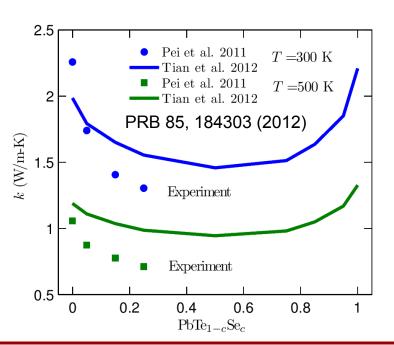


Motivation: experimental accuracy

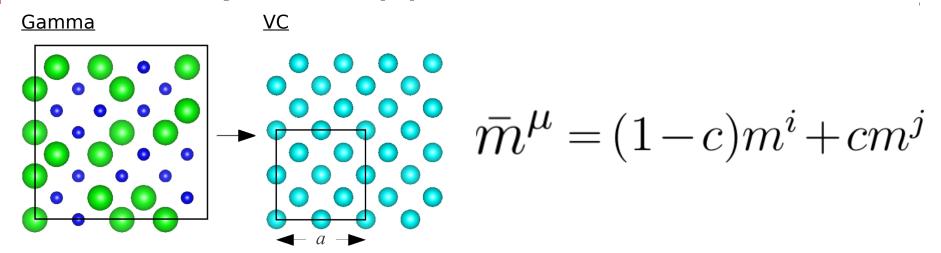
Density Functional Theory (DFT) + (VC-ALD)







Virtual Crystal Approximation



$$k_{ph,\mathbf{n}} = \sum_{\kappa} \sum_{\nu} \frac{k_B}{V} D_{ph,\mathbf{n}} \binom{\kappa}{\nu}$$

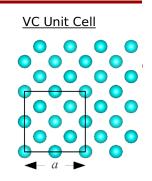
$$D_{ph,\mathbf{n}}(\mathbf{k}) = v_{g,\mathbf{n}}^2(\mathbf{k}) \tau(\mathbf{k})$$

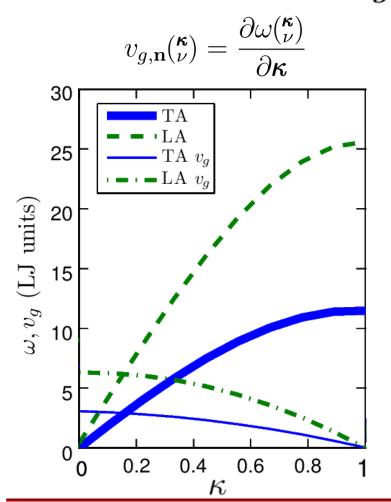
B. Abeles, Phys. Rev. 131, 19061911 (1963)



VC-ALD Diffusivities

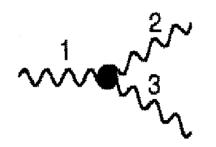
$$D_{ph,\mathbf{n}}(\mathbf{r}) = v_{g,\mathbf{n}}^2(\mathbf{r}) \, \tau(\mathbf{r})$$

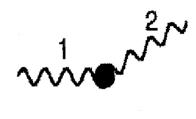




Matthiessen's Rule

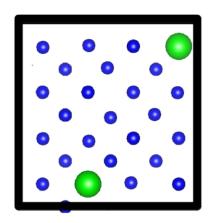
$$\frac{1}{\tau({}^{\kappa}_{\nu})} = \frac{1}{\tau_{p-p}({}^{\kappa}_{\nu})} + \frac{1}{\tau_{p-d}({}^{\kappa}_{\nu})}$$

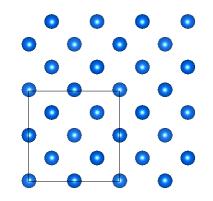


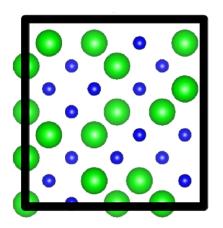


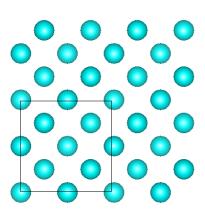
Explicit disorder: VC vs Gamma

Gamma

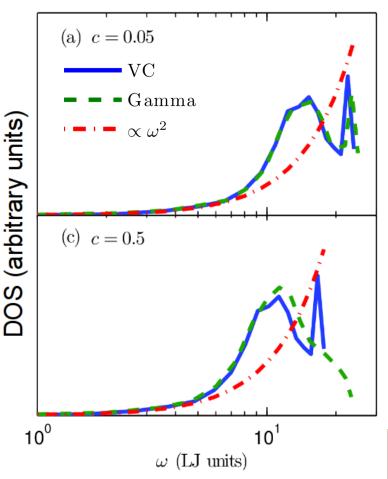






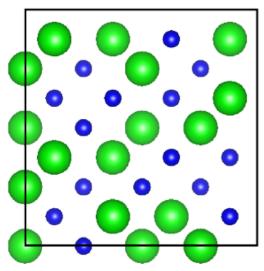


<u>Lennard-Jones Argon Alloys</u>



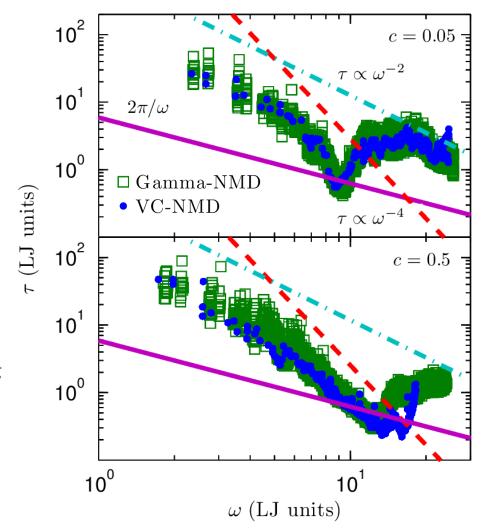
Normal Mode Decomposition (NMD)

Molecular Dynamics Gamma



$$\tau({}^{\kappa}_{\nu}) = \int_0^{t^*} \frac{\langle E({}^{\kappa}_{\nu};t) E({}^{\kappa}_{\nu};0) \rangle}{\langle E({}^{\kappa}_{\nu};0) E({}^{\kappa}_{\nu};0) \rangle} dt$$

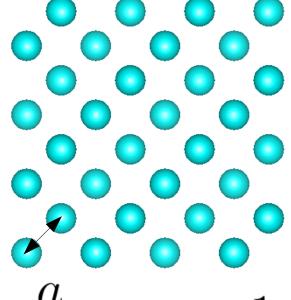
LJ Argon and Alloys, T=10 K



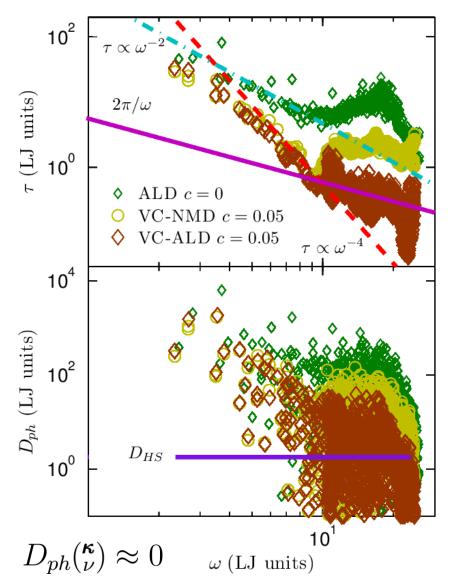
VC Diffusivities

LJ Argon and Alloys, T = 10 K

$$D_{ph,\mathbf{n}}(^{\kappa}_{\nu}) = v_{g,\mathbf{n}}^2(^{\kappa}_{\nu}) \, \tau(^{\kappa}_{\nu})$$



$$D_{HS} = \frac{1}{3}v_s a$$

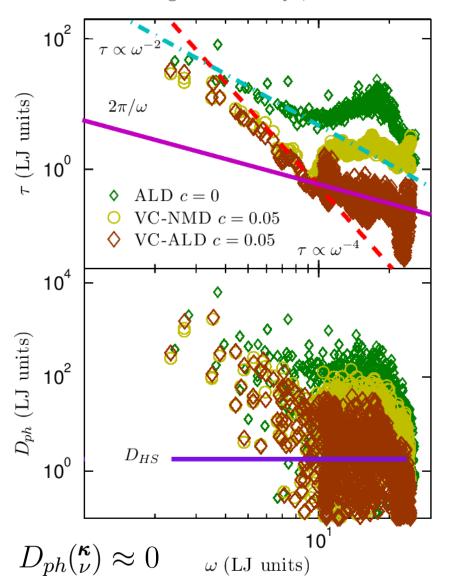


AF Diffusivities

LJ Argon and Alloys, T = 10 K

Allen-Feldman (AF) Theory:

$$k_{AF} = \sum_{\substack{\text{diffusons}}} \frac{k_B}{V} D_{AF,i}(\omega_i)$$

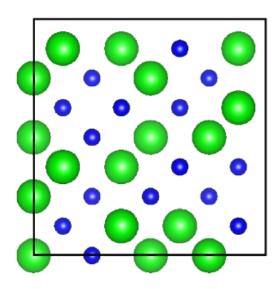






Thermal conductivity

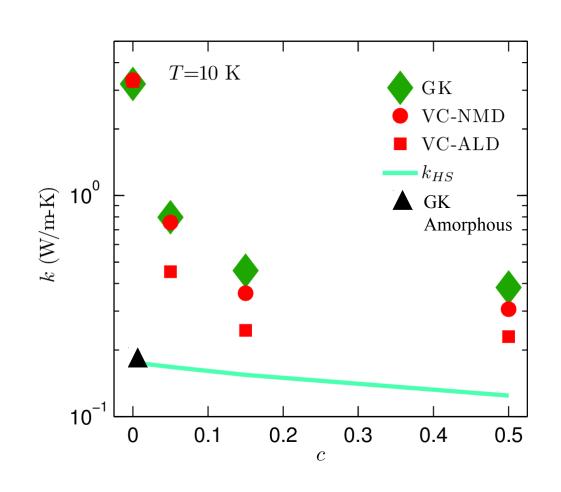
MD-based Green-Kubo (GK)



<u>High-scatter adjustment*:</u>

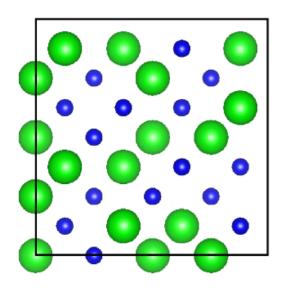
$$D_{ph}(^{\kappa}_{\nu}) < D_{HS}$$

$$D_{ph}({}^{\kappa}_{\nu}) = D_{HS}$$



Thermal conductivity

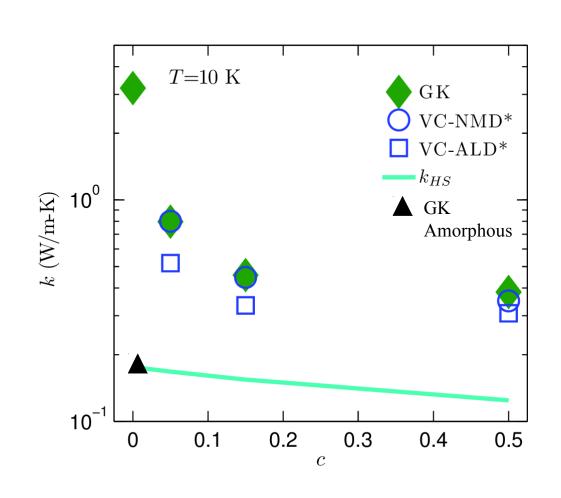
Gamma MD-based Green-Kubo



<u>High-scatter adjustment*:</u>

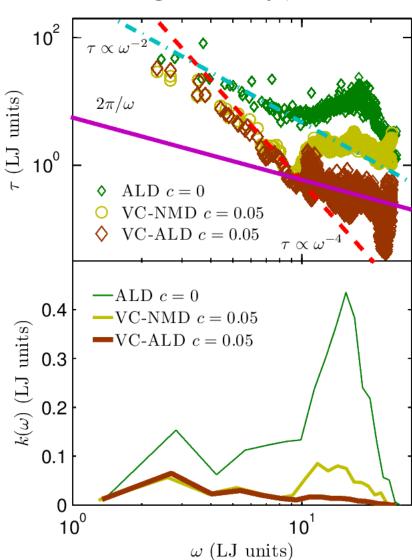
$$D_{ph}(^{\kappa}_{\nu}) < D_{HS}$$

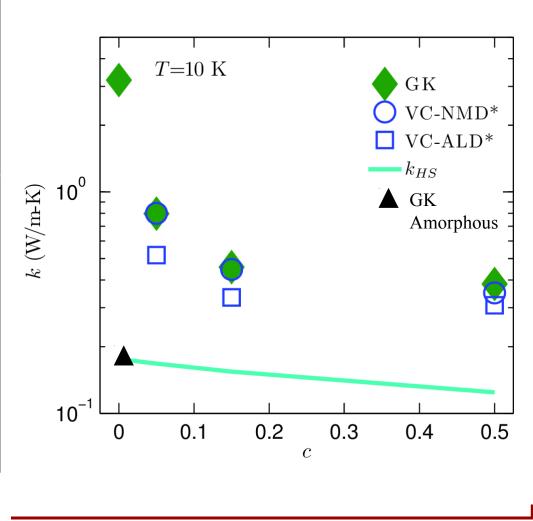
$$D_{ph}({}^{\kappa}_{\nu}) = D_{HS}$$



Thermal conductivity spectrum

LJ Argon and Alloys, T = 10 K





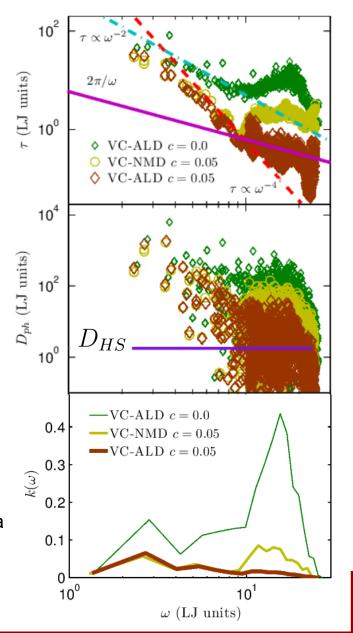
<u>Summary</u>

VC approximation underpredicts mode group velocities at high frequency.

VC-ALD underpredicts lifetimes at high-frequency.

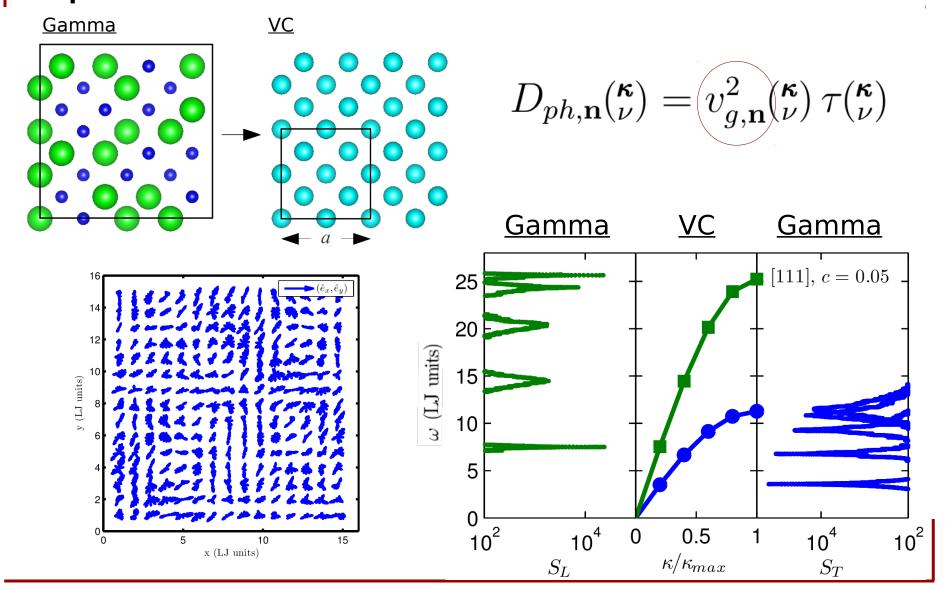
Breakdown of VC-ALD method is likely for materials near HS limit.

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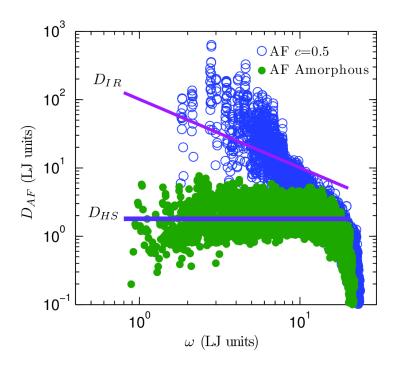


Explicit disorder: Structure Factor

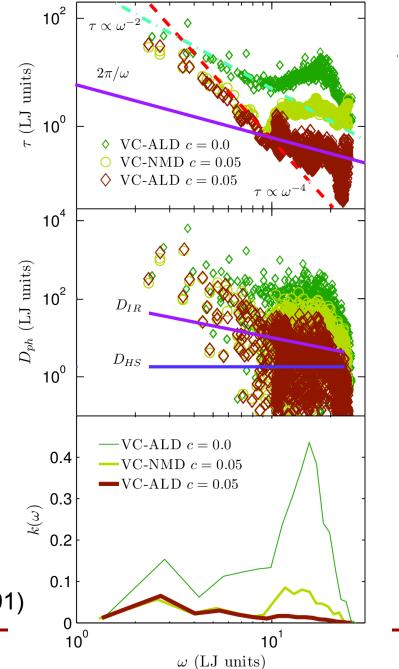


HS/IR Limit

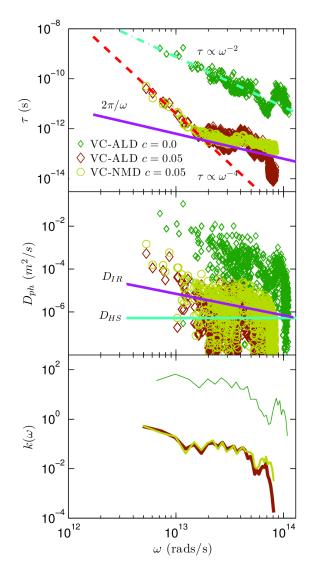
$$D_{IR} = \frac{2\pi}{3} \frac{v_s^2}{\omega}.$$

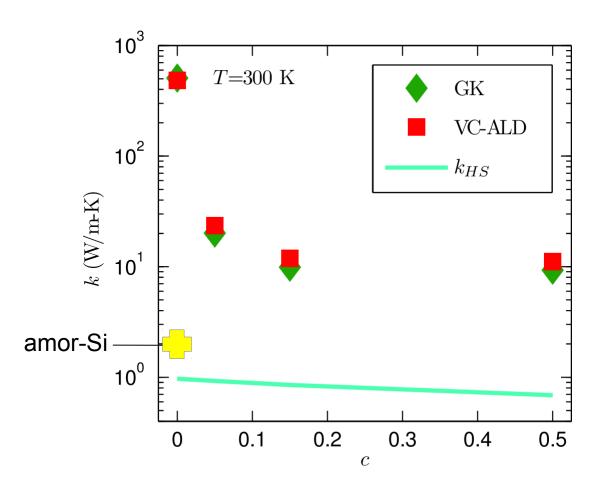


P. Sheng and M. Zhou, Science 253, 539542 (1991)



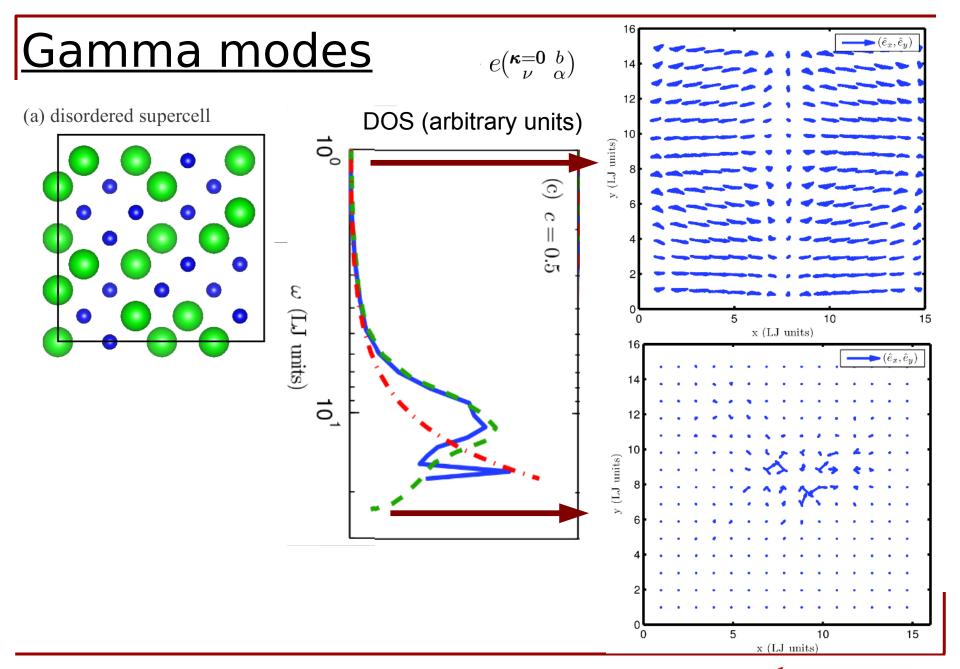
Thermal conductivity: SW silicon alloy



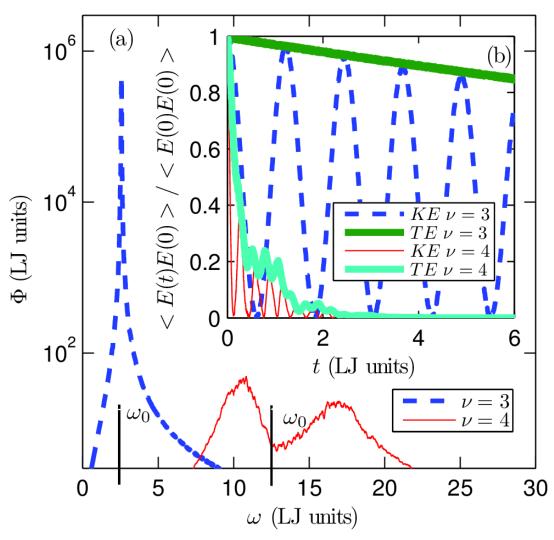




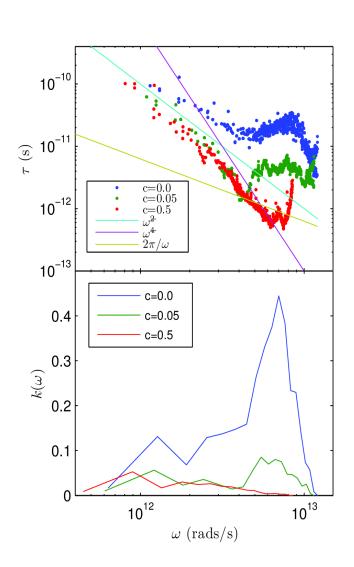


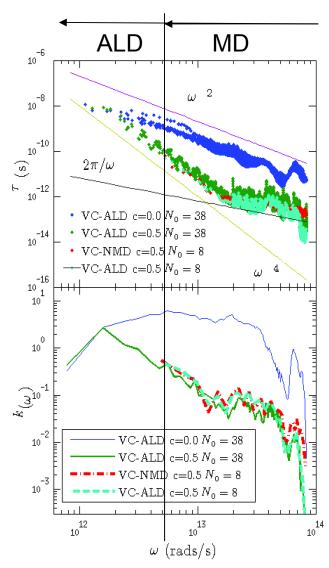


NMD using VC modes



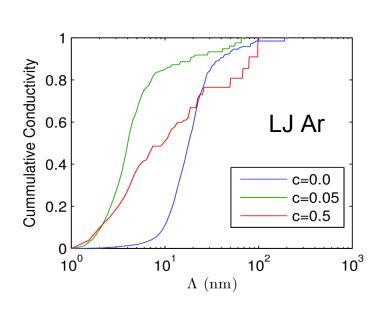
Phonon Spectrum: LJ Ar vs SW Si

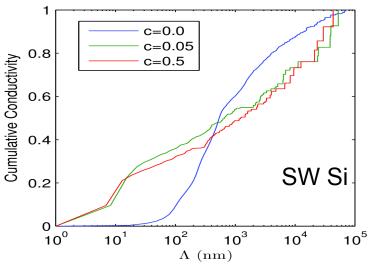


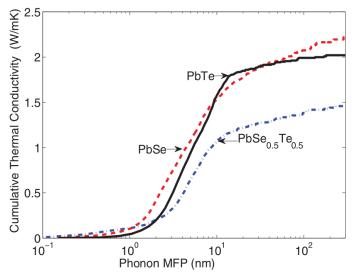




Conductivity Accumulation







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