

Fourier Continued:

$$F(f) = \sum_{n=0}^{N-1} A_n \cdot e^{-j \frac{2\pi f t_n}{N}} \quad a_n \quad t_n = n \cdot \text{Sampling time}$$

$$F_f = A_0 e^{-a_0 j} + A_1 e^{-a_1 j} + \dots + A_n e^{-a_{N-1} j} \quad N = \text{Samples}$$

$$F_f = A_0 [\cos(-a_0) + j \sin(-a_0)] + \dots$$

$$F_f = A_0 \cos(a_0) + A_0 j \sin(-a_0) + \dots$$

$$F_f = C_0 + D_0 j$$

↑
Amplitude at frequency f

$$F_{f_{\text{real}}} = A_0 \cos\left(-\frac{2\pi f t_0}{N}\right) + A_1 \cos\left(-\frac{2\pi f t_1}{N}\right) + \dots$$

$$F_{f_{\text{real}}} = \sum_{n=0}^{N-1} A_n \cos\left(-\frac{2\pi f t_n}{N}\right)$$