

2.7

1) $\forall x \in \mathbb{R}, x^2 > 0$

for every x in Real numbers $x^2 > 0$, false. 0>0

2) $\exists a \in \mathbb{R}, \forall x \in \mathbb{R}, ax = x$

there exist a in Real numbers that for every
 x in real numbers, $ax = x$. True $a=1$

5) $\forall n \in \mathbb{N}, \exists X \in P(\mathbb{N}), |X| < n$

for every n is an element of Natural #'s
there exist set X in Power set of Natural #'s
, where the cardinality of the set X is less than n
True empty set $|X|=0 < n$

7) $\forall X \subseteq \mathbb{N}, \exists n \in \mathbb{Z}, |X| = n$

for every subset X of Natural #'s there exist n :
is an element of integers where cardinality of the
set $X = n$ False

9) $\forall n \in \mathbb{Z}, \exists m \in \mathbb{Z}, m = n + 5$

for every integer n there exist an integer m where
 $m = n + 5$ True

2.9

1) $(P \wedge Q) \Rightarrow R$

$P = f$ is a polynomial $Q = f$ has a degree greater than 2

$R = f'$ is not constant

3) $P \Rightarrow Q$

$P = x$ is prime $Q = \sqrt{x}$ is not a rational #

5) $\forall \epsilon \in \mathbb{R}, \exists \delta \in \mathbb{R}, |f(a) - b| < \epsilon \rightarrow |f(a) - f(c)| < \epsilon$

7) $\exists a \in \mathbb{R}, \forall x \in \mathbb{R}, a + x = x$

9) $(P \wedge Q) \Rightarrow R$

$P = x$ is rational # $Q = x \neq 0$ $R = \tan(x)$ is not in \mathbb{Q}

11) $\exists x, \forall y \in X, P(x) \wedge R(x, y)$

$X = \{\text{idiot}, \text{drunkard}, \text{children}, \text{United States}\}$

$P(x) = \text{providence } x$

$R(x, y) = x \text{ protects } y$

13) $\forall x, (P(x) \wedge Q(x)) \Rightarrow R(x)$

$P(x) = x \text{ is not happening to me}$ $Q(x) = x \text{ is happening to someone else}$

$R(x) = x \text{ is funny}$

2.10

- 1) The # x is not positive or the # y is positive
 - 3) There exists a prime # p for every prime number q for which $q \leq p$
 - 5) There exist a positive # ε for every positive # M for which $x > M$ whenever $|f(x) - b| \geq \varepsilon$
 - 7) I will eat somethings that have a face
- 9) if $\sin(t) < 0$, then it is not the case that $0 \leq x \leq \pi$
 $\exists x, (\sin(x) < 0) \wedge (0 \leq x \leq \pi)$
There exist a number x where $\sin(x) < 0$ and $0 \leq x \leq \pi$
- 11) There is a person you can't fool all of the time