

- intro to single linked lists
- insert and delete for a list

**Next week and homework**

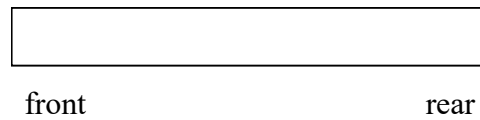
- next week: implementation of linked lists
- homework by next week:
  - (no example programs this week)
  - read Horstmann, section 16.1

**Lab**

- lab assigned in ‘Queues’. See Canvas for due date

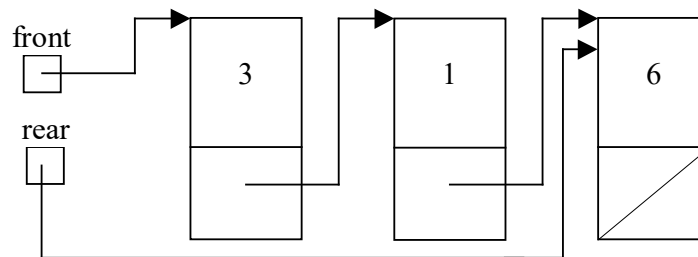
### Review prior work

- covered queues in the week before the Midterm:



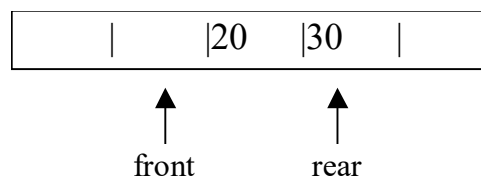
*Figure 1 illustration of a queue*

- FIFO data structure
  - remove from the front
  - insert at the rear
- began with a simple single linked list implementation of queue:



*Figure 2 single linked list implementation of queue*

- maintain 2 references `front` and `rear`
  - `front` is next element to be removed
  - `rear` is last element inserted
- queue lab assigned, to wrap queue inside a circular array



*Figure 3 wrap a queue inside a circular array*

- `front` – location before next item to be removed
- `rear` – last element inserted

**Introduction to this week**

- introduce next new data structure – single linked lists
- will concentrate on the important design technique of drawing pictures to design algorithms
- will work only in pseudocode this week

## Intro to single linked lists

Objective: review lists, see some primitive operations

### A list is an “ordered sequence of items”

- as we all know, "a list is an ordered sequence of items"
  - e.g. a shopping list:  
  
bread  
milk  
cereal  
cheese  
butter
  - is ordered: so first, last, next and previous items all make sense
  - unlike a queue, no restrictions on where we insert and delete items
  - ...so a list is more general / less restrictive than a queue
  - (note that there is no requirement that items be in any sorted order)

### Compare static and dynamic implementations

- we can do static and dynamic implementations of lists
  - static – "size and shape cannot change at runtime" e.g. use an array to implement a list
  - dynamic – "size and shape of data structure can change at runtime" e.g. use references to implement a single linked list
  - different advantages and disadvantages, will review below

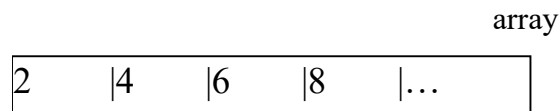
### Too much memory, otherwise not enough

- with a static implementation, we have to allocate too much memory, otherwise we may not have enough
  - as the size of the list changes, we must always have enough array locations in which to store it
  - therefore, have to allocate in advance the maximum memory required, even though not all of it is used all the time

- a dynamic implementation is more efficient here, as the amount of memory allocated increases and decreases as the size of the list changes

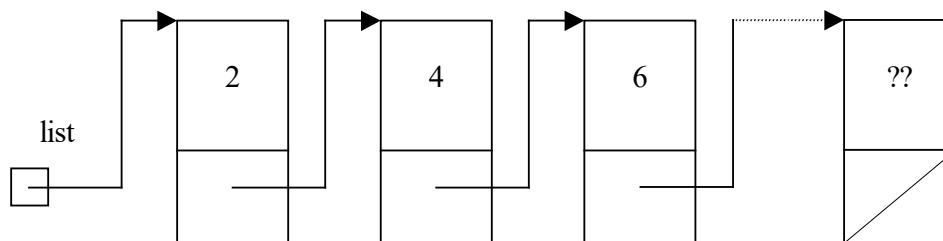
#### The update problem

- another disadvantage of static implementations occurs when we insert or delete items. Is called the 'update problem' e.g.
  - given a sorted list of numbers implemented statically:



*Figure 4 a sorted list of numbers implemented statically, as an array*

- to insert 3 – have to move elements from one memory location to another
  - to delete 2– have to move elements from one memory location to another
  - imagine having to move thousands of large objects!!!!
  - CONCLUDE: insert / delete in a static data structure is very expensive
- a dynamic implementation is very efficient when we insert or delete items
  - here's a picture of the list implemented dynamically as a single linked list of items



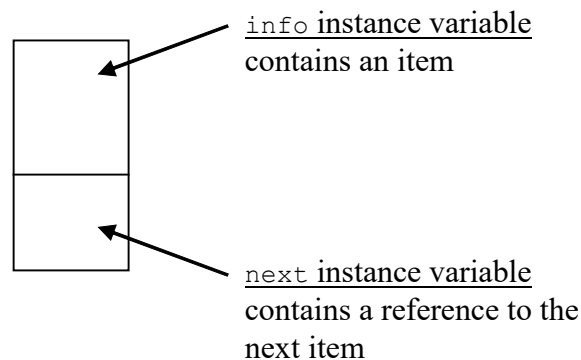
*Figure 5 the list implemented dynamically, as a single linked list of items*

- (see how the programmer must maintain a reference to the first item in the list, is named 'list' here)
- do insert and delete in this picture:
  - to insert 3 – only have to update two references

- to delete 2 – only have to update one reference
- never have to move elements from one memory location to another!!!!
- CONCLUDE: insert / delete in a dynamic data structure is much more efficient

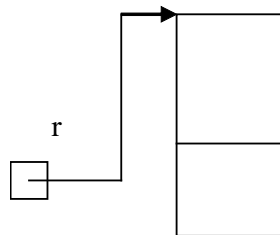
### Review working with references

- first, remember that our `Item` class has two instance variables:



*Figure 6 the Item class*

- `info` is just an `int`, for simplicity
- `next` is the reference to the next item in the list
- we declared these as protected for our convenience, so they can be directly accessed by classes that use the `Item` class
  - (otherwise we would write get and set methods to access instance variables declared private)
- here are pseudocode primitives for working with items, so that we can start to design list operators
- `r.info` – is the `info` instance variable of item referenced by `r`, e.g.



*Figure 7 the item object referenced by r*

- try the effects of the following, updating the pictures (don't worry about syntax here, this is just informal pseudocode):

```
r.info = 5  
x = r.info
```

- r.next – is the next instance variable of item referenced by r
  - e.g. given the following situation, with additional references p, q, r into a list of three items:

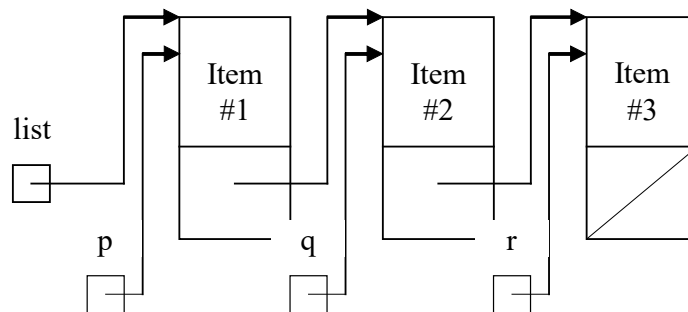


Figure 8 working with references example

- what do each of the following do? (Put the list back to this starting state each time.) The effect is given after each operation:

p = q.next      - sets p to reference Item #3

p.next = r      - sets Item #1 to reference Item #3. So it deletes Item #2

p.next = q.next      - again sets Item #1 to reference Item #3, removing Item #2

p.next = r.next      - deletes Items #2 and #3 from list

- r = getItem() – creates an item in memory and returns its address for assignment to r
  - e.g.

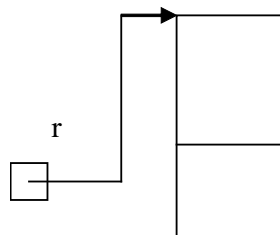
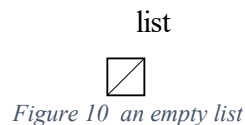


Figure 9 the getItem() primitive creates a new item

- `r.freeItem()` – frees item referenced by `r` i.e. returns to OS the memory allocated for item referenced by `r`
  - failing to free memory we previously requested is referred to as a memory leak
  - is bad programming!
  - can cause a program to crash!
  - (note that as Java programmers, we do not have to manually free memory that we have allocated. Instead this is the language's responsibility, implemented as automatic garbage collection)

### How to design algorithms

- will do four examples. Remember how to design algorithms for dynamic data structures:
  - draw picture of a start state
  - identify all possible cases
  - use pictures to design algorithms that get to required end state
- (BTW, be sure the algorithms work for empty lists also:)



1. Insert a new item at the beginning of a list
  - two different cases here, for an empty list and a !empty list
    - draw pictures of a start state
    - use this to identify the different cases
    - then use the pictures to figure out steps to get to the desired end state
    - e.g. add item containing 1 to beginning of this list:



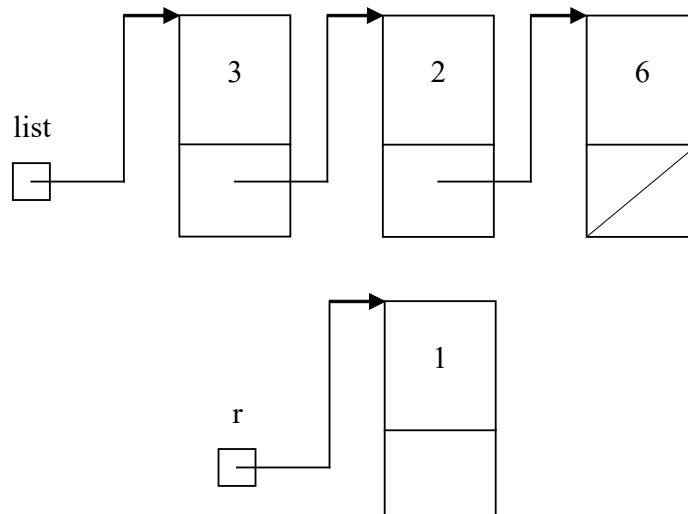


Figure 11 an example of a non-empty list

- or to the beginning of the empty list:



Figure 12 an example of an empty list

- using the pictures, we come up with an algorithm something like this, written as pseudocode. (Update the pictures as you work through the steps):

```
r = getItem() - create the new item
r.info = 1     - set its info field
r.next = list  - link it into the beginning of the list...
list = r       - ...and finished
```

- see that this algorithm works correctly for an empty list also

2. Remove the first item from the beginning of a list and retrieve its information

- two different cases, for an empty list and a !empty list. Will only consider here the !empty list, e.g.

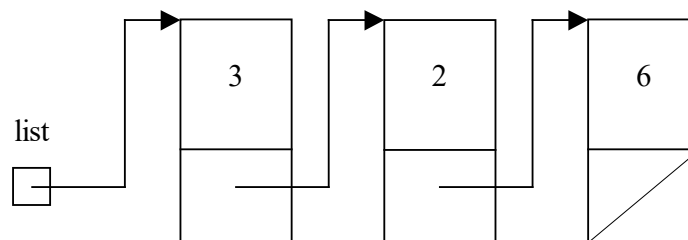


Figure 13 an example of a non-empty list

- several ways to do this. A good hint when removing something is:
    - "set a reference to item being removed"
  - applying this convention gives something like:  

```
r = list          - set r to item being removed
x = r.info        - get its info
list = r.next      - update the list
r.freeItem()      - don't forget to free memory we don't need!
```

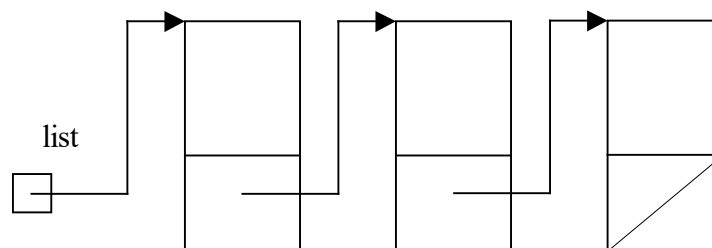
    - (note that we can't retrieve from an empty list – would have to handle this by testing first for `isEmpty()`, which we'll do next)
  - BTW, see that we just designed `push()` and `pop()`!
3. Test for an empty list
- this is easy! Draw the picture:



- gives us the test that a list is empty when:

`list == null`

4. Can only access items in a single linked list sequentially – is called a traversal
- e.g. count the number of items in this list:



*Figure 15 a non-empty list*

- HINT: list must always refer to the first item, we do not want to move it here. So use a ‘working’ reference to do the traversal. Call it r, for ‘reference’
- traverse r from the beginning to the end of the list  
  

```
count = 0
r = list
while (r != null)
    ++count
    r = r.next
print count
```
- traversal is very common, we do it all the time with lists
- (note that this works for an empty list also)

### Summary

- introduced the single linked list abstraction, designed some list processing algorithms
- it is essential to use pictures to design algorithms
  - particularly as data structures will become more complex!
- use simple pseudocode to express the algorithms at first
  - but with more experience in your programming language, you will find that your pcode becomes Java
  - eventually you will go directly from designing an algorithm with pictures to implementing it in code
- will continue to design linked list algorithms using pictures and our pseudocode...

## Insert and delete for a list

Objective: design these essential list operations

- unlike queues, we can insert and delete items from anywhere in a list, e.g.

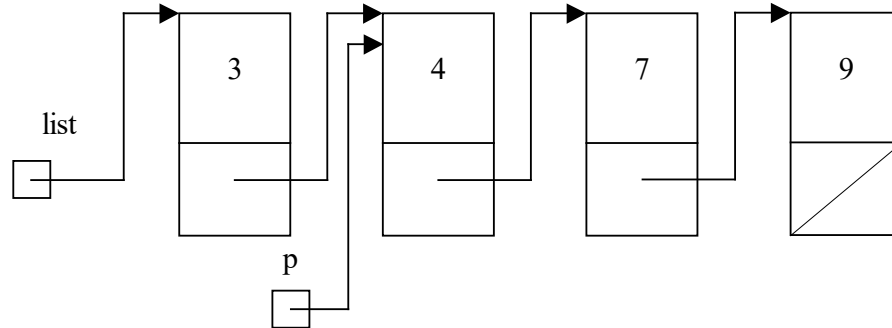


Figure 16 a reference *p* to “the item before the insertion or deletion point”

- assume we have a reference *p* to “the item before the insertion or deletion point”
- *p* will be set by searching for an item in the list, shortly
- algorithms have to work for all cases, including the empty list special case

### Design insertAfter() algorithm

- e.g. insert 6 after item pointed to by *p*
  - use the picture above to design the algorithm
  - we find two special cases. What if the list is empty? Or *p* does not refer to anything?
  - working with the picture, we come up with something like:

```
if (list is empty or p is not set)
    report error and exit
create a new item
initialize it
complete linking into list
```

- then more detailed, using our pseudocode:

```
if (isEmpty() || p == null)
    report error and exit
q = getItem()
```

```
g.info = 6
q.next = p.next
p.next = q
```

- note that we have to update the references in this order, otherwise the algorithm doesn't work
- see that there's no data movement – is very efficient!

### The deleteAfter() algorithm

- delete the item after the item referenced by p. Return the deleted item's info
  - use the picture above
  - two special cases. What if p does not refer to anything? Or p refers to the last item in the list, so there is no item to delete?
  - then remember: when deleting an item – "set a reference to item being deleted"
  - so something like:

```
if (p is not set or p is last item in list)
    report error and exit
set reference q to item after p
remove its information
update p
free old item q
```

- in pseudocode, something like:

```
if (p == null || p.next == null)
    report error and exit
q = p.next
x = q.info
p.next = q.next
q.freeItem()
```

- note that there's a subtle problem here in the error testing, where we must test whether p refers to an item BEFORE we access its next value
- more on this during implementation, next week

### The find() algorithm

- searches the list to find first occurrence of an item. Returns a reference to the item, or null if not found

- (so this is how we set the reference used by insert and delete)
- e.g. find 4 in the starting list above
- using the starting picture, we find just one special case, of an empty list
- then come up with something like this. Is sequential or linear search. Start at the beginning and search every item in turn:

```
if (list is empty)
    report error and exit
start at first item in the list
while there are items remaining in the list and info is not 4
    move to next item
return reference to matching item or null
```

- in pseudocode, something like:

```
if (isEmpty())
    report error and exit
r = list
while (r != null && r.info != 4)
    r = r.next
return r
```

- again, the same subtle problem here in the loop, where we must test whether r refers to an item BEFORE we access its info
- problem is solved during implementation, next week

### Summary

- update is easy and efficient when list is implemented dynamically
  - simply update one or two references!
- will implement these algorithms next week!

**Next week and homework**

- next week: implementation of linked lists
- homework by next week:
  - (no example programs this week)
  - read Horstmann, section 16.1

**Lab**

- lab assigned in 'Queues'. See Canvas for due date