

# New Energy Estimator for MAGIC Telescope

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## Abstract

MAGIC is a system of two Imaging Atmospheric Cherenkov Telescopes (IACT), to observe the gamma ray with the standard trigger threshold of  $\sim 50\text{GeV}$ . The previous energy estimation has exploited LookUpTable(LUT) method, whose energy resolution yields down to  $\sim 15\%$  in the energy range of  $\sim 500 - 700\text{GeV}$  in case of low zenith angle observations. But the performance is dependent on zenith angle, energy range and event cut condition.

We introduce the new energy estimator to be commonly used for the MAGIC observation data. It takes advantage of Random Forest, which is one of the Machine Learning algorithm, based on the re-investigation of the features of the events.

The energy resolution is always better above  $100\text{ GeV}$  than LUT method. In low zenith angle observation the energy resolution is around  $15\%$  down to  $\sim 13\%$  above  $200\text{GeV}$ . It is comparable with LUT below  $100\text{ GeV}$  at  $\sim 20\%$ . We also show it performs significantly better in high zenith angle observation, in which the energy resolution stays around  $18\%$ .

Furthermore, the energy resolution becomes more reasonable to be characterised as the width of gaussian when the distribution of normalised deviation from true value, i.e.  $(E_{est} - E_{true})/E_{true}$ . Highly deviated estimations from true value becomes so rare that the fitted gaus distribution contain most of the events. The disappearance of the tail gives proper evaluation of resolution in both RMS and the width of the gaus fit to the distribution, which are similar values of XX and XX.

Furthermore, the new estimator is robust on looser cut, and performance doesn't degrade significantly. This allows us to harvest from the performance in the standard analysis, which use only hadronness cuts and theta square cuts.

*Keywords:*

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## 1. Introduction

MAGIC (Major Atmospheric Gamma Imaging Cherenkov telescopes), located at the altitude of 2200 m a.s.l. on the Roque de los Muchachos Observatory on Canary Island of La Palma performs gamma-ray observations as Imaging Atmospheric Cherenkov Telescopes (IACT). It consists of two telescopes, to characterise the electro-magnetic cascade showers produced by gamma-ray of very high energy (VHE,  $\gtrsim 30$  GeV) penetrating the atmosphere, by detecting the Cherenkov photons generated by the cascade particles travelling faster than speed of light in the atmosphere. To detect very small number of photons arriving in very short time scale of  $\sim$  a few ns, Both have 17 m diameter mirror dish in parabolic shapes and 1039 photomultipliers (PMTs) at the focal planes, at the sampling rate of 1.6 GHz.

From the waveform of the PMTs, charge and timing information are extracted. The information of the noise pixels which are not related to the shower image are discarded, and the remaining pixel informations are used to calculate the features of the image of the shower, such as image shape parameters and the timing parameters, in particular the gradient measured along the main axis of the image. Those parameters are used to compute secondary parameters, namely, Hadronness, stereo parameters calculated from the crossing point of the main axes of the Hillas ellipses in the individual cameras ,and stereo parameters from the reconstructed direction using DISP RF method.

For the energy estimation, image shape parameters, timing parameters, stereo parameters from both the crossing point and the DISP RF reconstructed direction are widely used.

Among the features to determine energy, the primal parameters are Size The energy is estimated from the features.

We begin with explaining the data to supervise the estimator In section XX, and the estimators in the previous strategy( LUT) and the new strategy ( RF) in section XX. We compare the performances of LUT and RF in section XX, where we also show the performances of RF on looser cut condition and large zenith observation. In section XX we discuss the the validity comparing different methods and simulation data and the observation data.

## 2. Data for generation and test of the estimator

Since the shower event we detect cannot trace back to the original energy of the incoming gamma ray, simulated  $\gamma$  ray is used for generating estima-

tor and evaluating the performance. In the simulation of  $\gamma$  ray, the energy (true energy) of  $\gamma$  ray, incoming direction and impact point of the shower is assigned. From the generation of the shower and Cherenkov photons, thorough the detection with the telescopes to the calculation of the features is computed event by event. The estimator tries to predict the energy of the gamma-ray from those measured features using a set of simulated data. And the performance is evaluated as how well the estimator can predict the energies from the features in another set of simulated data, in terms of the deviation of estimated energy from the true energy.

Simulation data reflects the configuration of MAGIC telescopes in specific term to reproduce performance, specifying PSF, reflectivity, etc.. . Here we refer to the configuration in 20XX - 20XX.

### 3. Generation of the estimator

The previous version of the estimator adopted LookUp Table method the new estimator adopts Random Forest (RF). All the features are given to the estimator.

Basic idea is that Size is almost proportional to energy. And many correction parameters are needed. Especially, it varies because of the distance of the shower which radiate Cherenkov photons to the telescopes. The two main such effects are the impact point, namely the distance of the shower axis reaching on the ground, and displacement, namely the angular distance from source position to the brightest point of the shower. They can be regarded as the offset of the shower axis on the ground and the offset of the shower along the shower axis.

Those parameters are very well calculated using DISP RF method, and they both have the true values. In case of displacement, the source position assigned in the simulation can be used. In case of impact, the impact position assigned in the simulation can be used. As long as a feature true value and has negligible systematics to the true value, the estimator can be more precise to the true estimation, using the true value.

The impact parameters deduced from the reconstructed direction of  $\gamma$  ray by DISP RF method is very precise to the true impact parameters.

The fluctuation from true value is typically the order of several tens of meters.

However, in case of the high zenith observation above  $Z_d \gtrsim 50$  deg, the fluctuation becomes significantly larger as the shower location becomes more

distant from the ground. The order of a few 100 m of the fluctuation doesn't give useful information any longer, thus this feature cannot be used.

Instead, time gradient is directly related to the impact parameter, and higher energy threshold makes the entire energy range

Timing information is directly related to the distance to Impact point. But the time gradient has uncertainty in the direction, and until around 200 m the information is degenerated, because the sign flips around 120 m. Because of this, time gradient is not dominant information to determine Impact parameter. To overcome this problem, the impact parameter estimated by DISP RF method can be used.

## 4. Performance

We evaluated the performance of the energy estimation. Since the deviation of the estimated energy from true energy differs event by event, it is evaluated as the statistical sum, constructing the distribution of  $(E_{est} - E_{true})/E_{true}$ . We evaluate the energy resolution in two ways, the width of the fitted gaussian to the distribution and RMS.

While the width characterise typical deviation, it discard the outlier events which are not contained in the gaussian shape. Thus the performance should be evaluated also in RMS.

### 4.1. standard zenith

Here we show the comparison of the bias and resolution between LUT and the new estimator.

LUT has much larger RMS compared to the new estimator, due to the significant amount of events deviated outside the fitted gaussian.

While the performance of LUT degrades when looser cut is applied, the new estimator performs still well. Thus this performance can be taken into account also in practical cut condition, like the application of only Hadronness cut and ThetaSquare cut.

### 4.2. high zenith

The performance of the large zenith observation remains stable at around 18%.

## 5. Validation

Since the energy estimators are supervised fully by the simulated data, we need to investigate if it is consistent with the reality. Although we cannot know the true energy of the gamma rays and we can assign likelihood of gamma-ray event by event, we can indirectly approach through On - Off distribution.

### 5.1. Validation dataset

The observation data of Mrk421 in April in 2013, which recorded very high flux state.

### 5.2. Comparison between different estimators

The estimated values should not include systematic differences. The comparison between LUT method and StereoRF method. We compare the spectra obtained by them.

Even if the estimator miss the information from one telescope, the estimation should already be close to each other.

The comparison between the

### 5.3. Feature-value distributions

When a gamma ray at given energy enters the atmosphere from a given direction to a given point on the ground with respect to the telescopes, the observed parameters should be under certain probability distribution, fluctuated only by statistical uncertainty. Therefore, if the data is taken at sufficiently small zenith range, the effect of the direction becomes sufficiently small and the reaching position of the shower on the ground will be averaged out, consequently only the dependency on the energy remains in the observed parameters.

The event parameter distribution can be compared. The distribution of On region subtracted by the distribution of Off region should remain gamma-ray events.

To avoid the effect of migration between different  $E_{true}$ , the distribution is weighted based on the different spectrum between MC and real data.

Simulated gamma are produced with a spectral index of -1.6 (HE). On the other hand, the Mrk421 data shows the spectral function of

The population of simulated gamma is weighted by  $Spectrum_{ofMrk421}/spectrum_{ofMC}$  in

## 6. Conclusion

## References