

# Exercice : Test de Kolmogorov-Smirnov

```
install.packages("ggplot2",repos = "http://cran.us.r-project.org")

## Warning: unable to access index for repository http://cran.us.r-project.org/src/contrib:
## cannot open URL 'http://cran.us.r-project.org/src/contrib/PACKAGES'

## Warning: package 'ggplot2' is not available (for R version 3.5.1)

## Warning: unable to access index for repository http://cran.us.r-project.org/bin/macosx/el-capitan/contrib/3.5/PACKAGES'
## cannot open URL 'http://cran.us.r-project.org/bin/macosx/el-capitan/contrib/3.5/PACKAGES'

library(ggplot2)
set.seed(254)
k=1:100
l=1:100
for (i in 1:100)
{
  u=rexp(1,1)
  l[i]=u
}

so=l[order(l)]
so

## [1] 0.005143292 0.007998401 0.035032275 0.038825120 0.053518175
## [6] 0.079166044 0.107159502 0.131127127 0.136118233 0.158363834
## [11] 0.160438983 0.181117203 0.205961673 0.214485342 0.218351417
## [16] 0.223184937 0.224276716 0.228771869 0.232283868 0.233438427
## [21] 0.236372354 0.245644187 0.248222437 0.260990661 0.261556915
## [26] 0.267238777 0.272209368 0.272860450 0.276354577 0.278804836
## [31] 0.294241696 0.310352448 0.322630604 0.340961270 0.366683055
## [36] 0.368288236 0.397390094 0.413780637 0.418461236 0.420138591
## [41] 0.450135275 0.450721797 0.463897370 0.539803244 0.576316005
## [46] 0.605506711 0.621298573 0.639958588 0.643892045 0.667425530
## [51] 0.668248098 0.678926278 0.692402035 0.711499895 0.742813652
## [56] 0.767528851 0.769268951 0.778684772 0.860676320 0.863709202
## [61] 0.939297402 1.004607570 1.030692153 1.053208095 1.090745795
## [66] 1.104893157 1.248641727 1.254266503 1.277752831 1.285727725
## [71] 1.349126834 1.373063784 1.407445110 1.411408625 1.427030606
## [76] 1.451181516 1.456112422 1.463243833 1.476518646 1.482341621
## [81] 1.501251490 1.673895370 1.720761325 1.771965988 1.784164976
## [86] 1.795787865 1.878004692 2.016635647 2.145343950 2.356171688
## [91] 2.417059082 2.491645159 2.650724599 2.750335669 2.918883867
## [96] 3.131893150 3.420829050 4.086011892 4.841131080 5.591181144

#les statistiques d'ordre
l2=1:100
for (i in 1:100)
{
  l2[i]=i/100
}

#le zalpha du theoreme de Massart
alph=0.05
```

```
zalpha=sqrt(1/2*log(2/alph))
zalpha/10
```

```
## [1] 0.1358102
```

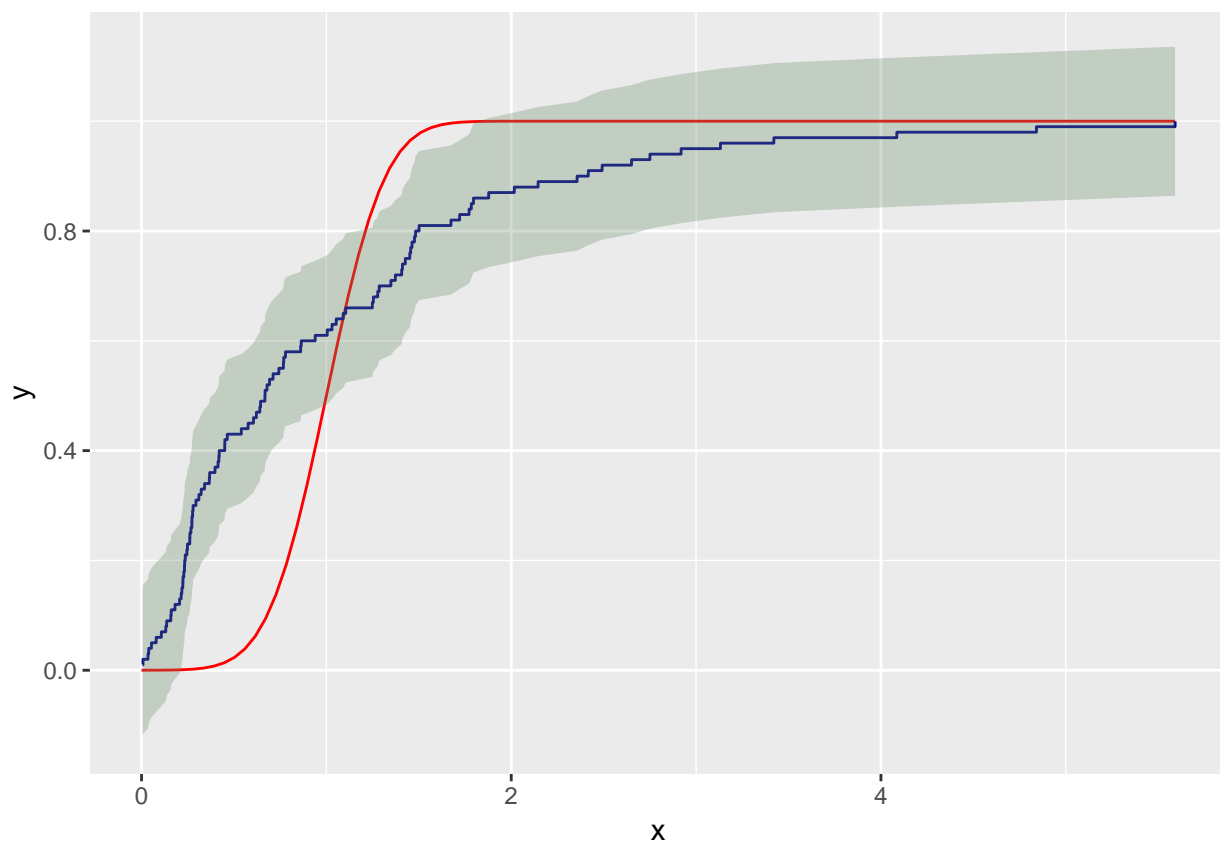
```
plotdata <- data.frame(x=so, y=l2, lower = (l2-zalpha/10), upper = (l2+zalpha/10), qdown=qnorm((l2-zalp
```

```
## Warning in qnorm((l2 - zalpha/10)): NaNs produced
```

```
## Warning in qnorm((l2 + zalpha/10)): NaNs produced
```

```
test <- function(x) {pnorm(x,1,1/4)}
```

```
p4 <- ggplot(data.frame(x = c(0, 4)), aes(x = x)) +
  stat_function(fun =test, colour="red") +geom_step(data=plotdata,aes(so,l2),colour="darkblue")+geom_ri
p4
```



```
#Après plusieurs essais on obtient une droite comprise entre les deux courbes
```

```
a=1.3
```

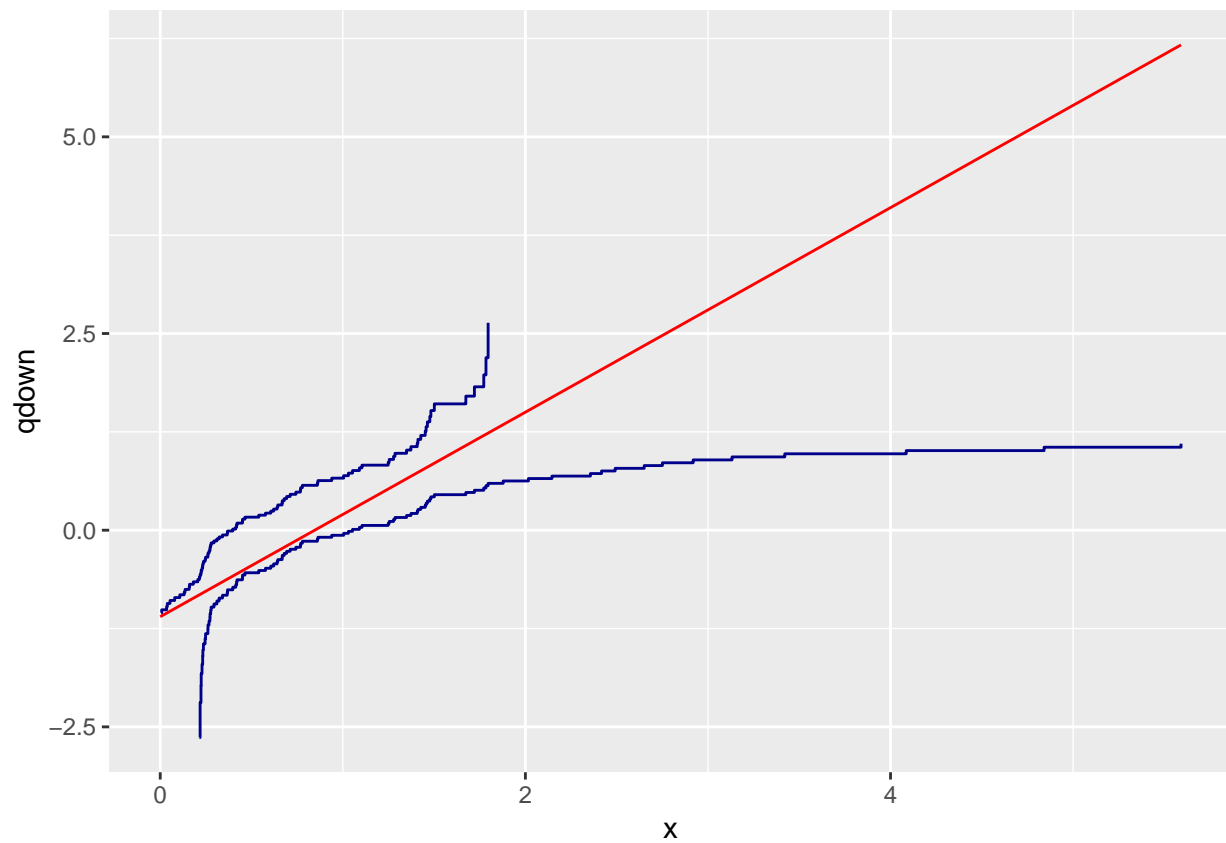
```
b=-1.1
```

```
droite<-function(x){a*x+b}
```

```
p4test<- ggplot(data.frame(x = c(0, 4)), aes(x = x)) +geom_step(data=plotdata,aes(so,qdown),colour="darkblue")+
  stat_function(fun =droite, colour="red")
p4test
```

```
## Warning: Removed 13 rows containing missing values (geom_path).
```

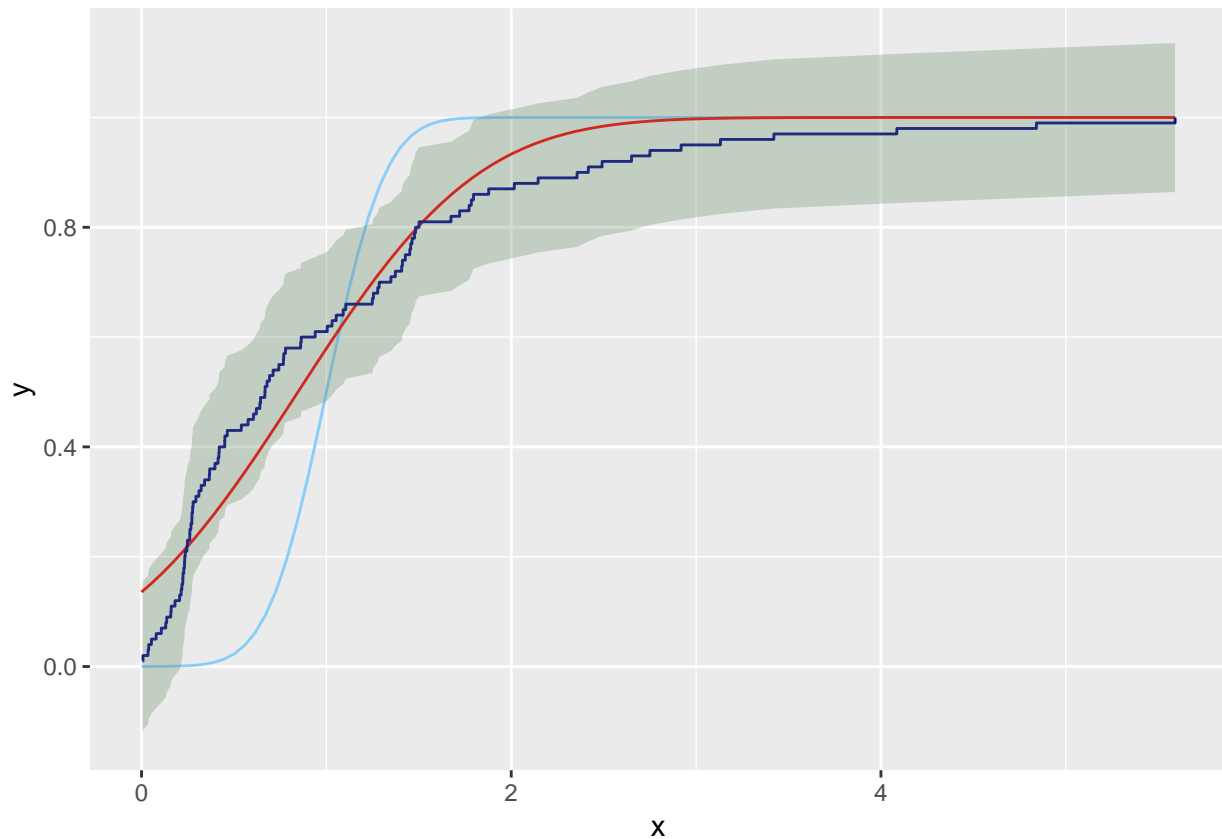
```
## Warning: Removed 14 rows containing missing values (geom_path).
```



```
test_norm<-function(x){pnorm(x,-b/a,1/a)}
```

*#On superpose la loi normale correspondante sur le graphe des fonctions de repartition*

```
ppp<- ggplot(data.frame(x = c(0, 4)), aes(x = x)) + stat_function(fun =test, colour="lightskyblue")+
  stat_function(fun =test_norm, colour="red") +geom_step(data=plotdata,aes(so,12),colour="darkblue")+ge
ppp
```



La fonction de repartition de la  $N(1,1/2)$  n est pas dans la bande de confiance de la fonction de repartition empirique basee sur les  $X_1, \dots, X_n \text{ iid} \sim \text{Exp}(1)$ . On rejette donc l hypothese nulle. Cela est coherent car on sait que les observations sont des observations d une  $\text{Exp}(1)$ . Pour le modele general avec un test portant sur la famille des loi normales, on trouve qu il existe une loi qui appartient a l intervalle et ne pouvant donc pas rejeter l hypothese nulle. Comme on sait qu en realite la loi des  $X_i$  est une  $\text{Exp}(1)$ , on effectue en fait une erreur de 2eme espece ( $H_1$  est vraie mais on decide  $H_0$ ).