Evaluation of the Virtual Crystal Approximation for Predicting Alloy Vibrational Mode Properties and Thermal Conductivity

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Department of Mechanical Engineering Carnegie Mellon University

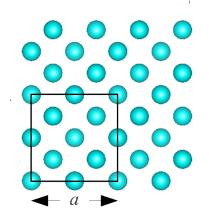
http://ntpl.me.cmu.edu/

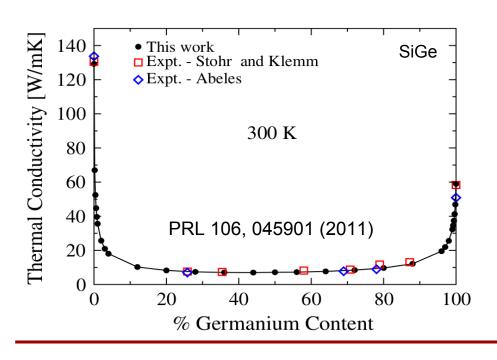
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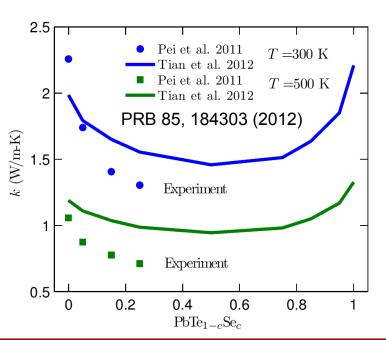


Motivation: experimental accuracy

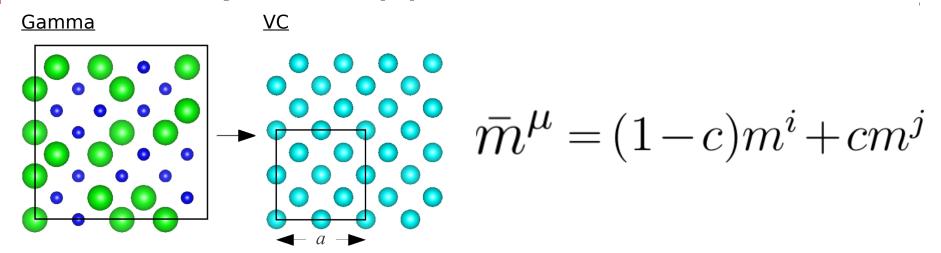
Density Functional Theory (DFT) + (VC-ALD)







Virtual Crystal Approximation



$$k_{ph,\mathbf{n}} = \sum_{\kappa} \sum_{\nu} \frac{k_B}{V} D_{ph,\mathbf{n}} \binom{\kappa}{\nu}$$

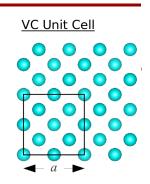
$$D_{ph,\mathbf{n}}(\mathbf{k}) = v_{g,\mathbf{n}}^2(\mathbf{k}) \tau(\mathbf{k})$$

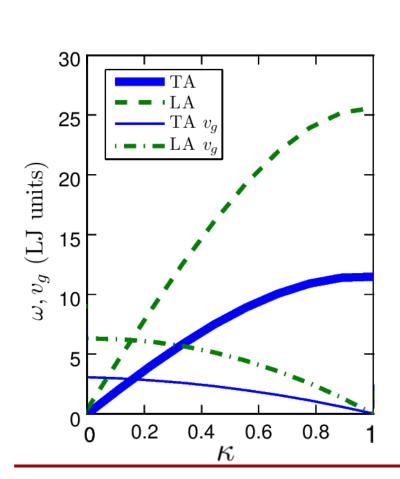
B. Abeles, Phys. Rev. 131, 19061911 (1963)



VC-ALD Diffusivities

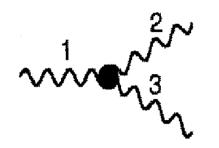
$$D_{ph,\mathbf{n}}(\mathbf{k}) = v_{g,\mathbf{n}}^2(\mathbf{k}) \tau(\mathbf{k})$$

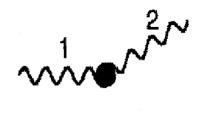




Matthiessen's Rule

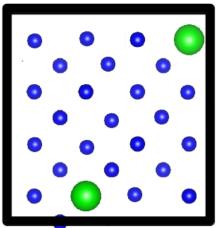
$$\frac{1}{\tau({}^{\kappa}_{\nu})} = \frac{1}{\tau_{p-p}({}^{\kappa}_{\nu})} + \frac{1}{\tau_{p-d}({}^{\kappa}_{\nu})}$$

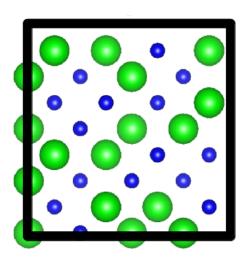




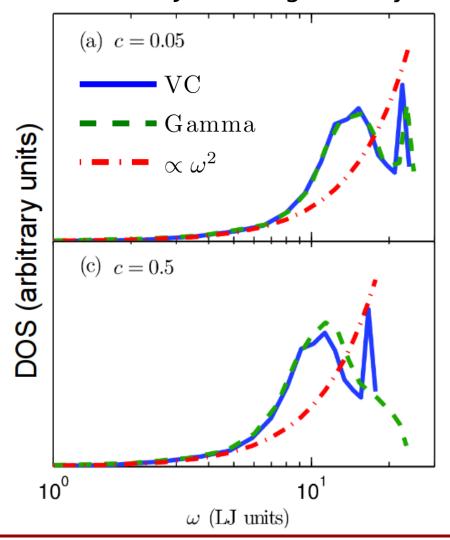
Explicit disorder: VC vs Gamma



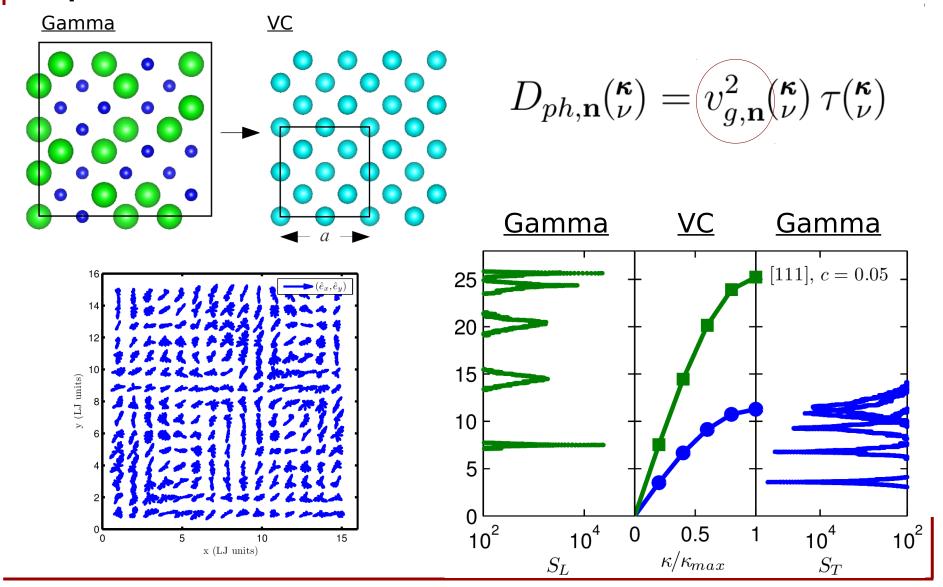




Lennard-Jones Argon Alloys

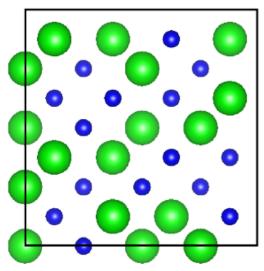


Explicit disorder: Structure Factor



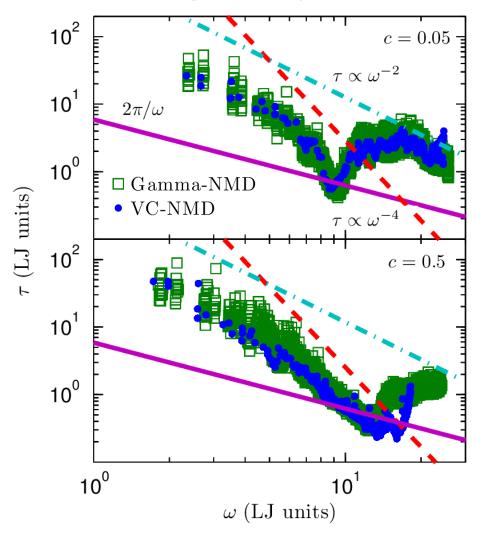
Normal Mode Decomposition (NMD)

Molecular Dynamics Gamma



$$\tau({}^{\kappa}_{\nu}) = \int_0^{t^*} \frac{\langle E({}^{\kappa}_{\nu};t) E({}^{\kappa}_{\nu};0) \rangle}{\langle E({}^{\kappa}_{\nu};0) E({}^{\kappa}_{\nu};0) \rangle} dt$$

LJ Argon and Alloys, T=10 K

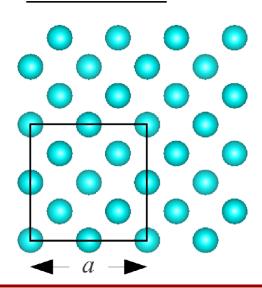


VC Diffusivities

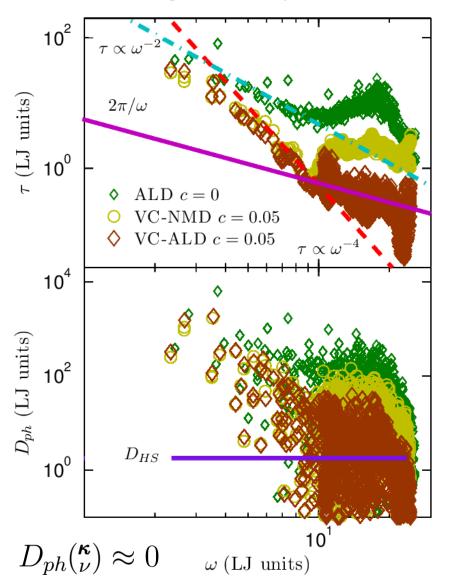
$$D_{ph,\mathbf{n}}(^{\kappa}_{\nu}) = v_{g,\mathbf{n}}^2(^{\kappa}_{\nu}) \, \tau(^{\kappa}_{\nu})$$

$$D_{HS} = \frac{1}{3}v_s a$$

VC Unit Cell



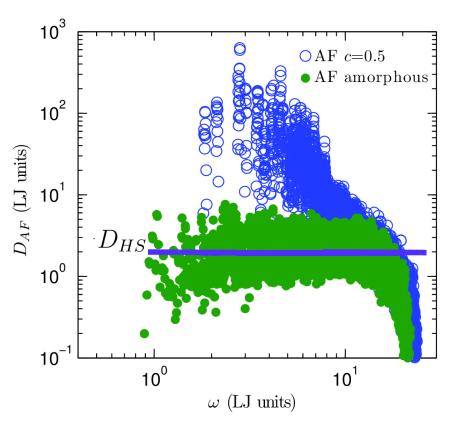
LJ Argon and Alloys, T = 10 K

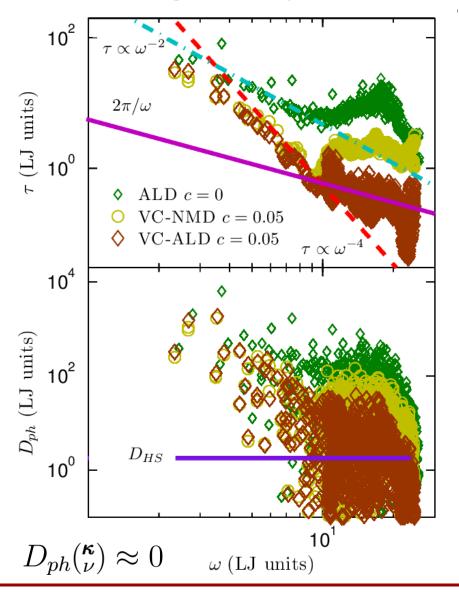


AF Diffusivities

LJ Argon and Alloys, T = 10 K







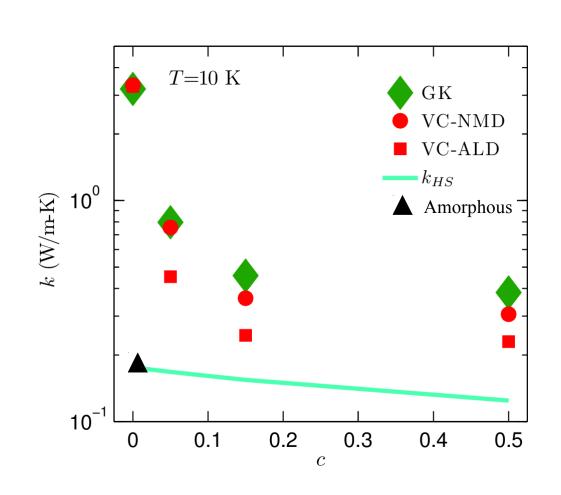
Thermal conductivity

<u>Green-Kubo (GK): top-down</u> <u>method, no assumptions</u>

<u>High-scatter adjustment*:</u>

$$D_{ph}(^{\kappa}_{\nu}) < D_{HS}$$

$$D_{ph}({}^{\kappa}_{\nu}) = D_{HS}$$



Thermal conductivity

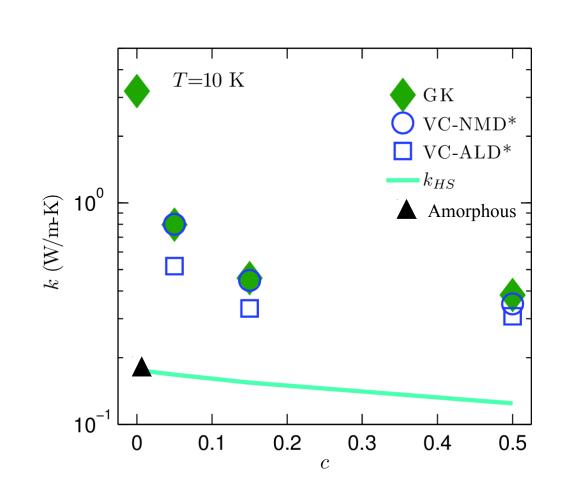
<u>Green-Kubo (GK): top-down</u> <u>method, no assumptions</u>

<u>High-scatter adjustment*:</u>

$$D_{ph}({}^{\kappa}_{\nu}) < D_{HS}$$

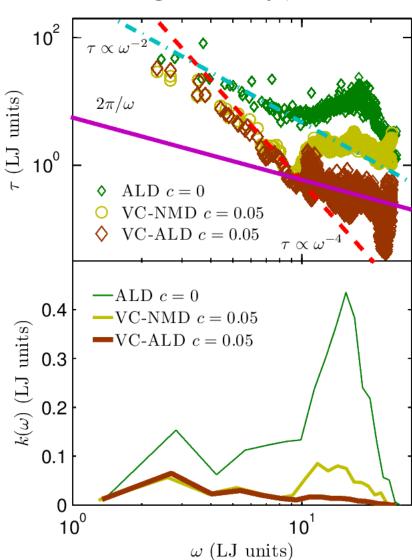
$$D_{ph}({}^{\kappa}_{\nu}) = D_{HS}$$

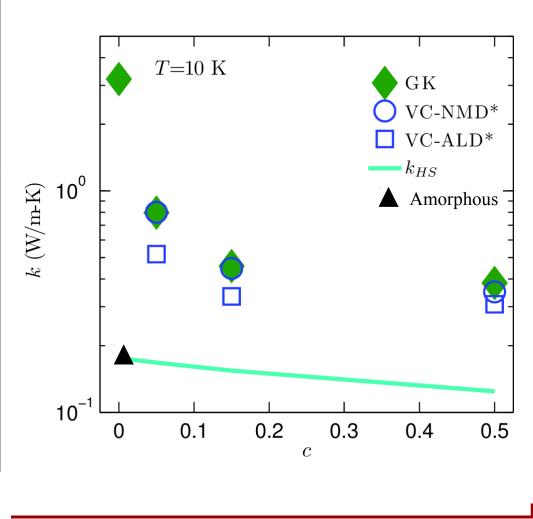
$$k_{HS} = \frac{k_B}{V_b} b v_s a$$



Thermal conductivity spectrum

LJ Argon and Alloys, T = 10 K





<u>Summary</u>

VC approximation underpredicts mode group velocities at high frequency, which lead to underprediction of mode diffusivity.

VC-ALD underpredicts lifetimes at high-frequency.

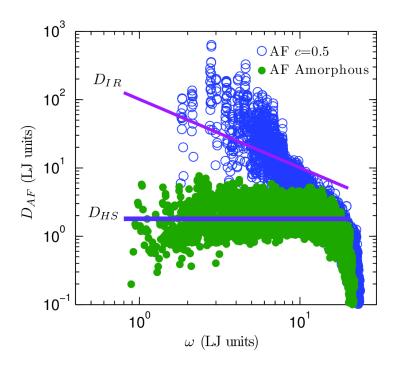
LJ Argon has important contribution from high-frequency modes to thermal conductivity.

<u>Breakdown of VC-ALD method</u> is likely for materials with thermal conductivity near the high-scatter limit, or for modes below the high-scatter limit.

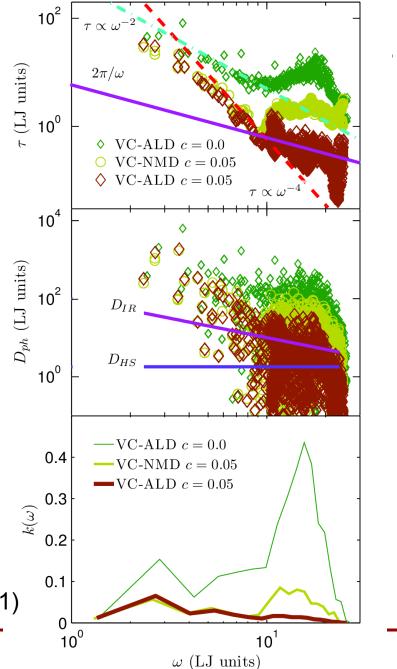
This work was supported by AFOSR award FA95501010098 and by a grant of computer time from the DOD High Performance Computing Modernization Program at the US Army Engineer Research and Development Center. We thank Davide Donadio, Jivtesh Garg, Asad Hasan, Craig Maloney, and Zhiting Tian for helpful discussions.

HS/IR Limit

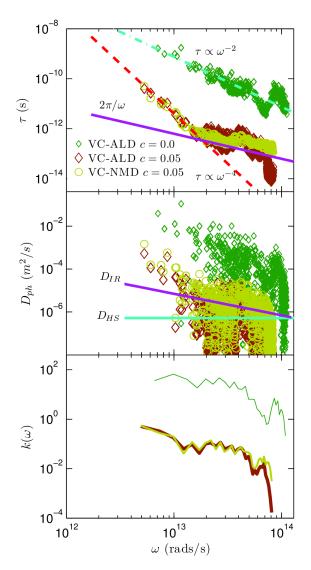
$$D_{IR} = \frac{2\pi}{3} \frac{v_s^2}{\omega}.$$

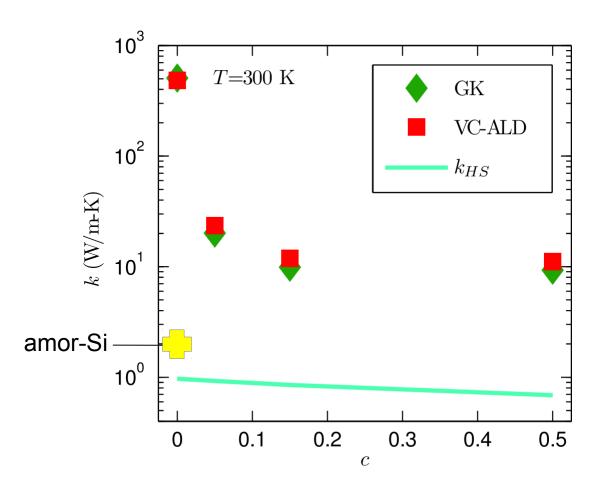


P. Sheng and M. Zhou, Science 253, 539542 (1991)



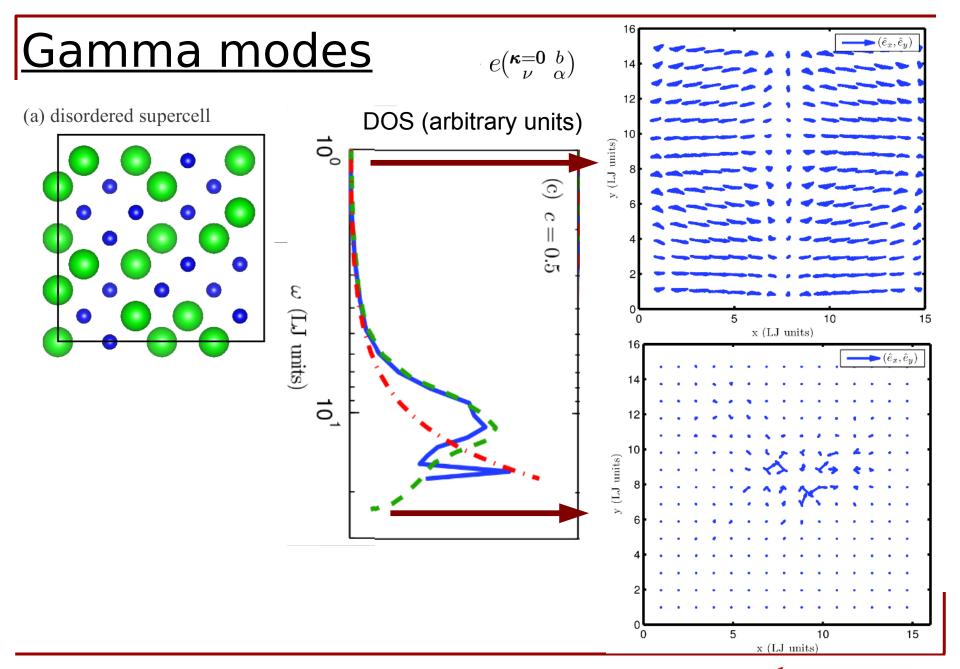
Thermal conductivity: SW silicon alloy



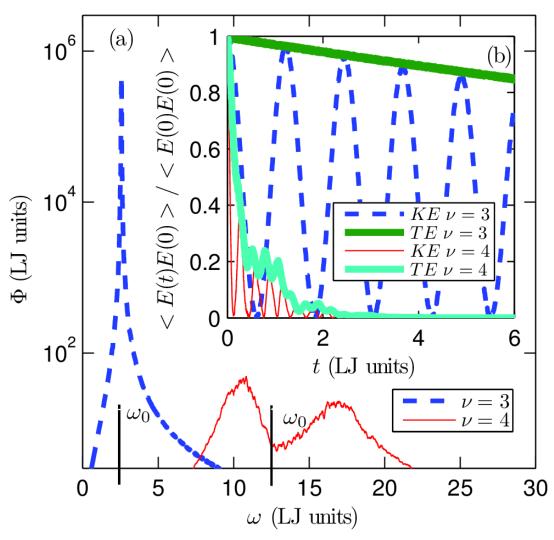




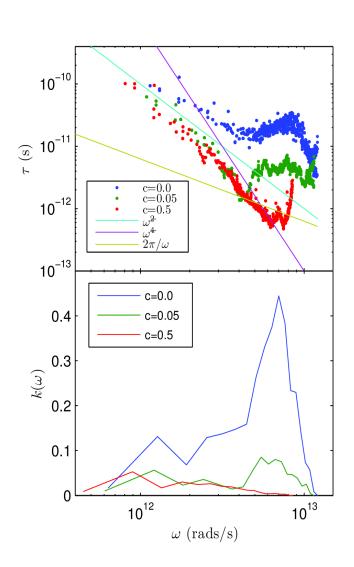


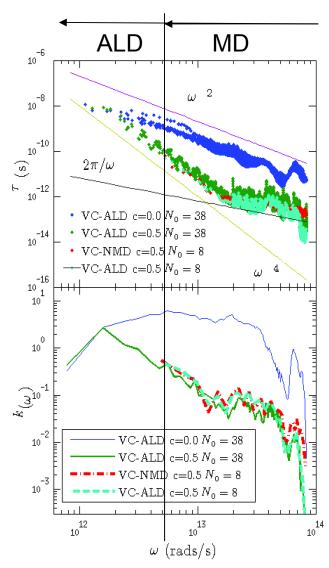


NMD using VC modes



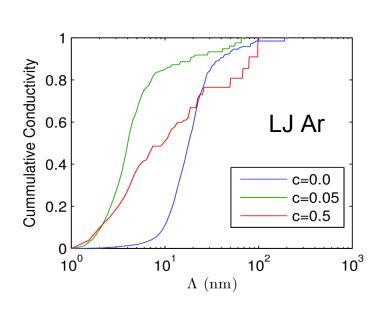
Phonon Spectrum: LJ Ar vs SW Si

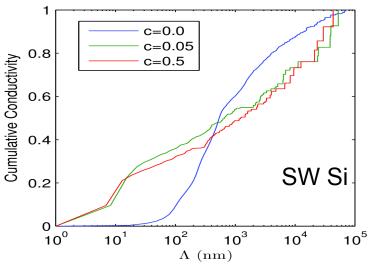


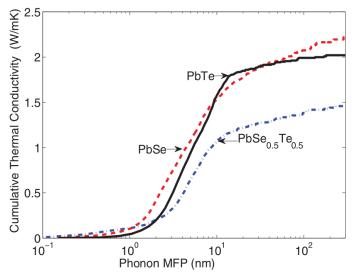




Conductivity Accumulation



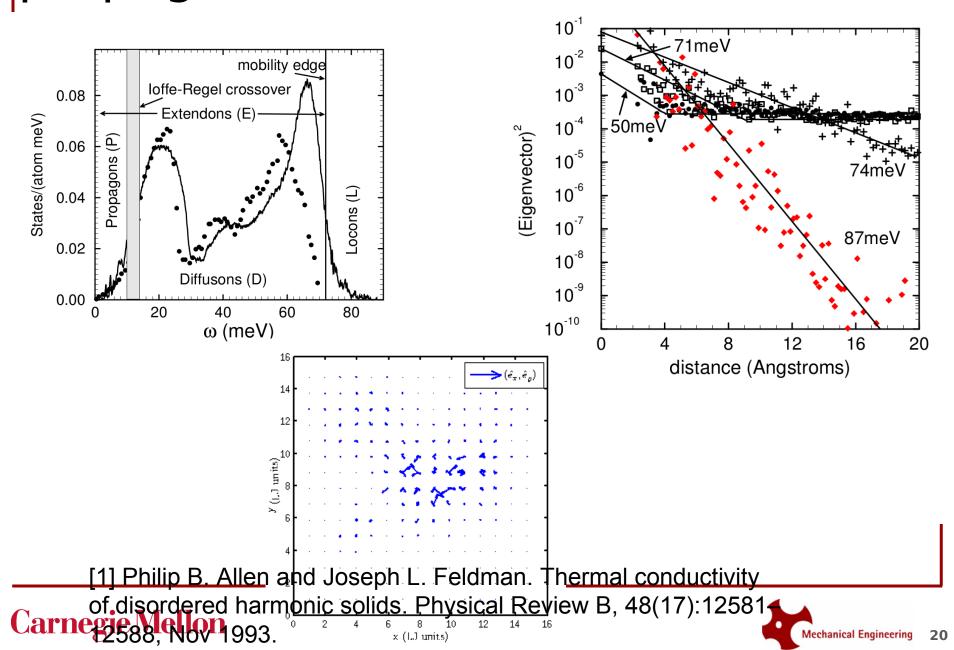




PHYSICAL REVIEW B 85, 184303 (2012)



propagons, diffusons, locons



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Mechanical Engineering

Diamond
GaN
si
Si,HS
Si/Ge

PbTe,PbTe/Se, (1/4)Tmelt = 300K LJ,20K,

(1/4)T_melt

Exponential trends in Information Technologies

Moore's Law: 2^{n}

http://boards.straightdope.com/sdmb/showthread.php?t=316530

Human Genome

http://en.wikipedia.org/wiki/Kurzweil_Music_Systems



Exponential trends music: orchestra

1980: \$100,000

http://boards.straightdope.com/sdmb/showthread.php?t=316530

2003: \$2,000 (my setup

http://en.wikipedia.org/wiki/Kurzweil_Music_Systems

VC-ALD: Group Velocity

