# NumPy for MATLAB users

# Help

MATLAB/Octave	Python	Description
doc	help()	Browse help interactively
help -i % browse with Info		
help help $or$ doc doc	help	Help on using help
help plot	help(plot) $\mathit{or}$ ?plot	Help for a function
help splines $\mathit{or}$ doc splines	help(pylab)	Help for a toolbox/library package
demo		Demonstration examples

#### Searching available documentation

MATLAB/Octave	Python	Description
lookfor plot		Search help files
help	help(); modules [Numeric]	List available packages
which plot	help(plot)	Locate functions

# Using interactively

MATLAB/Octave	Python	Description
octave -q	ipython -pylab	Start session
TAB <i>or</i> M-?	TAB	Auto completion
foo(.m)	execfile('foo.py') <i>or</i> run foo.py	Run code from file
history	hist -n	Command history
diary on [] diary off		Save command history
exit <i>or</i> quit	CTRL-D	End session
	CTRL-Z # windows	

sys.exit()

# **Operators**

MATLAB/Octave	Python	Description
help -		Help on operator syntax

# **Arithmetic operators**

MATLAB/Octave	Python	Description
a=1; b=2;	a=1; b=1	Assignment; defining a number
a + b	a + b or add(a,b)	Addition
a - b	a - b $\mathit{or}$ subtract(a,b)	Subtraction
a * b	a * b <i>or</i> multiply(a,b)	Multiplication

4/15/22, 12:43 PM
a / b
a .^ b

factorial(a)

a / b Or divide(a,b)
a \*\* b
power(a,b)

Division Power, \$a^b\$

rem(a,b)

pow(a,b)
a % b

remainder(a,b)
fmod(a,b)

a+=b Or add(a,b,a)

Remainder

a+=1

In place operation to save array

creation overhead Factorial, \$n!\$

#### **Relational operators**

MATLAB/Octave
a == b
a < b
a > b
a <= b
a >= b
a ~= b

# Python a == b Or equal(a,b) a < b Or less(a,b) a > b Or greater(a,b)

a > b or less(a,b)
a > b or greater(a,b)
a <= b or less\_equal(a,b)
a >= b or greater\_equal(a,b)
a != b or not\_equal(a,b)

# Description Equal Less than Greater than Less than or equal Greater than or equal Not Equal

#### Logical operators

MATLAB/Octave
a && b
a    b
a & b $\mathit{or}$ and(a,b)
$a \mid b or or(a,b)$
xor(a, b)
$\sim$ a $\mathit{or}$ not(a)
~a <i>or</i> !a
any(a)
all(a)

# Python a and b a or b logical\_and(a,b) or a and b logical\_or(a,b) or a or b logical\_xor(a,b) logical\_not(a) or not a

# Description Short-circuit logical AND Short-circuit logical OR Element-wise logical AND Element-wise logical OR Logical EXCLUSIVE OR Logical NOT

True if any element is nonzero True if all elements are nonzero

#### root and logarithm

MATLAB/Octave
sqrt(a)
log(a)
log10(a)
log2(a)
exp(a)

Python
math.sqrt(a)
math.log(a)
math.log10(a)
math.log(a, 2)
math.exp(a)

Description
Square root
Logarithm, base \$e\$ (natural)
Logarithm, base 10
Logarithm, base 2 (binary)
Exponential function

#### Round off

MATLAB/Octave	
round(a)	

#### Description Round

ceil(a)	ceil(a)	Round up
floor(a)	floor(a)	Round down

fix(a) Round towards zero

#### **Mathematical constants**

MATLAB/Octave	Python	Description
pi	math.pi	\$\pi=3.141592\$
exp(1)	$math.e\ \mathit{or}\ math.exp(1)$	\$e=2.718281\$

# Missing values; IEEE-754 floating point status flags

MATLAB/Octave	Python	Description
NaN	nan	Not a Number
Inf	inf	Infinity, \$\infty\$
	plus_inf	Infinity, \$+\infty\$
	minus_inf	Infinity, \$-\infty\$
	plus_zero	Plus zero, \$+0\$
	minus_zero	Minus zero, \$-0\$

#### **Complex numbers**

MATLAB/Octave	Python	Description
i	z = 1j	Imaginary unit
z = 3+4i	z = 3+4j Or z = complex(3,4)	A complex number, \$3+4i\$
abs(z)	abs(3+4j)	Absolute value (modulus)
real(z)	z.real	Real part
imag(z)	z.imag	Imaginary part
arg(z)		Argument
conj(z)	<pre>z.conj(); z.conjugate()</pre>	Complex conjugate

#### **Trigonometry**

MATLAB/Octave	Python	Description
atan(a,b)	atan2(b,a)	Arctangent, \$\arctan(b/a)\$
	hypot(x,y)	Hypotenus; Euclidean distance

#### **Generate random numbers**

MATLAB/Octave	Python	Description
rand(1,10)	<pre>random.random((10,))</pre>	Uniform distribution
	<pre>random.uniform((10,))</pre>	
2+5*rand(1,10)	random.uniform(2,7,(10,))	Uniform: Numbers between 2 and 7
rand(6)	random.uniform(0,1,(6,6))	Uniform: 6,6 array
randn(1,10)	<pre>random.standard_normal((10,))</pre>	Normal distribution

#### **Vectors**

MATLAB/Octave	Python	Description
a=[2 3 4 5];	a=array([2,3,4,5])	Row vector, \$1 \times n\\$-matrix
adash=[2 3 4 5]';	array([2,3,4,5])[:,NewAxis] array([2,3,4,5]).reshape(-1,1) r_[1:10,'c']	Column vector, \$m \times 1\$-matrix

# **Sequences**

MATLAB/Octave	Python	Description
1:10	<pre>arange(1,11, dtype=Float) range(1,11)</pre>	1,2,3, ,10
0:9	arange(10.)	0.0,1.0,2.0, ,9.0
1:3:10	arange(1,11,3)	1,4,7,10
10:-1:1	arange(10,0,-1)	10,9,8, ,1
10:-3:1	arange(10,0,-3)	10,7,4,1
linspace(1,10,7)	linspace(1,10,7)	Linearly spaced vector of n=7 points
reverse(a)	a[::-1] $or$	Reverse
a(:) = 3	a.fill(3), a[:] = 3	Set all values to same scalar value

#### **Concatenation (vectors)**

MATLAB/Octave	Python	Description
[a a]	<pre>concatenate((a,a))</pre>	Concatenate two vectors
[1:4 a]	<pre>concatenate((range(1,5),a),</pre>	
	axis=1)	

# Repeating

MATLAB/Octave	Python	Description
[a a]	<pre>concatenate((a,a))</pre>	1 2 3, 1 2 3
	a.repeat(3) $or$	1 1 1, 2 2 2, 3 3 3
	a.repeat(a) <i>Or</i>	1, 2 2, 3 3 3

#### Miss those elements out

MATLAB/Octave	Python	Description
a(2:end)	a[1:]	miss the first element
a([1:9])		miss the tenth element
a(end)	a[-1]	last element
a(end-1:end)	a[-2:]	last two elements

#### Maximum and minimum

MATLAB/Octave	Python	Description
max(a,b)	maximum(a,b)	pairwise max

 max of all values in two vectors

#### **Vector multiplication**

MATLAB/Octave	Python	Description
a.*a	a*a	Multiply two vectors
dot(u,v)	dot(u,v)	Vector dot product, \$u \cdot v\$

#### Matrices

MATLAB/Octave	Python	Description
$a = [2 \ 3; 4 \ 5]$	a = array([[2,3],[4,5]])	Define a matrix

#### Concatenation (matrices); rbind and cbind

MATLAB/Octave	Python	Description
[a ; b]	<pre>concatenate((a,b), axis=0) vstack((a,b))</pre>	Bind rows
[a , b]	<pre>concatenate((a,b), axis=1) hstack((a,b))</pre>	Bind columns
	<pre>concatenate((a,b), axis=2) dstack((a,b))</pre>	Bind slices (three-way arrays)
[a(:), b(:)]	<pre>concatenate((a,b), axis=None)</pre>	Concatenate matrices into one vector
[1:4 ; 1:4]	<pre>concatenate((r_[1:5],r_[1:5])).reshape vstack((r_[1:5],r_[1:5]))</pre>	(2,-1) Bind rows (from vectors)
[1:4 ; 1:4] '		Bind columns (from vectors)

# **Array creation**

MATLAB/Octave	Python	Description
zeros(3,5)	zeros((3,5),Float)	0 filled array
	zeros((3,5))	0 filled array of integers
ones(3,5)	ones((3,5),Float)	1 filled array
ones(3,5)*9		Any number filled array
eye(3)	identity(3)	Identity matrix
diag([4 5 6])	diag((4,5,6))	Diagonal
magic(3)		Magic squares; Lo Shu
	a = empty((3,3))	Empty array

#### Reshape and flatten matrices

MATLAB/Octave	Python	Description
reshape(1:6,3,2)';	<pre>arange(1,7).reshape(2,-1) a.setshape(2,3)</pre>	Reshaping (rows first)
reshape(1:6,2,3);	<pre>arange(1,7).reshape(-1,2).trans</pre>	pose() Reshaping (columns first)

#### **Shared data (slicing)**

MATLAB/Octave	Python	Description
b = a	b = a.copy()	Copy of a

#### Indexing and accessing elements (Python: slicing)

MATLAB/Octave	Python	Description
a = [ 11 12 13 14	a = array([[ 11, 12, 13, 14 ],	Input is a 3,4 array
21 22 23 24	[ 21, 22, 23, 24 ],	
31 32 33 34 ]	[ 31, 32, 33, 34 ]])	
a(2,3)	a[1,2]	Element 2,3 (row,col)
a(1,:)	a[0,]	First row
a(:,1)	a[:,0]	First column
a([1 3],[1 4]);	a.take([0,2]).take([0,3], axis=1)	Array as indices
a(2:end,:)	a[1:,]	All, except first row
a(end-1:end,:)	a[-2:,]	Last two rows
a(1:2:end,:)	a[::2,:]	Strides: Every other row
	a[,2]	Third in last dimension (axis)
a(:,[1 3 4])	a.take([0,2,3],axis=1)	Remove one column
	a.diagonal(offset=0)	Diagonal

#### Assignment

MATLAB/Octave	Python	Description
a(:,1) = 99	a[:,0] = 99	
a(:,1) = [99 98 97]'	a[:,0] = array([99,98,97])	
a(a>90) = 90;	<pre>(a&gt;90).choose(a,90) a.clip(min=None, max=90)</pre>	Clipping: Replace all elements over 90
	a.clip(min=2, max=5)	Clip upper and lower values

#### Transpose and inverse

MATLAB/Octave	Python	Description
a'	a.conj().transpose()	Transpose
a.' $or$ transpose(a)	a.transpose()	Non-conjugate transpose
det(a)	linalg.det(a) $or$	Determinant
inv(a)	linalg.inv(a) $\mathit{or}$	Inverse
pinv(a)	linalg.pinv(a)	Pseudo-inverse
norm(a)	norm(a)	Norms
eig(a)	linalg.eig(a)[0]	Eigenvalues

svd(a)	linalg.svd(a)	Singular values
chol(a)	linalg.cholesky(a)	Cholesky factorization
[v,l] = eig(a)	linalg.eig(a)[1]	Eigenvectors
rank(a)	rank(a)	Rank

#### Sum

MATLAB/Octave	Python	Description
sum(a)	a.sum(axis=0)	Sum of each column
sum(a')	a.sum(axis=1)	Sum of each row
sum(sum(a))	a.sum()	Sum of all elements
	a.trace(offset=0)	Sum along diagonal
cumsum(a)	a.cumsum(axis=0)	Cumulative sum (columns)

# **Sorting**

MATLAB/Octave	Python	Description
a = [ 4 3 2 ; 2 8 6 ; 1 4 7 ]	a = array([[4,3,2],[2,8,6], [1,4,7]])	Example data
sort(a(:))	a.ravel().sort() <i>or</i>	Flat and sorted
sort(a)	a.sort(axis=0) $\mathit{or}$ msort(a)	Sort each column
sort(a')'	a.sort(axis=1)	Sort each row
sortrows(a,1)	a[a[:,0].argsort(),]	Sort rows (by first row)
	a.ravel().argsort()	Sort, return indices
	a.argsort(axis=0)	Sort each column, return indices
	a.argsort(axis=1)	Sort each row, return indices

#### Maximum and minimum

MATLAB/Octave	Python	Description
max(a)	a.max(0) $or$ amax(a [,axis=0])	max in each column
max(a')	a.max(1) $or$ amax(a, axis=1)	max in each row
<pre>max(max(a))</pre>	a.max() <i>or</i>	max in array
[v i] = max(a)		return indices, i
max(b,c)	maximum(b,c)	pairwise max
cummax(a)		
	a.ptp(); a.ptp(0)	max-to-min range

# Matrix manipulation

MATLAB/Octave	Python	Description
fliplr(a)	fliplr(a) <i>or</i> a[:,::-1]	Flip left-right
flipud(a)	flipud(a) <i>or</i> a[::-1,]	Flip up-down
rot90(a)	rot90(a)	Rotate 90 degrees
repmat(a,2,3)	kron(ones((2,3)),a)	Repeat matrix: [ a a a ; a a a ]
kron(ones(2,3),a)		

triu(a)	triu(a)	Triangular, upper
tril(a)	tril(a)	Triangular, lower

# **Equivalents to "size"**

MATLAB/Octave	Python	Description
size(a)	a.shape $\mathit{or}$ a.getshape()	Matrix dimensions
size(a,2) <i>or</i> length(a)	a.shape[1] $\mathit{or}$ size(a, axis=1)	Number of columns
length(a(:))	a.size $or$ size(a[, axis=None])	Number of elements
ndims(a)	a.ndim	Number of dimensions
	a.nbytes	Number of bytes used in memory

# Matrix- and elementwise- multiplication

MATLAB/Octave	Python	Description
a .* b	a * b <i>or</i> multiply(a,b)	Elementwise operations
a * b	matrixmultiply(a,b)	Matrix product (dot product)
	inner(a,b) <i>or</i>	Inner matrix vector multiplication \$a\cdot b'\$
	outer(a,b) <i>or</i>	Outer product
kron(a,b)	kron(a,b)	Kronecker product
a / b		Matrix division, $b{\cdot}a^{-1}$
a \ b	linalg.solve(a,b)	Left matrix division, \$b^{-1} {\cdot}a\$ \newline (solve linear equations)
	vdot(a,b)	Vector dot product
	cross(a,b)	Cross product

# Find; conditional indexing

MATLAB/Octave	Python	Description
find(a)	a.ravel().nonzero()	Non-zero elements, indices
[i j] = find(a)	(i,j) = a.nonzero() (i,j) = where(a!=0)	Non-zero elements, array indices
[i j v] = find(a)	<pre>v = a.compress((a!=0).flat) v = extract(a!=0,a)</pre>	Vector of non-zero values
find(a>5.5)	(a>5.5).nonzero()	Condition, indices
	<pre>a.compress((a&gt;5.5).flat)</pre>	Return values
a .* (a>5.5)	where(a>5.5,0,a) $or$ a * (a>5.5)	Zero out elements above 5.5
	<pre>a.put(2,indices)</pre>	Replace values

# Multi-way arrays

MATLAB/Octave	Python	Description	
a = cat(3, [1 2; 1 2],[3 4; 3	a = array([[[1,2],[1,2]], [[3,4],	Define a 3-way array	
4]);	[3,4]]])		
a(1,:,:)	a[0,]		

# File input and output

MATLAB/Octave	Python	Description
<pre>f = load('data.txt')</pre>	<pre>f = fromfile("data.txt") f = load("data.txt")</pre>	Reading from a file (2d)
<pre>f = load('data.txt')</pre>	<pre>f = load("data.txt")</pre>	Reading from a file (2d)
<pre>x = dlmread('data.csv', ';')</pre>	<pre>f = load('data.csv', delimiter=';')</pre>	Reading fram a CSV file (2d)
save -ascii data.txt f	<pre>save('data.csv', f, fmt='%.6f', delimiter=';')</pre>	Writing to a file (2d)
	<pre>f.tofile(file='data.csv', format='%.6f', sep=';')</pre>	Writing to a file (1d)
	<pre>f = fromfile(file='data.csv', sep=';')</pre>	Reading from a file (1d)

# **Plotting**

# Basic x-y plots

MATLAB/Octave	Python	Description
plot(a)	plot(a)	1d line plot
plot(x(:,1),x(:,2),'o')	plot(x[:,0],x[:,1],'o')	2d scatter plot
plot(x1,y1, x2,y2)	plot(x1,y1,'bo', x2,y2,'go')	Two graphs in one plot
plot(x1,y1)	plot(x1,y1,'o')	Overplotting: Add new plots to
hold on	plot(x2,y2,'o')	current
plot(x2,y2)	<pre>show() # as normal</pre>	
subplot(211)	subplot(211)	subplots
plot(x,y,'ro-')	plot(x,y,'ro-')	Plotting symbols and color

#### Axes and titles

MATLAB/Octave	Python	Description
grid on	grid()	Turn on grid lines
<pre>axis equal axis('equal') replot</pre>	<pre>figure(figsize=(6,6))</pre>	1:1 aspect ratio
<pre>axis([ 0 10 0 5 ]) title('title') xlabel('x-axis') ylabel('y-axis')</pre>	axis([ 0, 10, 0, 5 ])	Set axes manually Axis labels and titles
	text(2,25,'hello')	Insert text

# Log plots

MATLAB/Octave	Python	Description
semilogy(a)	semilogy(a)	logarithmic y-axis
semilogx(a)	semilogx(a)	logarithmic x-axis
loglog(a)	loglog(a)	logarithmic x and y axes

# Filled plots and bar plots

MATLAB/Octave	Python	Description
fill(t,s,'b', t,c,'g')	fill(t,s,'b', t,c,'g', alpha=0.2)	Filled plot
% fill has a bug?		

#### **Functions**

MATLAB/Octave	Python	Description
f = inline('sin(x/3) - cos(x/5)	')	Defining functions
ezplot(f,[0,40])	x = arrayrange(0,40,.5)	Plot a function for given range
fplot('sin(x/3) - cos(x/5)',	$y = \sin(x/3) - \cos(x/5)$	
[0,40])	plot(x,y, 'o')	
% no ezplot		

#### **Polar plots**

MATLAB/Octave	Python	Description
theta = 0:.001:2*pi;	theta = arange(0,2*pi,0.001)	
r = sin(2*theta);	r = sin(2*theta)	
polar(theta, rho)	polar(theta, rho)	

# **Histogram plots**

MATLAB/Octave	Python	Description
hist(randn(1000,1))		
hist(randn(1000,1), -4:4)		
plot(sort(a))		

#### 3d data

# Contour and image plots

MATLAB/Octave	Python	Description
contour(z)	<pre>levels, colls = contour(Z, V, origin='lower', extent= (-3,3,-3,3)) clabel(colls, levels, inline=1, fmt='%1.1f', fontsize=10)</pre>	Contour plot
<pre>contourf(z); colormap(gray)</pre>	<pre>contourf(Z, V, cmap=cm.gray, origin='lower', extent=(-3,3,-3,3))</pre>	Filled contour plot
<pre>image(z) colormap(gray)</pre>	<pre>im = imshow(Z, interpolation='bilinear', origin='lower', extent=(-3,3,-3,3))</pre>	Plot image data
	<pre># imshow() and contour() as above</pre>	Image with contours

Direction field vectors

#### Perspective plots of surfaces over the x-y plane

MATLAB/Octave	Python	Description
n=-2:.1:2;	n=arrayrange(-2,2,.1)	
<pre>[x,y] = meshgrid(n,n);</pre>	[x,y] = meshgrid(n,n)	
z=x.*exp(-x.^2-y.^2);	z = x*power(math.e,-x**2-y**2)	
mesh(z)		Mesh plot
<pre>surf(x,y,z) or surfl(x,y,z)</pre>		Surface plot
% no surfl()		

# Scatter (cloud) plots

MATLAB/Octave	Python	Description
plot3(x,y,z,'k+')		3d scatter plot

#### Save plot to a graphics file

MATLAB/Octave	Python	Description
plot(1:10)	<pre>savefig('foo.eps')</pre>	PostScript
print -depsc2 foo.eps		
gset output "foo.eps"		
gset terminal postscript eps		
plot(1:10)		
	savefig('foo.pdf')	PDF
	savefig('foo.svg')	SVG (vector graphics for www)
print -dpng foo.png	<pre>savefig('foo.png')</pre>	PNG (raster graphics)

#### Data analysis

#### Set membership operators

MATLAB/Octave	Python	Description
a = [ 1 2 2 5 2 ]; b = [ 2 3 4 ];	<pre>a = array([1,2,2,5,2]) b = array([2,3,4]) a = set([1,2,2,5,2]) b = set([2,3,4])</pre>	Create sets
unique(a)	unique1d(a) unique(a) set(a)	Set unique
union(a,b)	union1d(a,b) a.union(b)	Set union
<pre>intersect(a,b)</pre>	<pre>intersect1d(a) a.intersection(b)</pre>	Set intersection
setdiff(a,b)	<pre>setdiff1d(a,b) a.difference(b)</pre>	Set difference
setxor(a,b)	<pre>setxor1d(a,b) a.symmetric_difference(b)</pre>	Set exclusion

ismember(2,a)
2 in a
setmember1d(2,a)
contains(a,2)

True for set member

#### **Statistics**

MATLAB/Octave	Python	Description
mean(a)	a.mean(axis=0)	Average
	mean(a [,axis=0])	
median(a)	median(a) $or$ median(a [,axis=0])	Median
std(a)	a.std(axis=0) $or$ std(a [,axis=0])	Standard deviation
var(a)	a.var(axis=0) $\mathit{or}$ var(a)	Variance
corr(x,y)	<pre>correlate(x,y) or corrcoef(x,y)</pre>	Correlation coefficient
cov(x,y)	cov(x,y)	Covariance

# Interpolation and regression

MATLAB/Octave	Python	Description
<pre>z = polyval(polyfit(x,y,1),x) plot(x,y,'o', x,z ,'-')</pre>	(a,b) = polyfit(x,y,1) plot(x,y,'o', x,a*x+b,'-')	Straight line fit
a = x\y	linalg.lstsq(x,y)	Linear least squares $y = ax + b$
polyfit(x,y,3)	<pre>polyfit(x,y,3)</pre>	Polynomial fit

#### **Non-linear methods**

# Polynomials, root finding

MATLAB/Octave	Python	Description
	poly()	Polynomial
roots([1 -1 -1])	roots()	Find zeros of polynomial
f = inline('1/x - (x-1)')		Find a zero near $x = 1$
fzero(f,1)		
solve('1/x = x-1')		Solve symbolic equations
polyval([1 2 1 2],1:10)	polyval(array([1,2,1,2]),arange(1,11)	Evaluate polynomial

#### **Differential equations**

MATLAB/Octave	Python	Description
diff(a)	<pre>diff(x, n=1, axis=0)</pre>	Discrete difference function and
		approximate derivative
		Solve differential equations

#### Fourier analysis

MATLAB/Octave	Python	Description
fft(a)	fft(a) <i>or</i>	Fast fourier transform
ifft(a)	ifft(a) <i>or</i>	Inverse fourier transform

convolve(x,y)

Linear convolution

# Symbolic algebra; calculus

MATLAB/Octave	Python	Description
factor()		Factorization

# **Programming**

MATLAB/Octave	Python	Description
. m	. py	Script file extension
%	#	Comment symbol (rest of line)
% or #		
% must be in MATLABPATH	from pylab import *	Import library functions
% must be in LOADPATH		
string='a=234';	string="a=234"	Eval
eval(string)	eval(string)	

# Loops

MATLAB/Octave	Python	Description
for i=1:5; disp(i); end	for i in range(1,6): print(i)	for-statement
for i=1:5	for i in range(1,6):	Multiline for statements
disp(i)	print(i)	
disp(i*2)	print(i*2)	
end		

#### **Conditionals**

MATLAB/Octave	Python	Description
if 1>0 a=100; end	if 1>0: a=100	if-statement
if 1>0 a=100: else a=0: end		if-else-statement

# Debugging

MATLAB/Octave	Python	Description
ans		Most recent evaluated expression
whos $\mathit{or}$ who		List variables loaded into memory
clear x $\mathit{or}$ clear [all]		Clear variable \$x\$ from memory
disp(a)	print a	Print

# Working directory and OS

MATLAB/Octave	Python	Description
dir <i>or</i> ls	os.listdir(".")	List files in directory
what	<pre>grep.grep("*.py")</pre>	List script files in directory
pwd	os.getcwd()	Displays the current working directory

cd foo os.chdir('foo') !notepad os.system('notepad') os.popen('notepad') system("notepad")

Change working directory Invoke a System Command

Time-stamp: "2007-11-09T16:46:36 vidar" ©2006 Vidar Bronken Gundersen, /mathesaurus.sf.net Permission is granted to copy, distribute and/or modify this document as long as the above attribution is retained.