

# **Report 01**

## **DC Motor Model**

MCT 621

Motion Control and Servo Systems

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Submitted By/

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# Introduction

DC motor Simulink Block is generated in this report according to equations. The block is having 2 inputs which are voltage and load torque. And one output which is its angular velocity.

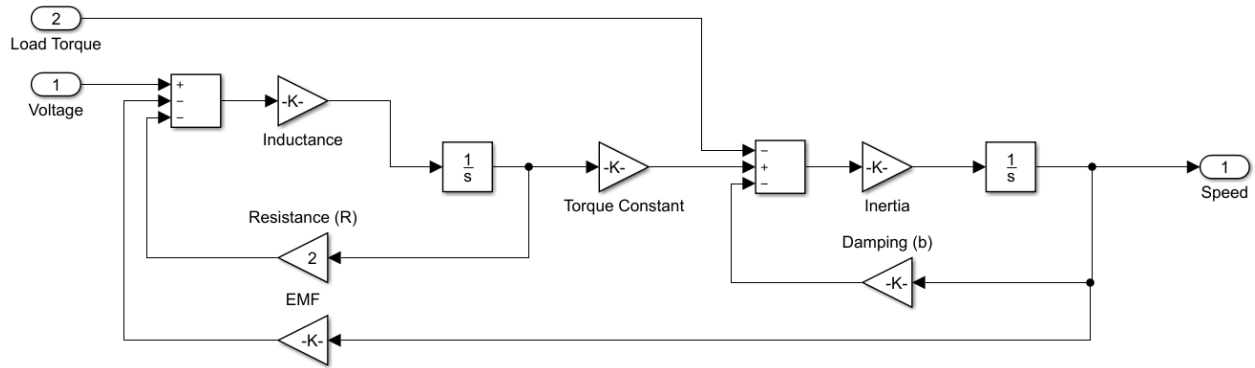
## Equations

A linear model of permanent magnet (PM) DC motor can be represented by their mechanical equation and electrical equation as follows.

$$v_a = L_a \frac{dI_a}{dt} + R_a I_a + e_b$$

$$K_m I_a = J_m \frac{d\omega_m}{dt} + B_m \omega_m + T_L$$

where  $v_a$  is the applied armature input voltage,  $e_b = K_b \omega_m$  is the back electro-motive-force (EMF) voltage,  $I_a$  is the armature current  $T_L$  is the load torque and  $\omega_m$  is the rotor angular speed. The dynamic model of the system is formed using these differential equations and Matlab simulink blocks as shown in following pages. The armature reactions effects are neglected since the motor used has either inter-poles or compensating winding.

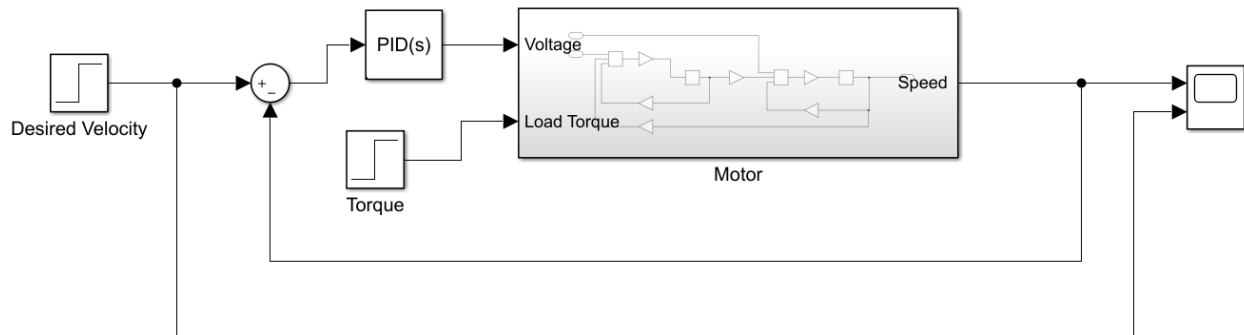


## Used Parameters

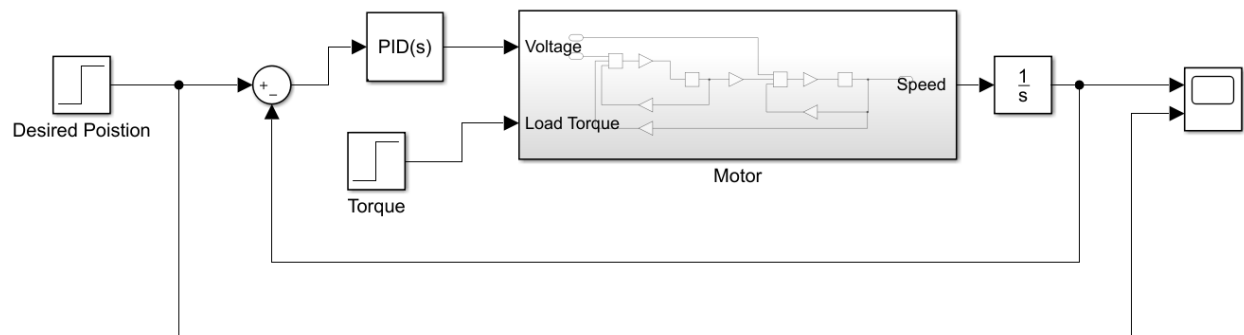
Parameter	Symbol	Value
Moment of Inertia	$J_m$	$0.000052 \text{ Kg.m}^2$
Friction Coefficient	$B_m$	$0.01 \text{ N.ms}$
Back EMF Constant	$K_b$	$0.235 \text{ V/ms}^{-1}$
Torque Constant	$K_t$	$0.235 \text{ Nm/A}$
Electric Resistance	$R_a$	$2 \Omega$
Electric Inductance	$L_a$	$0.23 \text{ H}$

# Ideal Closed Loop Control Block Diagram

## 1. Velocity



## 2. Position



# Tuned PID Parameters

## Velocity

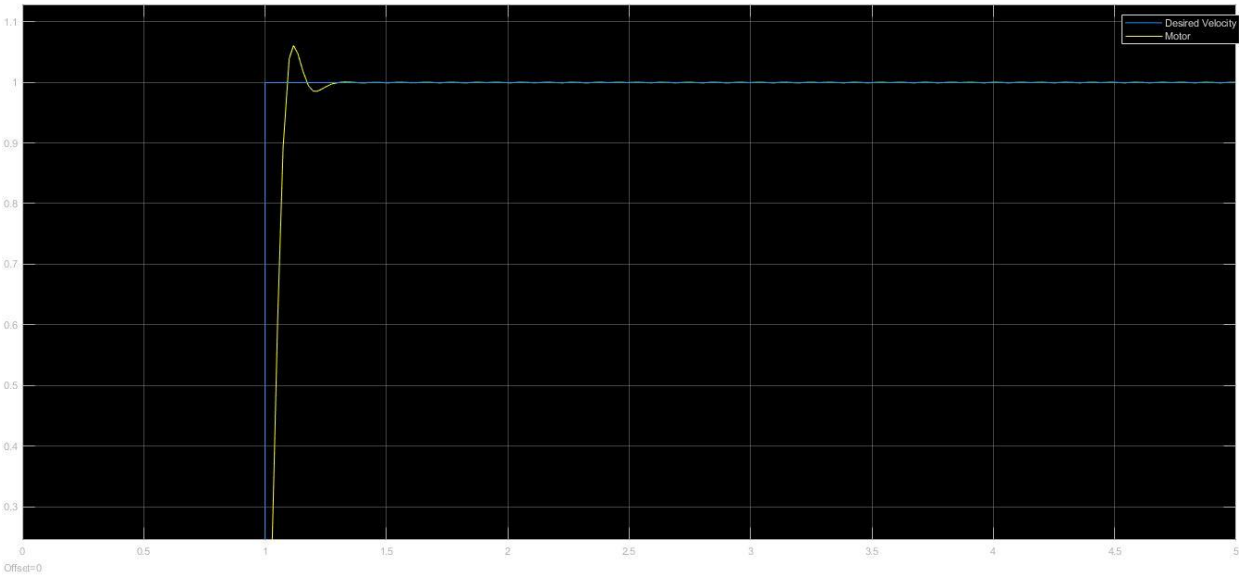
Parameter	Symbol	Value
Proportional	P	0.135543358908684
Integrator	I	8.75873319223285
Derivative	D	-0.00291149276467624

## Position

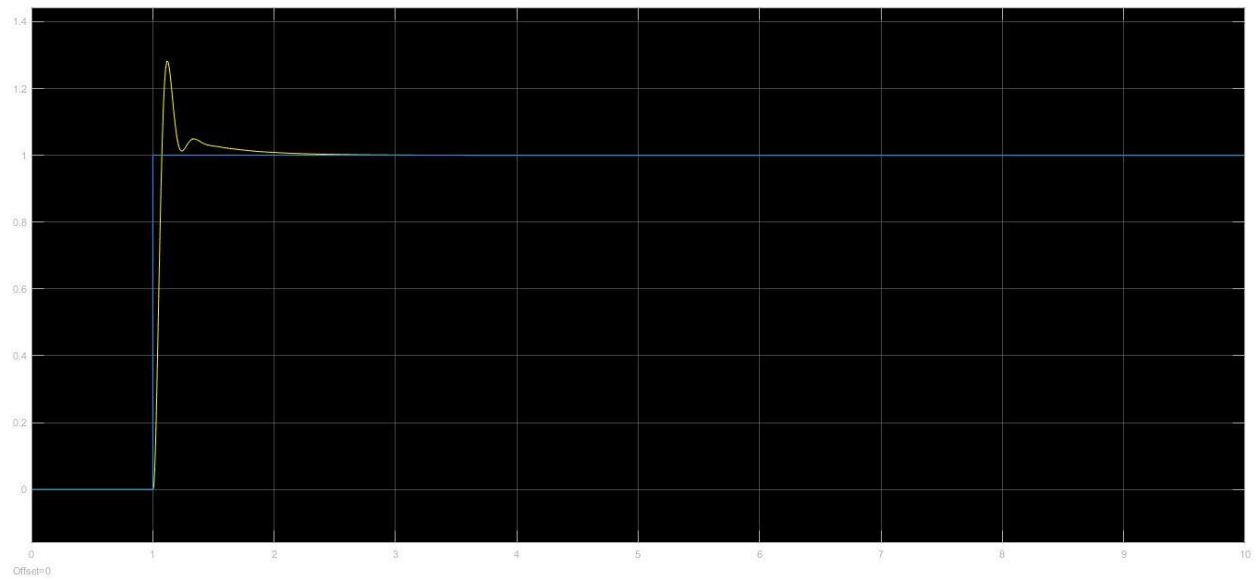
Parameter	Symbol	Value
Proportional	P	8.87419991192869
Integrator	I	19.9549307770635
Derivative	D	-0.00329477712149354

# Results

## Velocity



## Position



## Conclusion

The Tuned PID controller for the given motor in the ideal case outputs a smooth results in both position and velocity manners.