16th AIMMS-MOPTA Optimization Modeling Competition Report

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Executive Summary

In this report, we present our solution to the 16th AIMMS-MOPTA Optimization Modeling Competition on whether a fully renewable energy grid would benefit from adding green hydrogen as a supplemental flexible source to the power generation.

We propose a two-stage stochastic optimization model where investment decisions in renewable plants and hydrogen storage are minimized in the first stage, and operational costs of running the hydrogen storage systems in the second stage. This model accounts for uncertainties in both solar and wind generation.

All in all, the results in this report show that there is potential in green hydrogen as a source of baseload support in the transition to a fully renewable-powered energy grid. For the data considered, we see that a fully-renewable network driven by green hydrogen has a greater potential to succeed under realities where wind generation is high. In addition, we note that the main driver for the potential and profitability of green hydrogen lies in the electricity demand and prices, as opposed to those for gas. Finally, we conclude that the investment in long-term liquid hydrogen storage is more valuable for taking full advantage of hydrogen as a baseload source than that in shorter-term intraday hydrogen gas storage.

For future work, we suggest a further exploration of uncertainties, by using more accurate scenarios for the wind and solar generation, or by considering other sources of uncertainty, such as the residential demand patterns or variability of technology investment costs. Lastly, a more extensive long-term analysis of the green hydrogen viability could be carry by studying the impact of expected technology cost reductions overtime, performing further sensibility analyses, and computing net discounted present value for the long-term investments.

This report has the following structure. In Section 1, we describe the motivation this work on the study of hydrogen storage as a complementary electrical and gas supply source to ensure the liability and resilience of the energy grid. On Section 2, we explain the modeling approach used to formulate the problem, as well as describe the data used and user interface developed. Then, in Section 3, we present the solution of a minimum non-trivial solution, we analyze the economics of the loss of load, and discuss the current viability green hydrogen. Finally, the main conclusions and future work are described in Section 4.

1 Motivation

In pursuit of decarbonization goals, it becomes imperative to integrate renewable energy technologies into energy grids at a large scale. However, an important challenge arises concerning the stability of the energy grid's baseload. This baseload stability can not be provided consistently by renewable sources', due to their dependence on the weather and uncertain generation. Thus, the transition towards decarbonization needs a departure from coal and natural gas as baseload supporters. This creates the challenge of finding flexible green sources that would allow the power network to work continuously and safely by offering baseload support.

The operation of a fully-renewable energy grid needs a reliable energy source and storage to provide a continuous supply of energy to the grid. Green hydrogen emerges as a promising candidate, not only for decarbonizing big industries gas demand, but also for offering baseload power. Stored hydrogen as compressed gas or liquid can either be converted back to electricity or used as feedstock for industry, or as fuel for vehicles.

In the remainder of this section, we briefly describe the problem that we propose solving, why it is a relevant problem, and detail some other pieces of work which have studied it.

1.1 Problem Description

In order to study the viability of green hydrogen, we want to find the optimal renewable mix of solar and wind power to be built, such that the electricity and gas demands are met, using hydrogen as a means to store energy in a fully renewable system. In order to achieve this, we assume that relying on electricity from other power sources, such as coal and natural gas, is not a possibility. Therefore, one of the main questions of the problem is how much long- and short-term hydrogen energy storage is needed and how much this set-up will cost.

In our work, we consider an energy grid as presented in Figure 1 with 7 different types of location: solar and wind plants, hydrogen systems such as electrolyzers, tanks and fuel cells, and industrial and residential demand areas. Solar and wind power plants provide the generation, and they can supply the demand locations, both industry and residential areas, directly or feed into the electrolyzer to convert the electricity into hydrogen gas. Hydrogen gas can be stored for intraday use only. It can used to meet the gas demand in the industry sectors, or it can be liquefied and stored in long-term storage tanks. Later, this liquid hydrogen can be converted back into electricity using the fuel cell to meet demand and offer baseload support.

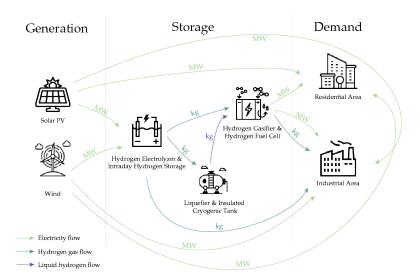


Figure 1: Scheme of the types of locations and energy flows in the network considered.

The goal of the problem is to determine how much electricity needs to be injected into the energy grid to meet demand during a given period. It is essential that the electricity and gas demand is matched precisely with the supply, as deviations from this could severely damage the

grid infrastructure or cause blackouts. For this, an optimization model was used to solve the problem whilst incorporating all the features of an integrated and fully renewable energy system, for both gas and electricity simultaneously, as green hydrogen can be a source of either.

1.2 Background

As previously mentioned, hydrogen energy storage systems can help renewable energy sources overcome the challenges associated with higher penetrations of wind and solar power [1, 15]. In periods of excess generation, electricity can be converted into green hydrogen and stored as a compressed gas or liquid for later use. The hydrogen stored can be converted back into electricity in times of supply shortage [12, 16]. Especially for tactical decisions that span multiple days, weeks, or months, as is the case for this study, hydrogen storage can be attractive.

The efficiency of the hydrogen conversion from and to electricity is one of the drawbacks of this technology. For example, the electrolyzer efficiency varies with input power, and according to [5], it should be operated with constant input power corresponding to max efficiency to minimize losses. Also, even though there is almost no loss of stored hydrogen, the total energy loss in a hydrogen system used for storing electricity is substantial, in particular when compared to battery systems. The authors explain that typical efficiencies for electrolyzers are in the range of 60-80%, and typical efficiencies for fuel cells are in the range of 40-60%. In summary, around 54 to 72% of electric energy is lost in the electrolyzer and fuel cell combined, and in addition to this, you lose about 20% of the energy if hydrogen is stored as high-pressure gas, and 25-45% if it is stored as liquid hydrogen. Therefore, these concerns should be taken into account in future work.

Furthermore, the authors propose a solution for the loss of efficiency: a hybrid energy storage system where hydrogen storage is combined with batteries and supercapacitors as a possible third component to handle extremely rapid and large power fluctuations (if there are any). Since batteries are very suitable for short-term energy storage and hydrogen for long-term storage, the two technologies combine well in a system where batteries can deal with high-frequency fluctuations in power demand and hydrogen handles the remaining low-frequency fluctuations [5].

On the other hand, an investment model with uncertain information, like the renewable generation in this case, is normally approached using a two-stage stochastic model, where the first stage minimizes the investment decisions and the second stage deals with the operational side of the problem [10, 13]. There are some works that use this technique for hydrogen storage. Namely, the authors in [7] take the investment decisions in the first stage, and operational decisions for minimizing CO2 emissions in the second. In [11], a risk averse two-stage stochastic model is used, with the decisions on transactions with bilateral electrical contracts as the first-stage decision variables and the other decision variables taken in the second stage, using uncertain demand and electricity prices in the day-ahead market.

2 Our Approach

In this section, we detail the formulation developed to tackle this problem, detail how the data input used in our computational experiments was created, and how our user interface can be used to further study the potential of green hydrogen for different realities.

2.1 Modelling Approach

In order to study the problem described in Section 1.1, we developed a 2-stage stochastic mixed-integer linear optimization program. We have chosen a stochastic model to account for the uncertainties in renewable generation and opted for a 2-stage model to capture both the impact of the strategic investment decisions and of the operational grid flows on the total costs.

Below, we briefly introduce the optimization model that was developed. A complete list of the notation used, the corresponding description, and units can be found in Appendix A. First, in the objective function, we minimize the first-stage investment costs in renewable plants and storage

technologies:

$$\sum_{i \in \mathcal{V}^S} B_i^S b_i^S + \sum_{i \in \mathcal{V}^W} B_i^W b_i^W + \sum_{i \in \mathcal{V}^E} B_i^G y_i^G + \sum_{i \in \mathcal{V}^T} B_i^L y_i^L$$
 (1)

as well as the second-stage expected operational costs for using the available storage:

$$\sum_{s \in \mathcal{S}} w_s \left(\sum_{\substack{i \in \mathcal{V}^E \\ t \in \mathcal{T}}} C^G s_{i,t,s}^G + \sum_{\substack{i \in \mathcal{V}^T \\ t \in \mathcal{T}}} C^L s_{i,t,s}^L \right)$$
 (2)

where b_i^S (respectively b_i^W) is the number of rows of solar plants (resp. wind turbines) to be built at candidate location i where a solar (resp. wind) plant can be built. The parameters B_i^S and B_i^W are the associated costs of building a row of solar panels and wind turbines, respectively. Similarly, the variables y_i^G and y_i^L denote the number of intraday gas storage tanks and of long-term liquid hydrogen tanks to be built, respectively, and B_i^G and B_i^L the associated investment costs. In the second-stage objective term, we consider an average of operation cost weighted on each renewable generation scenario $s \in \mathcal{S}$ according to the weight w_s . The operational costs account for the cost of storage, where $s_{i,t,s}^G$ and $s_{i,t,s}^L$ are the amount of hydrogen gas and liquid hydrogen stored at location i, at time period t, respectively, and C^G and C^L are the associate costs.

Most of our constraints concern flow balance equations that ensure a feasible flow of electricity and gas through the energy grid under all generation scenarios over the time horizon considered. In particular, these flows ensure that the demand of residential and industrial areas is met in a way that guarantees the loss of load doesn't exceed a maximum as:

$$\sum_{i \in \mathcal{V}} f_{j,i,t,s}^{E} = D_{i,t}^{E} - u_{i,t,s}^{E} \qquad \forall i \in \mathcal{V}^{I} \cup \mathcal{V}^{R}, t \in \mathcal{T}, s \in \mathcal{S}$$
 (3)

$$\sum_{i \in \mathcal{V}} f_{j,i,t,s}^G = D_{i,t}^G - u_{i,t,s}^G \qquad \forall i \in i \in \mathcal{V}^I, t \in \mathcal{T}, s \in \mathcal{S}$$
 (4)

$$\sum_{i \in \mathcal{V}^I \bigcup \mathcal{V}^R} u_{i,t,s}^E \le L^E \left(\sum_{i \in \mathcal{V}^I \bigcup \mathcal{V}^R \atop t \in \mathcal{T}} D_{i,t}^E \right) \qquad \forall s \in \mathcal{S}$$
 (5)

$$\sum_{\substack{i \in \mathcal{V}^I \\ t \in \mathcal{T}}} u_{i,t,s}^G \le L^G \left(\sum_{\substack{i \in \mathcal{V}^I \\ t \in \mathcal{T}}} D_{i,t}^G \right) \qquad \forall s \in \mathcal{S}$$
 (6)

where constraints (3) and (4) ensure that the electricity and gas that flows into demand areas meets the electricity demand $D_{i,t}^E$ and the gas demand $D_{i,t}^G$, respectively. These equations allow for losing electricity and gas demand through the loss of load variables $u_{i,t,s}^E$ and $u_{i,t,s}^G$, respectively. Constraints (5) and (6) ensure that the percentage of loss of load does not exceed L^E and L^G for electricity and gas, respectively.

Furthermore, we consider flow balance for the other types of locations in our network, namely renewable plants (Equation (7)), electrolyzers (Equation (8)), liquid hydrogen tanks (Equation (9)), and fuel cells (Equation (10)).

$$G_{i,t,s}^{S} \boldsymbol{b}_{i}^{S} + G_{i,t,s}^{W} \boldsymbol{b}_{i}^{W} = \sum_{i \in \mathcal{V}} f_{i,j,t,s}^{E} + a_{i,t,s} \qquad \forall i \in \mathcal{V}^{S} \cup \mathcal{V}^{W}, t \in \mathcal{T}, s \in \mathcal{S}$$
 (7)

$$\sum_{j \in \mathcal{V}} f_{j,i,t,s}^E = \eta_i^E U^{EG} \left(\sum_{j \in \mathcal{V}} f_{i,j,t,s}^G + c_{i,t,s}^G - d_{i,t,s}^G \right) \qquad \forall i \in \mathcal{V}^E, t \in \mathcal{T}, s \in \mathcal{S}$$
 (8)

$$\sum_{j \in \mathcal{V}} f_{j,i,t,s}^G = \eta_i^T U^{GL} \left(\sum_{j \in \mathcal{V}} f_{i,j,t,s}^L + c_{i,t,s}^L - d_{i,t,s}^L \right) \qquad \forall i \in \mathcal{V}^T, t \in \mathcal{T}, s \in \mathcal{S}$$
 (9)

$$\eta_i^F \left(\sum_{j \in \mathcal{V}} f_{j,i,t,s}^G + U^{GL} \sum_{j \in \mathcal{V}} f_{j,i,t,s}^L \right) = \sum_{j \in \mathcal{V}} f_{i,j,t,s}^G + \frac{1}{U^{EG}} \sum_{j \in \mathcal{V}} f_{i,j,t,s}^E$$

$$\forall i \in \mathcal{V}^F, t \in \mathcal{T}, s \in \mathcal{S}$$

$$(10)$$

where $f_{i,j,t,s}^E$, $f_{j,i,t,s}^G$ and $f_{i,j,t,s}^L$ represent the flow of electricity, hydrogen gas and liquid hydrogen between locations i and j at time period t under scenario s, respectively.

In constraint (7), we ensure that the solar $G_{i,t,s}^S$ and wind $G_{i,t,s}^W$ electricity generated scaled

In constraint (7), we ensure that the solar $G_{i,t,s}^S$ and wind $G_{i,t,s}^W$ electricity generated scaled to the installed capacity $(b_i^S \text{ and } b_i^W)$ flows into any of the locations connected to the renewable plants or is spilled $(a_{i,t,s})$.

Constraint (8) states that each unit of electricity that flows into an electrolyzer is converted into U^{EG} units of hydrogen gas, and this electrolysis process has an efficiency of η_i^E . Note that here we account for the flows of hydrogen gas going into and out of the intraday gas storage (located at electrolyzer locations) with variables $c_{i,t,s}^G$ and $d_{i,t,s}^G$, respectively.

In an analogous way, constraint (9) ensures that each unit of hydrogen gas that flows into a

In an analogous way, constraint (9) ensures that each unit of hydrogen gas that flows into a tank location is converted into U^{GL} units of liquid hydrogen, and this liquefaction process has an efficiency of η_i^T . This is achieved while accounting for the flows of liquid hydrogen being charged and discharged from the hydrogen tank storage with variables $c_{i,t,s}^L$ and $d_{i,t,s}^L$, respectively.

Lastly, in constraint (10), we enforce that the flows of liquid and gas hydrogen going into the fuel cell match the flows of hydrogen gas and electricity going out, where η_i^F is the efficiency of the gasification process.

In addition, we consider constraints (11)-(14) to keep track of the state of charge of the intraday hydrogen gas storage and of long-term hydrogen tanks. These constraints are modeled using the linear DC flow equations.

$$s_{i,t,s}^G = (1 - \alpha_i^G) s_{i,t-1,s}^G + \gamma_i^G c_{i,t-1,s}^G - \frac{d_{i,t-1,s}^G}{\mu_i^G} \qquad \forall i \in \mathcal{V}^E, t \in \mathcal{T} \setminus \bigcup_{d \in \mathcal{D}} \{t_d^I\}, s \in \mathcal{S}$$
 (11)

$$s_{i,t_{d}^{I},s}^{G} = (1 - \alpha_{i}^{G})s_{i,t_{d}^{F},s}^{G} + \gamma_{i}^{G}c_{i,t_{d}^{F},s}^{G} - \frac{d_{i,t_{d}^{F},s}^{G}}{\mu_{i}^{G}} \qquad \forall i \in \mathcal{V}^{E}, d \in \mathcal{D}, s \in \mathcal{S}$$
(12)

$$s_{i,t,s}^{L} = (1 - \alpha_i^L) s_{i,t-1,s}^{L} + \gamma_i^L c_{i,t-1,s}^{L} - \frac{d_{i,t-1,s}^L}{\mu_i^L} \qquad \forall i \in \mathcal{V}^T, t \in \mathcal{T} \setminus \{0\}, s \in \mathcal{S}$$
 (13)

$$s_{i,0,s}^{L} = (1 - \alpha_i^L) s_{i,|\mathcal{T}|,s}^{L} + \gamma_i^L c_{i,|\mathcal{T}|,s}^{L} - \frac{d_{i,|\mathcal{T}|,s}^L}{\mu_i^L} \qquad \forall i \in \mathcal{V}^T, s \in \mathcal{S}$$

$$(14)$$

where $s_{i,t,s}^G$ and $s_{i,t,s}^L$ represent the state of charge of the gas and liquid hydrogen storage, respectively. The parameters α_i^G , γ_i^G , and μ_i^G are the self-discharge rate and efficiencies of charge and discharge of the gas storage, respectively. Similarly, the parameters α_i^L , γ_i^L , and μ_i^L are the corresponding efficiencies of the liquid tank. Since the gas storage is only for intraday use, constraint (12) ensures that the state of charge at start of time period t_d^I (which is the first period of day $d \in \mathcal{D}$) is the same as that at the end of time period t_d^F (which is the last period of day $d \in \mathcal{D}$). Constraint (14) ensures that the state of charge of the long-term liquid tank is the same at the start and end of the time horizon, a typical restriction used to prevent the model from making use of "free energy".

Finally, we also add constraints to define the domain and bounds of the model's variables.

$$0 \le b_i^S \le \bar{P}_i; \ b_i^S \in \mathbb{Z}$$
 $\forall i \in \mathcal{V}^S$ (15)

$$0 \le b_i^W \le \bar{W}_i; \ b_i^W \in \mathbb{Z}$$
 $\forall i \in \mathcal{V}^W$ (16)

$$0 \le f_{i,j,t,s}^{E} \le \bar{E}_{i,j} \qquad \forall (i,j) \in \mathcal{E}^{E}, t \in \mathcal{T}, s \in \mathcal{S}$$

$$(17)$$

$$0 \le f_{i,j,t,s}^G \le \bar{G}_{i,j} \qquad \forall (i,j) \in \mathcal{E}^G, t \in \mathcal{T}, s \in \mathcal{S}$$
 (18)

$$0 \le f_{i,j,t,s}^{L} \le \bar{L}_{i,j} \qquad \forall (i,j) \in \mathcal{E}^{L}, t \in \mathcal{T}, s \in \mathcal{S}$$

$$\tag{19}$$

$$0 \le s_{i,t,s}^G \le \bar{S} \cdot \mathbf{y}_i^G \qquad \forall i \in \mathcal{V}^E, t \in \mathcal{T}, s \in \mathcal{S}$$
 (20)

$$0 \le s_{i,t,s}^{L} \le \bar{T} \cdot y_{i}^{L} \qquad \forall i \in \mathcal{V}^{T}, t \in \mathcal{T}, s \in \mathcal{S}$$
 (21)

$$0 \le c_{i,t,s}^G, d_{i,t,s}^G \le \bar{S}^G \cdot y_i^G \qquad \forall i \in \mathcal{V}^E, t \in \mathcal{T}, s \in \mathcal{S}$$
 (22)

$$0 \le c_{i,t,s}^L, d_{i,t,s}^L \le \bar{S}^L \cdot y_i^L \qquad \forall i \in \mathcal{V}^E, t \in \mathcal{T}, s \in \mathcal{S}$$
 (23)

$$u_{i,t,s}^E \ge 0$$
 $\forall i \in \mathcal{V}^I \cup \mathcal{V}^R, t \in \mathcal{T}, s \in \mathcal{S}$ (24)

$$u_{i,t,s}^G \ge 0$$
 $\forall i \in \mathcal{V}^I, t \in \mathcal{T}, s \in \mathcal{S}$ (25)

$$\mathbf{y}_{i}^{G} \in \mathbb{Z}$$
 $\forall i \in \mathcal{V}^{E}$ (26)

$$\mathbf{y}_{i}^{L} \in \mathbb{Z}$$
 $\forall i \in \mathcal{V}^{T}$ (27)

All in all, our 2-stage stochastic mixed-integer linear model is given by:

$$\min_{ \substack{ \pmb{b}_{i}^{E}, \pmb{b}_{i}^{W}, \pmb{z}_{i}^{E}, \pmb{z}_{i}^{W} \\ f_{i,j,t,s}^{E}, f_{i,j,t,s}^{G}, f_{i,j,t,s}^{L}, g_{i,t,s}, u_{i,t,s}^{E}, u_{i,t,s}^{G}, \\ s_{i,t,s}^{L}, c_{i,t,s}^{L}, c_{i,t,s}^{L}, c_{i,t,s}^{G}, c_{i,t,s}^{G}, c_{i,t,s}^{G}, d_{i,t,s}^{G} \\ \text{s.t.} }$$
 (3) - (27)

Note that we do not consider complementarity constraints between the charge and discharge variables of the storage systems ($c_{i,t-1,s}^G$ and $d_{i,t-1,s}^G$, $c_{i,t-1,s}^L$ and $d_{i,t-1,s}^L$). In fact, charging and discharging a storage system in the same time period is not optimal because of the inefficiencies in these systems.

Finally, we also assume that there is no wear and tear on equipment and that the efficiencies of the technologies and processes do not deteriorate over time. Our investigation also indicated that the cost of installing renewables was mostly variable; this is dependent on the number of turbines/panels installed. Therefore, we do not consider one-off setup costs for this investment.

2.2 Data Input

Through the input of data parameters that describe different realities (e.g. cities, climates, costs), the model presented in Section 2.1 can be utilized to study the viability of green hydrogen for various contexts. In this section, we provide a brief overview of how we build the data instances used in the computational experiments in Section 3. Graphs that visualise the data instance described in this section can be found on the interface as described in Section 2.3.

We have considered standard data units in our instances and measured electricity in MW, gas and liquid hydrogen in kg, and money in \$. For the parameters (and variables) concerning the dimensions of renewable plants, the minimum units are one row with 100 panels for solar plants and one wind turbine for wind plants.

We design a network of 12 locations. According to the data provided, we consider 5 residential areas, 2 industrial areas, 2 candidate renewable plant locations (one solar and one wind), and 3 locations with an electrolyzer, liquid tank, and fuel cell technologies, respectively. We consider 4 days representative of the 4 quarters in a year, and each day is subdivided into 96 15-minute time periods. Note that all possible lines between locations according to our network scheme in Figure 1 are present in the data instance.

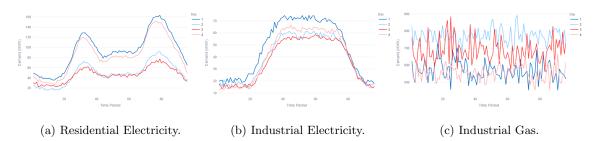


Figure 2: Total Network Demand.

Some data parameters were provided by the competition organizers in the problem description. Namely, the investment costs in solar PV panels B_i^S and wind turbines B_i^W , the electricity ($D_{i,t}^E$) and gas ($D_{i,t}^G$) demand of 5 residential and 2 industrial areas. The total demand of these areas for electricity and gas is presented in Figure 2.

In addition, an average scenario of renewable generation $G_{i,t,s}^S$, $G_{i,t,s}^W$ is also provided. We consider 9 scenarios by combining low, medium, and high cases for both solar and wind. We build the generation data for the remaining scenarios by considering deviations of +20% and -20% from the given (medium) scenario as depicted in Figure 3 and Figure 4. Note that we consider in-shore

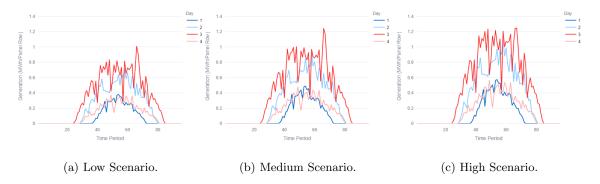


Figure 3: Solar Generation.

wind generation, but by adapting these inputs, the model would be suitable to study off-shore wind potential as well. These scenarios have different weights w_s in the operational costs of the

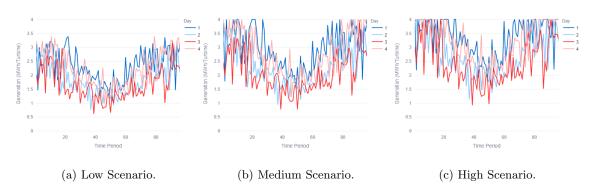


Figure 4: Wind Generation.

objective function as depicted in Figure 5. The values were chosen by assigning the likeliness of

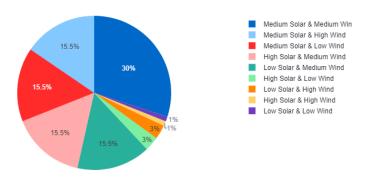


Figure 5: Scenario Weights.

the scenarios in real life where an average scenario is more probable than the extremes. Therefore, the medium solar and medium wind scenario has the biggest probability with 30%, then a 15.5% for all the other combinations with a medium, 3% for the the mix of high and low solar and wind, and 1% for the low/low and high/high scenarios, which should be less likely to occur.

Next, we detail the remaining costs. We set the cost of intraday gas storage B_i^G at 20,000\$ per storage system where each storage system has a maximum capacity \bar{T} of 9kg [3]. Similarly, the cost of long-term liquid hydrogen tanks is 800,000\$ per tank, and tanks have a maximum capacity \bar{S} of 4,000kg [2]. Moreover, we set the operational costs of the intraday gas storage C^G at 10\$/kg [14, 9], and those of the long-term liquid tanks C^L at 0.2\$/kg [4].

The efficiencies of the electrolysis process at electrolyzers η_i^E and of the gasification process at fuel cells η_i^F are provided in the problem description as 70% and 75%, respectively. For the hydrogen tank, we assume the gasification process is entirely efficient with an efficiency of 100%. For the efficiencies associated with the storage technologies, we consider both self-discharge rates α_i^G and α_i^L to be 1.5%, the charging and discharging efficiencies of intraday gas storage to be 70% and those of long-term liquid storage to be 75%.

We allow for a maximum loss of load of 3.5% for both electricity L^E and gas L^G , which is equivalent to 3 hours per year. In addition, we consider a maximum capacity \bar{P}_i of 5,000 rows of 100 panels corresponding to a solar plant of 1 km², and a maximum capacity \bar{W}_i of 100 turbines corresponding to a wind farm of 50km². We assume that the lines between two locations in our network have a maximum capacity of 500MW for electricity lines $\bar{E}_{i,j}$, 100,000kg for hydrogen gas lines $\bar{G}_{i,j}$ [8], or 500,000kg for liquid hydrogen lines $\bar{L}_{i,j}$.

lines $\bar{G}_{i,j}$ [8], or 500,000kg for liquid hydrogen lines $\bar{L}_{i,j}$. Finally, according to the problem description, we consider that 1MW of electricity corresponds to 0.05kg of gas (U^{EG}) , and 1kg of hydrogen gas is equivalent to 1kg of liquid hydrogen (U^{GL}) .

2.3 User Interface

In order to simplify the interaction of decision-makers with our optimization model and allow them to use the model's solutions to extract practical insights to inform their decisions, we have implemented a user interface. This interface can be accessed in the following URL: https://hydrogenius-edinborgh-mopta24.streamlit.app/.

This interface allows the user to personalize the data as needed in the *Data Input* page and visualize it in the *Data Visualization* page. The default instance which we consider in this report and which we detail in Section 2.2 is also directly available on these pages. In addition, the user can visualize the model's solution for the data input provided in the *Solution Visualization* page. This allows the user to try out different data inputs and see how they affect the solution.

This interface can alternatively be run locally by downloading the contents of the following GitHub repository which hosts it: HYDROGENius-EdinbORgh_MOPTA24.git.

3 Results & Discussion

In this section, we present the computational results obtained from our model's solution and discuss their significance to the study of the viability of green hydrogen.

3.1 Solution Analysis of Minimum Non-trivial Case

In this section, we discuss the solution of our optimization model given the 12-location network data described in Section 2.2.

This instance results in a total cost of circa \$251 Million, given that around \$250 Million results from investment costs, and the \$443 Thousand in operational costs for the 4 days representative of the 4 quarters. The solution consists of building 3 rows of 100 solar PV panels each, 78 wind turbines, and 19 liquid hydrogen storage tanks. At the optimal solution, no intraday gas storage is invested in.

When looking at the investment costs per technology type (solar, wind, hydrogen gas, and liquid hydrogen storages) in Figure 6, we notice that the majority of costs come from an investment in wind turbines, with the second most relevant investment being the liquid hydrogen storage. When considering the approximate operational costs per scenario in Table 1, we can see that the wind



Wind	Operational Cost
Scenario	(Thousands of \$)
High	5 Thousand
Medium	102-109 Thousand
Low	2 Million

 $\label{eq:Figure 6: Investment Costs - Breakdown per Technology.}$

Table 1: Approximate Operational Costs - Breakdown per Scenario.

scenarios are the ones with the highest impact on the operational costs. In other words, scenarios with low wind generation result in significantly higher operational costs of storage systems. This is coherent with the fact that the model has chosen to invest in a large wind plant and a small solar plant to offer some flexibility.

We can also see the high impact of the wind scenario in other parts of the solution, such as the amount of renewable electricity spilled and the use of liquid hydrogen tank storage.

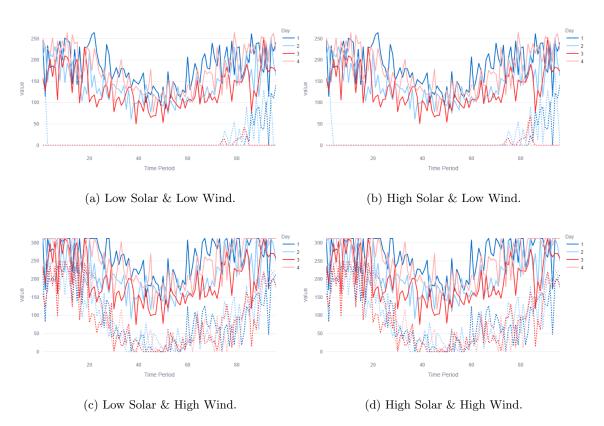


Figure 7: Electricity Generation (continuous lines) and Electricity Spillage (dotted lines).

In Figure 7, we can confirm that under scenarios with similar wind, the spillage is similar independently of solar generation being high or low. While in scenarios with low wind, there is little spillage which mostly occurs at the end of the day, in scenarios where there is a lot of wind generation, renewable electricity is spilled in more period of the day and in higher amount.

A similar pattern can be observed when investigating how the liquid hydrogen storage is used and managed throughout the time horizon. In Figure 8, we present the storage level of the liquid

hydrogen tank for the 3 wind scenarios and for the medium solar generation scenario. Note that similar patterns will be observed for high and low solar generation, once again depicting that the solar generation scenarios do not have as big of an impact as the wind generation ones do.

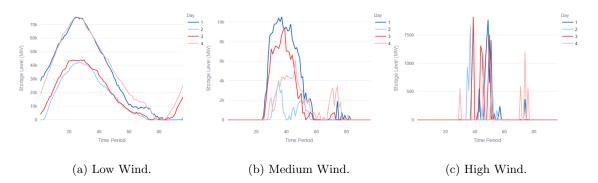


Figure 8: State-of-charge of Liquid Hydrogen Tank Storage.

On the one hand, when wind generation is low (Figure 8a), the storage is more carefully managed to leverage the generation at the start of the day to meet the peak of electricity demand between time periods 25 and 85 (see Figure 2a and Figure 2b). On the other hand, when wind generation is high (Figure 8c), the storage is only used more sporadically, and the state-of-charge is orders of magnitude lower. These observation attest that the Hydrogen storage has a clearer value for the network when renewable generation is lower.

Finally, we note that the loss of load constraints for both electricity (5) and gas (6) are active under every scenario. This is expected as operational costs can be reduced by not meeting demand, even if the same investment needs to be done initially. We discuss this theme further in Section 3.2 where we study the shadow prices of these constraints and how the optimal objective cost changes with different values of maximum loss of load allowed.

3.2 Economics of the Loss of Load

For a green-hydrogen-powered grid to become a reality, one may need to buy non-renewable energy during the investment stages while hydrogen systems and renewable plants are being built, or as a back-up energy source for extreme, unfavorable scenarios. However, in the long-run, for renewable energy and green hydrogen to be viable, their prices will have to be comparable and competitive with those of non-renewable energy.

In Section 3.1, we alluded to the fact that the loss of load bounding constraints (5) for electricity and (6) for gas remain active in the solutions found. In this section, we consider that same data instance and study the shadow prices (or dual values) associated with those constraints. These shadow prices provide information of how much one would be willing to pay for being allowed one additional unit (MW) of loss of load. In other words, they represent the price that we would be willing to pay for non-renewable energy. Consequently, for a green-hydrogen-powered grid to have practical potential, we would like to verify shadow prices comparable to current energy prices.

Throughout this section, we present computational results that we obtain by solving our model over a grid of values of loss of load for electricity and gas. Since our model is a mixed-integer linear model, we take the following steps to obtain shadow prices for the loss of load constraints. First, we fix the integer investment decision variables $(b_i^S, b_i^W, y_i^G, y_i^L)$ at their optimal values. Then, we solve the remaining linear model to compute the shadow prices associated with constraints (5) and (6). Note that these shadow prices are only valid while the integer solution which is fixed remains optimal.

Before discussing how the shadow prices vary over this grid, we show the total expected operational costs for these different loss of loads percentages in Figure 9. As expected, Figure 9 reveals that the smaller the levels of loss of load allowed the higher the operational costs. We note that the difference in the total operational costs between allowing 0% loss of load for electricity and 1.5% is over \$2,000,000. It is also possible to observe that changes in the percentage of loss of load

Total Expected Operational Cost

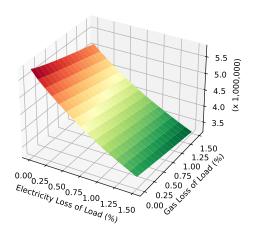


Figure 9: Total expected operational cost for a grid of loss of load percentages for electricity and gas.

for electricity have a much greater impact on the expected operational costs than changes in the gas loss of load.

In Figure 10, we can see the shadow prices for loss of electricity load (10a) and of gas load (10b). We observe that the shadow prices for the loss of gas load are smaller both in range and in

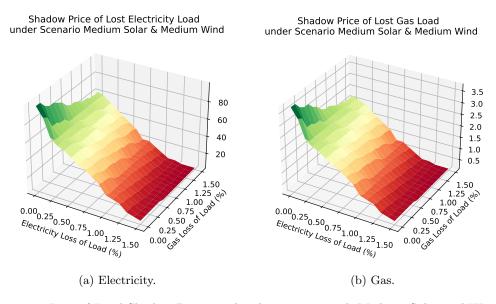


Figure 10: Loss of Load Shadow Prices under the scenario with Medium Solar and Wind.

value than those of electricity load. This confirms what we noticed in Figure 9 that the electricity loss of load is more valuable than that of gas, this is it has a greater impact in the operational costs.

Throughout the rest of this section, we focus on the loss of electricity load shadow prices and compare its behaviour under different renewable generation scenarios. In Figure 11 we show how the behaviour of the shadow prices of loss of electricity load changes with changes in wind generation (under the same solar generation scenario). We can see that the graphs 11a and 11b are significantly different in the range of shadow prices they present. As expected, when there is more wind generation (Figure 11b), the shadow prices are smaller as we are willing to pay less for losing

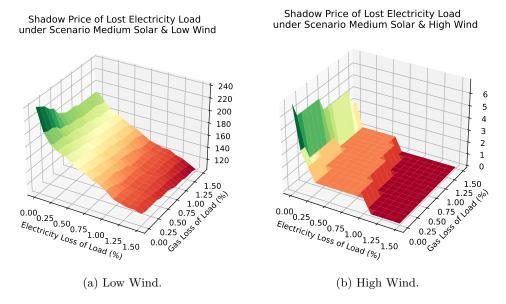


Figure 11: Electricity loss of load shadow prices of constraint (5) under scenarios with medium solar generation.

load as our generation is abundant. When wind generation is low, the shadow prices increase as meeting demand in this case is more difficult in this case and being able to lose more load results in higher savings.

In Figure 12, we show these same changes are not as noticeable when we change the solar generation instead (under the same wind generation scenario). In fact, the two graphs 12a and 12b look fairly similar. This is once again coherent with the model's decision to invest in a large

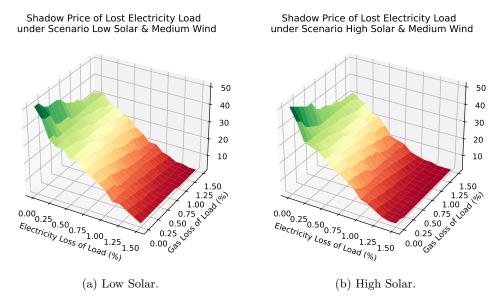


Figure 12: Electricity loss of load shadow prices of constraint (5) under scenarios with medium wind generation.

wind plant, but only a small solar plant. Note that the scenario weights are not causing these differences in the influence of wind and solar, as they are created to be symmetrical with respect to wind and solar as seen in Figure 5.

3.3 Green Hydrogen Viability

In this section, we discuss how the shadow prices for the loss of electricity load compare with current electricity prices in the USA, and what that says about the viability of green hydrogen.

Considering the data instance detailed in Section 2.2, where the percentage of loss of electricity load is 0.035%, we obtain the shadow prices in Table 2. In this same instance the total electricity

Solar Scenario	Wind Scenario	Shadow Price (\$)
Medium	Medium	99.16
Medium	High	5.77
Medium	Low	240.06
High	Medium	49.36
High	High	0.37
High	Low	46.46
Low	Medium	51.23
Low	High	1.12
Low	Low	15.49

Table 2: Electricity shadow prices for a loss of electricity load of 0.035% under each scenario

demand (over all load locations and time periods) is 10,522.30 MWh, and hence the maximum loss of electricity load is 3.68 MWh.

If we consider instead a loss of load of 0.0326241%, which translates into 1MW less of loss of load similarly to the interpretation of shadow prices, we would be able to lose 3.43 MWh of load. In other words, we would have to lose 0.25 MWh less of load. Assuming the average electricity rate in the USA of \$161/MWh [6], buying these 0.25 MWh of load from the grid would cost \$40.25.

When the cost of non-renewable energy \$40.25 is smaller than the shadow price in Table 2, which is the price we would be willing to pay for buying that energy elsewhere (or in other words the savings in operational costs we obtain from being able to lose that extra load), then it would be more profitable to buy non-renewable energy, and green-hydrogen would not desirable.

We can observe that in the scenarios with high wind, this is the case. Since a big investment in wind is made in the optimal solution, then when wind is high we are not willing to pay too much for losing electricity load. Consequently, green hydrogen becomes the more profitable source of energy. On other scenarios, this is not the case, which shows that under the current technology and energy prices considered in our input data, in these scenarios green hydrogen would be more costly than non-renewable energy.

If we have an electricity price of 105\$/MWh on the lower end of the spectrum (like in North Dakota [6]), then the same conclusions still hold. If instead we have a higher electricity price of 439.3\$/MWh (like in Hawaii [6]), then green hydrogen becomes the more profitable option in almost all the scenarios.

Finally, the user interface discussed in Section 2.3 can be used to better investigate different case studies, by adjusting the investment and operational costs, generation scenarios and respective weights, so that a similar analysis can be conducted for different regulatory and weather realities.

4 Conclusion

In this section, we briefly summarize the most relevant findings of our report and detail how this work could be further improved in future work.

4.1 Key findings

All in all, the results in this report show that there is potential in green hydrogen as a source of baseload support in the transition to a fully renewable-powered energy grid.

For the data considered, we see that a fully-renewable network driven by green hydrogen has a greater potential to succeed under realities where wind generation is high. In addition, we note

that the main driver for the potential and profitability of green hydrogen lies in the electricity demand and prices, as opposed to those for gas. Finally, we conclude that the investment in long-term liquid hydrogen storage is more valuable for taking full advantage of hydrogen as a baseload source than that in shorter-term intraday hydrogen gas storage.

4.2 Future Improvements

The approached presented in this report have further potential to bring valuable insights to the adoption of green hydrogen. In this section, we suggest some direction for future work.

First, uncertainties in the model could be further explored. One could consider a larger or more relevant set of renewable generation scenarios by developing a more accurate generation forecast based on weather data. Alternatively, other sources of uncertainty could be consider, such as residential demand patterns or technology investment costs.

Moreover, we could extend the optimization model developed to detail other aspects of the grid's operation. For example, we could account for economy of scale in prices when designing the objective function and its cost parameters or for the impact of ramping in charging and discharging of intraday gas storage by modelling the corresponding constraints.

Finally, we could carry out a more extensive long-term analysis of the viability of green hydrogen. Namely, we could study the impact in expected reductions in the cost of technologies and performing a detailed sensitivity analysis on these model inputs. This study would allows us to suggest policy changes that would address the main obstacles that green hydrogen faces today by allowing us to identify which components would have to become cheaper to make green hydrogen more desirable economically. Alternatively, we could better account for long time horizon of investments. For example by computing the net discounted present value of the investments, or by allowing for an initial set up to be installed already. In other words, assume that some renewable plants and hydrogen storage systems are already build. From a modelling perspective, this can be achieved by enforcing lower-bounds on the corresponding investment variables.

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A Notation

In this appendix, we present Table 3, Table 4 and Table 5 which summarise the notation used for sets, parameters and variables, respectively.

Table 3: List of Sets and their description.

Set	Definition
\overline{v}	Set of vertices in the energy grid.
${\cal E}$	Subset of $\mathcal{V} \times \mathcal{V}$ of edges in the energy grid.
${\mathcal T}$	Set of time periods.
${\cal D}$	Set of days in the time periods.
${\cal S}$	Set of renewable generation uncertainty scenarios.
\mathcal{V}^E	Subset of vertices where there is a hydrogen electrolyzer.
\mathcal{V}^F	Subset of vertices where there is a fuel cell.
\mathcal{V}^T	Subset of vertices where there is a insulated cryogenic tank.
\mathcal{V}^I	Subset of vertices where there is a industrial demand area.
\mathcal{V}^R	Subset of vertices where there is a residential demand area.
\mathcal{V}^S	Subset of candidate vertices where a solar PV plant can be built.
\mathcal{V}^W	Subset of candidate vertices where a wind turbine plant can be built.
\mathcal{E}^{E}	Subset of edges where electricity flows.
\mathcal{E}^G	Subset of edges where hydrogen gas flows.
\mathcal{E}^L	Subset of edges where liquid hydrogen flows.
t_d^I, t_d^F	Indexes of \mathcal{T} representing the start and end of day $d \in \mathcal{D}$, respectively.

Table 4: List of Parameters, their description and units.

Param.	Definition	\mathbf{Unit}
B_i^S	Cost of building one solar panel at location $i \in \mathcal{V}^S$ adjusted to the time horizon \mathcal{T} given an expected life-time.	£/Panel
B_i^W	Cost of building one wind turbine at location $i \in \mathcal{V}^W$ adjusted to the time horizon \mathcal{T} for an expected life-time.	£/Turbine
Z_i^S	Fixed cost of setting up a solar plant at location $i \in \mathcal{V}^S$ adjusted to the time horizon \mathcal{T} given an expected life-time.	£
Z_i^W	Fixed cost of setting up a wind plant at location $i \in \mathcal{V}^W$ adjusted to the time horizon \mathcal{T} for an expected life-time.	£
B_i^G	Cost of building one gas storage of size \bar{S} at location $i \in \mathcal{V}^E$ adjusted to the time horizon \mathcal{T} given an expected life-time.	£/Storage System
B_i^L	Cost of building one liquid tank of size \bar{T} at location $i \in \mathcal{V}^T$ adjusted to the time horizon \mathcal{T} for an expected life-time.	£/Tank
w_s	Weight of scenario $s \in \mathcal{S}$ for the second-stage expected value objective.	%
$C^G \ C^L$	Storage cost of hydrogen gas	\pounds/kg
	Storage cost of liquid hydrogen	£/kg
$ar{ar{P}_i}$	Maximum number of rows of solar panels that can be built with at location $i \in \mathcal{V}^S$.	Panel Rows
$ar{W}_i$	Maximum number of wind turbines that can be built with at location $i \in \mathcal{V}^W$.	Turbines
$ar{ar{T}} ar{ar{S}}$	Standard capacity of one hydrogen liquid tank $i \in \mathcal{V}^T$.	kg
\bar{S}	Standard capacity of one electrolyser gas storage $i \in \mathcal{V}^E$.	kg

$ar{E}_{i,j}$	Maximum capacity of electricity line $(i, j) \in \mathcal{E}^E$. Maximum capacity of gas line $(i, j) \in \mathcal{E}^G$.	MW
$egin{array}{c} ar{E}_{i,j} \ ar{G}_{i,j} \ ar{L}_{i,j} \end{array}$	Maximum capacity of gas line $(i,j) \in \mathcal{E}^L$. Maximum capacity of liquid hydrogen line $(i,j) \in \mathcal{E}^L$.	kg kg
L^E	Upper bound on worst case percentage total loss of electricity load arriving at vertices $i \in \mathcal{V}^I \bigcup \mathcal{V}^R$.	%
L^G	Upper bound on worst case percentage total loss of gas load arriving at vertices $i \in \mathcal{V}^I$.	%
$D_{i,t}^E$	Electricity demand at vertex $i \in \mathcal{V}^I \cup \mathcal{V}^R$.	MW
$D_{i,t}^G$	Gas demand at vertex $i \in \mathcal{V}^I$.	kg
$\frac{D_{i,t}^E}{D_{i,t}^G}$ $\frac{G_{i,t,s}^S}{G_{i,t,s}^S}$	Electricity generation per solar panel at location $i \in \mathcal{V}^S$ at time	MW/Panel
$G^W_{i,t,s}$	period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$. Electricity generation per wind turbine at location $i \in \mathcal{V}^W$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	Row MW/Turbine
U^{EG} U^{GL}	Unit conversion factor between electricity and hydrogen gas. Unit conversion factor between gas and liquid hydrogen.	MW/kg kg/kg
α_i^G	Self-discharge rate of intraday gas storage at electrolyzer.	%
α_i^L	Self-discharge rate of liquid hydrogen tank storage.	%
$\frac{\alpha_i^G}{\alpha_i^L}$ $\frac{\eta_i^E}{\eta_i^T}$ $\frac{\eta_i^F}{\eta_i^G}$ $\frac{\gamma_i^G}{\mu_i^G}$ $\frac{\gamma_i^L}{\mu_i^L}$	Efficiency of electrolysis process at electrolyzer.	%
$\eta_{i_{E}}^{T}$	Efficiency of liquefaction process at liquid hydrogen tank.	%
η_i^F	Efficiency of gasification process at fuel cells.	%
$\gamma_{i_{-}}^{G}$	Charging efficiency of intraday gas storage at electrolyzer.	%
μ^G_i	Discharging efficiency of intraday gas storage at electrolyzer.	%
$\gamma_{i_{_{_{I}}}}^{\scriptscriptstyle L}$	Charging efficiency of liquid hydrogen tank storage.	%
$\mu_i^{\scriptscriptstyle L}$	Discharging efficiency of liquid hydrogen tank storage.	%

Table 5: List of Variables, their description and units.

Variable	Definition	\mathbf{Unit}
$\frac{b_i^S}{b_i^W}\\ y_i^G$	Number of solar panels to be build at location $i \in \mathcal{V}^S$. Number of wind turbines to be build at location $i \in \mathcal{V}^W$.	Panels Turbines
y_i^L	Number of gas storage/electrolysers of size \bar{S} to be build at location $i \in \mathcal{V}^E$. Number of liquid storage tanks of size \bar{T} to be build at location $i \in \mathcal{V}^T$.	electrolysers Tanks
$f_{i,j,t,s}^{E}$ $f_{i,j,t,s}^{G}$ $f_{i,j,t,s}^{L}$	Flow of electricity along edge $(i, j) \in \mathcal{E}^E$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	MW
$f_{i,j,t,s}^G$	Flow of hydrogen gas along edge $(i, j) \in \mathcal{E}^G$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	kg
	Flow of liquid hydrogen along edge $(i, j) \in \mathcal{E}^L$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	kg
$u^E_{i,t,s} \ u^G_{i,t,s}$	Flow of loss of electricity load arriving at vertex $i \in \mathcal{V}^I \bigcup \mathcal{V}^R$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	MW
$u_{i,t,s}^G$	Flow of loss of gas load arriving at vertex $i \in \mathcal{V}^I$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	kg
$g_{i,t,s}$	Renewable electricity generation at location $i \in \mathcal{V}^S \cup \mathcal{V}^W$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	MW
$a_{i,t,s}$	Renewable electricity spillage at location $i \in \mathcal{V}^S \cup \mathcal{V}^W$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	MW

$s_{i,t,s}^G$	Hydrogen gas stored at the intraday gas storage at vertex $i \in \mathcal{V}^E$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	kg
$c_{i,t,s}^G$	Hydrogen gas charged to the intraday gas storage at vertex $i \in \mathcal{V}^E$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	kg
$d_{i,t,s}^G$	Hydrogen gas discharged from the intraday gas storage at vertex $i \in \mathcal{V}^E$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	kg
$s_{i,t,s}^L$	Liquid hydrogen stored at the tank storage at vertex $i \in \mathcal{V}^T$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	kg
$c_{i,t,s}^L$	Liquid hydrogen charged to the tank storage at vertex $i \in \mathcal{V}^T$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	kg
$d_{i,t,s}^L$	Liquid hydrogen discharged from the tank storage at vertex $i \in \mathcal{V}^T$ at time period $t \in \mathcal{T}$ under scenario $s \in \mathcal{S}$.	kg