MQE: Economic Inference from Data: Module 3: Instrumental Variables

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Even with fixed effects, certain types of unobservables can still bias our estimates.

For OVB to not be a problem, we want a treatment variable x_i where we know that there does not exist some omitted variable x_{ov} such that

- $ightharpoonup cor(x_i, x_{ov}) \neq 0$
- ▶ and $cor(y_i, x_{ov}) \neq 0$.

This is a tall order...

But if you try sometimes,

But if you try <u>sometimes</u>, you just <u>might</u> find,

But if you try <u>sometimes</u>,
you just <u>might</u> find,
you get what you need: a good instrumental variable.

An instrument for what?

I am interested in the relationship between y and x_1 .

The true data generating process looks like this:

$$y_i = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \epsilon$$

- \triangleright x_i and x_2 are uncorrelated with ϵ
- x_i and x_2 they are correlated with each other such that $Cov(x_1, x_2) \neq 0$

So whats the problem?

you don't actually observe x₂.

Uh oh.

The problem:

The naive approach (but you of course know better then to do this...)

Regress y on just x_1 :

$$y_i = \beta_0 + \beta_1 x_1 + \nu$$

where

$$\nu = \beta_2 x_2 + \epsilon.$$

The problem:

$$\begin{split} \hat{\beta}_{1,OLS} &= \frac{cov(x_1, y)}{var(x_1)} \\ &= \frac{cov(x_1, \beta_0 + \beta_1 x_1 + \nu)}{var(x_1)} \\ &= \frac{cov(x_1, \beta_0) + cov(x_1, \beta_1 x_1) + cov(x_1, \nu)}{var(x_1)} \\ &= \frac{\beta_1 var(x_1) + cov(x_1, \nu)}{var(x_1)} \\ &= \beta_1 + \frac{cov(x_1, \nu)}{var(x_1)} \end{split}$$

 $cov(x_1, \nu) \neq 0 \Rightarrow \hat{\beta}_{1,OLS}$ is biased.

All is not lost!

An instrumental variable (IV) is a variable that

- ightharpoonup is correlated with the "good" or "exogenous" variation in x_1
- ▶ is unrelated to the "bad" or "endogenous" or "related-to-x₂" variation in x₁.

Formally

An IV is a variable, z that satisfies two important properties:

- ► $Cov(z, x_1) \neq 0$ (the first stage).
- $Cov(z, \nu) = 0$ (the exclusion restriction).

The First Stage

 $Cov(z, x_1) \neq 0$

- \triangleright z and x_1 are correlated
- the IV is useless without a first stage.

We are trying to get a $\hat{\beta}_1$ such that $E[\hat{\beta}_1] = \beta_1$. If our instrument is totally unrelated to x_1 , we won't have any hope of using it to get at β_1 .

The exclusion restriction

$$Cov(z, \nu) = 0$$

- \triangleright z has to affect y **only** through x_1 .
- ightharpoonup \Rightarrow $Cov(z,\epsilon)=0$ (because we've already assumed that x_2 is uncorrelated with ϵ).

The IV estimator

$$\hat{\beta}_{1,IV} = \frac{cov(z,y)}{cov(z,x)}$$

$$= \frac{cov(z,\beta_0 + \beta_1 x_1 + \nu)}{cov(z,x_1)}$$

$$= \beta_1 \frac{cov(z,x_1)}{cov(z,x_1)} + \frac{cov(z,\nu)}{cov(z,x_1)}$$

$$= \beta_1 + \frac{cov(z,\nu)}{cov(z,x_1)}.$$

With the exclusion restriction: $cov(z, \nu) = 0 \Rightarrow E[\hat{\beta}_{1,IV}] = \beta_1$ Woot Woot! We have an unbiased estimator!

Chasing Unicorns

- \triangleright z's that satisfy the first condition are easy to find, and we can test that $Cov(z, x_1) \neq 0$
- ightharpoonup z's that satisfy the exclusion restriction are rare and we cannot test that $Cov(z, \nu) = 0$ since we don't observe ϵ .

Chasing Unicorns

A good IV is not unlike a unicorn. It is quite powerful/magical as it will allow you to recover a consistent estimate of $\hat{\beta}_1$ in a situation that was otherwise hopeless.



Chasing Unicorns

It is also a rare, (some may argue imaginary) beast, that usually turns out to be a horse with an overly optimistic rider (author).



- be skeptical of instrumental variables regressions
- be wary of trying them yourself
- be prepared to convince people the exclusion restriction is satisfied

I generate some simulated data, with properties I fully understand:

The DGP: Y depends on two variables, X_1 and X_2 such that

$$Y_i = \beta_0 + \beta_1 x_{1i} + \beta_2 x_{2i} + \epsilon_i$$

- \triangleright x_1 and x_2 are correlated with $Cor(x_1, x_2) = 0.75$
- ightharpoonup z is correlated with x_1 such that $Cor(x_1, z) = 0.25$
- ightharpoonup z is not correlated with x_2 (so $Cor(x_2,z)=0$).

```
library(MASS)
library(ggplot2)
## Warning: package 'ggplot2' was built under R version 3.6.2
library(stargazer)
##
## Please cite as:
## Hlavac, Marek (2018), stargazer: Well-Formatted Regression and Summary Statistics Tables.
## R package version 5.2.2. https://CRAN.R-project.org/package=stargazer
sigmaMat<-matrix(c(1,0.75,0.25,0.75,1,0,0.25,0,1), nrow=3)
sigmaMat
        [.1] [.2] [.3]
## [1,] 1.00 0.75 0.25
## [2,] 0.75 1.00 0.00
## [3.] 0.25 0.00 1.00
set.seed(3221)
ivdat<- as.data.frame(mvrnorm(10000, mu = c(0.0.0),</pre>
                     Sigma = sigmaMat))
names(ivdat) <- c("x_1", "x_2", "z")
cor(ivdat)
```

```
## x_1 x_2 z
## x_1 1.000000 0.753135403 0.237314050
## x_2 0.7531354 1.000000000 -0.008862925
## z 0.2373140 -0.008862925 1.00000000
```

```
ivdat$error<-rnorm(10000, mean=0, sd=1)
#The data generating process
B1<-10
B2<-(-20)
ivdat$Y<-ivdat$x_1*B1+ivdat$x_2*B2+ivdat$error
knitr::kable(head(ivdat))</pre>
```

Y	error	z	x_2	×_1
-9.253636	-0.6100699	0.6043023	0.8895539	0.9147512
1.736550	-0.9436084	1.6537624	0.7578459	1.7837077
11.994118	1.2663896	-0.0728647	-0.8811583	-0.6895438
-15.679784	0.1740300	0.2623387	1.0688671	0.5523528
38.493805	-0.5827891	0.6425111	-3.1155154	-2.3233713
4.483690	-0.6097235	0.2199799	-0.3597693	-0.2101972

```
simiv1<-lm(Y~x_1+x_2, data=ivdat)
simiv2<-lm(Y~x_1, data=ivdat)</pre>
```

How will our estimate of $\hat{\beta}_1$ in model 2 compare to the true β ?

 \Rightarrow Top Hat

```
stargazer(simiv1, simiv2, header=FALSE, type='latex', omit.stat = "all", single.row = TRUE)
```

Table 2

	Dependent variable:		
	(1)	(2)	
x_1 x_2	10.011*** (0.015) -20.009*** (0.015)	-5.233*** (0.134)	
Constant	0.016 (0.010)	0.079 (0.134)	
Note:	*p<0.1; *	**p<0.05; ***p<0.01	

- With the correctly specified model $E[\hat{\beta}_1] = \beta_1$.
- ▶ If I do not observe x_2 , the naive approach is biased.

Suppose there exists a variable z that satisfies the two conditions outlined above:

- $ightharpoonup Cov(z, V_1) \neq 0$ (the first stage).
- $Cov(z, \nu) = 0$ (the exclusion restriction).

Our simulated data includes z, a variable with these properties cor(ivdat\$z, ivdat\$x 1)

```
[1] 0.237314
```

#note: we can test this correlation because I am working with simulated data and observe \mathbf{x}_2 .
#In the wild \mathbf{x}_2 would be unobservable and you would have to argue that this condition holds.

ivdat\$nu<-B2*ivdat\$x_2+ivdat\$error
cor(ivdat\$z, ivdat\$nu)</pre>

I instrument my endogenous variable, x_1 , with my instrument z: $_{\mathtt{library(lfe)}}$

```
## Loading required package: Matrix
simiv3<-felm(Y~1|0|(x_1~z),ivdat)</pre>
```



- ▶ I get an unbiased estimate of β_1 !
- Careful: R² values get real funky (negative!?!) don't use.

Table 3

	Dependent variable:		
		Υ	
	Ol	LS	felm
	(1)	(2)	(3)
x_1	10.011*** (0.015)	-5.233*** (0.134)	
x_2	-20.009*** (0.015)		
'x_1(fit)'			10.766*** (0.878)
Constant	0.016 (0.010)	0.079 (0.134)	-0.036 (0.209)
R ²	0.995	0.133	-1.111
Adjusted R ²	0.995	0.133	-1.112
Noto:	*n<0.1: **n<0.05: ***n<0.01		

Note: *p<0.1; **p<0.05; ***p<0.01

2SLS:

How does β_{IV} uses the instrumental variable to retrieve an unbiased estimate?

To build intuition, let's look at the two-stage least squares (2SLS) estimator β_{2SLS} .

When we are working with only one instrument and one endogenous regressor, $\beta_{IV}=\beta_{2SLS}.$

2SLS:

2SLS proceeds in two (least squares regression) stages:

▶ the "first stage," a regression of our endogenous variable on our instrument

$$x_1 = \gamma_0 + \gamma_1 z + u.$$

• using the estimated $\hat{\gamma}$ coefficients we generate predicted values, \hat{x}_1 :

$$\hat{x}_1 = \hat{\gamma}_0 + \hat{\gamma}_1 z$$

▶ the "second stage" where we regress our outcome on the predicted values of the endogenous variable

$$y = \beta_0 + \beta_1 \hat{x}_1 + \epsilon$$

The first stage:

```
sim2slsfs<-felm(x_1~z,ivdat)
summary(sim2s1sfs)
##
## Call:
     felm(formula = x_1 \sim z, data = ivdat)
##
## Residuals:
      Min
              10 Median
                                     Max
## -3.6955 -0.6508 -0.0001 0.6500 3.7093
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.006807 0.009723 0.70
                                            0.484
              0.239464 0.009803 24.43 <2e-16 ***
## 2.
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9723 on 9998 degrees of freedom
## Multiple R-squared(full model): 0.05632 Adjusted R-squared: 0.05622
## Multiple R-squared(proj model): 0.05632 Adjusted R-squared: 0.05622
## F-statistic(full model):596.7 on 1 and 9998 DF, p-value: < 2.2e-16
## F-statistic(proj model): 596.7 on 1 and 9998 DF, p-value: < 2.2e-16
```

The second stage:

```
hatgamma0<-sim2slsfs$coefficients[1]
hatgamma1<-sim2slsfs$coefficients[2]
ivdat$hatx_1<-hatgamma0+hatgamma1*ivdat$z
sim2slsss<-felm(Y-hatx 1,ivdat)
```

The second stage:

```
hatgamma0<-sim2slsfs$coefficients[1]
hatgamma1<-sim2slsfs$coefficients[2]
ivdat$hatx_1<-hatgamma0+hatgamma1*ivdat$z
sim2slsss<-felm(Y-hatx_1,ivdat)
```



The second stage:

stargazer(simiv1, simiv2, simiv3, sim2slsss, header=FALSE, type='latex', omit.stat = "all", no.space=TRUE

Table 4

	Dependent variable:				
		Y			
	OL	OLS		elm	
	(1)	(2)	(3)	(4)	
x_1	10.011*** (0.015)	-5.233*** (0.134)			
x_2	-20.009*** (0.015)	()			
'x_1(fit)'	()		10.766*** (0.878)		
hatx_1			(0.070)	10.766*** (0.595)	
Constant	0.016 (0.010)	0.079 (0.134)	-0.036 (0.209)	-0.036 (0.141)	
Note:	*p<0.1; **p<0.05; ***p<0.01				

- ▶ Math Magic! $\hat{\beta}_{1,2SLS}$ consistently estimates β_1 and $\hat{\beta}_{1,2SLS} = \hat{\beta}_{1,IV}$!
- Note: The standard errors reported from the second stage of 2SLS will not be correct (because they are based on \hat{x}_1 rather than x_1).(There are ways to correct this but the math and coding is a bit complicated.)

The Reduced Form (and more cool IV intuition)

The **reduced form** regresses the outcome directly on the exogenous instrument (and any other exogenous variables if you have them):

$$y_i = \pi_0 + \pi_1 z + \eta$$

```
sim2slsrf<-felm(Y-z,ivdat)
stargazer(sim2slsfs, sim2slsss, sim2slsrf, type='latex', header=FALSE, omit.stat = "all")</pre>
```

Table 5

	Dependent variable:		
	×_1	Y	
	(1)	(2)	(3)
z	0.239***		2.578***
	(0.010)		(0.142)
hatx_1		10.766*** (0.595)	
Constant	0.007 (0.010)	-0.036 (0.141)	0.037 (0.141)
Note:	*1	o<0.1; **p<0.05;	***p<0.01

The Reduced Form (and more cool IV intuition)

We can recover $\hat{\beta}_1$ by taking the $\hat{\pi}_1$ from the reduced form and dividing it by $\hat{\gamma}_1$ from the first stage:

$$\hat{\beta}_1 = \frac{\hat{\pi}_1}{\hat{\gamma}_1} = \frac{2.578}{0.239} = 10.786$$

- ► Math Magic!
- Why does this work?



The Reduced Form (and more cool IV intuition)

We can recover $\hat{\beta}_1$ by taking the $\hat{\pi}_1$ from the reduced form and dividing it by $\hat{\gamma}_1$ from the first stage:

$$\hat{\beta}_1 = \frac{\hat{\pi}_1}{\hat{\gamma}_1} = \frac{2.578}{0.239} = 10.786$$

- ► Math Magic!
- Why does this work? We are taking the effect of z on y and scaling it by the effect of z on x₁ (since z affects y via x₁).



We saw the good. Now for the bad and ugly.

- ► The Forbidden Regression
- ► Weak Instruments



The Bad: The Forbidden Regression

Be weary of the **forbidden regression**!

People sometimes try to run a logit, probit, Poisson or some other non-linear regression as the first stage of a 2SLS procedure. This is a bad idea. Don't do it.

The Ugly: Weak Instruments

Recall that

$$\hat{\beta}_{IV} = \beta + \frac{cov(z, \nu)}{cov(z, x_1)}.$$

A weak instrument is an instrument with a weak first stage: $Cov(z, x_1)$, is small.

Why is this a problem?

The Ugly: Weak Instruments

A weak instrument will amplify any endogeneity that exists in your model.

For $E[\hat{\beta}_{IV}] = \beta_1$, we need $cov(z, \nu) = 0$ (the exclusion restriction) to hold.

Suppose this assumption is violated in a small way, meaning that $cov(z, \nu) \neq 0$ but that it was a vary small value.

If $cov(z, x_1)$ is also small, the violation of the exclusion restriction will get amplified leading to potentially severe bias in our estimator.

The Ugly: Simulation

I generate a simulated dataset with:

- ▶ a week first stage $cov(z, x_1) = 0.03$
- ightharpoonup a small violation of the exclusion restriction, $cov(z,x_2)=0.01$

```
## x_1 x_2 z

## x_1 0.98285285 0.74457303 0.02472936

## x_2 0.74457303 1.00432318 0.01277121

## z 0.02472936 0.01277121 0.98892020

ivdatwk$error<-rnorm(10000, mean=0, sd=1)

ivdatwk$nu=(-20)*ivdatwk$x_2*ivdatwk$error
```

The Ugly: Simulation

```
#The data generating process
B1<-10
B2<-(-20)
ivdatwk$Y<-ivdatwk$x_1*B1+ivdatwk$x_2*B2+ivdatwk$error

simivweakfs<-lm(x_1-z,ivdatwk)
simivweak<-felm(Y-1|0|(x_1-z),ivdatwk)
stargazer(simivweakfs,simivweak, type='latex', omit.stat = c("n", "adj.rsq", "rsq", "ser"), header=FALSE</pre>
```

Table 6

	Dependent variable:	
	x_1	Υ
	OLS	felm
	(1)	(2)
Z	0.025** (0.010)	
'x_1(fit)'		-0.415 (5.685)
Constant	0.007 (0.010)	0.137 (0.146)
F Statistic	6.295** (df = 1; 9998)	
Note:	*p<0.1; **p<0.05; ***p<0.01	

The Ugly: Simulation

cov(ivdatwk\$z,ivdatwk\$x_1)

[1] 0.02472936

cov(ivdatwk\$z,ivdatwk\$nu)

[1] -0.2575614

We can see that $cov(z, x_1) = 0.02473$ and $cov(z, \nu) = -0.25756$ so

$$\hat{\beta}_{1,IV} = 10 + \frac{-0.25756}{0.02473} = -0.415 \neq \beta_1 = 10.$$



The Ugly: Weak Instruments

This is a major problem because:

- ▶ It is rare that an instrument would be perfectly independent of all confounding factors, and
- it is impossible to test the exclusion restriction.
- \Rightarrow be very cautious about results when there is a weak first stage.

What constitutes a "weak" instrument?

The standard benchmark is a first stage F-test that is less than 10.

Dealing with Multiples

See the lecture notes for example of how to deal with more complicated specifications:

- Control variables
- Multiple Instruments
- Multiple endogenous variables and multiple instruments

Unicorns and Work-horses



The real Siberian unicorn, Elasmotherium sibiricum, 29,000 BC.

Unicorns and Work-horses

IV estimations show up in two different types of situations:

- ► IV projects:
 - the validity of the instrumental variable is central to the identification strategy
 - can be very interesting because they are often looking at an important but highly endogenous variable
 - the validity of the causal claims, depends <u>heavily</u> on the validity of the instrument.
- Cameo appearances in other projects:
 - in randomized control trials (RCT)
 - ▶ in regression discontinuity (RD) projects
 - the random assignment of treatment is used as an instrument to estimate treatment effects

"Work Horse" IV intuition and medical trials (RCT)

Medical trials are a fantastic example of an application of instrumental variables:

- socially important (perhaps the most important application of IV to date)
- very clean experimental design

And this is a good segway to the RCT module.

The model for a medical trial:

$$y_i = \beta_0 + \beta_1 d_i + \epsilon_i.$$

- \triangleright y_i represents a medical outcome (continuous or discreet).
- $ightharpoonup d_i$ is generally a dummy variable (1 if treated and 0 if not).
- ▶ The error term, ϵ_i represents all other factors that affect the health outcome

This regression model corresponds to the potential outcome model with constant treatment effects:

$$y = dy_1 + (1 - d)y_0$$

 $y_0 = \beta_0 + \epsilon$
 $y_1 = y_0 + \beta_1$.

Our goal:

- estimate the effect that the treatment (say a pill) has on our outcome (say blood pressure)
- \blacktriangleright our hope is that β_1 is large and negative.

Options: Non-Experimental estimates:

- Selling the drug to the general population.
- Collect some data
- Regress blood pressure on whether or not you take the pill
- Problem:
 - people who take the pill are the ones who have high blood pressure to begin with!
 - We will likely get a positive estimate of β_1 (even with controls).

Options: A Medical Trial:

- randomly assign some patients to the treatment group and others to the control group.
- Treatment group is given the pill and told to take it
- Control group are given a placebo (or nothing at all).

Back in the old days: the **intention to treat** (or ITT) estimate:

- ightharpoonup Calculate $\bar{y}_{i,treat} \bar{y}_{i,control}$
- This is the equivalent to estimating $y_i = \beta_0 + \beta_1 d_i + \epsilon$ where $d_i = 1$ if in the treatment group and 0 if in the control group
- intention to treat because you compare the group that you intended to treat and the group that you do not intend to treat.

What is the problem with this?

Non-compliance:

- some (selected) people in the treatment group would fail to take the pill
- some (selected) people in the control group would obtain the pill from another source (even though they were not supposed to)

Non-compliance can bias in the estimate of β_1 .

How can this bias be corrected?

The "Work Horse" IV:

This is actually a simple IV problem:

- ▶ The instrument, z_i is the intention to treat:
 - $z_i = 1$ if you are assigned to the treatment group (we intend to treat you)
 - $z_i = 0$ if you are assigned to the control group (we do not intend to treat you)

Does z_i satisfies the two properties of a good instrument?

The "Work Horse" IV:

Does z_i satisfies the two properties of a good instrument?

- \triangleright z_i is randomly assigned so by construction will be uncorrelated with ν_i so $cov(z_i, \nu_i) = 0$ (the exclusion restriction).
- > z_i is correlated with d_i , because you are going to be more likely to take the pill if you are in the treatment group so $cov(z_i, d_i) \neq 0$ (the first stage).
- \Rightarrow z_i is a valid instrument for d_i and the IV estimator gives us a consistent estimate of β_1 , the effect of taking the pill on blood pressure.

How does this fix the non-compliance problem?

Example:

- Assume the non-compliance problem only exists for the people in the treatment group.
- Only half the people in the treatment group take the pill (ie half of the treatment group fails to comply and does not take the pill while the other half takes the pill as they were told to)

What will the IV look like?

The first stage will regress whether you took the pill on whether you were in the treatment group d_i on z_i :

$$d_i = \gamma_0 + \gamma_1 z_i + u_i$$

Zero people in the control group took the pill while half in the treatment group took the pill:

$$\Rightarrow E[\hat{\gamma}_0] = 0$$
 and $E[\hat{\gamma}_1] = 0.5$.

The IV estimate is the reduced form scaled by the first stage:

The reduced form is a regression of y_i (your blood pressure) on z_i (whether you were assigned to the treatment or control group):

$$y_i = \pi_0 + \pi_1 z_i + v_i$$

Therefore our IV estimate,

$$\hat{\beta}_{IV} = \frac{\hat{\pi}_1}{\hat{\gamma}_1} = \frac{\hat{\pi}_1}{0.5}.$$

How is this fixing the non-complier problem?

How is this fixing the non-complier problem?

The reduced form is estimating the effect that being assigned to the treatment group has on blood pressure.

If there were a perfect compliance:

- the reduced form estimate would be the effect of taking the pill
 - the first stage would give us $\hat{\gamma}_1=1$
 - the IV estimate would be $\hat{\beta}_{IV} = \frac{\hat{\pi}_1}{1} = \hat{\pi}_1$.

If compliance isn't perfect:

- the reduced form estimates the effect of increasing the probability you take the pill
 - This means that the reduced form is not estimating the full effect of taking the pill

The "Work Horse" IV: Intuition: Example

- ▶ 10 people in the treatment group. 5 take the pill and 5 do not.
 - ▶ The (expected) mean blood pressure for the treatment group:

$$E[y_i|\mathit{TreatGroup}_i] = \frac{5\beta_0 + 5(\beta_0 + \beta_1)}{10} = \beta_0 + \frac{\beta_1}{2}$$

- ▶ 10 people in the control group, no one takes the pill.
 - ► The (expected) mean blood pressure for the control group:

$$E[y_i|ContGroup_i] = \beta_0$$

So the reduced form coefficient(=the difference of means):

$$\hat{\pi}_1 = \beta_0 + \frac{\beta_1}{2} - \beta_0 = \frac{\beta_1}{2}$$

is half the effect of taking the pill (since only half the treated group takes it).

The "Work Horse" IV: Intuition: Example

Thus,

$$E[\beta_{1,IV}] = \frac{\pi_1}{\gamma_1} = \frac{0.5\beta_1}{0.5} = \beta_1.$$

The IV estimate gives us a consistent estimate because it is scaling the reduced form by the first stage.

We re-scale the reduced form because:

- being in the treatment group only increases your probability of taking the pill by 50 percentage points not by a full 100 percentage points.
- the reduced form only represents half of the effect of taking the pill

Also, the IV is different from simply taking the mean of y_i for those in the treatment group who took the pill and subtracting the mean of y_i for those in the control group who did not take the pill.

This would be affected by the same selection issues as a simple OLS regression of y_i on d_i .

(The people in the treatment group who choose not to take the pill do so because their blood pressure was not very high to begin with. Those who take the pill are the ones that all had high blood pressure so we will tend to underestimate the pill's effect).

Recall Arseneaux, Gerber and Green (2006):

Evaluate a "Get out the Vote" mobilization:

- ▶ Who gets called (Call_i) is random
- ▶ Who answers the call (Contact_i) is not

In the paper they generate:

- estimates that controlled for observable characteristics
- "experimental" estimates in order to gauge bias from unobservables

The "experimental" estimates use an instrumental variable.

They are interested in estimating how getting contacted by the "Get out the Vote" mobilization affect the likelihood of actually voting:

$$Votes_i = \beta_0 + \beta_1 Contacted_i + \beta_j X_j + \epsilon_i$$
.

But who gets contacted however is not random as not everyone will pick up the phone!

They instrument $Contacted_i$, with being randomly assigned to receive a call from the campaign. Thus the first stage is

$$Contacted_i = \gamma_0 + \gamma_1 Called_i + \gamma_j X_j + u_i$$

Replicating results of columns 1 of p.49 and p.50:

library(haven)

```
## Warning: package 'haven' was built under R version 3.6.3
agg_data<-read_dta("../../data/data_M3_IV/IA_MI_merge040504.dta")

#scalling the vote02 variable to remove excess 0's from tables
agg_data$vote02<-100*as.numeric(agg_data$vote02)

regols1<-felm(vote02-contact+state+comp_mi+comp_ia,agg_data)
regiv1<-felm(vote02-state+comp_mi+comp_ia|0|(contact-treat_real+state+comp_mi+comp_ia),agg_data)</pre>
```

```
## Warning in chol.default(mat, pivot = TRUE, tol = tol): the matrix is either
## rank-deficient or indefinite
```

Replicating results of columns 1 of p.49 and p.50:

stargazer(regols1,regiv1,type='latex', se = list(regols1\$rse, regiv1\$rse), header=FALSE, omit.stat = "al

Table 7

	Dependent variable: vote02	
	(1)	(2)
contact	6.207***	
	(0.306)	
state	6.671***	7.388***
	(0.347)	(0.350)
comp_mi	4.836***	4.911***
	(0.098)	(0.098)
comp_ia	6.353***	6.083***
. —	(0.177)	(0.178)
'contact(fit)'		0.360
. ,		(0.498)
Constant	46.128***	46.081***
	(0.126)	(0.126)
Note:	*p<0.1; **p<0.05; ***p<0.01	