



Birzeit University-Faculty Of Engineering

Electrical Engineering Department

Signals and Systems –EE2312

MATLAB _Assignment I

Name: Baraa Nasar

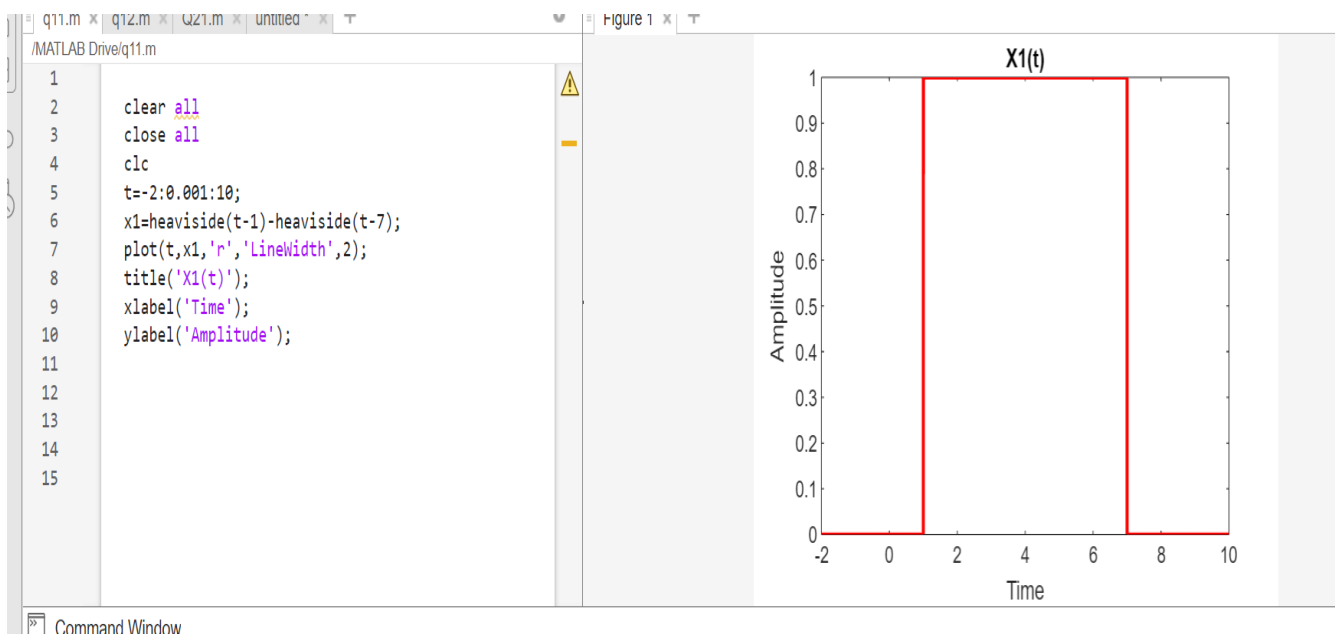
ID: 1210880

Instructor: Dr. Ashraf Al-Rimawi

Question I >> Generate and plot the following signals using MATLAB:

1- $x_1(t) = u(t-1) - u(t-7)$

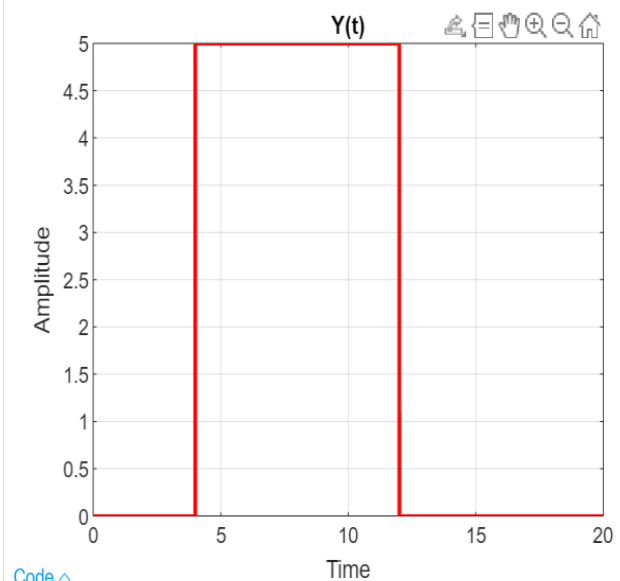
>> Code and Graph:



2- A finite pulse ($\pi(t)$) with value = 5 and extension between and center=8

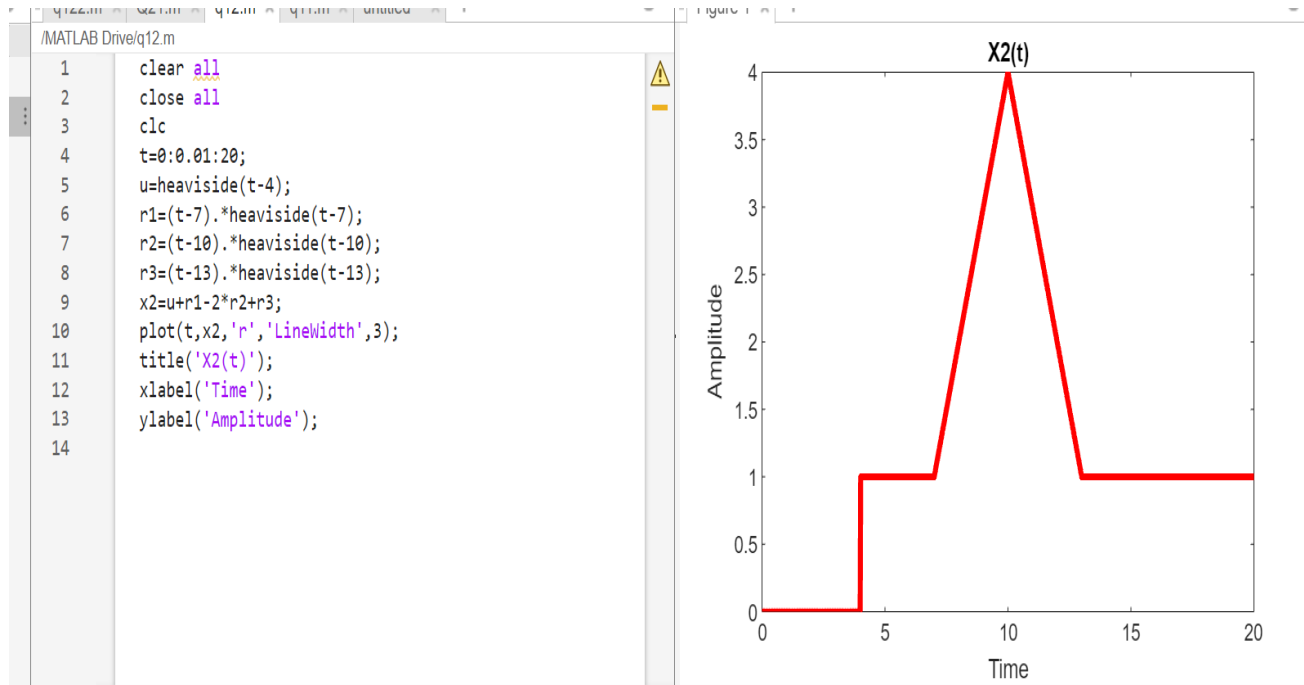
>> Code and Graph:

```
1 clear all
2 close all
3 clc
4 t=0:0.001:20;
5 y=5*rectangularPulse(4,12,t);
6 plot(t,y,'r','LineWidth',2);
7 title('Y(t)');
8 xlabel('Time');
9 ylabel('Amplitude');
```



3- $x_2(t) = u(t-4) + r(t-7) - 2r(t-10) + r(t-13)$ in the time interval [0 20]

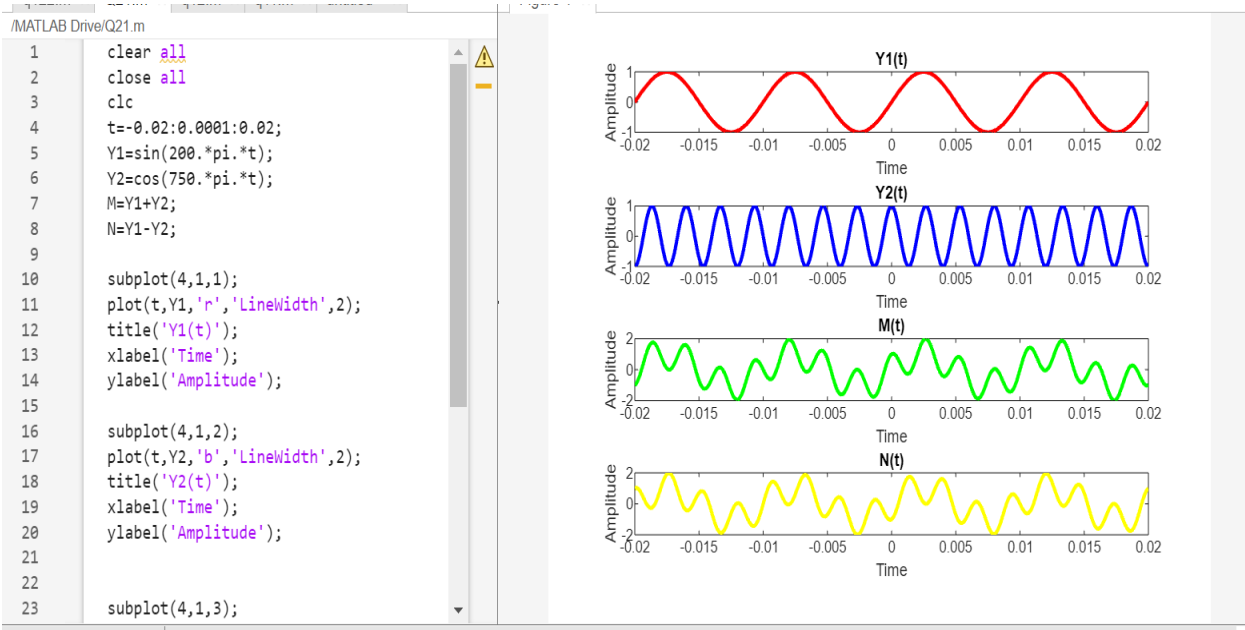
>>Code and Graph:

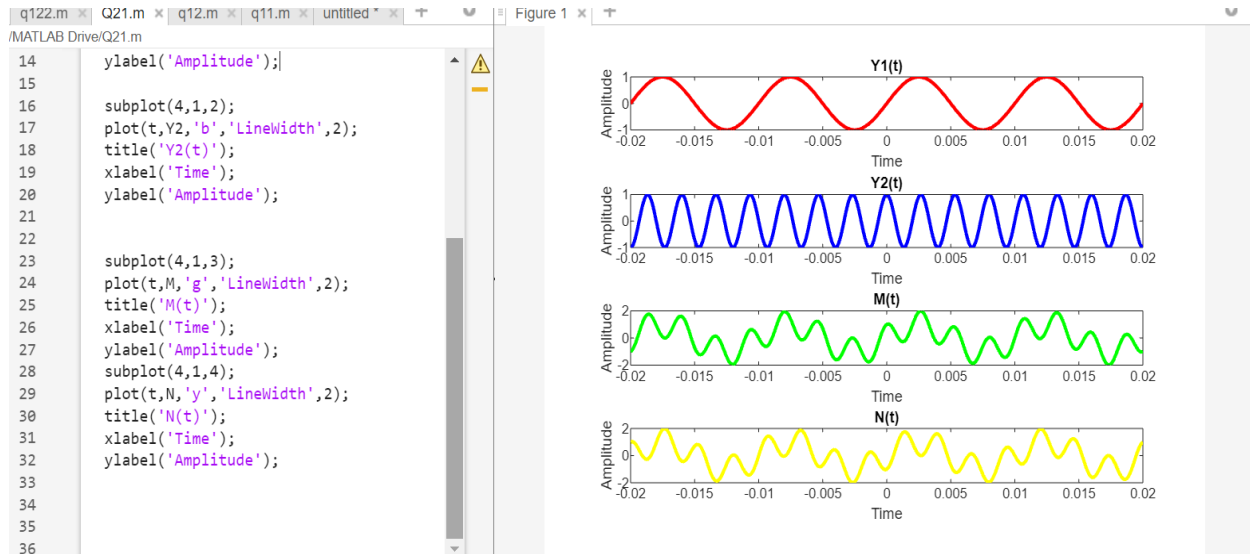


Question II :

1- Generate and plot the signals $y_1(t) = \sin 200\pi t$, $y_2(t) = \cos 750\pi t$, then determine y_1 and plot the signals $m(t) = y_1 + y_2$ and $n(t) = y_1 - y_2$.

>>Code and Graph:





2-Determine, using the MATLAB plots, if the sum and/or difference signals are periodic. In case a signal is periodic, determine its fundamental frequency.)

The sum and difference of the signals are periodic and the fundamental frequency is 100HZ

Question III: Write the programs that solve the following differential equations using zero initial conditions.

1- $5 \frac{dy(t)}{dt} + 20y(t) = 15$

>>Code and solution:

```

MATLAB Drive/q31.m
1  clear all
2  close all
3  clc
4  syms y(t);
5  dy(t)=diff(y(t),t);
6  initial_condition2=y(0)==0;
7  cond=[initial_condition2];
8  equation=5*dy(t)+20*y(t)==15;
9  solution=dsolve(equation,cond)
10 simple_solution=simplify(solution);

Command Window

New to MATLAB? See resources for Getting Started.

solution =

3/4 - (3*exp(-4*t))/4

>>
```

$$2\frac{d^2y(t)}{dt^2} + 2\frac{dy(t)}{dt} + 4y(t) = 5\cos(1000t).$$

>>Code and solution:

```

AB Drive
q122.m x Q21.m x q12.m x q11.m x q31.m x +
/MATLAB Drive/q31.m
1      clear all
2      close all
3      clc
4      syms y(t);
5      dy(t)=diff(y,t);
6      dy2(t)=diff(y,t,2);
7      initial_condition1=y(0)==0;
8      initial_condition2=dy(0)==0;
9      equation= dy2(t)+2*dy(t)+4*y(t)==5*cos(1000*t);
10     solution=dsolve(equation,initial_condition1,initial_condition2)
11     simple_solution=simplify(solution);

```

solution =

```

sin(3^(1/2)*t)*((625*cos(1000*t - 3^(1/2)*t))/124999500002 -
(625*cos(1000*t + 3^(1/2)*t))/124999500002 - (1249995*sin(1000*t +
3^(1/2)*t))/499998000008 + (1249995*sin(1000*t -
3^(1/2)*t))/499998000008 + (1250005*3^(1/2)*cos(1000*t +
3^(1/2)*t))/1499994000024 + (1250005*3^(1/2)*cos(1000*t -
3^(1/2)*t))/1499994000024 + (312499375*3^(1/2)*sin(1000*t +
3^(1/2)*t))/374998500006 + (312499375*3^(1/2)*sin(1000*t -
3^(1/2)*t))/374998500006) - (5*3^(1/2)*cos(3^(1/2)*t)*((sin(t*(3^(1/2)
- 1000)) - cos(t*(3^(1/2) - 1000))*(3^(1/2) - 1000))/((3^(1/2) -
1000)^2
+ 1) + (sin(t*(3^(1/2) + 1000)) - cos(t*(3^(1/2) + 1000))*(3^(1/2) +
1000))/((3^(1/2) + 1000)^2 + 1))/6 - (1250005*3^(1/2)*exp(-
t)*sin(3^(1/2)*t))/749997000012 - (1249995*exp(-
t)*cos(3^(1/2)*t))/(4*(500*3^(1/2) - 250001)*(500*3^(1/2) + 250001))

```


Question IV: Write the programs that determine the response of the linear time invariant system to the given input and the given initial conditions:

$$1 - \frac{dy(t)}{dt} + 2y(t) = 7u(t) \quad y(0) = 2;$$

>>Code and solution:

```
1 clear all
2 close all
3 clc
4 syms y(t);
5 dy(t)=diff(y(t),t);
6 initial_condition1=y(0)==2;
7 equation=dy(t)+2*y(t)==7*heaviside(t);
8 solution=dsolve(equation,initial_condition1)
9 simple_solution=simplify(solution);
```

Command Window

New to MATLAB? See resources for [Getting Started](#).

```
solution =
exp(-2*t)/4 - exp(-2*t)*((7*sign(t))/4 - (7*exp(2*t)*(sign(t) + 1))/4)
>>
```

$$2\text{-d } 2y(t)/dt^2 + 4 dy/dt + 5y(t) = 5 \cos 2000t \quad (y(0) = 1, y'(0) = 2);$$

>>Code and solution:

```

1 clear all
2 close all
3 clc
4 syms y(t);
5 dy(t)=diff(y,t);
6 dy2(t)=diff(y,t,2);
7 initial_condition1=y(0)==1;
8 initial_condition2=dy(0)==2;
9 equation=dy2(t)+4*dy(t)+5*y(t)==5*cos(2000*t);
10 solution=dsolve(equation,initial_condition1,initial_condition2)
11 simple_solution=simplify(solution);

```

Solution=

```

sin(t)*(cos(1999*t)/799201 + cos(2001*t)/800801 + (1999
sin(1999*t))/1598402 + (2001*sin(2001*t))/1601602) - cos(t)
((1999*cos(1999*t))/1598402 - (2001*cos(2001*t))/1601602 -
sin(1999*t)/799201 + sin(2001*t)/800801) + (640001760000*exp(-
2*t)*cos(t))/640000960001 + (2560002240002*exp(-
2*t)*sin(t))/640000960001

```

Question V: Use Simulink (MATLAB) to simulate the following systems then show and plot the step response of the system.

$$1-5 \frac{d^4 y(t)}{dt^4} + 8 \frac{dy(t)}{dt} + 2y(t) = 4 \frac{d^2 x(t)}{dt^2} - 12x(t)$$

Solution:

Handwritten solution for the differential equation:

$$1-5 \frac{d^4 y(t)}{dt^4} + 8 \frac{dy(t)}{dt} + 2y(t) = 4 \frac{d^2 x(t)}{dt^2} - 12x(t)$$

$$\frac{d^4 y(t)}{dt^4} + 1.6 \frac{dy(t)}{dt} + 0.4y(t) = 0.8 \frac{d^2 x(t)}{dt^2} - 2.4x(t)$$

$$a_0 = 0.4, a_1 = 1.6, b_0 = -2.4, b_1 = 0.8$$

$$\frac{d^4 y(t)}{dt^4} + 1.6 \frac{dy(t)}{dt} - 0.8 \frac{d^2 x(t)}{dt^2} = \underbrace{-0.4y(t)}_{q_0} - \underbrace{2.4x(t)}_{q_1}$$

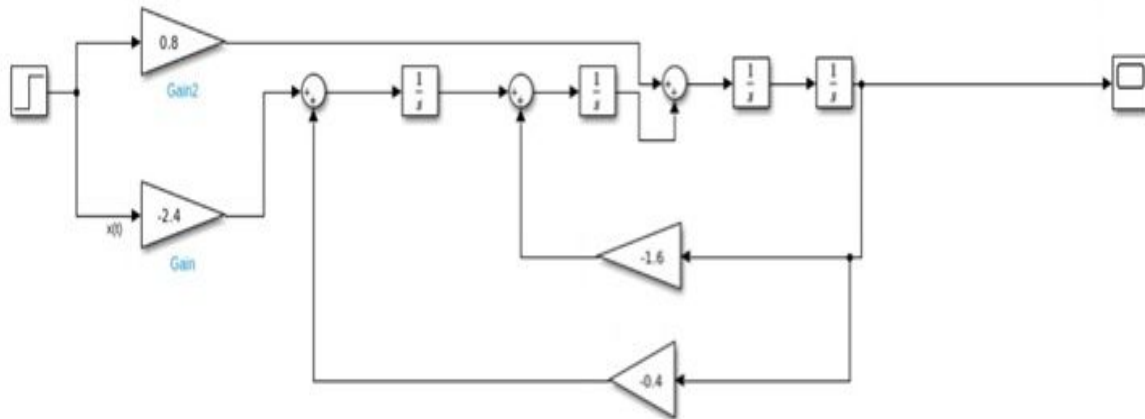
$$\frac{d^3 y(t)}{dt^3} - 0.8 \frac{dx(t)}{dt} = \int \underbrace{q_0 - 1.6y(t)}_{q_1}$$

$$\frac{d^2 y(t)}{dt^2} = \int \underbrace{q_1 + 0.8x(t)}_{q_2}$$

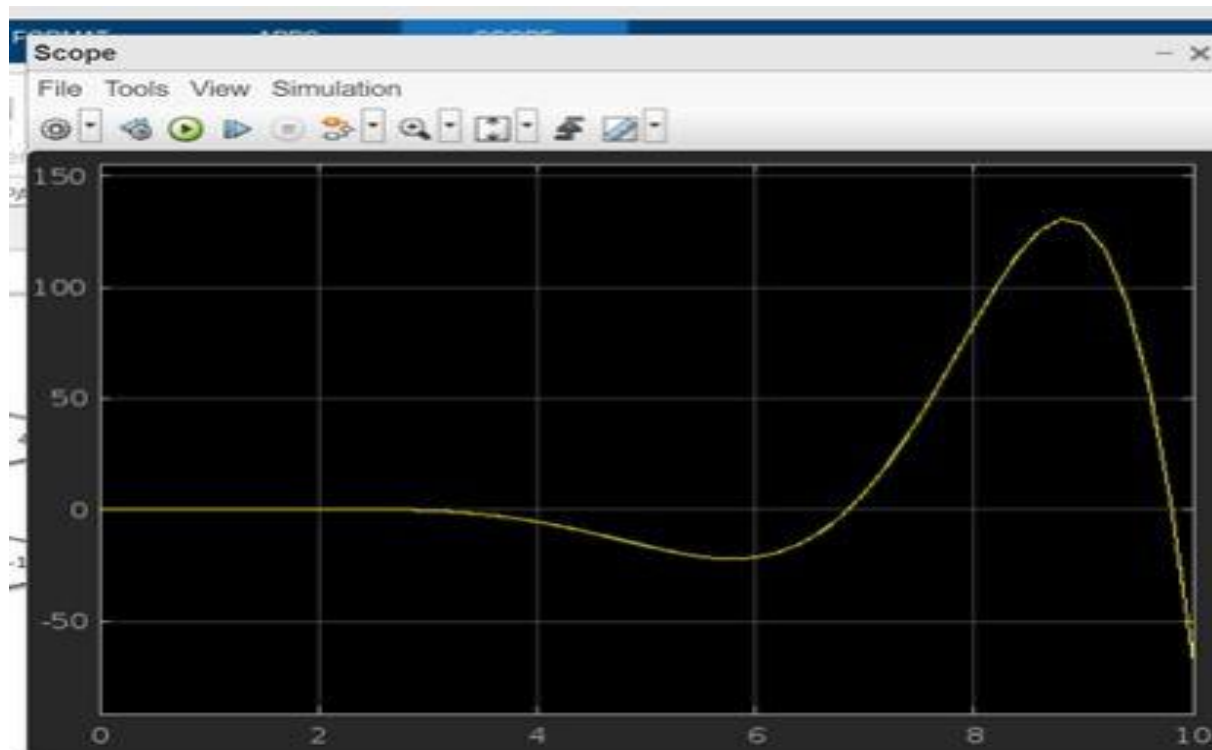
$$\frac{dy(t)}{dt} = \int q_2$$

$$y(t) = \iint q_2$$

Simulation:



Graph:



$$2 \frac{d^2 y(t)}{dt^2} + 2 \frac{dy}{dt} + 4y(t) = 5x(t)$$

Solution:

$$2. \frac{d^2 y(t)}{dt^2} + 2 \frac{dy}{dt} + 4y(t) = 5x(t)$$

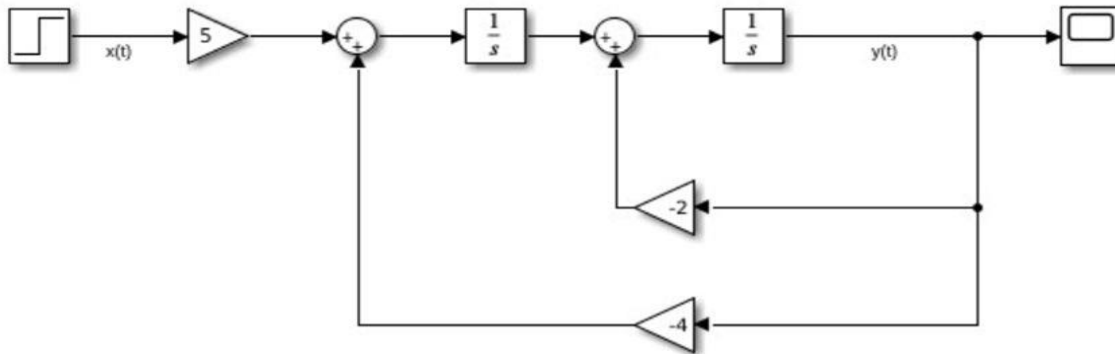
$$a_0 = 4, a_1 = 2, b_0 = 5$$

$$\frac{d^2 y(t)}{dt^2} + 2 \frac{dy}{dt} = \underbrace{5x(t) - 4y(t)}_{q_0}$$

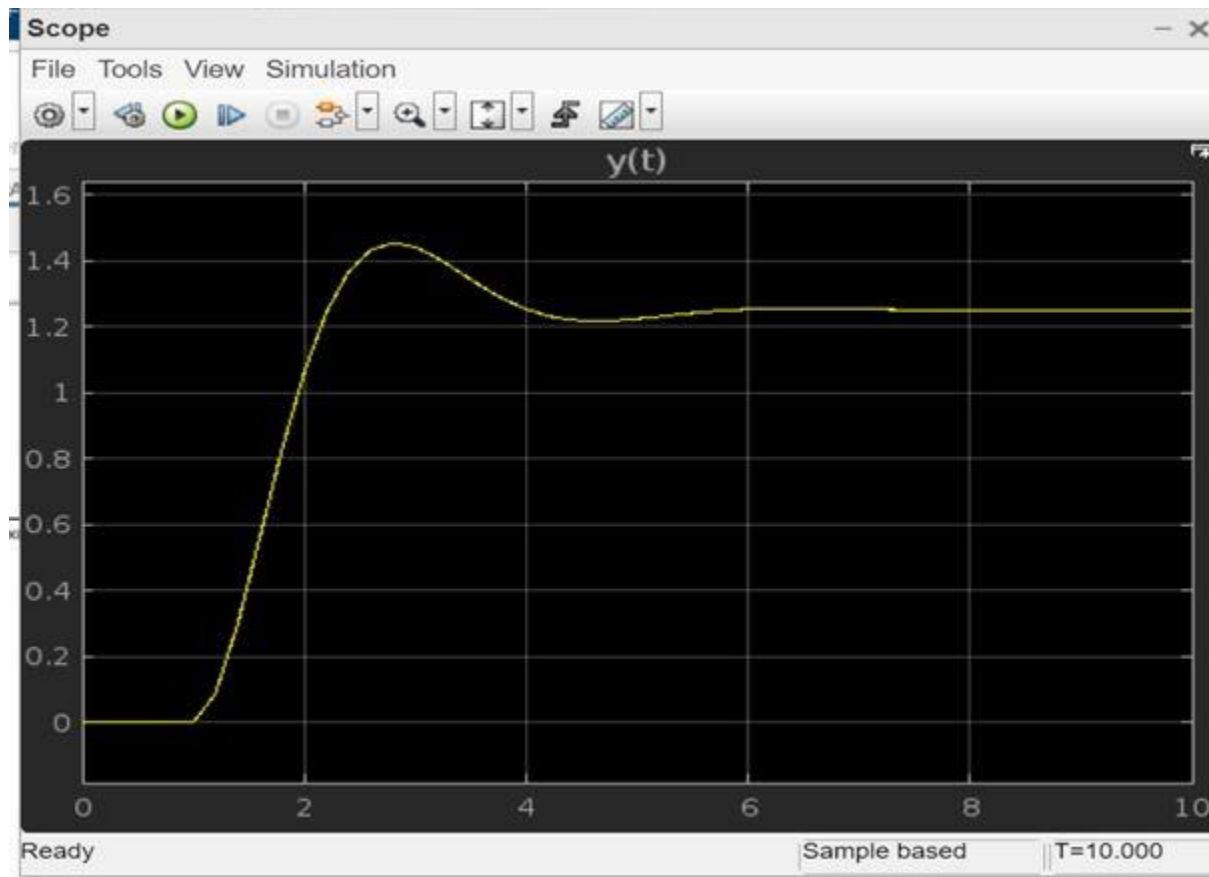
$$\frac{dy(t)}{dt} = \int \underbrace{q_0}_{q_1} - 2y(t)$$

$$y(t) = \int q_1$$

Simulation:



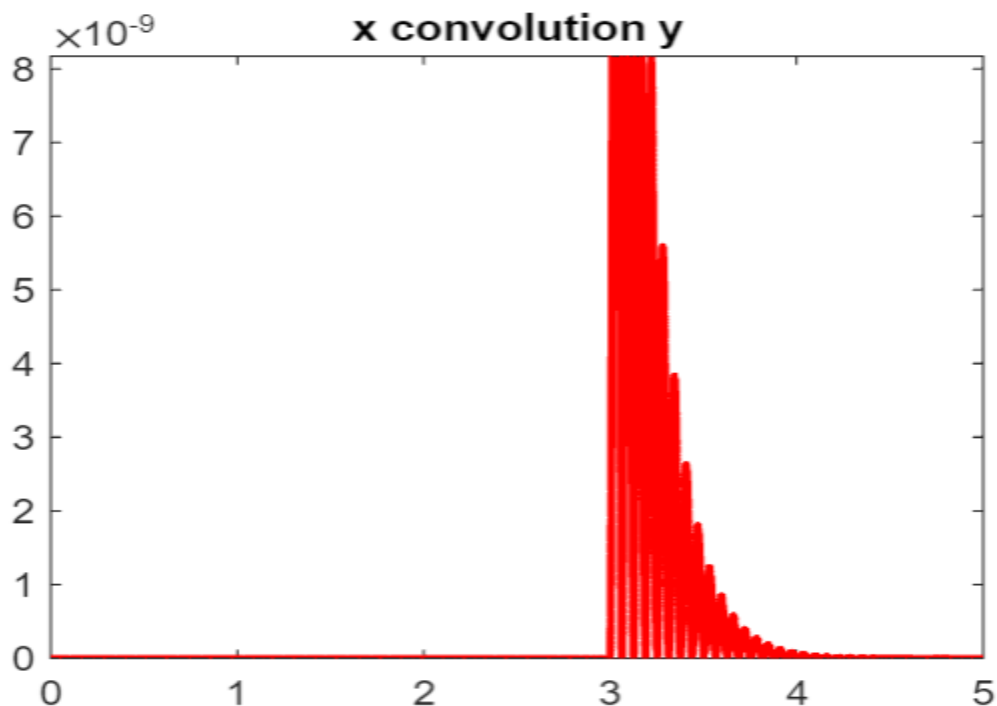
Graph:



Question VI: Write a program that computes and plots the convolution of the functions $x(t) = (10e^{-6t})\pi((t-2)/4)$, $y(t) = (10e^{-6t}\cos 100t)\pi((t-6)/6)$

>>Code and Graph:

```
1 clear all
2 close all
3 clc
4 syms toe t
5 x=10.*exp(-6*toe).*rectangularPulse(0,4,toe);
6 y=10.*exp(-6*(t-toe)).*cos(100*(t-toe)).*rectangularPulse(3,9,t-toe);
7 conv_ans=int(x*y,toe,-inf,inf)
8 fplot(conv_ans,[0 5],'r','LineWidth',2);
9 title('x convolution y');
10
```



>> Solution:

conv_ans =

$$\text{heaviside}(t-3) e^{-6t} (\sin(100t) - \sin(300)) - \text{heaviside}(t-9) e^{-6t} (\sin(100t) - \sin(900)) + \text{heaviside}(t-7) e^{-6t} (\sin(300) - \sigma_1)$$

where

$$\sigma_1 = \sin(100t - 400)$$

uz3a/matlab/matricesAndArraysGSEExample/matricesAndArraysGSEExample.mlx

$$000)) - \text{heaviside}(t-9) e^{-6t} (\sin(100t) - \sin(900)) + \text{heaviside}(t-7) e^{-6t} (\sin(300) - \sigma_1) - \text{heaviside}(t-13) e^{-6t} (\sin(900) - \sigma_1)$$

Question VII: Write a program that computes and plots the spectral representation of the function

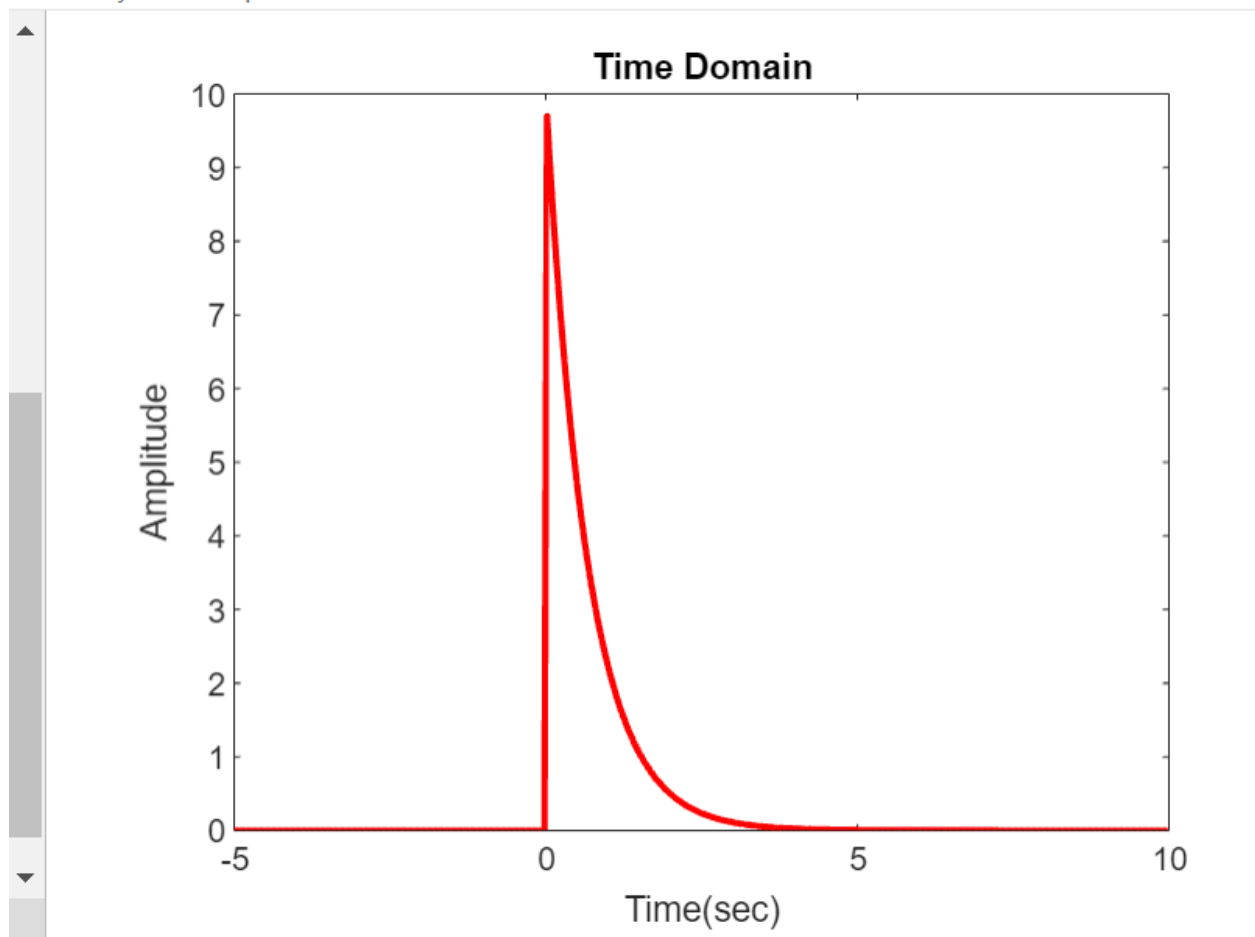
$$1-y(t) = (10e^{-(3/2)t})u(t)$$

>> Code:

```
1 clear all
2 close all
3 clc
4 Ts=1/50;
5 t=-5:Ts:10-Ts;
6 y=(10*exp(-(3/2)*t).*heaviside(t));
7 plot(t,y,'r','LineWidth',2);
8 xlabel('Time(sec)');
9 ylabel('Amplitude');
10 title('Time Domain');
11
12 y=fft(y);
13 fs=1/Ts;
14 f=(0:length(y)-1)*fs/length(y);
15 ymag=abs(y);
16 yphase=phasez(y);
17
18
19
```

```
15 ymag=abs(y);
16 yphase=phasez(y);
17
18
19
20 figure
21 plot(f,ymag,'r','LineWidth',2)
22 xlabel('Frequency (HZ)')
23 ylabel('Magnititude')
24 title('Magnititude')
25 n=length(y);
26 fshift=(-n/2:n/2-1)*(fs/n);
27 yshift=fftshift(y);
28
29 figure
30 plot(fshift,abs(yshift),'r','LineWidth',2);
31 xlabel('Frequency (HZ)')
32 ylabel('Phase')
33 title('Phase spectra')
34
```

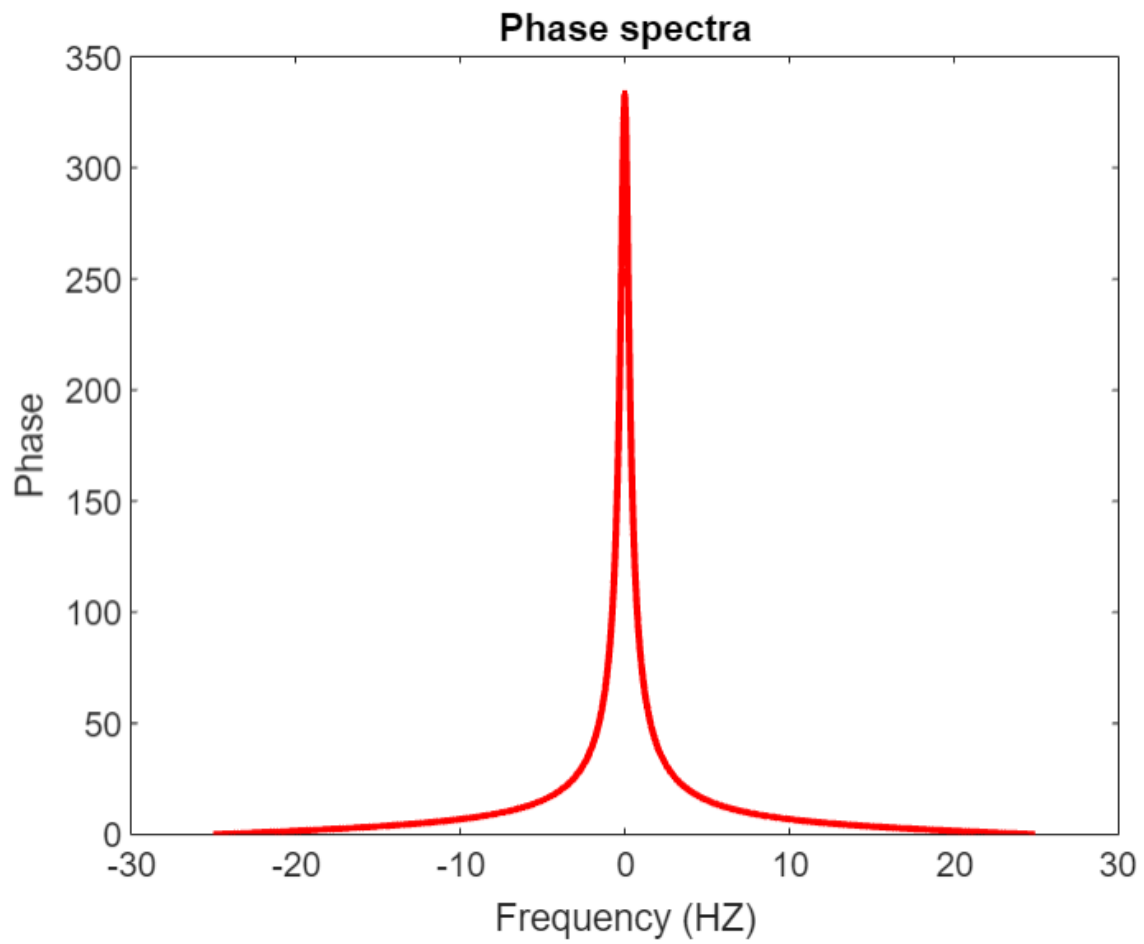
Graph 1:



www.sagepub.com/journalsPermissions.nav

Graph 3:

may300Example.mlx



3- $y(t) = (10e^{-0.5t} \cos 300t)u(t)$

>> Code:

```

1      clear all
2      close all
3      clc
4      Ts=1/20;
5      t=-5:Ts:10-Ts;
6      y=(10*exp((-0.5).*t).*cos(300*t)).*heaviside(t);
7      plot(t,y,'r','LineWidth',2);
8      xlabel('Time(Sec)');
9      ylabel('Amplitude');
10     title('Time Domain');
11     y=fft(y);
12     fs=1/Ts;
13     f=(0:length(y)-1)*fs/length(y);
14     ymag=abs(y);
15     yphase=phasez(y);
16     figure
17     n=length(y);
18     fshift=(-n/2:n/2-1)*(fs/n);
19     yshift=fftshift(y);
20     plot(fshift,ymag,'r','LineWidth',2);
21     xlabel('Frequency(HZ)');
22     ylabel('Magnitude');

```

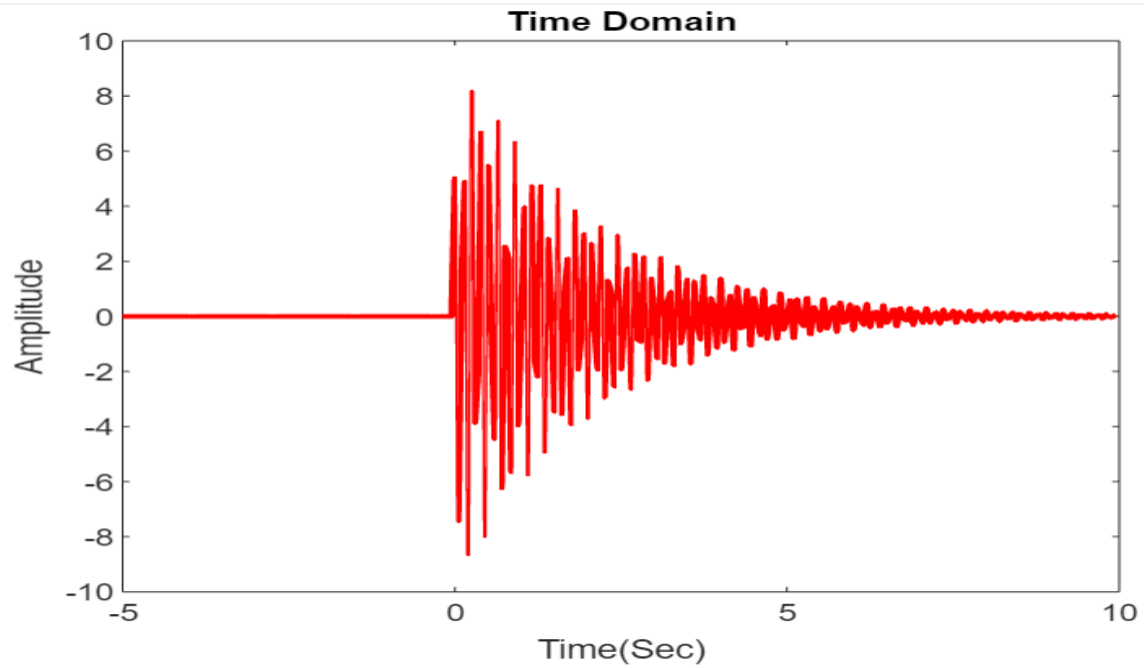
```

10     title('Time Domain');
11     y=fft(y);
12     fs=1/Ts;
13     f=(0:length(y)-1)*fs/length(y);
14     ymag=abs(y);
15     yphase=phasez(y);
16     figure
17     n=length(y);
18     fshift=(-n/2:n/2-1)*(fs/n);
19     yshift=fftshift(y);
20     plot(fshift,ymag,'r','LineWidth',2);
21     xlabel('Frequency(HZ)');
22     ylabel('Magnitude');
23     title('Magnitude');
24     figure
25     plot(fshift,abs(yshift),'r','LineWidth',2);
26     xlabel('Frequency(HZ)');
27     ylabel('Phase');
28     title('Phase spectra');
29
30

```

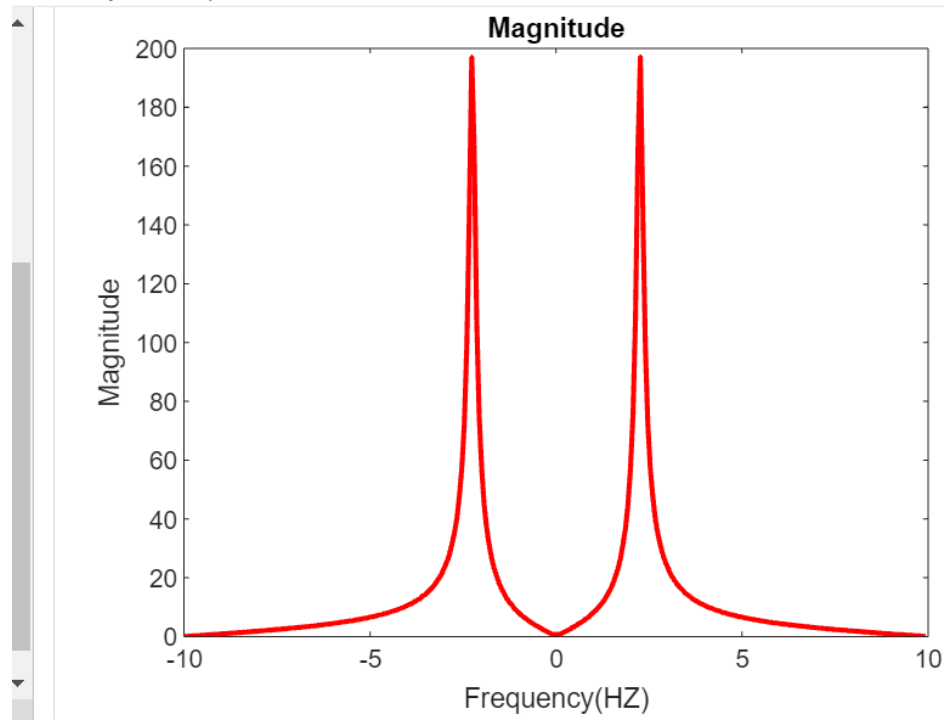
Graph 1:

esAndArraysGSEExample.mlx



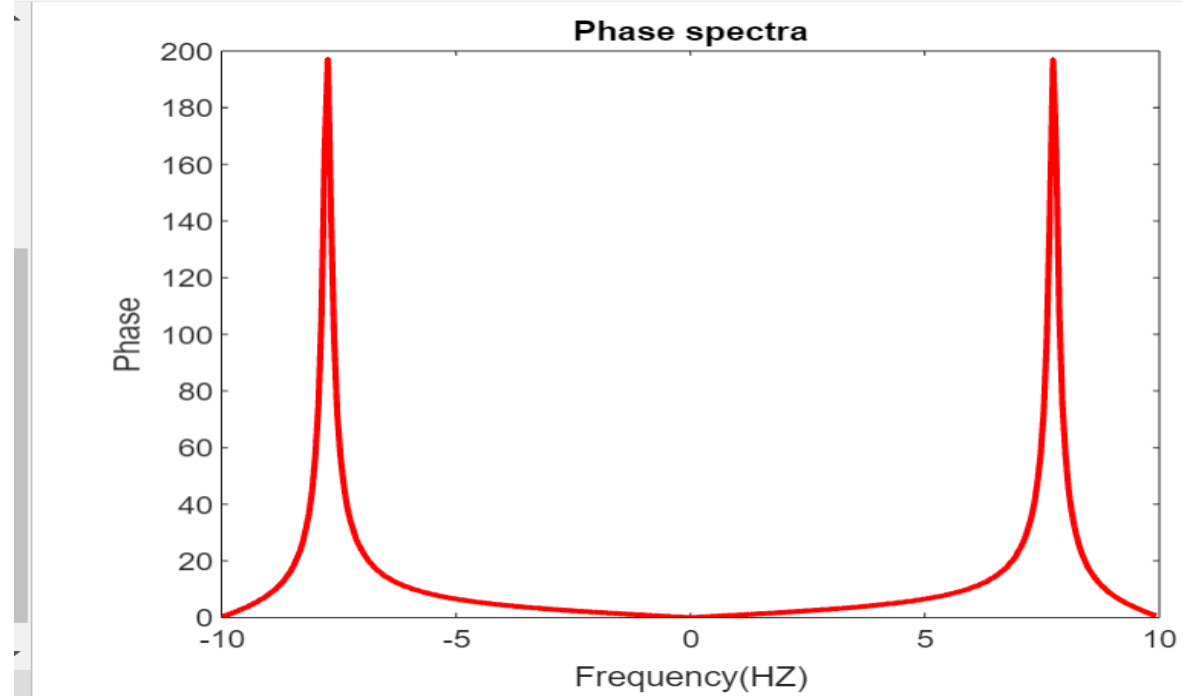
Graph 2:

esAndArraysGSEExample.mlx



Graph 3:

»sAndArraysGSEExample.mlx



Question VIII: Write a program that computes the Laplace transform of the function.

$$3-y(t) = (15 - 15e^{-0.25t})u(t)$$

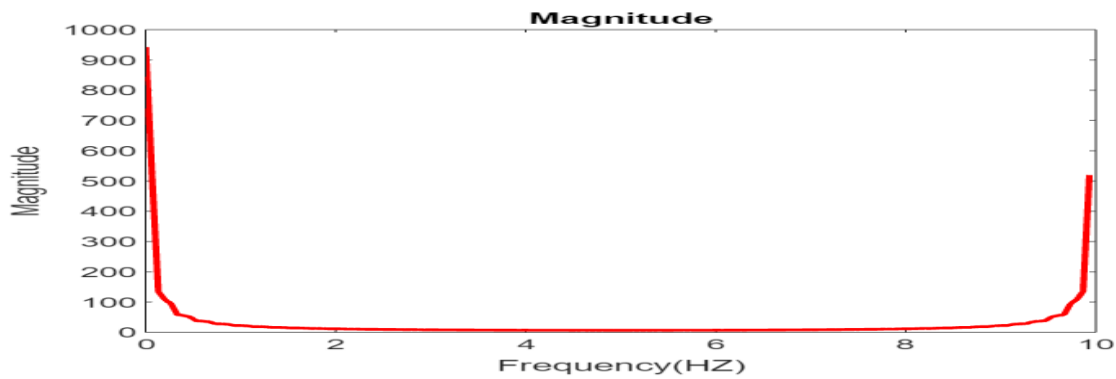
>> Code:

```
1 clear all
2 close all
3 clc
4 syms t1;
5 y=(15-15*exp((-0.25).*t1)).*heaviside(t1);
6 syms f;
7 yf=fourier(y,f);
8 syms s;
9
10 ys=laplace(y,s)
11 Ts=1/10;
12 t=-5:Ts:10-Ts;
13 y=(15-15*exp((-0.25).*t)).*heaviside(t);
14 y=fft(y);
15 fs=1/Ts;
16 f=(0:length(y)-1)*fs/length(y);
17 ymag=abs(y);
18 yphase=phasez(y);
19
20 figure
21 plot(f,ymag,'r','LineWidth',2);
```

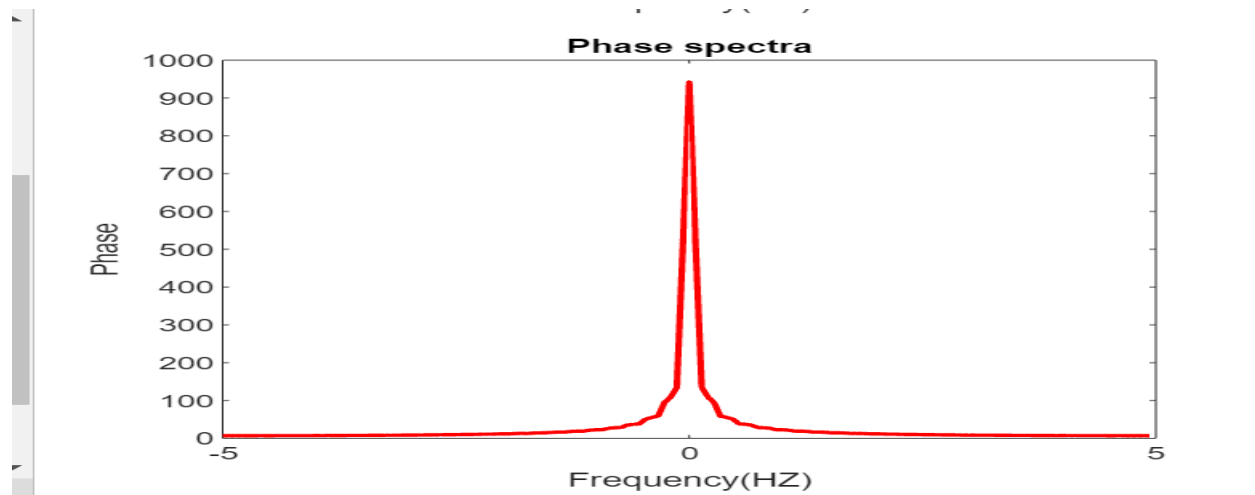
/MATLAB Drive/Examples/R2023a/matlab/MatricesAndArraysGSEExample/MatricesAndArraysGSEExample.mlx

```
15 fs=1/Ts;
16 f=(0:length(y)-1)*fs/length(y);
17 ymag=abs(y);
18 yphase=phasez(y);
19
20 figure
21 plot(f,ymag,'r','LineWidth',2);
22 xlabel('Frequency(HZ)');
23 ylabel('Magnititude');
24 title('Magnititude');
25 n=length(y);
26 fshift=(-n/2:n/2-1)*(fs/n);
27 yshift=fftshift(y);
28
29 figure
30 plot(fshift,abs(yshift),'r','LineWidth',2);
31 xlabel('Frequency(HZ)');
32 ylabel('Phase');
33 title('Phase spectra');
34
35
```


Graph 1:



Graph 2:



Lablase transform:

$$y_s = \frac{15}{s} - \frac{15}{s + \frac{1}{4}}$$

Fourier transform:

$$y_f = 30\pi\delta(f) - \frac{15}{\frac{1}{4} + fi}$$

$$4-y(t) = (20 - 8e^{-3t} \cos 100t)u(t)$$

>> Code:

MatricesAndArraysGSEExample.mlx
/MATLAB Drive/Examples/R2023a/matlab/MatricesAndArraysGSEExample/MatricesAndArraysGSEExample.mlx

```

1      syms t1;
2      y=(20-(8*exp(-3*t1)).*cos(100*t1)).*heaviside(t1);
3      syms f;
4      yf=fourier(y,f);
5
6      syms s;
7      ys=laplace(y,s);
8
9      Ts=1/5;
10     t=0:Ts:10-Ts;
11     y=(20-(8*exp(-3*t)).*cos(100*t)).*heaviside(t));
12     plot(t,y,'r','LineWidth',2);
13     xlabel('Frequency(HZ)');
14     ylabel('Phase');
15     title('Phase spectra')
16
17
18     y=fft(y);
19     fs=1/Ts;
20     f=(0:length(y)-1)*fs/length(y);
21     ymag=abs(y);

```

```

y=fft(y);
fs=1/Ts;
f=(0:length(y)-1)*fs/length(y);
ymag=abs(y);
yphase=phasez(y);

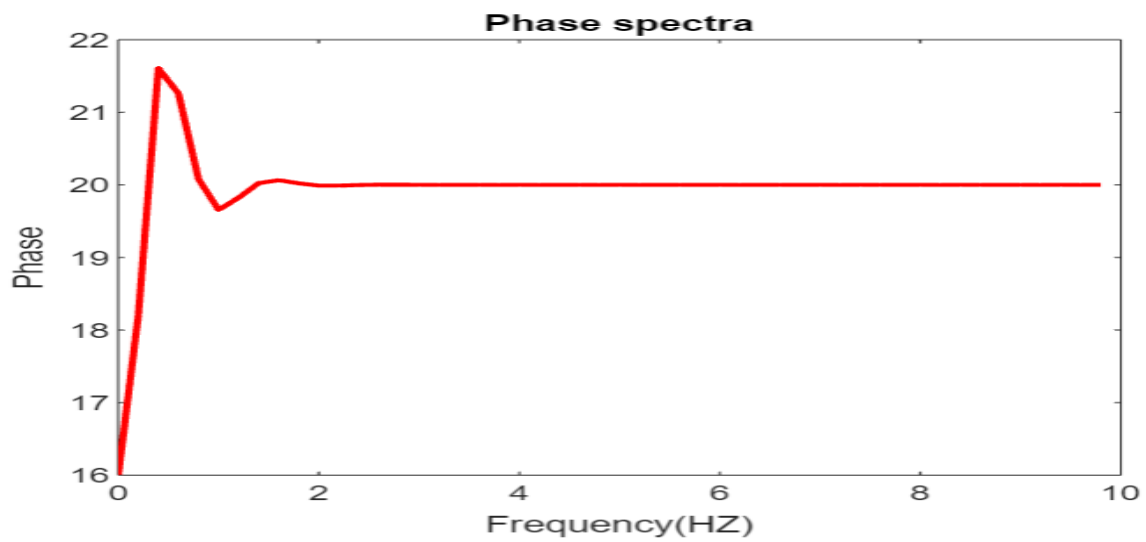
figure
plot(f,ymag,'g','LineWidth',2);
xlabel('Frequency(HZ)');
ylabel('Magnititude');
title('Magnititude');

n=length(y);
fshift=(-n/2:n/2-1)*(fs/n);
yshift=fftshift(y);

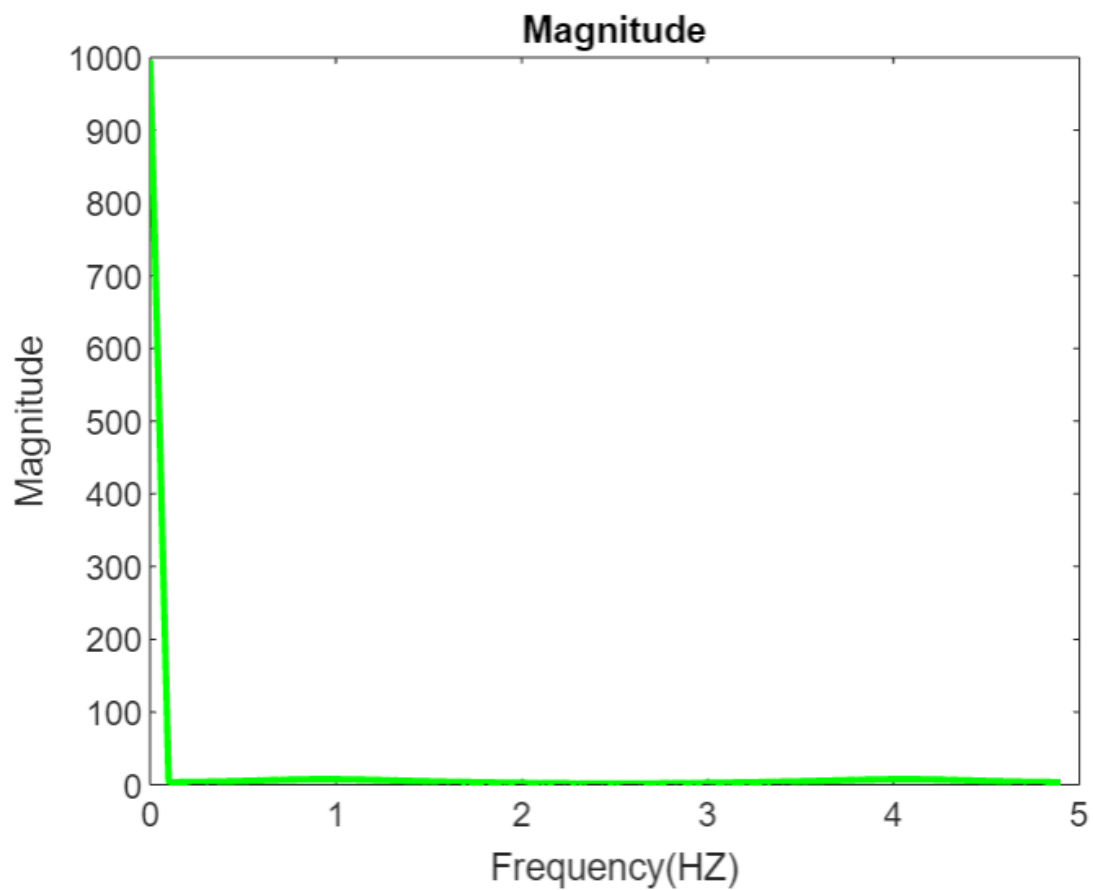
figure
plot(fshift,abs(yshift),'r','LineWidth',2);
xlabel('Frequency(HZ)');
ylabel('Magnititude');
title('Magnititude');

```

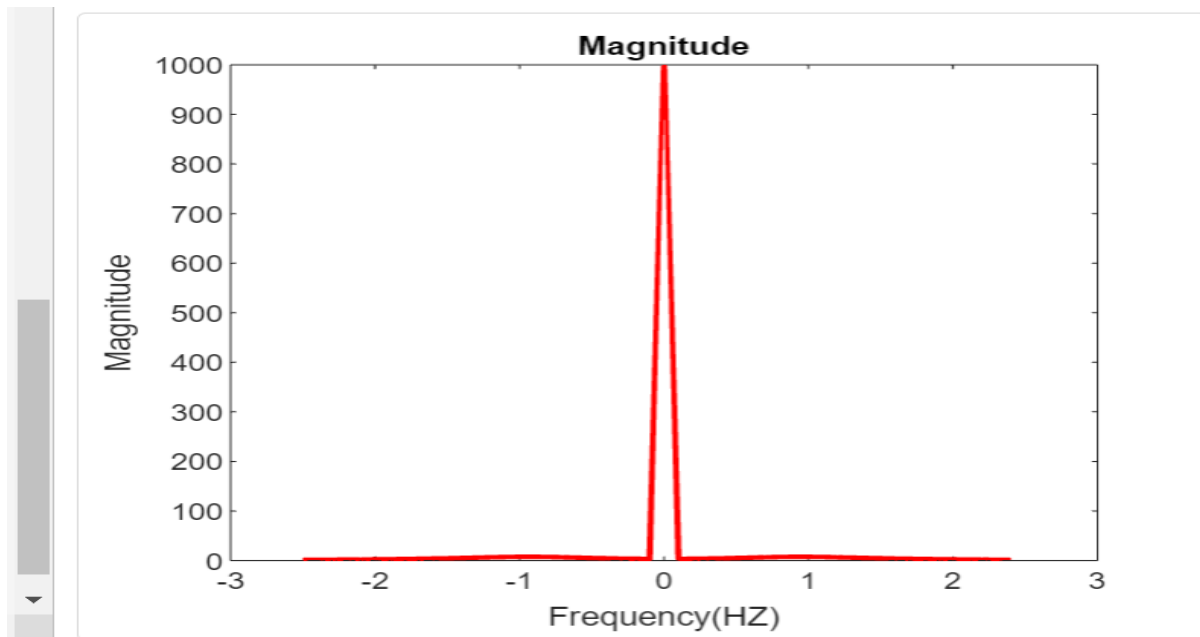
Graph 1:



Graph 2:



Graph 3:



Lablase transform:

$$y_s = \frac{20}{s} - \frac{8(s+3)}{(s+3)^2 + 10000}$$

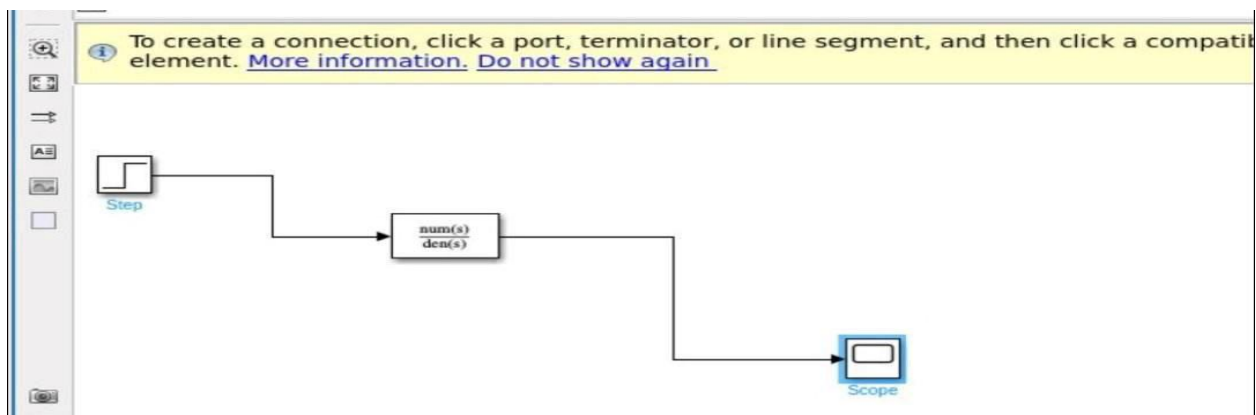
Fourier transform:

$$y_f = 20\pi\delta(f) - \frac{4}{f i + 3 - 100 i} - \frac{4}{f i + 3 + 100 i} - \frac{20 i}{f}$$

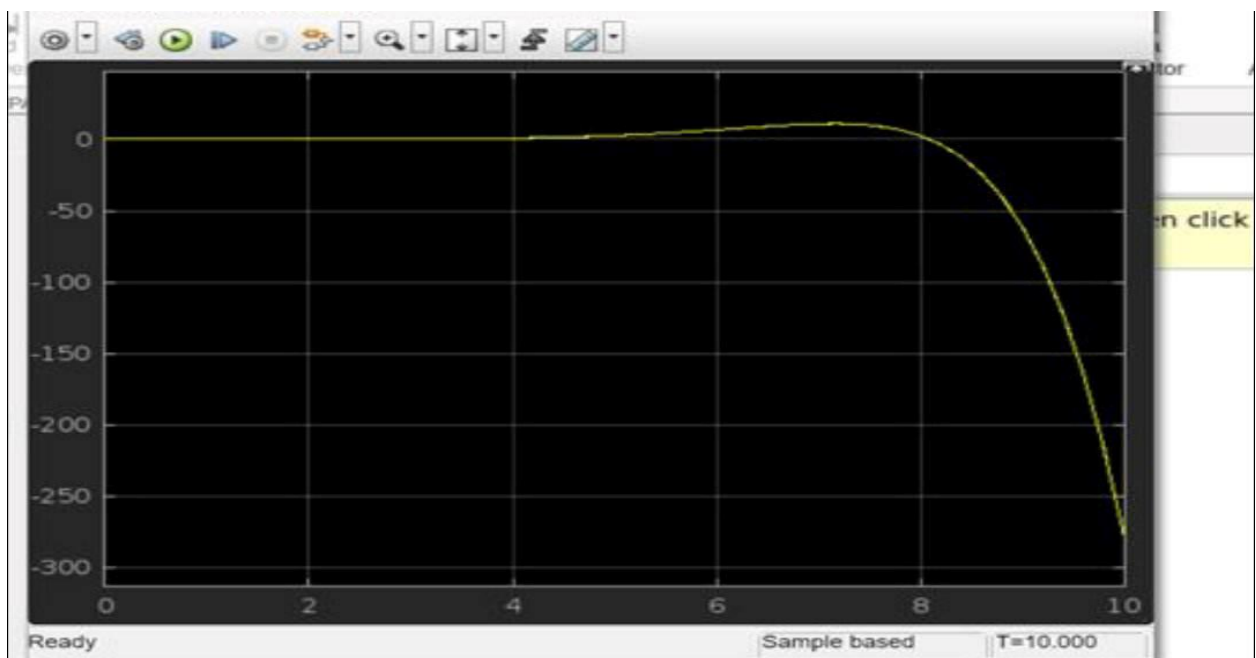
Question IX: Use Simulink (MATLAB) to simulate the following systems in Laplace domain then show and plot the step response of the system.

$$6 \frac{d^4 y(t)}{dt^4} - 7 \frac{d^2 y(t)}{dt^2} + \frac{dy(t)}{dt} + 9y(t) = \frac{d^3 x(t)}{dt^3} +$$

Simulation:



Graph :



Question X: Write a program that determine the inverse Laplace transform of the transfer functions in IV.

>>Code and soluation:

```
1  syms s t y;
2  H1=(7/(s+2));
3  H2=(5/(s^2+(4*s)+5));
4
5  h1=ilaplace(H1,s,t);
6  h2=ilaplace(H2,s,t);
7
8  disp('Inverse Laplace Transform of H1:');
9  disp(h1);
10
11 disp('Inverse Laplace Transform of H2:');
12 disp(h2);
```

Inverse Laplace Transform of H1:
 $7e^{-2t}$

Inverse Laplace Transform of H2:
 $5e^{-2t}\sin(t)$

Question XII: Consider the transfer function: $H(s) = \frac{10000s + 3}{s^2 + 6s + 8}$

- Compute the step response of the system.
- Plot the frequency response (semi-log scale) of the system with transfer function

