ETHEREUM: A SECURE DECENTRALISED GENERALISED TRANSACTION LEDGER PROOF-OF-CONCEPT V

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ABSTRACT. The blockchain paradigm when coupled with cryptographically-secured transactions has demonstrated its utility through a number of projects, not least Bitcoin. Each such project can be seen as a simple application on a decentralised, but singleton, compute resource. We can call this paradigm a transactional singleton machine with shared-state.

Ethereum implements this paradigm in a generalised manner. Furthermore it provides a plurality of such resources, each with a distinct state and operating code but able to interact through a message-passing framework with others. We discuss its design, implementation issues, the opportunities it provides and the future hurdles we envisage.

1. Introduction

With ubiquitous internet connections in most places of the world, global information transmission has become incredibly cheap. Technology-rooted movements like Bitcoin have demonstrated, through the power of the default, consensus mechanisms and voluntary respect of the social contract that it is possible to use the internet to make a decentralised value-transfer system, shared across the world and virtually free to use. This system can be said to be a very specialised version of a cryptographically secure, transaction-based state machine. Follow-up systems such as Namecoin adapted this original "currency application" of the technology into other applications albeit rather simplistic ones.

Ethereum is a project which attempts to build the generalised technology; technology on which all transaction-based state machine concepts may be built. Moreover it aims to provide to the end-developer a tightly integrated end-to-end system for building software on a hitherto unexplored compute paradigm in the mainstream: a trustful object messaging compute framework.

1.1. **Driving Factors.** There are many goals of this project; one key goal is to facilitate transactions between consenting individuals who would otherwise have no means to trust one another. This may be due to geographical separation, interfacing difficulty, or perhaps the incompatibility, incompetence, unwillingness, expense, uncertainty, inconvenience or corruption of existing legal systems. By specifying a state-change system through a rich and unambiguous language, and furthermore architecting a system such that we can reasonably expect that an agreement will be thus enforced autonomously, we can provide a means to this end.

Dealings in this proposed system would have several attributes not often found in the real world. The incorruptibility of judgement, often difficult to find, comes naturally from a disinterested algorithmic interpreter. Transparency, or being able to see exactly how a state or judgement came about through the transaction log and rules or instructional codes, never happens perfectly in human-based systems since natural language is necessarily vague,

information is often lacking, and plain old prejudices are difficult to shake.

Overall, I wish to provide a system such that users can be guaranteed that no matter with which other individuals, systems or organisations they interact, they can do so with absolute confidence in the possible outcomes and how those outcomes might come about.

1.2. **Previous Work.** Buterin [2013] first proposed the kernel of this work in late November, 2013. Though now evolved in many ways, the key functionality of a block-chain with a Turing-complete language and an effectively unlimited inter-transaction storage capability remains unchanged.

Hashcash, introduced by Back [2002] (in a five-year retrospective), provided the first work into the usage of a cryptographic proof of computational expenditure as a means of transmitting a value signal over the Internet. Though not widely adopted, the work was later utilised and expanded upon by Nakamoto [2008] in order to devise a cryptographically secure mechanism for coming to a decentralised social consensus over the order and contents of a series of cryptographically signed financial transactions. The fruits of this project, Bitcoin, provided a first glimpse into a decentralised transaction ledger.

Other projects built on Bitcoin's success; the alt-coins introduced numerous other currencies through alteration to the protocol. Some of the best known are Litecoin and Primecoin, discussed by Sprankel [2013]. Other projects sought to take the core value content mechanism of the protocol and repurpose it; Aron [2012] discusses, for example, the Namecoin project which aims to provide a decentralised name-resolution system.

Other projects still aim to build upon the Bitcoin network itself, leveraging the large amount of value placed in the system and the vast amount of computation that goes into the consensus mechanism. The Mastercoin project, first proposed by Willett [2013], aims to build a richer protocol involving many additional high-level features on top of the Bitcoin protocol through utilisation of a number of auxiliary parts to the core protocol. The Coloured Coins project, proposed by Rosenfeld [2012], takes a similar but more simplified strategy, embellishing the rules

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of a transaction in order to break the fungibility of Bitcoin's base currency and allow the creation and tracking of tokens through a special "chroma-wallet"-protocol-aware piece of software.

Additional work has been done in the area with discarding the decentralisation foundation; Ripple, discussed by Boutellier and Heinzen [2014], has sought to create a "federated" system for currency exchange, effectively creating a new financial clearing system. It has demonstrated that high efficiency gains can be made if the decentralisation premise is discarded.

Early work on smart contracts has been done by Szabo [1997] and Miller [1997]. Around the 1990s it became clear that algorithmic enforcement of agreements could become a significant force in human cooperation. Though no specific system was proposed to implement such a system, it was proposed that the future of law would be heavily affected by such systems. In this light, Ethereum may be seen as a general implementation of such a *crypto-law* system.

2. The Blockchain Paradigm

Ethereum, taken as a whole, can be viewed as a transaction-based state machine: we begin with a genesis state and incrementally execute transactions to morph it into some final state. It is this final state which we accept as the canonical "version" of the world of Ethereum. The state can include such information as account balances, reputations, trust arrangements, data pertaining to information of the physical world; in short, anything that can currently be represented by a computer is admissible. Transactions thus represent a valid arc between two states; the 'valid' part is important—there exist far more invalid state changes than valid state changes. Invalid state changes might, e.g. be things such as reducing an account balance without an equal and opposite increase elsewhere. A valid state transition is one which comes about through a transaction. Formally:

(1)
$$\sigma_{t+1} \equiv \Upsilon(\sigma_t, T)$$

where Υ is the Ethereum state transition function. In Ethereum, Υ , together with σ are considerably more powerful then any existing comparable system; Υ allows components to carry out arbitrary computation, while σ allows components to store arbitrary state between transactions.

Transactions are collated into blocks; blocks are chained together using a cryptographic hash as a means of reference. Blocks function as a journal, recording a series of transactions together with the previous block and an identifier for the final state (though do not store the final state itself—that would be far too big). They also punctuate the transaction series with incentives for nodes to *mine*. This incentivisation takes places as a state-transition function, adding value to a nominated account.

Mining is the process of dedicating effort (working) to bolster one series of transactions (a block) over any other potential competitor block. It is achieved thanks to a cryptographically secure proof. This scheme is known as a proof-of-work and is discussed in detail in section 11.5. Formally, we expand to:

- (2) $\sigma_{t+1} \equiv \Pi(\sigma_t, B)$
- (3) $B \equiv (..., (T_0, T_1, ...))$

(4)
$$\Pi(\boldsymbol{\sigma}, B) \equiv \Omega(B, \Upsilon(\Upsilon(\boldsymbol{\sigma}, T_0), T_1)...)$$

Where Ω is the block-finalisation state transition function (a function that rewards a nominated party); B is this block, which includes a series of transactions amongst some other components; and Π is the block-level state-transition function.

This is the basis of the blockchain paradigm, a model that forms the backbone of not only Ethereum, but all decentralised consensus-based transaction systems to date.

2.1. Value. In order to incentivise computation within the network, there needs to be an agreed method for transmitting value. To address this issue, Ethereum has an intrinsic currency, Ether, known also as ETH and sometimes referred to by the Old English $\mathfrak D$. The smallest subdenomination of Ether, and thus the one in which all integer values of the currency are counted, is the Wei. One Ether is defined as being 10^{18} Wei. There exist other subdenominations of Ether:

Multiplier	Name
10 ⁰	Wei
10^{12}	Szabo
10^{15}	Finney
10^{18}	Ether

Throughout the present work, any reference to value, in the context of Ether, currency, a balance or a payment, should be assumed to be counted in Wei.

2.2. Which History? Since the system is decentralised and all parties have an opportunity to create a new block on some older pre-existing block, the resultant structure is necessarily a tree of blocks. In order to form a consensus as to which path, from root (the genesis block) to leaf (the block containing the most recent transactions) through this tree structure, known as the blockchain, there must be an agreed-upon scheme. If there is ever a disagreement between nodes as to which root-to-leaf path down the block tree is the 'best' blockchain, then a *fork* occurs.

This would mean that past a given point in time (block), multiple states of the system may coexist: some nodes believing one block to contain the canonical transactions, other nodes believing some other block to be canonical, potentially containing radically different or incompatible transactions. This is to be avoided at all costs as the uncertainty that would ensue would likely kill all confidence in the entire system.

The scheme we use in order to generate consensus is a simplified version of the GHOST protocol introduced by Sompolinsky and Zohar [2013]. This process is described in detail in section 10.

3. Conventions

I use a number of typographical conventions for the formal notation, some of which are quite particular to the present work:

The two sets of highly structured, 'top-level', state values, are denoted with bold lowercase Greek letters. They fall into those of world-state, which are denoted σ (or a variant thereupon) and those of machine-state, μ .

Functions operating on highly structured values are denoted with an upper-case greek letter, e.g. Υ , the Ethereum state transition function.

For most functions, an uppercase letter is used, e.g. C, the general cost function. These may be subscripted to denote specialised variants, e.g. $C_{\rm SSTORE}$, the cost function for the sstore operation. For specialised and possibly externally defined functions, I may format as typewriter text, e.g. the SHA3 hash function is denoted SHA3.

Tuples are typically denoted with an upper-case letter, e.g. T, is used to denote an Ethereum transaction. This symbol may, if accordingly defined, be subscripted to refer to an individual component, e.g. T_s , denotes the timestamp of said transaction. The form of the subscript is used to denote its type; e.g. uppercase subscripts refer to tuples with subscriptable components.

Scalars and fixed-size byte sequences (or, synony-mously, arrays) are denoted with a normal lower-case letter, e.g. n is used in the document to denote a transaction nonce. Those with a particularly special meaning may be greek, e.g. δ , the number of items required on the stack for a given operation.

Arbitrary-length sequences are typically denoted as a bold lower-case letter, e.g. \mathbf{o} is used to denote the byte-sequence given as the output data of a message call. For particularly important values, a bold uppercase letter may be used.

Throughout, we assume scalars are positive integers and thus belong to the set \mathbb{P} . The set of all byte sequences is \mathbb{B} , formally defined in Appendix C. If such a set of sequences is restricted to those of a particular length, it is denoted with a subscript, thus the set of all byte sequences of length 32 is named \mathbb{B}_{32} . This is formally defined in section 4.3

Square brackets are used to index into and reference individual components or subsequences of sequences, e.g. $\mu_s[0]$ denotes the first item on the machine's stack. For subsequences, ellipses are used to specify the intended range, to include elements at both limits, e.g. $\mu_m[0..31]$ denotes the first 32 items of the machine's memory.

In the case of the global state σ , which is a sequence of accounts, themselves tuples, the square brackets are used to reference an individual account.

When considering variants of existing values, I follow the rule that within a given scope for definition, if we assume that the unmodified 'input' value be denoted by the placeholder \square then the modified and utilisable value is denoted as \square' , and intermediate values would be \square^* , \square^{**} &c. On very particular occasions, in order to maximise readability and only if unambiguous in meaning, I may use alpha-numeric subscripts to denote intermediate values, especially those of particular note.

When considering the use of existing functions, given a function f, the function f^* denotes a similar, elementwise version of the function mapping instead between sequences. It is formally defined in section 4.3.

I define a number of useful functions throughout. One of the more common is ℓ , which evaluates to the last item in the given sequence:

(5)
$$\ell(\mathbf{x}) \equiv \mathbf{x}[\|\mathbf{x}\| - 1]$$

4. Blocks, State and Transactions

Having introduced the basic concepts behind Ethereum, we will discuss the meaning of a transaction, a block and the state in more detail.

4.1. World State. The world state (state), is a mapping between addresses (160-bit identifiers) and account states (a data structure serialised as RLP, see Appendix C). Though not stored on the blockchain, it is assumed that the implementation will maintain this mapping in a modified Merkle Patricia tree (trie, see Appendix E). The trie requires a simple database backend that maintains a mapping of bytearrays to bytearrays; we name this underlying database the state database. This has a number of benefits; firstly the root node of this structure is cryptographically dependent on all internal data and as such its hash can be used as a secure identity for the entire system state. Secondly, being an immutable data structure, it allows any previous state (whose root hash is known) to be recalled by simply altering the root hash accordingly. Since we store all such root hashes in the blockchain, we are able to trivially revert to old states.

The account state comprises the first two, and potentially the last two, of the following fields:

nonce: A scalar value equal to the number of transactions sent from this address or, in the case of accounts with associated code, the number of contract-creations made by this account. For account of address a in state σ , this would be formally denoted $\sigma[a]_n$.

balance: A scalar value equal to the number of Wei owned by this address. Formally denoted $\sigma[a]_b$.

stateRoot: A 256-bit hash of the root node of a trie structure that encodes the storage contents of the account (a mapping between 256-bit integer values), encoded into the trie as a mapping from a byte array of size 32 to an RLP-encoded integer. The hash is formally denoted $\sigma[a]_s$.

codeHash: The hash of the EVM code of this account—this is the code that gets executed should this address receive a message call; it is immutable and thus, unlike all other fields, cannot be changed after construction. All such code fragments are contained in the state database under their corresponding hashes for later retrieval. This hash is formally denoted $\sigma[a]_c$, and thus the code may be denoted as \mathbf{b} , given that $\mathtt{SHA3}(\mathbf{b}) = \sigma[a]_c$.

Since I typically wish to refer not to the trie's root hash but to the underlying set of key/value pairs stored within, I define a convenient equivalence:

(6)
$$TRIE(L_I^*(\boldsymbol{\sigma}[a]_s)) \equiv \boldsymbol{\sigma}[a]_s$$

The collapse function for the set of key/value pairs in the trie, L_I^* , is defined as the element-wise transformation of the base function L_I , given as:

(7)
$$L_I((k,v)) \equiv (k, \text{RLP}(v))$$

where:

It shall be understood that $\sigma[a]_s$ is not a 'physical' member of the account and does not contribute to its later serialisation.

If the **codeHash** field is the SHA3 hash of the empty string, i.e. $\sigma[a]_c = \text{SHA3}(())$, then the node represents a simple account, sometimes referred to as a "non-contract" account.

Thus we may define a world-state collapse function L_S :

(9)
$$L_S(\boldsymbol{\sigma}) \equiv \{p(a) : \boldsymbol{\sigma}[a] \neq \emptyset\}$$

where

(10)
$$p(a) \equiv (a, \text{RLP}((\boldsymbol{\sigma}[a]_n, \boldsymbol{\sigma}[a]_b, \boldsymbol{\sigma}[a]_s, \boldsymbol{\sigma}[a]_c)))$$

This function, L_S , is used alongside the trie function to provide a short identity (hash) of the world state. We assume:

(11)
$$\forall a : \boldsymbol{\sigma}[a] = \varnothing \lor (a \in \mathbb{B}_{20} \land v(\boldsymbol{\sigma}[a]))$$

where v is the account validity function:

$$(12) v(x) \equiv x_n \in \mathbb{P} \land x_b \in \mathbb{P} \land x_s \in \mathbb{B}_{32} \land x_c \in \mathbb{B}_{32}$$

4.2. The Transaction. A transaction (formally, T) is a single cryptographically-signed instruction sent by an actor external to Ethereum. An external actor can be a person (via a mobile device or desktop computer) or could be from a piece of automated software running on a server. There are two types of transactions: those which result in message calls and those which result in the creation of new accounts with associated code (known informally as 'contract creation'). Both types specify a number of common fields:

nonce: A scalar value equal to the number of transactions sent by the sender; formally T_n .

gasPrice: A scalar value equal to the number of Wei to be paid per unit of gas for all computation costs incurred as a result of the execution of this transaction; formally T_p .

gasLimit: A scalar value equal to the maximum amount of gas that should be used in executing this transaction. This is paid up-front, before any computation is done and may not be increased later; formally T_g .

to: The 160-bit address of the message call's recipient or the zero address for a contract creation transaction; formally T_t .

value: A scalar value equal to the number of Wei to be transferred to the message call's recipient or, in the case of contract creation, as an endowment to the newly created account; formally T_v .

v, **r**, **s**: Values corresponding to the signature of the transaction and used to determine the sender of the transaction; formally T_w , T_r and T_s . This is expanded in Appendix F.

Additionally, a contract creation transaction contains:

init: An unlimited size byte array specifying the EVM-code for the account initialisation procedure, formally T_i .

init is an EVM-code fragment; it returns the **body**, a second fragment of code that executes each time the account receives a message call (either through a transaction or due to the internal execution of code). init is executed only once at account creation and gets discarded immediately thereafter.

However, a message call transaction contains:

data: An unlimited size byte array specifying the input data of the message call, formally T_{d} .

Appendix F specifies the function, S, which maps transactions to the sender, and happens through the ECDSA of the SECP-256k1 curve, using the hash of the transaction (excepting the latter three signature fields) as the datum to sign. For the present we simply assert that the sender of a given transaction T can be represented with S(T).

(13)
$$L_T(T) \equiv \begin{cases} (T_n, T_p, T_g, T_t, T_v, T_i, T_w, T_r, T_s) & \text{if } T_t = 0\\ (T_n, T_p, T_g, T_t, T_v, T_d, T_w, T_r, T_s) & \text{otherwise} \end{cases}$$

Here, we assume all components are interpreted by the RLP as integer values, with the exception of the arbitrary length byte arrays $T_{\mathbf{i}}$ and $T_{\mathbf{d}}$ and the address hash $T_{\mathbf{t}}$:

(14)
$$T_{n} \in \mathbb{P} \quad \wedge \quad T_{v} \in \mathbb{P} \quad \wedge \quad T_{p} \in \mathbb{P} \quad \wedge \\ T_{g} \in \mathbb{P} \quad \wedge \quad T_{w} \in \mathbb{P} \quad \wedge \quad T_{r} \in \mathbb{P} \quad \wedge \\ T_{s} \in \mathbb{P} \quad \wedge \quad T_{\mathbf{d}} \in \mathbb{B} \quad \wedge \quad T_{\mathbf{i}} \in \mathbb{B} \quad \wedge \\ T_{t} \in \mathbb{B}_{20}$$

4.3. The Block. The block in Ethereum is the collection of relevant pieces of information (known as the block header), H, together with information corresponding to the comprised transactions, \mathbf{R} , and a set of other block headers \mathbf{U} that are known to have a parent equal to the present block's parent's parent (such blocks are known as uncles). The block header contains several pieces of information:

parentHash: The SHA3 256-bit hash of the parent block, in its entirety; formally H_p .

unclesHash: The SHA3 256-bit hash of the uncles list portion of this block; formally H_u .

coinbase: The 160-bit address to which all fees collected from the successful mining of this block be transferred; formally H_b .

stateRoot: The SHA3 256-bit hash of the root node of the state trie, after all transactions are executed and finalisations applied; formally H_r .

transactionsTrie: The SHA3 256-bit hash of the root node of the trie structure populated with each transaction in the transactions list portion of the block; formally H_t .

difficulty: A scalar value corresponding to the difficulty level of this block. This can be calculated from the previous block's difficulty level and the timestamp; formally H_d .

number: A scalar value equal to the number of ancestor blocks. The genesis block has a number of zero; formally H_i .

minGasPrice: A scalar value equal to the minimum price of gas a transaction must have provided in order to be sufficient for inclusion by this miner in this block; formally H_m .

gasLimit: A scalar value equal to the current limit of gas expenditure per block; formally H_l .

gasUsed: A scalar value equal to the total gas used in transactions in this block; formally H_u .

timestamp: A scalar value equal to the reasonable output of Unix's time() at this block's inception; formally H_s .

extraData: An arbitrary byte array containing data relevant to this block. With the exception of

the genesis block, this must be 32 bytes or fewer; formally H_x .

nonce: A 256-bit hash which proves that a sufficient amount of computation has been carried out on this block; formally H_n .

The other two components in the block are simply a list of uncle block headers (of the same format as above) and a series of the transaction receipts. Formally, we can refer to a block B:

$$(15) B \equiv (B_H, B_{\mathbf{R}}, B_{\mathbf{U}})$$

4.3.1. Transaction Receipt. The transaction receipt is a tuple of three items comprising the transaction, R_T , together with the post-transaction state, R_{σ} , and the cumulative gas used in the block containing the transaction receipt as of immediately after the transaction has happened, R_u :

(16)
$$R \equiv (R_T, R_{\sigma}, R_u)$$

The function L_R trivially prepares a transaction receipt for being transformed into an RLP-serialised byte array:

(17)
$$L_R(R) \equiv (L_T(R_T), \text{TRIE}(L_S(R_{\sigma})), R_u)$$

thus the post-transaction state, R_{σ} is encoded into a trie structure, the root of which forms the second item.

We assert R_u , the cumulative gas used is a positive integer:

$$(18) R_u \in \mathbb{P}$$

For convenience, I also name B_T the series of transactions encoded by the transaction receipts $B_{\mathbf{R}}$:

(19)
$$B_{\mathbf{T}} \equiv (B_{\mathbf{R}}[0]_T, B_{\mathbf{R}}[1]_T, ...)$$

Notably $B_{\mathbf{T}}$ does not get serialised into the block by the block preparation function L_B ; it is merely a convenience equivalence.

4.3.2. Holistic Validity. We can assert its validity if and only if it satisfies several conditions: It must be internally consistent with the uncle and transaction block hashes and the given transactions $B_{\mathbf{T}}$, when executed in order on the base state σ (derived from the final state of the parent block), result in a new state of the identity H_r : (20)

$$\begin{array}{lll} H_u & \equiv & \mathrm{SHA3}(\mathrm{RLP}(L_H^*(B_{\mathbf{U}}))) & \wedge \\ H_t & \equiv & \mathrm{TRIE}(\{\forall i < \|B_{\mathbf{T}}\|, i \in \mathbb{P} : p(i, L_R(B_{\mathbf{R}}[i])\})) & \wedge \\ H_r & \equiv & \mathrm{TRIE}(L_S(\Pi(\pmb{\sigma}, B))) \end{array}$$

where p(k, v) is simply the pairwise RLP transformation, in this case, the first being the index of the transaction in the block and the second being the transaction receipt:

(21)
$$P(k,v) \equiv (RLP(k), RLP(v))$$

Furthermore:

(22)
$$TRIE(L_S(\boldsymbol{\sigma})) = P(B_H)_{H_r}$$

Thus $\mathtt{TRIE}(L_S(\boldsymbol{\sigma}))$ is the root node hash of the Merkle Patricia tree structure containing the key-value pairs of the state σ with values encoded using RLP, and $P(B_H)$ is the parent block of B, defined directly.

4.3.3. Serialisation. The function L_B and L_H are the preparation functions for a block and block header respectively. Much like the transaction receipt preparation function L_R , we assert the types and order of the structure for when the RLP transformation is required:

(23)
$$L_H(H) \equiv (H_p, H_u, H_b, H_r, H_t, H_d, H_i, H_m, H_l, H_u, H_s, H_x, H_n)$$

(24)
$$L_B(B) \equiv (L_H(B_H), L_R^*(B_R), L_H^*(B_U))$$

With L_T^* and L_H^* being element-wise sequence transformations, thus:

(25)
$$f^*((x_0, x_1, \dots)) \equiv (f(x_0), f(x_1), \dots) \quad \text{for any function } f$$

The component types are defined thus:

$$(26) \qquad H_{p} \in \mathbb{B}_{32} \quad \wedge \quad H_{u} \in \mathbb{B}_{32} \quad \wedge \quad H_{b} \in \mathbb{B}_{20} \quad \wedge \\ H_{r} \in \mathbb{B}_{32} \quad \wedge \quad H_{t} \in \mathbb{B}_{32} \quad \wedge \quad H_{d} \in \mathbb{P} \quad \wedge \\ H_{i} \in \mathbb{P} \quad \wedge \quad H_{m} \in \mathbb{P} \quad \wedge \quad H_{l} \in \mathbb{P} \quad \wedge \\ H_{u} \in \mathbb{P} \quad \wedge \quad H_{s} \in \mathbb{P} \quad \wedge \quad H_{x} \in \mathbb{B} \quad \wedge \\ H_{n} \in \mathbb{B}_{32}$$

where

(27)
$$\mathbb{B}_n = \{B : B \in \mathbb{B} \land ||B|| = n\}$$

We now have a rigorous specification for the construction of a formal block structure. The RLP function RLP (see Appendix C) provides the canonical method for transforming this structure into a sequence of bytes ready for transmission over the wire or storage locally.

4.3.4. Block Header Validity. We define $P(B_H)$ to be the parent block of B, formally:

(28)
$$P(H) \equiv B' : SHA3(RLP(B')) = H_p$$

The canonical difficulty of a block of header H is defined as D(H):

$$D(H) \equiv \begin{cases} 2^{22} & \text{if } H_i = 0 \\ P(H)_{H_d} + \lfloor \frac{P(H)_{H_d}}{1024} \rfloor & \text{if } H_s < P(H)_{H_s} + 42 \\ P(H)_{H_d} - \lfloor \frac{P(H)_{H_d}}{1024} \rfloor & \text{otherwise} \end{cases}$$

The canonical gas limit of a block of header H is defined as L(H):

(30)
$$L(H) \equiv \begin{cases} 10^6 & \text{if } H_i = 0\\ 125000 & \text{if } L'(H) < 125000\\ L'(H) & \text{otherwise} \end{cases}$$
(31) $L'(H) \equiv \lfloor \frac{1023P(H)_{H_l} + \lfloor \frac{6}{5}P(H)_{H_u} \rfloor}{1024} \rfloor$

(31)
$$L'(H) \equiv \lfloor \frac{1023P(H)_{H_l} + \lfloor \frac{6}{5}P(H)_{H_u} \rfloor}{1024} \rfloor$$

 H_s is the timestamp of block H and must fulfil the relation:

$$(32) H_s > P(H)_{H_s}$$

This mechanism enforces a homeostasis in terms of the time between blocks; a smaller period between the last two blocks results in an increase in the difficulty level and thus additional computation required, lengthening the likely next period. Conversely, if the period is too large, the difficulty, and expected time to the next block, is reduced.

The nonce, H_n , must satisfy the relation:

$$\mathrm{PoW}(H,H_n)\leqslant \frac{2^{256}}{H_d}$$

Where PoW is the proof-of-work function (see section 11.5): this evaluates to an pseudo-random number cryptographically dependent on the parameters H and H_n . Given an approximately uniform distribution in the range $[0, 2^{256})$, the expected time to find a solution is proportional to the difficulty, H_d .

This is the foundation of the security of the blockchain and is the fundamental reason why a malicious node cannot propagate newly created blocks that would otherwise overwrite ("rewrite") history. Because the nonce must satisfy this requirement, and because its satisfaction depends on the contents of the block and in turn its composed transactions, creating new, valid, blocks is difficult and, over time, requires approximately the total compute power of the trustworthy portion of the mining peers.

Thus we are able to define the block header validity function V(H):

$$(34) \hspace{1cm} V(H) \hspace{2mm} \equiv \hspace{2mm} \operatorname{PoW}(H,H_n) \leqslant \frac{2^{256}}{H_d} \hspace{4mm} \wedge \hspace{4mm}$$

$$(35) H_d = D(H) \land$$

$$(36) H_l = L(H) \land$$

$$(37) H_s > P(H)_{H_s} \wedge$$

$$||H_x|| < 1024$$

Noting additionally that $\mathbf{extraData}$ must be at most 1024 bytes.

5. Gas and Payment

In order to avoid issues of network abuse and to sidestep the inevitable questions stemming from Turing completeness, all programmable computation in Ethereum is subject to fees. The fee schedule is specified in units of gas (see Appendix B for the fees associated with various computation). Thus any given fragment of programmable computation (this includes creating contracts, making message calls, utilising and accessing account storage and executing operations on the virtual machine) has a universally agreed cost in terms of gas.

Every transaction has a specific amount of gas associated with it: **gasLimit**. This is the amount of gas which is implicitly purchased from the sender's account balance. The purchase happens at the according **gasPrice**, also specified in the transaction. The transaction is considered invalid if the account balance cannot support such a purchase. It is named **gasLimit** since any unused gas at the end of the transaction is refunded (at the same rate of purchase) to the sender's account. Gas does not exist outside of the execution of a transaction. Thus for accounts with trusted code associated, a relatively high gas limit may be set and left alone.

In general, Ether used to purchase gas that is not refunded is delivered to the *coinbase* address, the address of an account typically under the control of the miner. Transactors are free to specify any **gasPrice** that they wish, however miners are free to ignore transactions as they choose. A higher gas price on a transaction will therefore cost the sender more in terms of Ether and deliver a greater value to the miner and thus will more likely be selected for inclusion by more miners. Miners, in general, will choose to advertise the minimum gas price for which they will execute transactions and transactors will be free to canvas these prices in determining what gas price to

offer. Since there will be a (weighted) distribution of minimum acceptable gas prices, transactors will necessarily have a trade-off to make between lowering the gas price and maximising the chance that their transaction will be mined in a timely manner.

6. Transaction Execution

The execution of a transaction is the most complex part of the Ethereum protocol: it defines the state transition function Υ . It is assumed that any transactions executed first pass the initial tests of intrinsic validity. These include:

- (1) The transaction signature is valid;
- the transaction nonce is valid (equivalent to the sender account's current nonce);
- (3) the gas limit is no smaller than the intrinsic gas, g_0 , used by the transaction;
- (4) the sender account balance contains at least the cost, v_0 , required in up-front payment.

Formally, we consider the function Υ , with T being a transaction and σ the state:

(39)
$$\boldsymbol{\sigma}' = \Upsilon(\boldsymbol{\sigma}, T)$$

Thus σ' is the post-transactional state. We also define Υ^g to evaluate to the amount of gas used in the execution of a transaction, to be defined later.

We define intrinsic gas g_0 , the amount of gas this transaction requires to be paid prior to execution, as follows:

(40)
$$g_0 \equiv \begin{cases} ||T_{\mathbf{i}}|| G_{txdata} + G_{transaction} & \text{if} \quad T_t = 0 \\ ||T_{\mathbf{d}}|| G_{txdata} + G_{transaction} & \text{otherwise} \end{cases}$$

where $||T_{\mathbf{d}}||$ and $||T_{\mathbf{i}}||$ are the sizes, in bytes, of the transaction's associated data and initialisation EVM-code, respectively and G is defined in Appendix B.

The up-front cost v_0 is calculated as:

$$(41) v_0 \equiv T_q T_p + T_v$$

The validity is determined as:

$$(42) S(T) \neq \varnothing \land \sigma[S(T)] \neq \varnothing \land T_n = \sigma[S(T)]_n \land g_0 \leq T_g \land v_0 \leq \sigma[S(T)]_b \land T_l \leq B_{H_l} - \ell(B_{\mathbf{R}})_u$$

Note the final condition; the sum of the transaction's gas limit, T_l , and the gas utilised in this block prior, given by $\ell(B_{\mathbf{R}})_u$, must be no greater than the block's **gasLimit**, B_{Hl} :

The execution of a valid transaction begins with an irrevocable change made to the state: the nonce of the account of the sender, S(T), is incremented by one and the balance is reduced by the up-front cost, v_0 . The gas available for the proceeding computation, g, is defined as $T_g - g_0$. The computation, whether contract creation or a message call, results in an eventual state (which may legally be equivalent to the current state), the change to which is deterministic and never invalid: there can be no invalid transactions from this point.

We define the checkpoint state σ_0 :

(43)
$$\sigma_0 \equiv \sigma \text{ except:}$$

(44)
$$\boldsymbol{\sigma}_0[S(T)]_b \equiv \boldsymbol{\sigma}[S(T)]_b - v_0$$

(45)
$$\boldsymbol{\sigma}_0[S(T)]_n \equiv \boldsymbol{\sigma}[S(T)]_n + 1$$

Evaluating σ_P from σ_0 depends on the transaction type; either contract creation or message call; we define the pairing of post-execution provisional state (σ_P) and remaining gas (g'):

$$(\boldsymbol{\sigma}_P, g') \equiv \begin{cases} \Lambda(\boldsymbol{\sigma}_0, S(T), T_o, g, T_p, T_v, T_{\mathbf{i}}, T_{\mathbf{b}}) & \text{if} \quad T_t = 0\\ \Theta_{0,1}(\boldsymbol{\sigma}_0, S(T), T_o, T_t, g, T_p, T_v, T_{\mathbf{d}}) & \text{otherwise} \end{cases}$$

where

$$(47) g \equiv T_q - g_0$$

Note we use $\Theta_{0,1}$ to denote the fact that only the first two components of the function's value are taken; the third represents the message-call's output value (a byte array) and is unused in the context of transaction evaluation.

After the message call or contract creation is processed, the state is finalised by refunding g', the remaining gas, to the sender at the original rate. The Ether for the gas that was actually used is given to the miner, whose address is specified as the coinbase of the present block B. So we define the final state σ' in terms of the provisional state σ_P :

(48)
$$\sigma' \equiv \sigma_P \text{ except}$$

(49)
$$\boldsymbol{\sigma}'[s]_b \equiv \boldsymbol{\sigma}_P[s]_b + q'T_x$$

(49)
$$\boldsymbol{\sigma}'[s]_{b} \equiv \boldsymbol{\sigma}_{P}[s]_{b} + g'T_{p}$$
(50)
$$\boldsymbol{\sigma}'[m]_{b} \equiv \boldsymbol{\sigma}_{P}[m]_{b} + (T_{g} - g')T_{p}$$

$$(51) m \equiv B_{Hb}$$

And finally specify Υ^g , the total gas used in this transaction:

(52)
$$\Upsilon^g(\boldsymbol{\sigma}, T) \equiv g_0 + g'$$

7. Contract Creation

There are number of intrinsic parameters used when creating an account: sender (s), nonce (n), available gas (g), gas price (p), endowment (v) together with an arbitrary length byte array, i, the initialisation EVM code.

We define the creation function formally as the function Λ , which evaluates from these values, together with the state σ_0 to the tuple containing the new state, additional database entries and remaining gas (σ_P, g') , as in section 6:

(53)
$$(\boldsymbol{\sigma}_P, g') \equiv \Lambda(\boldsymbol{\sigma}_0, s, n, g, p, v, \mathbf{i})$$

The address of the new account is defined as being the rightmost 160 bits of the SHA3 hash of RLP encoding of the structure containing only the sender and the nonce. In the unlikely event that the address is already in use, it is treated as a big-endian integer and incremented by one until an unused address is arrived at. Thus we define the creation address function A:

(54)
$$A(s,n) \equiv a$$
 where:

(55)
$$a = \arg\min_{x} : x \geqslant a' \land \boldsymbol{\sigma}_{0}[x] = \emptyset$$

$$(56) \hspace{1cm} a' \hspace{2mm} = \hspace{2mm} \mathcal{B}_{96..255} \Big(\mathtt{SHA3} \Big(\mathtt{RLP} \big(\hspace{1mm} (s,n) \hspace{1mm} \big) \Big) \Big)$$

where SHA3 is the SHA3 256-bit hash function, RLP is the RLP encoding function, $\mathcal{B}_{a..b}(X)$ evaluates to binary value containing the bits of indices in the range [a, b] of the binary data X and $\sigma_0[x]$ is the address state of x or \emptyset if none exists. Note we use one fewer than the sender's nonce value; we assert that we have incremented the sender account's nonce prior to this call, and so the value used is the sender's nonce at the beginning of the responsible transaction or VM operation.

The account's nonce is initially defined as zero, the balance as the value passed, the storage as empty and the code hash as the SHA3 256-bit hash of the empty string, thus the mutated state becomes σ^* :

(57)
$$\sigma^* \equiv \sigma \text{ except:}$$

(58)
$$\sigma^*[a] \equiv (0, v, TRIE(\emptyset), SHA3(()))$$

where a is the address of the new account, as defined above. It is asserted that the state database will also change such that it defines the pair (SHA3(b), b).

Finally, the account is initialised through the execution of the initialising EVM code i according to the execution model (see section 9). Code execution can effect several events that are not internal to the execution state: the account's storage can be altered, further accounts can be created and further message calls can be made. As such, the code execution function Ξ evaluates to a tuple of the resultant state σ^{**} and available gas remaining g'.

Code execution depletes gas; thus it may exit before the code has come to a natural halting state. In this exceptional case we say an Out-of-Gas exception has occurred: The evaluated state is defined as being the empty set \varnothing and the entire create operation should have no effect on the state, effectively leaving it as it was immediately prior to attempting the creation. The gas remaining should be zero. If the creation was conducted as the receiptation of a transaction, then this doesn't affect payment of the intrinsic cost: it is paid regardless.

If such an exception does not occur, then the remaining gas is refunded to the originator and the now-altered state is allowed to persevere. Thus formally, we may specify the resultant state and gas as $(\boldsymbol{\sigma}_P, g')$ where:

(59)
$$(\boldsymbol{\sigma}^{**}, g', \mathbf{o}) \equiv \Xi(\boldsymbol{\sigma}^*, g, I)$$

(60)
$$\sigma_P \equiv \begin{cases} \sigma^{**} & \text{if } \sigma^{**}[a] = \emptyset \\ \sigma^{**} & \text{except:} \\ \sigma_P[a]_{\mathbf{b}} = \mathbf{o} & \text{otherwise} \end{cases}$$

- (61)
- (62)
- (63)
- (64)
- (65)
- I_v (66) $\equiv v$

 $I_{\mathbf{d}}$ evaluates to the empty tuple. I_H has no special treatment and are determined from the blockchain. The exception in the determination of σ_P dictates that the resultant byte sequence from the execution of the initialisation code specifies the final body code for the newlycreated account, with $\sigma_P[A(s,\sigma[s]_n)]_b$ being the newly created account's body code and o the output byte sequence of the code execution.

7.1. **Subtleties.** Note that while the initialisation code is executing, the newly created address exists but with no intrinsic body code. Thus any message call received by it during this time causes no code to be executed. If the initialisation execution ends with a SUICIDE instruction, no code is set. For a normal STOP code, or if the code returned is otherwise empty, then the state is left with a zombie account, and any remaining balance will be locked into the account forever.

8. Message Call

In the case of executing a message call, several parameters are required: sender (s), transaction originator (o), recipient (r), available gas (g), value (v) and gas price (p) together with an arbitrary length byte array, \mathbf{d} , the input data of the call. Aside from evaluating to a new state and additional database entries, message calls also have an extra component—the output data denoted by the byte array \mathbf{o} . This is ignored when executing transactions, however message calls can be initiated due to VM-code execution and in this case this information is used.

(68)
$$(\boldsymbol{\sigma}_P, g', \mathbf{o}) \equiv \Theta(\boldsymbol{\sigma}, s, o, r, g, p, v, \mathbf{d})$$

We define σ_1 , the checkpoint state as the original state but with the value transferred to the recipient:

(69)
$$\sigma_1 \equiv \sigma \text{ except:}$$

(70)
$$\boldsymbol{\sigma}_1[r]_b \equiv \boldsymbol{\sigma}_1[r]_b + v$$

The account's associated code (identified as the fragment whose SHA3 hash is $\sigma[r]_c$) is executed according to the execution model (see section 9). Just as with contract creation, if the execution halts due to an exhausted gas supply, then no gas is refunded to the caller and the state is reverted to the point immediately prior to code execution.

(71)
$$\boldsymbol{\sigma}_{P} \equiv \begin{cases} \boldsymbol{\sigma}_{1} & \text{if } \boldsymbol{\sigma}_{1}[r]_{c} = \varnothing \\ \boldsymbol{\sigma}_{1} & \text{if } \boldsymbol{\sigma}^{**} = \varnothing \\ \boldsymbol{\sigma}^{**} & \text{otherwise} \end{cases}$$

(72)
$$(\boldsymbol{\sigma}^{**}, g', \mathbf{o}) \equiv \Xi(\boldsymbol{\sigma}_1, g, I)$$

$$(73) I_a \equiv a$$

$$(74) I_o \equiv o$$

$$(75) I_p \equiv p$$

$$(76) I_{\mathbf{d}} \equiv \mathbf{d}$$

$$(77) I_s \equiv s$$

$$(78) I_v \equiv v$$

(79) Let SHA3
$$(I_{\mathbf{b}}) = \boldsymbol{\sigma}[r]_c$$

It is assumed that the client will have stored the pair $(SHA3(I_b), I_b)$ at some point prior in order to make the determination of I_b feasible.

9. Execution Model

The execution model specifies how the system state is altered given a series of bytecode instructions and a small tuple of environmental data. This is specified through a formal model of a virtual state machine, known as the Ethereum Virtual Machine (EVM). It is a *quasi*-Turing-complete machine; the *quasi* qualification comes from the fact that the computation is intrinsically bounded through a parameter, *gas*, which limits the total amount of computation done.

9.1. Basics. The EVM is a simple stack-based architecture. The word size of the machine (and thus size of stack item) is 256-bit. This was chosen to facilitate the SHA3-256 hash scheme and elliptic-curve computations. The memory model is a simple word-addressed byte array. The stack has an unlimited size. The machine also has an independent storage model; this is similar in concept to the memory but rather than a byte array, it is a word-addressable word array. Unlike memory, which is volatile, storage is non volatile and is maintained as part of the system state. All locations in both storage and memory are well-defined initially as zero.

The machine does not follow the standard von Neumann architecture. Rather than storing program code in generally-accessible memory or storage, it is stored separately in a virtual ROM interactable only through a specialised instruction.

The machine can have exceptional execution for several reasons, including stack underflows and invalid instructions. These unambiguously and validly result in immediate halting of the machine with all state changes left intact. The one piece of exceptional execution that does not leave state changes intact is the out-of-gas (OOG) exception. Here, the machine halts immediately and reports the issue to the execution agent (either the transaction processor or, recursively, the spawning execution environment) and which will deal with it separately.

9.2. Fees Overview. Fees (denominated in gas) are charged under three distinct circumstances, all three as prerequisite to the execution of an operation. The first and most common is the fee intrinsic to the computation of the operation. Most operations require a single gas fee to be paid for their execution; exceptions include SSTORE, SLOAD, CALL, CREATE, BALANCE and SHA3. Secondly, gas may be deducted in order to form the payment for a subordinate message call or contract creation; this forms part of the payment for CREATE and CALL. Finally, gas may be paid due to an increase in the usage of the memory.

Over a account's execution, the total fee for memory-usage payable is proportional to smallest multiple of 32 bytes that are required such that all memory indices (whether for read or write) are included in the range. This is paid for on a just-in-time basis; as such, referencing an area of memory at least 32 bytes greater than any previously indexed memory will certainly result in an additional memory usage fee. Due to this fee it is highly unlikely addresses will ever go above 32-bit bounds since at the present price of Ether and default gas price, that would cost around US\$20M for the memory fee alone.

Storage fees have a slightly nuanced behaviour—to incentivise minimisation of the use of storage (which corresponds directly to a larger state database on all nodes), the execution fee for an operation that clears an entry in the storage is waived; in fact, it is effectively paid up-front since the initial usage of a storage location costs twice as much as the normal usage.

More formally, given an instruction, it is possible to calculate the gas cost of executing it as follows:

- SHA3 costs G_{sha3} gas
- SLOAD costs G_{sload} gas
- BALANCE costs $G_{balance}$ gas
- SSTORE costs $d.G_{sstore}$ gas where:

- -d=2 if the new value of the storage is non-zero and the old is zero;
- d = 0 if the new value of the storage is zero and the old is non-zero;
- -d=1 otherwise.
- CALL costs G_{call}, though additional gas may be taken for the execution of the account's associated code, if non-empty.
- CREATE costs G_{create}, though additional gas may be taken for the execution of the account initialisation code.
- STOP costs G_{stop} gas
- SUICIDE costs $G_{suicide}$ gas
- All other operations cost G_{step} gas.

Additionally, when memory is accessed with MSTORE, MSTORES, MLOAD, CALLDATACOPY, CODECOPY, RETURN, SHA3, CREATE or CALL, the memory should be enlarged to the smallest multiple of words such that all addressed bytes now fit in it. See Appendix G for a rigorous definition of the EVM gas cost.

- 9.3. Execution Environment. In addition to the system state σ , and the remaining gas for computation g, there are several pieces of important information used in the execution environment that the execution agent must provide; these are contained in the tuple I:
 - I_a, the address of the account which owns the code that is executing.
 - I_o, the sender address of the transaction that originated this execution.
 - I_p, the price of gas in the transaction that originated this execution.
 - I_d , the byte array that is the input data to this execution; if the execution agent is a transaction, this would be the transaction data.
 - I_s , the address of the account which caused the code to be executing; if the execution agent is a transaction, this would be the transaction sender.
 - I_v , the value, in Wei, passed to this account as part of the same procedure as execution; if the execution agent is a transaction, this would be the transaction value.
 - I_b, the byte array that is the machine code to be executed.
 - \bullet I_H , the block header of the present block.

The execution model defines the function Ξ , which can compute the resultant state σ' and the remaining gas g', given these definitions:

(80)
$$(\boldsymbol{\sigma}', g') \equiv \Xi(\boldsymbol{\sigma}, g, I)$$

9.4. Execution Overview. We must now define the Ξ function. In most practical implementations this will be modelled as an iterative progression of the pair comprising the full system state, σ and the machine state, μ . Formally, we define it recursively with a function X. This uses an iterator function O (which defines the result of a single cycle of the state machine) together with functions Z which determines if the present state is an exceptional halting state of the machine and H, specifying the output data of the instruction if and only if the present state is a normal halting state of the machine. The empty sequence,

denoted (), is not equal to the empty set, denoted \varnothing .

(81)
$$\Xi(\boldsymbol{\sigma}, g, I) \equiv X(\boldsymbol{\sigma}, \boldsymbol{\mu}, I)$$

$$\mu_a \equiv g$$

$$\mu_{nc} \equiv 0$$

$$\boldsymbol{\mu}_{\mathbf{m}} \quad \equiv \quad (0,0,\ldots)$$

$$(85) \boldsymbol{\mu}_i \equiv 0$$

$$\mu_{\mathbf{s}} \equiv ()$$

$$(87) \qquad X(\boldsymbol{\sigma},\boldsymbol{\mu},I) \equiv \begin{cases} (\boldsymbol{\sigma},\boldsymbol{\mu},I,()) & \text{if} \quad Z(\boldsymbol{\sigma},\boldsymbol{\mu},I) \\ O(\boldsymbol{\sigma},\boldsymbol{\mu},I) \cdot \mathbf{o} & \text{if} \quad \mathbf{o} \neq \varnothing \\ X(O(\boldsymbol{\sigma},\boldsymbol{\mu},I)) & \text{otherwise} \end{cases}$$

where

(88)
$$\mathbf{o} \equiv H(\boldsymbol{\mu}, I)$$

(89)
$$(a,b,c) \cdot d \equiv (a,b,c,d)$$

The machine state μ is defined as the tuple $(g,pc,\mathbf{m},i,\mathbf{s})$ which are the gas available, the program counter, the memory contents, the active number of words in memory (counting continuously from position 0), and the stack contents. The memory contents $\mu_{\mathbf{m}}$ are a series of zeroes of size 2^{256} .

For the ease of reading, the instruction mnemonics, written in smallcaps (e.g. ADD), should be interpreted as their numeric equivalents; the full table of instructions and their specifics is given in Appendix G.

For the purposes of defining Z, H and O, we define w as the current operation to be executed:

(90)
$$w \equiv \begin{cases} I_{\mathbf{b}}[\boldsymbol{\mu}_{pc}] & \text{if } \boldsymbol{\mu}_{pc} < ||I_{\mathbf{b}}|| \\ \text{STOP} & \text{otherwise} \end{cases}$$

We also assume the fixed amounts of δ and α , specifying the stack items removed and added, both subscriptable on the instruction and an instruction cost function C evaluating to the full cost, in gas, of executing the given instruction.

9.4.1. Exceptional Halting. The exceptional halting function Z is defined as:

(91)
$$Z(\boldsymbol{\sigma}, \boldsymbol{\mu}, I) \equiv \begin{array}{ccc} \boldsymbol{\mu}_g < C(\boldsymbol{\sigma}, \boldsymbol{\mu}, I) & \vee \\ \delta_w = \varnothing & \vee \\ \|\boldsymbol{\mu}_{\mathbf{s}}\| < \delta_w \end{array}$$

This states that the execution is in an exceptional halting state if there is insufficient gas, if the instruction is invalid (and therefore its δ subscript is undefined) or if there are insufficient stack items. The astute reader will realise that this implies that no instruction can, through its execution, cause an exceptional halt.

9.4.2. Normal Halting. The normal halting function H is defined:

$$H(\boldsymbol{\mu}, I) \equiv \begin{cases} H_{\text{RETURN}}(\boldsymbol{\mu}) & \text{if} \quad w = \text{RETURN} \\ () & \text{if} \quad w \in \{\text{STOP}, \text{SUICIDE}\} \\ \varnothing & \text{otherwise} \end{cases}$$

The data-returning halt operation, RETURN, has a special function H_{RETURN} , defined in Appendix G.

9.5. The Execution Cycle. Stack items are added or removed from the left-most, lower-indexed portion of the series; all other items remain unchanged:

(93)
$$O(\boldsymbol{\sigma}, \boldsymbol{\mu}, I) \equiv (\boldsymbol{\sigma}', \boldsymbol{\mu}', I)$$

$$(94) \Delta \equiv \alpha_w - \delta_w$$

(95)
$$\|\boldsymbol{\mu}_{\mathbf{s}}'\| \equiv \|\boldsymbol{\mu}_{\mathbf{s}}\| + \Delta$$

(96)
$$\forall x \in [\alpha_w, \|\boldsymbol{\mu}_s'\|) : \boldsymbol{\mu}_s'[x] \equiv \boldsymbol{\mu}_s[x + \Delta]$$

The gas is reduced by the instruction's gas cost and for most instructions, the program counter increments on each cycle, for the three exceptions, we assume a function J, subscripted by one of two instructions, which evaluates to the according value:

$$(97) \ \boldsymbol{\mu}_g' \equiv \boldsymbol{\mu}_g - C(\boldsymbol{\sigma}, \boldsymbol{\mu}, I)$$

$$(98) \ \boldsymbol{\mu}_{pc}' \equiv \begin{cases} J_{\text{JUMP}}(\boldsymbol{\mu}) & \text{if } w = \text{JUMP} \\ J_{\text{JUMPI}}(\boldsymbol{\mu}) & \text{if } w = \text{JUMPI} \\ \boldsymbol{\mu}_{pc} + p & \text{if } w \in [\text{PUSH1}, \text{PUSH32}] \\ \boldsymbol{\mu}_{pc} + 1 & \text{otherwise} \end{cases}$$

where p is the byte size of the push instruction, defined as:

$$(99) p \equiv w - PUSH1 + 2$$

In general, we assume the memory and system state don't change:

$$\mu_{\mathbf{m}}' \equiv \mu_{\mathbf{m}}$$

(102)
$$\sigma' \equiv \sigma$$

However, instructions do typically alter one or several components of these values. Altered components listed by instruction are noted in Appendix G, alongside values for α and δ and a formal description of the gas requirements.

10. Blocktree to Blockchain

The canonical blockchain is a path from root to leaf through the entire block tree. In order to have consensus over which path it is, conceptually we identify the path that has had the most computation done upon it, or, the heaviest path. Clearly one factor that helps determine the heaviest path is the block number of the leaf, equivalent to the number of blocks, not counting the unmined genesis block, in the path. The longer the path, the greater the total mining effort that must have been done in order to arrive at the leaf. This is akin to existing schemes, such as that employed in Bitcoin-derived protocols.

This scheme notably ignores so-called *stale* blocks: valid, mined blocks, which were propagated too late into the network and thus were beaten to network consensus by a sibling block (one with the same parent). Such blocks become more common as the network propagation time approaches the ideal inter-block time. However, by counting the computation work of stale block headers, we are able to do better: we can utilise this otherwise wasted computation and put it to use in helping to buttress the more popular blockchain making it a stronger choice over less popular (though potentially longer) competitors.

This increases overall network security by making it much harder for an adversary to silently mine a canonical blockchain (which, it is assumed, would contain different transactions to the current consensus) and dump it on the network with the effect of overriding existing blocks and reversing the transactions within.

In order to validate the extra computation, a given block B may include the block headers from any known uncle blocks (i.e. blocks whose parent is equivalent to the grandparent of B). Since a block header includes the nonce, a proof-of-work, then the header alone is enough to validate the computation done. Any such blocks contribute toward the total computation or total difficulty of a chain that includes them. To incentivise computation and inclusion, a reward is given both to the miner of the stale block and the miner of the block that references it.

Thus we define the total difficulty of block B recursively as:

$$(103) B_t \equiv B'_t + B_d + \sum_{U \in B_{\mathbf{U}}} U_d$$

$$(104) B' \equiv P(B_H)$$

As such given a block B, B_t is its total difficulty, B' is its parent block, B_d is its difficulty and $B_{\mathbf{U}}$ is its set of uncle blocks.

11. Block Finalisation

The process of finalising a block involves four stages:

- (1) Validate (or, if mining, determine) uncles;
- (2) validate (or, if mining, determine) transactions;
- (3) apply rewards;
- (4) verify (or, if mining, compute a valid) state and nonce.

11.1. **Uncle Validation.** The validation of uncle headers means nothing more than verifying that each uncle header is both a valid header and satisfies the relation of uncle to the present block. Formally:

(105)
$$\bigwedge_{U \in B_{\mathbf{U}}} V(U) \wedge P(U) = P(P(B_H)) \wedge P(B_H) \neq B$$

11.2. **Transaction Validation.** The given **gasUsed** and **minGasPrice** must correspond faithfully to the transactions listed. In the case of B_{Hm} , the minimum gas price, all transactions included in the transaction receipt must have a gas price, T_{0p} , that is at least this value:

$$(106) \forall T \in B_{\mathbf{T}} : T_p \ge B_{Hm}$$

In the case of B_{Hu} , the total gas used in the block, it must be equal to the accumulated gas used according to the final transaction:

$$(107) B_{Hu} = \ell(\mathbf{R})_u$$

11.3. **Reward Application.** The application of rewards to a block involves raising the balance of the accounts of the coinbase address of the block and each uncle by a certain amount. We raise the block's coinbase account by R_b , the block reward, and the coinbase of each uncle by $\frac{7}{8}$ of that. Formally we define the function Ω :

(108)
$$\Omega(B, \boldsymbol{\sigma}) \equiv \boldsymbol{\sigma}' : \boldsymbol{\sigma}' = \boldsymbol{\sigma} \text{ except:}$$

(109)
$$\boldsymbol{\sigma}'[B_{Hb}]_b = \boldsymbol{\sigma}[B_{Hb}]_b + R_b$$

$$(110) \quad \forall_{U \in B_{\mathbf{U}}} \quad \boldsymbol{\sigma}'[U_b]_b \quad = \quad \boldsymbol{\sigma}[U_b]_b + \frac{7}{8}R_b$$

We define the block reward as 1500 Finney:

(111) Let
$$R_b = 1.5 \times 10^{18}$$

11.4. **State & Nonce Validation.** We may now define the function, Γ , that maps a block B to its initiation state: (112)

(112)
$$\Gamma(B) \equiv \begin{cases} \boldsymbol{\sigma}_0 & \text{if } P(B_H) = \varnothing \\ \boldsymbol{\sigma}_i : \text{TRIE}(L_S(\boldsymbol{\sigma}_i)) = P(B_H)_{H_r} & \text{otherwise} \end{cases}$$

Here, $\mathtt{TRIE}(L_S(\sigma_i))$ means the hash of the root node of a trie of state σ_i ; it is assumed that implementations will store this in the state database, trivial and efficient since the trie is by nature a mutable data structure.

And finally define Φ , the block transition function, which maps an incomplete block B to a complete block B':

(113)
$$\Phi(B) \equiv B': B' = B^*$$
 except:

$$(114) \quad B'_n = n: \quad \text{PoW}(B^*, n) < \frac{2^{256}}{H_d}$$

(115)
$$B^* \equiv B \text{ except: } B'_r = r(\Pi(\Gamma(B), B))$$

As specified at the beginning of the present work, Π is the state-transition function, which is defined in terms of Ω , the block finalisation function and Υ , the transaction-evaluation function, both now well-defined.

As previously detailed, $\mathbf{R}[n]_{\sigma}$ and $\mathbf{R}[n]_{u}$ are the *n*th corresponding states and cumulative gas used after each transaction. The former is defined simply as the state resulting from applying the corresponding transaction to the state resulting from the previous transaction (or the block's initial state in the case of the first such transaction):

(116)
$$B_{\mathbf{R}}[n]_{\boldsymbol{\sigma}} = \begin{cases} \Gamma(B) & \text{if } n < 0 \\ \Upsilon(B_{\mathbf{R}}[n-1]_{\boldsymbol{\sigma}}, B_{\mathbf{T}}[n]) & \text{otherwise} \end{cases}$$

In the case of **g**, we take a similar approach defining each item as the gas used in evaluating the corresponding transaction summed with the previous item (or zero, if it is the first), giving us a running total:

(117)
$$B_{\mathbf{R}}[n]_u = \begin{cases} 0 & \text{if} \quad n < 0 \\ \Upsilon^g(B_{\mathbf{R}}[n-1]_{\sigma}, B_{\mathbf{T}}[n]) \\ +B_{\mathbf{R}}[n-1]_u & \text{otherwise} \end{cases}$$

Finally, we define Π as the new state given the block reward function Ω applied to the final transaction's resultant state, $\ell(B_{\mathbf{R}})_{\sigma}$:

(118)
$$\Pi(\boldsymbol{\sigma}, B) \equiv \Omega(B, \ell(B_{\mathbf{R}})_{\boldsymbol{\sigma}})$$

Thus the complete block-transition mechanism, less PoW, the proof-of-work function is defined.

11.5. Mining Proof-of-Work. The mining proof-of-work (PoW) exists as a cryptographically secure nonce that proves beyond reasonable doubt that a particular amount of computation has been expended in the determination of some token value n. It is utilised to enforce the blockchain security by giving meaning and credence to the notion of difficulty (and, by extension, total difficulty). However, since mining new blocks comes with an attached reward, the proof-of-work not only functions as a method of securing confidence that the blockchain will remain canonical into the future, but also as a wealth distribution mechanism.

For both reasons, there are two important goals of the proof-of-work function; firstly, it should be as accessible as possible to as many people as possible. The requirement of, or reward from, specialised and uncommon hardware should be minimised. This makes the distribution model as open as possible, and, ideally, makes the act of mining a simple swap from electricity to Ether at roughly the same rate for anyone around the world.

Secondly, it should not be possible to make super-linear profits, and especially not so with a high initial barrier. Such a mechanism allows a well-funded adversary to gain a troublesome amount of the network's total mining power and as such gives them a super-linear reward (thus skewing distribution in their favour) as well as reducing the network security.

One plague of the Bitcoin world is ASICs. These are specialised pieces of compute hardware that exist only to do a single task. In Bitcoin's case the task is the SHA256 hash function. While ASICs exist for a proof-of-work function, both goals are placed in jeopardy. Because of this, a proof-of-work function that is ASIC-resistant (i.e. difficult or economically inefficient to implement in specialised compute hardware) has been identified as the proverbial silver bullet.

Two directions exist for ASIC resistance; firstly make it sequential memory-hard, i.e. engineer the function such that the determination of the nonce requires a lot of memory and that the memory cannot be used in parallel to discover multiple nonces simultaneously. The second is to make the type of computation it would need to do general-purpose; the meaning of "specialised hardware" for a general-purpose task set is, naturally, general purpose hardware and as such commodity desktop computers are likely to be pretty close to "specialised hardware" for the task.

More formally, the proof-of-work function takes the form of PoW:

(119)
$$PoW(H_{\rm H},n) < \frac{2^{256}}{H_d}$$

Where $H_{\mathbb{H}}$ is the new block's header H, but without the nonce component; H_d is the new block's difficulty value (i.e. the block difficulty from section 10).

As of the proof-of-concept (PoC) series of the Ethereum software, the proof-of-work function is simplistic and does not attempt to secure these goals. It will be described here for completeness.

11.5.1. *PoC Series*. For the PoC series, we use a simplified proof-of-work. This is not ASIC resistant and is meant merely as a placeholder. It utilises the bare SHA3 hash function to secure the block chain by requiring the SHA3 hash of the concatenation of the nonce and the header's SHA3 hash to be sufficiently low.

It is formally defined as PoW:

(120)
$$PoW(H, n) \equiv BE(SHA3(SHA3(RLP(H_{\aleph})) \circ n))$$

where: $\mathtt{RLP}(H_{\mathtt{M}})$ is the RLP encoding of the block header H, not including the final nonce component; SHA3 is the SHA3 hash function accepting an arbitrary length series of bytes and evaluating to a series of 32 bytes (i.e. 256-bit); n is the nonce, a series of 32 bytes; \circ is the series concatenation operator; $\mathtt{BE}(X)$ evaluates to the value equal to X when interpreted as a big-endian-encoded integer.

11.5.2. Release Series. For the release series, we use a more complex proof-of-work. This has yet to be formally defined, but involves two components; firstly that it concerns the evaluation of programs on the EVM. Secondly that it concerns the utilisation of either the blockchain or the full state trie.

As an overview, the output of the function is based upon the system state, defined as the hash of the root node of the state trie. A set of transactions, pseudo-randomly determined from the nonce value and selected from the last N blocks is taken. N is large enough and the selection criteria are such that execution of the transactions requires some non-negligible amount of processing by the EVM. Whenever code is executed on the EVM, it is pseudorandomly (seeded again by the nonce) corrupted before alteration. Corruption could involve switching addresses with other transactions or rotating them through in the state trie (perhaps to the next address with the same order of magnitude of funds), rotating through instructions that have equivalent stack behaviour (e.g. swapping ADD for SUB or GT for EQ), or more destructive techniques such as randomly changing opcodes. This results in a problem that both require generalised computation hardware and is sequentially memory (and perhaps even disk) hard.

Any specialised hardware to perform this task could also be leveraged to speed up (and thus drive down costs) of general Ethereum transaction processing.

12. Implementing Contracts

There are several patterns of contracts engineering that allow particular useful behaviours; two of these that I will briefly discuss are data feeds and random numbers.

12.1. **Data Feeds.** A data feed contract is one which provides a single service: it gives access to information from the external world within Ethereum. The accuracy and timeliness of this information is not guaranteed and it is the task of a secondary contract author—the contract that utilises the data feed—to determine how much trust can be placed in any single data feed.

The general pattern involves a single contract within Ethereum which, when given a message call, replies with some timely information concerning an external phenomenon. An example might be the local temperature of New York City. This would be implemented as a contract that returned that value of some known point in storage. Of course this point in storage must be maintained with the correct such temperature, and thus the second part of the pattern would be for an external server to run an Ethereum node, and immediately on discovery of a new block, creates a new valid transaction, sent to the contract, updating said value in storage. The contract's code would accept such updates only from the identity contained on said server.

12.2. Random Numbers. Providing random numbers within a deterministic system is, naturally, an impossible task. However, we can approximate with pseudo-random numbers by utilising data which is generally unknowable at the time of transacting. Such data might include the block's hash, the block's timestamp and the block's coinbase address. For a series of such numbers, a trivial solution would be to work from the previous pseudo-random

number, adding some constant amount and hashing the result.

This strategy does have a downside: a miner with sufficient power could alter any of the above values in order to deliver a seed in order to alter the outcome of the pseudorandom-based executions. For a more secure pseudo-random offering, all involved parties could agree on a number of data feed contracts; these could be combined along with the block timestamp and hashed to produce the first number in the series. By spreading the inputs and thus the trust between numerous parties the likelihood of a malicious miner altering the outcome becomes increasingly less likely.

13. Future Directions

The state database won't be forced to maintain all past state trie structures into the future. It should maintain an age for each node and eventually discard nodes that are neither recent enough nor checkpoints; checkpoints, or a set of nodes in the database that allow a particular block's state trie to be traversed, could be used to place a maximum limit on the amount of computation needed in order to retrieve any state throughout the blockchain.

Blockchain consolidation could be used in order to reduce the amount of blocks a client would need to download to act as a full, mining, node. A compressed archive of the trie structure at given points in time (perhaps one in every 10000th block) could be maintained by the peer network, effectively recasting the genesis block. This would reduce the amount to be downloaded to a single archive plus a hard maximum limit of blocks.

Finally, blockchain compression could perhaps be conducted: nodes in state trie that haven't sent/received a transaction in some constant amount of blocks could be thrown out, reducing both Ether-leakage and the growth of the state database.

13.1. Scalability. Scalability remains an eternal concern. With a generalised state transition function, it becomes difficult to partition and parallelise transactions to apply the divide-and-conquer strategy. Unaddressed, the dynamic value-range of the system remains essentially fixed and as the average transaction value increases, the less valuable of them become ignored, being economically pointless to include in the main ledger. However, several strategies exist that may potentially be exploited to provide a considerably more scalable protocol.

Some form of hierarchical structure, achieved by either consolidating smaller lighter-weight chains into the main block or building the main block through the incremental combination and adhesion (through proof-of-work) of smaller transaction sets may allow parallelisation of transaction combination and block-building. Parallelism could also come from a prioritised set of parallel blockchains, consolidated each block and with duplicate or invalid transactions thrown out accordingly.

Finally, verifiable computation, if made generally available and efficient enough, may provide a route to allow the proof-of-work to be the verification of final state.

14. Conclusion

I have introduced, discussed and formally defined the protocol of Ethereum. Through this protocol the reader may implement a node on the Ethereum network and join others in a decentralised secure social operating system. Contracts may be authored in order to algorithmically specify and autonomously enforce rules of interaction.

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APPENDIX A. TERMINOLOGY

External Actor: A person or other entity able to interface to an Ethereum node, but external to the world of Ethereum. It can interact with Ethereum through depositing signed Transactions and inspecting the blockchain and associated state. Has one (or more) intrinsic Accounts.

Address: A 160-bit code used for identifying Accounts.

Account: Accounts have an intrinsic balance and transaction count maintained as part of the Ethereum state. They also have some (possibly empty) EVM Code and a (possibly empty) Storage State associated with them. Though homogenous, it makes sense to distinguish between two practical types of account: those with empty associated EVM Code (thus the account balance is controlled, if at all, by some external entity) and those with non-empty associated EVM Code (thus the account represents an Autonomous Object). Each Account has a single Address that identifies it.

Transaction: A piece of data, signed by an External Actor. It represents either a Message or a new Autonomous Object. Transactions are recorded into each block of the blockchain.

Autonomous Object: A notional object existent only within the hypothetical state of Ethereum. Has an intrinsic address and thus an associated account; the account will have non-empty associated EVM Code. Incorporated only as the Storage State of that account.

Storage State: The information particular to a given Account that is maintained between the times that the Account's associated EVM Code runs.

Message: Data (as a set of bytes) and Value (specified as Ether) that is passed between two Accounts, either through the deterministic operation of an Autonomous Object or the cryptographically secure signature of the Transaction.

Message Call: The act of passing a message from one Account to another. If the destination account is associated with non-empty EVM Code, then the VM will be started with the state of said Object and the Message acted upon. If the message sender is an Autonomous Object, then the Call passes any data returned from the VM operation.

Gas: The fundamental network cost unit. Paid for exclusively by Ether (as of PoC-4), which is converted freely to and from Gas as required. Gas does not exist outside of the internal Ethereum computation engine; its price is set by the Transaction and miners are free to ignore Transactions whose Gas price is too low.

Contract: Informal term used to mean both a piece of EVM Code that may be associated with an Account or an Autonomous Object.

Object: Synonym for Autonomous Object.

App: An end-user-visible application hosted in the Ethereum Browser.

Ethereum Browser: (aka Ethereum Reference Client) A cross-platform GUI of an interface similar to a simplified browser (a la Chrome) that is able to host sandboxed applications whose backend is purely on the Ethereum protocol.

Ethereum Virtual Machine: (aka EVM) The virtual machine that forms the key part of the execution model for an Account's associated EVM Code.

Ethereum Runtime Environment: (aka ERE) The environment which is provided to an Autonomous Object executing in the EVM. Includes the EVM but also the structure of the world state on which the EVM relies for certain I/O instructions including CALL & CREATE.

EVM Code: The bytecode that the EVM can natively execute. Used to formally specify the meaning and ramifications of a message to an Account.

EVM Assembly: The human-readable form of EVM-code.

LLL: The Lisp-like Low-level Language, a human-writable language used for authoring simple contracts and general low-level language toolkit for trans-piling to.

Appendix B. Fee Schedule

The fee schedule G is a tuple of 10 scalar values corresponding to the relative costs, in gas, of a number of abstract operations that a transaction may effect.

Name	Value	Description*
G_{step}	1	Default amount of gas to pay for execution cycle.
G_{stop}	0	Nothing paid for the STOP operation.
$G_{suicide}$	0	Nothing paid for the SUICIDE operation.
G_{sha3}	20	Paid for a SHA3 operation.
G_{sload}	20	Paid for a SLOAD operation.
G_{sstore}	100	Paid for a normal SSTORE operation (doubled or waived sometimes).
$G_{balance}$	20	Paid for a BALANCE operation.
G_{create}	100	Paid for a CREATE operation.
G_{call}	20	Paid for a CALL operation.
G_{memory}	1	Paid for every additional word when expanding memory.
G_{txdata}	5	Paid for every byte of data or code for a transaction.
$G_{transaction}$	500	Paid for every transaction.

APPENDIX C. RECURSIVE LENGTH PREFIX

This is a serialisation method for encoding arbitrarily structured binary data (byte arrays). We define the set of possible structures \mathbb{T} :

$$\mathbb{T} \equiv \mathbb{L} \cup \mathbb{B}$$

(122)
$$\mathbb{L} \equiv \{\mathbf{t} : \mathbf{t} = (\mathbf{t}[0], \mathbf{t}[1], \dots) \land \forall_{n < \|\mathbf{t}\|} \mathbf{t}[n] \in \mathbb{T}\}$$

$$\mathbb{B} \equiv \{\mathbf{b} : \mathbf{b} = (\mathbf{b}[0], \mathbf{b}[1], \dots) \land \forall_{n < \|\mathbf{b}\|} \mathbf{b}[n] \in \mathbb{Y}\}$$

Where \mathbb{Y} is the set of bytes. Thus \mathbb{B} is the set of all sequences of bytes (otherwise known as byte-arrays, and a leaf if imagined as a tree), L is the set of all tree-like (sub-)structures that are not a single leaf (a branch node if imagined as a tree) and \mathbb{T} is the set of all byte-arrays and such structural sequences.

We define the RLP function as RLP through two sub-functions, the first handling the instance when the value is a byte array, the second when it is a sequence of further values:

(124)
$$RLP(\mathbf{x}) \equiv \begin{cases} R_b(\mathbf{x}) & \text{if } \mathbf{x} \in \mathbb{B} \\ R_l(\mathbf{x}) & \text{otherwise} \end{cases}$$

If the value to be serialised is a byte-array, the RLP serialisation takes one of three forms:

- If the byte-array contains solely a single byte and that single byte is less than 128, then the input is exactly equal to the output.
- If the byte-array contains fewer than 56 bytes, then the output is equal to the input prefixed by the byte equal to the length of the byte array plus 128.
- Otherwise, the output is equal to the input prefixed by the minimal-length byte-array which when interpreted as a big-endian integer is equal to the length of the input byte array, which is itself prefixed by the number of bytes required to faithfully encode this length value plus 183.

Formally, we define R_b :

(125)
$$R_{b}(\mathbf{x}) \equiv \begin{cases} \mathbf{x} & \text{if } \|\mathbf{x}\| = 1 \land \mathbf{x}[0] < 128 \\ (128 + \|\mathbf{x}\|) \cdot \mathbf{x} & \text{else if } \|\mathbf{x}\| < 56 \\ (183 + \|\mathbf{BE}(\|\mathbf{x}\|)\|) \cdot \mathbf{BE}(\|\mathbf{x}\|) \cdot \mathbf{x} & \text{otherwise} \end{cases}$$
(126)
$$\mathbf{BE}(x) \equiv (b_{0}, b_{1}, \dots) : b_{0} \neq 0 \land \sum_{n < \|\mathbf{b}\|}^{n=0} b_{n} 256^{\|\mathbf{b}\| - 1 - n}$$

(126)
$$BE(x) \equiv (b_0, b_1, \dots) : b_0 \neq 0 \land \sum_{n \leq \|\mathbf{b}\|}^{n=0} b_n 256^{\|\mathbf{b}\| - 1 - n}$$

$$(127) (a) \cdot (b,c) \cdot (d,e) = (a,b,c,d,e)$$

Thus BE is the function that expands a positive integer value to a big-endian byte array of minimal length and the dot operator performs sequence concatenation.

If instead, the value to be serialised is a sequence of other items then the RLP serialisation takes one of two forms:

- If the concatenated serialisations of each contained item is less than 56 bytes in length, then the output is equal to that concatenation prefixed by the byte equal to the length of this byte array plus 192.
- Otherwise, the output is equal to the concatenated serialisations prefixed by the minimal-length byte-array which when interpreted as a big-endian integer is equal to the length of the concatenated serialisations byte array, which is itself prefixed by the number of bytes required to faithfully encode this length value plus 247.

Thus we finish by formally defining R_l

(128)
$$R_l(\mathbf{x}) \equiv \begin{cases} (192 + ||s(\mathbf{x})||) \cdot s(\mathbf{x}) & \text{if } ||s(\mathbf{x})|| < 56 \\ (247 + ||\mathsf{BE}(||s(\mathbf{x})||)||) \cdot \mathsf{BE}(||s(\mathbf{x})||) \cdot s(\mathbf{x}) & \text{otherwise} \end{cases}$$

$$(129) s(\mathbf{x}) \equiv RLP(\mathbf{x}_0) \cdot RLP(\mathbf{x}_1)..$$

If RLP is used to encode a scalar, defined only as a positive integer, it must be specified as the shortest byte array such that the big-endian interpretation of it is equal. Thus the RLP of some positive integer i is defined as:

(130)
$$RLP(i:i \in \mathbb{P}) \equiv RLP(BE(i))$$

When interpreting RLP data, if an expected fragment is decoded as a scalar and leading zeroes are found in the byte sequence, clients are required to consider it non-canonical and treat it in the same manner as otherwise invalid RLP data, dismissing it completely.

There is no specific canonical encoding format for signed or floating-point values.

Appendix D. Hex-Prefix Encoding

Hex-prefix encoding is an efficient method of encoding an arbitrary number of nibbles as a byte array. It is able to store an additional flag which, when used in the context of the trie (the only context in which it is used), disambiguates between node types.

It is defined as the function HP which maps from a sequence of nibbles (represented by the set Y) together with a boolean value to a sequence of bytes (represented by the set \mathbb{B}):

(131)
$$\text{HP}(\mathbf{x},t) : \mathbf{x} \in \mathbb{Y} \equiv \begin{cases} (16f(t), 16\mathbf{x}[0] + \mathbf{x}[1], 16\mathbf{x}[2] + \mathbf{x}[3], \dots) & \text{if } \|\mathbf{x}\| \text{ is even} \\ (16(f(t) + 1) + \mathbf{x}[0], 16\mathbf{x}[1] + \mathbf{x}[2], 16\mathbf{x}[3] + \mathbf{x}[4], \dots) & \text{otherwise} \end{cases}$$

$$f(t) \equiv \begin{cases} 2 & \text{if } t \\ 0 & \text{otherwise} \end{cases}$$

$$f(t) \equiv \begin{cases} 2 & \text{if } t \\ 0 & \text{otherwise} \end{cases}$$

Thus the high nibble of the first byte contains two flags; the lowest bit encoding the oddness of the length and the second-lowest encoding the flag t. The low nibble of the first byte is zero in the case of an even number of nibbles and the first nibble in the case of an odd number. All remaining nibbles (now an even number) fit properly into the remaining bytes.

Appendix E. Modified Merkle Patricia Tree

The modified Merkle Patricia tree (trie) provides a persistent data structure to map between arbitrary-length binary data (byte arrays). It is defined in terms of a mutable data structure to map between 256-bit binary fragments and arbitrary-length binary data, typically implemented as a database. The core of the trie, and its sole requirement in terms of the protocol specification is to provide a single value that identifies a given set of key-value pairs, which may either a 32 byte sequence or the empty byte sequence. It is left as an implementation consideration to store and maintain the structure of the trie in a manner the allows effective and efficient realisation of the protocol.

Formally, we assume the input value \mathfrak{I} , a set containing pairs of byte sequences:

(133)
$$\mathfrak{I} = \{ (\mathbf{k}_0 \in \mathbb{B}, \mathbf{v}_0 \in \mathbb{B}), (\mathbf{k}_1 \in \mathbb{B}, \mathbf{v}_1 \in \mathbb{B}), \ldots \}$$

When considering such a sequence, we use the common numeric subscript notation to refer to a tuple's key or value, thus:

$$\forall_{I:\in\mathfrak{I}} I \equiv (I_0, I_1)$$

Any series of bytes may also trivially be viewed as a series of nibbles, given an endian-specific notation; here we assume big-endian. Thus:

$$y(\mathfrak{I}) = \{ (\mathbf{k}'_0 \in \mathbb{Y}, \mathbf{v}_0 \in \mathbb{B}), (\mathbf{k}'_1 \in \mathbb{Y}, \mathbf{v}_1 \in \mathbb{B}), \ldots \}$$

(135)
$$y(\mathfrak{I}) = \{ (\mathbf{k}'_0 \in \mathbb{Y}, \mathbf{v}_0 \in \mathbb{B}), (\mathbf{k}'_1 \in \mathbb{Y}, \mathbf{v}_1 \in \mathbb{B}), ... \}$$
(136)
$$\forall_n \ \forall_{i:i<2\parallel\mathbf{k}_n\parallel} \ \mathbf{k}'_n[i] \equiv \begin{cases} \lfloor \mathbf{k}_n[\lfloor i \div 2 \rfloor] \div 16 \rfloor & \text{if } i \text{ is even} \\ \mathbf{k}_n[\lfloor i \div 2 \rfloor] & \text{mod } 16 & \text{otherwise} \end{cases}$$

We define the function TRIE, which evaluates to the root of the trie that represents this set when encoded in this structure. The empty trie is defined as being a the empty byte sequence, ():

(137)
$$\text{TRIE}(\mathfrak{I}) \equiv \begin{cases} () & \text{if} \quad \mathfrak{I} = \emptyset \\ \text{SHA3}(c(\mathfrak{I},0)) & \text{otherwise} \end{cases}$$

We also assume a function n, the trie's node cap function. When composing a node, we use RLP to encode the structure. As a means of reducing storage complexity, for nodes whose composed RLP is fewer than 32 bytes, we store the RLP directly; for those larger we assert prescience of the byte array whose SHA3 hash evaluates to our reference. Thus we define in terms of c, the node composition function:

(138)
$$n(\mathfrak{I},i) \equiv \begin{cases} () & \text{if} \quad \mathfrak{I} = \varnothing \\ c(\mathfrak{I},i) & \text{if} \quad \|c(\mathfrak{I},i)\| < 32 \\ \text{Sha3}(c(\mathfrak{I},i)) & \text{otherwise} \end{cases}$$

In a manner similar to a radix tree, when the trie is traversed from root to leaf, one may build a single key-value pair. The key is accumulated through the traversal, acquiring a single nibble from each branch node (just as with a radix tree). Unlike a radix tree, in the case of multiple keys shared the same prefix or in the case of a single key having a unique suffix, two optimising nodes are provided. Thus while traversing, one may potentially acquire multiple nibbles from each of the other two node types, extension and leaf. There are three kinds of nodes in the trie:

Leaf: A two-item structure whose first item corresponds to the nibbles in the key not already accounted for by the accumulation of keys and branches traversed from the root. The hex-prefix encoding method is used and the second parameter to the function is required to be *true*.

Extension: A two-item structure whose first item corresponds to a series of nibbles of size greater than one that are shared by at least two distinct keys past the accumulation of nibbles keys and branches as traversed from the root. The hex-prefix encoding method is used and the second parameter to the function is required to be false.

Branch: A 17-item structure whose first sixteen items correspond to each of the sixteen possible nibble values for the keys at this point in their traversal. The 17th item is used in the case of this being a terminator node and thus a key being ended at this point in its traversal.

A branch is then only used when necessary; no branch nodes may exist that contain only a single non-zero entry. We may formally define this structure with the structural composition function c:

(130)

may formally define this structure with the structural composition function
$$c$$
:
$$(139)$$

$$c(\mathfrak{I},i) \equiv \begin{cases} \text{RLP}\left((\text{HP}(I_0[i..(||I_0||-1)], true), I_1) \right) & \text{if} \quad ||\mathfrak{I}|| = 1 \quad \text{where } \exists I:I \in \mathfrak{I} \\ \text{RLP}\left((\text{HP}(I_0[i..(j-1)], false), n(\mathfrak{I},j)) \right) & \text{if} \quad i \neq j \quad \text{where } j = \arg\max_x : \exists I: ||I|| = x: \forall_{I \in \mathfrak{I}} : I_0[0..(x-1)] = I \\ \text{RLP}\left((u(0), u(1), ..., u(15), v) \right) & \text{otherwise} \quad \text{where } u(j) \equiv n(\{I:I \in \mathfrak{I} \land I_0[i] = j\}, i+1) \\ v = \begin{cases} I_1 & \text{if} \quad \exists I:I \in \mathfrak{I} \land ||I_0|| = i \\ () & \text{otherwise} \end{cases}$$

$$\text{E.1. Trie. Database.} \text{ Thus no explicit assumptions are made concerning what data is stored and what is not since the since the sum of t$$

E.1. **Trie Database.** Thus no explicit assumptions are made concerning what data is stored and what is not, since that is an implementation-specific consideration; we simply define the identity function mapping the key-value set \Im to a 32-byte hash and assert that only a single such hash exists for any \Im , which though not strictly true is accurate within acceptable precision given the SHA3 hash's collision resistance. In reality, a sensible implementation will not fully recompute the trie root hash for each set.

A reasonable implementation will maintain a database of nodes determined from the computation of various tries or, more formally, it will memoise the function c. This strategy uses the nature of the trie to both easily recall the contents of any previous key-value set and to store multiple such sets in a very efficient manner. Due to the dependency relationship, Merkle-proofs may be constructed with an $O(\log N)$ space requirement that can demonstrate a particular leaf must exist within a trie of a given root hash.

APPENDIX F. SIGNING TRANSACTIONS

The method of signing transactions is similar to the 'Electrum style signatures'; it utilises the SECP-256k1 curve as described by Gura et al. [2004].

It is assumed that the sender has a valid private key p_r , a randomly selected positive integer in the range $(0, 2^{256})$ represented as a byte array of length 32 in big-endian form.

We assert the functions ECDSASIGN, ECDSARESTORE and ECDSAPUBKEY. These are formally defined in the literature.

(140)
$$ECDSAPUBKEY(p_r \in \mathbb{B}_{32}) \equiv p_u \in \mathbb{B}_{64}$$

(141)
$$ECDSASIGN(e \in \mathbb{B}_{32}, p_r \in \mathbb{B}_{32}) \equiv (v \in \mathbb{B}_2, r \in \mathbb{B}_{32}, s \in \mathbb{B}_{32})$$

$$(142) \qquad \qquad \mathsf{ECDSARESTORE}(e \in \mathbb{B}_{32}, v \in \mathbb{B}_{2}, r \in \mathbb{B}_{32}, s \in \mathbb{B}_{32}) \quad \equiv \quad p_u \in \mathbb{B}_{64}$$

Where p_u is the public key, assumed to be a byte array of size 64 (formed from the concatenation of two positive integers each $< 2^{256}$) and p_r is the private key, a byte array of size 32 (or a single positive integer $< 2^{256}$). It is assumed that v is the 'recovery id', a 2-bit value specifying the sign and finiteness of the curve point; unlike some implementations which keep this value in the range of [27, 30], we subtract the lower bound thus reducing it to a pure 2-bit value in the range [0, 3].

For a given private key, p_r , the Ethereum address $A(p_r)$ (a 160-bit value) to which it corresponds is defined as the right most 160-bits of the SHA3 hash of the corresponding ECDSA public key:

$$A(p_r) = \mathcal{B}_{96..255} (SHA3(ECDSAPUBKEY(p_r)))$$

The message hash, h(T), to be signed is the SHA3 hash of the transaction without the latter three signature components, formally described as T_r , T_s and T_w :

(144)
$$L_{S}(T) \equiv \begin{cases} (T_{n}, T_{p}, T_{g}, T_{t}, T_{v}, T_{\mathbf{i}}) & \text{if } T_{t} = 0 \\ (T_{n}, T_{p}, T_{g}, T_{t}, T_{v}, T_{\mathbf{d}}) & \text{otherwise} \end{cases}$$

$$h(T) \equiv \text{SHA3}(L_{S}(T))$$

$$h(T) \equiv SHA3(L_S(T))$$

The signed transaction $G(T, p_r)$ is defined as:

(146)
$$G(T, p_r) \equiv T \quad \text{except}$$

$$(T_w, T_r, T_s) = \mathtt{ECDSASIGN}(h(T), p_r)$$

gc We may then define the sender function S of the transaction as:

(148)
$$S(T) \equiv \mathcal{B}_{96..255} \big(\text{SHA3} \big(\text{ECDSARESTORE}(h(T), T_w, T_r, T_s) \big) \big)$$

The assertion that the sender of the a signed transaction equals the address of the signer should be self-evident:

(149)
$$\forall T : \forall p_r : S(G(T, p_r)) \equiv A(p_r)$$

APPENDIX G. VIRTUAL MACHINE SPECIFICATION

When interpreting 256-bit binary values as integers, the representation is big-endian.

When a 256-bit machine datum is converted to and from a 160-bit address or hash, the rightwards (low-order for BE) 20 bytes are used and the left most 12 are discarded or filled with zeroes, thus the integer values (when the bytes are interpreted as big-endian) are equivalent.

G.1. **Gas Cost.** The general gas cost function, C, is defined as:

(150)
$$C(\boldsymbol{\sigma}, \boldsymbol{\mu}, I) \equiv G_{memory}(\boldsymbol{\mu}_i' - \boldsymbol{\mu}_i) + \begin{cases} C_{\text{SSTORE}}(\boldsymbol{\sigma}, \boldsymbol{\mu}) & \text{if } w = \text{SSTORE} \\ G_{call} + \boldsymbol{\mu}_s[0] & \text{if } w = \text{CALL} \\ G_{create} & \text{if } w = \text{CREATE} \\ G_{sha3} & \text{if } w = \text{SHA3} \\ G_{sload} & \text{if } w = \text{SLOAD} \\ G_{balance} & \text{if } w = \text{SLOAD} \\ G_{stop} & \text{if } w = \text{STOP} \\ G_{suicide} & \text{if } w = \text{SUICIDE} \\ G_{step} & \text{otherwise} \end{cases}$$

$$(151) \qquad w \equiv \begin{cases} I_{\mathbf{b}}[\boldsymbol{\mu}_{pc}] & \text{if } \boldsymbol{\mu}_{pc} < \|I_{\mathbf{b}}\| \\ \text{STOP} & \text{otherwise} \end{cases}$$

where C_{SSTORE} is specified in the appropriate section below. Note the memory cost component, given as the product of G_{memory} and the maximum of 0 and the ceiling of the number of words in size that the memory must be over the current number of words, μ_i in order that all accesses reference valid memory whether for read or write; μ_i' is defined as this new maximum number of words of active memory; special-cases are given where these two are not equal.

G.2. Instruction Set. As previously specified in section 9, these definitions take place in the final context there. In particular we assume O is the EVM state-progression function and define the terms pertaining to the next cycle's state $(\boldsymbol{\sigma}', \boldsymbol{\mu}')$ such that:

(152)
$$O(\boldsymbol{\sigma}, \boldsymbol{\mu}, I) \equiv (\boldsymbol{\sigma}', \boldsymbol{\mu}', I)$$
 with exceptions, as noted

Here given are the various exceptions to the state transition rules given in section 9 specified for each instruction, together with the additional instruction-specific definitions of J and C. For each instruction, also specified is α , the additional items placed on the stack and δ , the items removed from stack, as defined in section 9.

0s: Stop and Arithmetic Operations

All arithmetic is	s modulo 2 ²	256
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Value	Mnemonic	δ	α	Description
0x00	STOP	0	0	Halts execution. $\mu_R' = []$
0x01	ADD	2	1	Addition operation. $\mu_{\mathbf{s}}'[0] \equiv \mu_{\mathbf{s}}[0] + \mu_{\mathbf{s}}[1]$
0x02	MUL	2	1	Multiplication operation. $\mu_{\mathbf{s}}'[0] \equiv \mu_{\mathbf{s}}[0] \times \mu_{\mathbf{s}}[1]$
0x03	SUB	2	1	Subtraction operation. $\mu_{\mathbf{s}}'[0] \equiv \mu_{\mathbf{s}}[0] - \mu_{\mathbf{s}}[1]$
0x04	DIV	2	1	Integer division operation. $\boldsymbol{\mu}_{\mathbf{s}}'[0] \equiv \begin{cases} 0 & \text{if} \boldsymbol{\mu}_{\mathbf{s}}[1] = 0 \\ \lfloor \boldsymbol{\mu}_{\mathbf{s}}[0] \div \boldsymbol{\mu}_{\mathbf{s}}[1] \rfloor & \text{otherwise} \end{cases}$
0x05	SDIV	2	1	Signed integer division operation. $\boldsymbol{\mu}_{\mathbf{s}}'[0] \equiv \begin{cases} 0 & \text{if } \boldsymbol{\mu}_{\mathbf{s}}[1] = 0 \\ \lfloor \boldsymbol{\mu}_{\mathbf{s}}[0] \div \boldsymbol{\mu}_{\mathbf{s}}[1] \rfloor & \text{otherwise} \end{cases}$ Where all values are treated as signed 256-bit integers for the purposes of this operation
0x06	MOD	2	1	Modulo remainder operation. $\boldsymbol{\mu}_{\mathbf{s}}'[0] \equiv \begin{cases} 0 & \text{if } \boldsymbol{\mu}_{\mathbf{s}}[1] = 0 \\ \boldsymbol{\mu}_{\mathbf{s}}[0] \bmod \boldsymbol{\mu}_{\mathbf{s}}[1] & \text{otherwise} \end{cases}$
0x07	SMOD	2	1	Signed modulo remainder operation. $\boldsymbol{\mu}_{\mathbf{s}}'[0] \equiv \begin{cases} 0 & \text{if } \boldsymbol{\mu}_{\mathbf{s}}[1] = 0 \\ \boldsymbol{\mu}_{\mathbf{s}}[0] \bmod \boldsymbol{\mu}_{\mathbf{s}}[1] & \text{otherwise} \end{cases}$ Where all values are treated as signed 256-bit integers for the purposes of this operation
0x08	EXP	2	1	Exponential operation. $\mu_{\mathbf{s}}'[0] \equiv \mu_{\mathbf{s}}[0]^{\mu_{\mathbf{s}}[1]}$
0x09	NEG	1	1	Negation operation. $\mu_s'[0] \equiv -\mu_s[0]$ Where all values are treated as signed 256-bit integers for the purposes of this operation
0x0a	LT	2	1	Less-than comparision. $\boldsymbol{\mu}_{\mathbf{s}}'[0] \equiv \begin{cases} 1 & \text{if} \boldsymbol{\mu}_{\mathbf{s}}[0] < \boldsymbol{\mu}_{\mathbf{s}}[1] \\ 0 & \text{otherwise} \end{cases}$
0x0b	GT	2	1	Greater-than comparision. $\boldsymbol{\mu}_{\mathbf{s}}'[0] \equiv \begin{cases} 1 & \text{if } \boldsymbol{\mu}_{\mathbf{s}}[0] > \boldsymbol{\mu}_{\mathbf{s}}[1] \\ 0 & \text{otherwise} \end{cases}$
0x0c	SLT	2	1	Signed less-than comparision. $\boldsymbol{\mu}_{\mathbf{s}}'[0] \equiv \begin{cases} 1 & \text{if } \boldsymbol{\mu}_{\mathbf{s}}[0] < \boldsymbol{\mu}_{\mathbf{s}}[1] \\ 0 & \text{otherwise} \end{cases}$ Where all values are treated as signed 256-bit integers for the purposes of this operation
0x0d	SGT	2	1	Signed greater-than comparision. $\boldsymbol{\mu}_{\mathbf{s}}'[0] \equiv \begin{cases} 1 & \text{if } \boldsymbol{\mu}_{\mathbf{s}}[0] > \boldsymbol{\mu}_{\mathbf{s}}[1] \\ 0 & \text{otherwise} \end{cases}$ Where all values are treated as signed 256-bit integers for the purposes of this operation
0x0e	EQ	2	1	Equality comparision. $\boldsymbol{\mu}_{\mathbf{s}}'[0] \equiv \begin{cases} 1 & \text{if } \boldsymbol{\mu}_{\mathbf{s}}[0] = \boldsymbol{\mu}_{\mathbf{s}}[1] \\ 0 & \text{otherwise} \end{cases}$
0x0f	NOT	1	1	Simple not operator. $\mu'_{\mathbf{s}}[0] \equiv \begin{cases} 1 & \text{if } \mu_{\mathbf{s}}[0] = 0 \\ 0 & \text{otherwise} \end{cases}$

ives the ith hit ((col	anti	no fr	10s: Bitwise Logic Operations
		1	Bitw	vise AND operation. $[0255]: \boldsymbol{\mu}_{\mathbf{s}}'[0]_i \equiv \boldsymbol{\mu}_{\mathbf{s}}[0]_i \wedge \boldsymbol{\mu}_{\mathbf{s}}[1]_i$
OR 2	2	1	Bitw	vise OR operation. $[0255]: \boldsymbol{\mu}_{\mathbf{s}}'[0]_i \equiv \boldsymbol{\mu}_{\mathbf{s}}[0]_i \vee \boldsymbol{\mu}_{\mathbf{s}}[1]_i$
XOR 2	2			vise XOR operation. $[0255]: \boldsymbol{\mu}_{\mathbf{s}}'[0]_i \equiv \boldsymbol{\mu}_{\mathbf{s}}[0]_i \oplus \boldsymbol{\mu}_{\mathbf{s}}[1]_i$
BYTE 2	2		$\forall i \in$	rieve single byte from word. $[07]: \boldsymbol{\mu}_{\mathbf{s}}'[0]_i \equiv \begin{cases} \boldsymbol{\mu}_{\mathbf{s}}[1]_{(i+8\boldsymbol{\mu}_{\mathbf{s}}[0])} & \text{if} \boldsymbol{\mu}_{\mathbf{s}}[0] < 32\\ 0 & \text{otherwise} \end{cases}$ Nth byte, we count from the left (i.e. N=0 would be the most significant in big endian).
				s: SHA3
${\bf Mnemonic} \delta$	δ	α		
		1	$Com \mu'_{\mathbf{s}}[0]$	pute SHA3-256 hash. $[\mathbf{m}_{\mathbf{s}}] \equiv \mathbf{SHA3}(\boldsymbol{\mu}_{\mathbf{m}}[\boldsymbol{\mu}_{\mathbf{s}}[0] \dots (\boldsymbol{\mu}_{\mathbf{s}}[0] + \boldsymbol{\mu}_{\mathbf{s}}[1] - 1)])$ $= \max(\boldsymbol{\mu}_{i}, \lceil (\boldsymbol{\mu}_{\mathbf{s}}[0] + \boldsymbol{\mu}_{\mathbf{s}}[1]) \div 32 \rceil)$
				30s: Environmental Information
Mnemonic		δ	α	Description
ADDRESS		0	1	Get address of currently executing account. $\mu'_{\mathbf{s}}[0] \equiv I_a$
BALANCE		1	1	Get balance of the given account. $\boldsymbol{\mu}_{\mathbf{s}}'[0] \equiv \begin{cases} \boldsymbol{\sigma}[\boldsymbol{\mu}_{\mathbf{s}}[0]]_b & \text{when} \boldsymbol{\sigma}[\boldsymbol{\mu}_{\mathbf{s}}[0]] \neq \varnothing \\ 0 & \text{otherwise} \end{cases}$
ORIGIN		0	0 1 Get execution origination address. $\mu_s'[0] \equiv I_o$ This is the sender of original transaction; it is never an account with non-empty ass	
CALLER	CALLER 0 1 Get caller address. $\mu_{\mathbf{s}}'[0] \equiv I_c$ This is the address of the account that is directly responsible for this execution.		$oldsymbol{\mu_s'}[0] \equiv I_c$	
		Get deposited value by the instruction/transaction responsible for this execution. $\mu_{\mathbf{s}}'[0] \equiv I_v$		
5 CALLDATALOAD 1		1	1	Get input data of current environment. $\mu_{\mathbf{s}}'[0] \equiv I_{\mathbf{d}}[\mu_{\mathbf{s}}[0] \dots (\mu_{\mathbf{s}}[0] + 31)]$ This pertains to the input data passed with the message call instruction or transaction.
6 CALLDATASIZE 0		0	1	Get size of input data in current environment. $\mu_s'[0] \equiv I_d $ This pertains to the input data passed with the message call instruction or transaction.
CALLDATACOF	PY	3	0	Copy input data in current environment to memory.
				$\forall_{i \in \{0\boldsymbol{\mu_s}[2]-1\}}\boldsymbol{\mu_m'}[\boldsymbol{\mu_s}[0]+i] \equiv \begin{cases} I_{\mathbf{d}}[\boldsymbol{\mu_s}[1]+i] & \text{if} i < \ I_{\mathbf{d}}\ \\ 0 & \text{otherwise} \end{cases}$ This partials to the input data passed with the massage call instruction or transaction.
CODESIZE		0	1	This pertains to the input data passed with the message call instruction or transaction. Get size of code running in current environment.
CODESIZE		0	1	Get size of code running in current environment. $\mu_{\mathbf{s}}'[0] \equiv \ I_{\mathbf{b}}\ $
CODECOPY		3	0	Copy code running in current environment to memory. $\forall_{i \in \{0\boldsymbol{\mu_s}[2]-1\}} \boldsymbol{\mu_m'}[\boldsymbol{\mu_s}[0]+i] \equiv \begin{cases} I_{\mathbf{b}}[\boldsymbol{\mu_s}[1]+i] & \text{if} i < \ I_{\mathbf{b}}\ \\ \text{STOP} & \text{otherwise} \end{cases}$
GASPRICE		0	1	Get price of gas in current environment. $\boldsymbol{\mu}_{\mathbf{s}}'[0] \equiv I_p$
				$\mu'_{\mathbf{s}}[0] \equiv I_p$ This is gas price specified by the originating transaction.
	Mnemonic ADDRESS BALANCE CALLDATALUE CALLDATACUE CODESIZE CODECOPY AND A STATE TO THE STATE	Mnemonic δ δ AND 2 XOR 2 BYTE 2 Mnemonic δ SHA3 2 BALANCE 3 CALLER 4 CALLER 4 CALLDATALUATALUATALUATALUATALUATALUATALUA	Mnemonic δ α AND 2 1 COR 2 1 BYTE 2 1 Mnemonic 2 2 SHA3 2 1 BALANCE 2 1 CALLER 2 1 CALLER 2 1 CALLDATALUE 2 0 CALLDATALUATALUE 3 0 CALLDATACUPY 3 0 CODESIZE 3 0 CODECOPY 3 3	OR 2 1 Bitwody (1 €) XOR 2 1 Bitwody (1 €) BYTE 2 1 Retriction (2 €) Mnemonic 2 1 Description (2 €) SHA3 2 1 Description (2 €) SHA3 2 1 Compa/s [0] BALANCE 2 1 Compa/s [0] BALANCE 2 1 1 CALLER 3 0 1 CALLOATALUATALUATALUATALUATALUATALUATALUA

		40 s:	В	lock Information		
Value	Mnemonic	δ	α	Description		
0x40	PREVHASH	0	1	Get hash of most recent complete block. $\mu'_{\mathbf{s}}[0] \equiv I_{Hp}$ I_{Hp} is the previous block's hash.		
0x41	COINBASE	0	1	Get the block's coinbase address. $\mu_{\mathbf{s}}'[0] \equiv I_{Hb}$		
0x42	TIMESTAMP	0	1	Get the block's timestamp. $\mu_{\mathbf{s}}'[0] \equiv I_{Ht}$		
0x43	NUMBER	0	1	Get the block's number. $\mu_{\mathbf{s}}'[0] \equiv I_{H_i}$		
0x44	DIFFICULTY	0	1	Get the block's difficulty. $\mu_{\mathbf{s}}'[0] \equiv I_{Hd}$		
0x45	GASLIMIT	0	1	Get the block's gas limit. $\mu_{\mathbf{s}}'[0] \equiv I_{Hl}$		
	50s:	Sta	ck,	Memory, Storage and Flow Operations		
Value	Mnemonic	δ	α	Description		
0x50	POP	1	0	Remove item from stack.		
0x51	DUP	1	2	Duplicate stack item. $\mu_{\mathbf{s}}'[0] \equiv \mu_{\mathbf{s}}[0]$		
0x52	SWAP	2	2	Exchange stack items. $ \mu_{\mathbf{s}}'[0] \equiv \mu_{\mathbf{s}}[1] $ $ \mu_{\mathbf{s}}'[1] \equiv \mu_{\mathbf{s}}[0] $		
0x53	MLOAD	1	1	Load word from memory. $\boldsymbol{\mu}_{\mathbf{s}}'[0] \equiv \boldsymbol{\mu}_{\mathbf{m}}[\boldsymbol{\mu}_{\mathbf{s}}[0] \dots (\boldsymbol{\mu}_{\mathbf{s}}[0] + 31)]$ $\boldsymbol{\mu}_{i} \equiv \max(\boldsymbol{\mu}_{i}, \lceil (\boldsymbol{\mu}_{\mathbf{s}}[0] + 32) \div 32 \rceil)$		
0x54	MSTORE	2	0	Save word to memory. $\boldsymbol{\mu}_{\mathbf{m}}'[\boldsymbol{\mu}_{\mathbf{s}}[0] \dots (\boldsymbol{\mu}_{\mathbf{s}}[0] + 31)] \equiv \boldsymbol{\mu}_{\mathbf{s}}[1]$ $\boldsymbol{\mu}_{i}' \equiv \max(\boldsymbol{\mu}_{i}, \lceil (\boldsymbol{\mu}_{\mathbf{s}}[0] + 32) \div 32 \rceil)$		
0x55	MSTORE8	2	0	Save byte to memory. $\boldsymbol{\mu}_{\mathbf{m}}'[\boldsymbol{\mu}_{\mathbf{s}}[0]] \equiv (\boldsymbol{\mu}_{\mathbf{s}}[1] \mod 256)$ $\boldsymbol{\mu}_{i}' \equiv \max(\boldsymbol{\mu}_{i}, \lceil (\boldsymbol{\mu}_{\mathbf{s}}[0] + 1) \div 32 \rceil)$		
0x56	SLOAD	1	1	Load word from storage. $\mu_{\mathbf{s}}'[0] \equiv \boldsymbol{\sigma}[I_a]_{\mathbf{s}}[\mu_{\mathbf{s}}[0]]$		
0x57	SSTORE	2	0	Save word to storage. $\boldsymbol{\sigma}'[I_a]_{\mathbf{s}}[\boldsymbol{\mu}_{\mathbf{s}}[0]] \equiv \boldsymbol{\mu}_{\mathbf{s}}[1]$ $C_{\text{SSTORE}}(\boldsymbol{\sigma}, \boldsymbol{\mu}) \equiv \begin{cases} 2G_{sstore} & \text{if } \boldsymbol{\mu}_{\mathbf{s}}[1] \neq 0 \ \land \ \boldsymbol{\sigma}[I_a]_{\mathbf{s}}[\boldsymbol{\mu}_{\mathbf{s}}[0]] = 0 \\ 0 & \text{if } \boldsymbol{\mu}_{\mathbf{s}}[1] = 0 \ \land \ \boldsymbol{\sigma}[I_a]_{\mathbf{s}}[\boldsymbol{\mu}_{\mathbf{s}}[0]] \neq 0 \end{cases}$ $G_{sstore} & \text{otherwise}$		
0x58	JUMP	1	0	Alter the program counter. $J_{\text{JUMP}}(\boldsymbol{\mu}) \equiv \boldsymbol{\mu}_{\mathbf{s}}[0]$ This has the effect of writing said value to $\boldsymbol{\mu}_{pc}$. See section 9.		
0x59	JUMPI	2	0	Conditionally alter the program counter. $J_{\text{Jumpi}}(\boldsymbol{\mu}) \equiv \begin{cases} \boldsymbol{\mu}_{\mathbf{s}}[0] & \text{if } \boldsymbol{\mu}_{\mathbf{s}}[1] \neq 0 \\ \boldsymbol{\mu}_{pc} + 1 & \text{otherwise} \end{cases}$ This has the effect of writing said value to $\boldsymbol{\mu}_{pc}$. See section 9.		
0x5a	PC	0	1	Get the program counter. $\mu_{\mathbf{s}}'[0] \equiv \mu_{pc}$		
0x5b	MSIZE	0	1	Get the size of active memory. $\mu_{\mathbf{s}}'[0] \equiv \mu_{i}$		
0x5c	GAS	0	1	Get the amount of available gas. $\mu_{\mathbf{s}}'[0] \equiv \mu_g$		

60s & 70s: Push Operations					
Value	Mnemonic	δ	α	Description	
0x60	PUSH1	0	1	Place 1 byte item on stack. $\mu'_{\mathbf{s}}[0] \equiv I_{\mathbf{b}}[\mu_{pc} + 1]$ The byte is right-aligned (takes the lowest significant place in big endian).	
0x61	PUSH2	0	1	Place 2-byte item on stack. $\mu_{\mathbf{s}}'[0] \equiv I_{\mathbf{b}}[(\mu_{pc}+1)\dots(\mu_{pc}+2)]$ The bytes are right-aligned (takes the lowest significant place in big endian).	
:	:	:	:	<u>:</u>	
0x7f	PUSH32	0	1	Place 32-byte (full word) item on stack. $\mu_{\mathbf{s}}'[0] \equiv I_{\mathbf{b}}[(\boldsymbol{\mu}_{pc}+1)\dots(\boldsymbol{\mu}_{pc}+32)]$	
				f0s: System operations	
Value	Mnemonic	δ	α	Description	
0xf0	CREATE	3	1	Create a new account with associated code. $\mathbf{i} \equiv \boldsymbol{\mu}_{\mathbf{m}}[\boldsymbol{\mu}_{\mathbf{s}}[1] \dots (\boldsymbol{\mu}_{\mathbf{s}}[1] + \boldsymbol{\mu}_{\mathbf{s}}[2] - 1)]$ $\left(\Lambda(\boldsymbol{\sigma}^* I, I, \boldsymbol{\mu}, I, \boldsymbol{\mu}, [0], \mathbf{i}, \mathbf{b}) \right) \text{ when } \boldsymbol{\mu}[0] \leq \boldsymbol{\sigma}[I].$	
				$(\boldsymbol{\sigma}', \boldsymbol{\mu}_g') \equiv egin{cases} \Lambda(\boldsymbol{\sigma}^*, I_a, I_o, \boldsymbol{\mu}_g, I_p, \boldsymbol{\mu}_{\mathbf{s}}[0], \mathbf{i}, \mathbf{b}) & ext{when} \boldsymbol{\mu}_{\mathbf{s}}[0] \leqslant \boldsymbol{\sigma}[I_a]_b \\ (\boldsymbol{\sigma}, \boldsymbol{\mu}_g) & ext{otherwise} \end{cases}$	
				$\sigma^* \equiv \sigma$ except $\sigma^*[I_a]_n = \sigma[I_a]_n + 1 \wedge \sigma^*[I_a]_b = \sigma[I_a]_b - \mu_s[0]$ $\mu_s'[0] \equiv x$	
				where $x = 0$ if the code execution for this operation failed due to lack of gas or	
				$\mu_{\mathbf{s}}[0] > \sigma[I_a]_b$; $x = A(I_a, \sigma[I_a]_n)$, the address of the newly created account, otherwise. $\mu'_i \equiv \max(\mu_i, \lceil (\mu_{\mathbf{s}}[1] + \mu_{\mathbf{s}}[2]) \div 32 \rceil)$ Thus the operand order is: value, input offset, input size.	
0xf1	CALL	7	1	Message-call into an account. $\mathbf{i} \equiv \boldsymbol{\mu}_{\mathbf{m}}[\boldsymbol{\mu}_{\mathbf{s}}[3] \dots (\boldsymbol{\mu}_{\mathbf{s}}[3] + \boldsymbol{\mu}_{\mathbf{s}}[4] - 1)]$	
				$\mathbf{o} \equiv \boldsymbol{\mu}_{\mathbf{m}}[\boldsymbol{\mu}_{\mathbf{s}}[5]\dots(\boldsymbol{\mu}_{\mathbf{s}}[5]+\boldsymbol{\mu}_{\mathbf{s}}[6]-1)]$	
				$(\boldsymbol{\sigma}', g', \mathbf{o}) \equiv \begin{cases} \Theta(\boldsymbol{\sigma}^*, I_a, I_o, \boldsymbol{\mu}_{\mathbf{s}}[1], \boldsymbol{\mu}_{\mathbf{s}}[0], I_p, \boldsymbol{\mu}_{\mathbf{s}}[2], \mathbf{i}) & \text{when } \boldsymbol{\mu}_{\mathbf{s}}[2] \leqslant \boldsymbol{\sigma}[I_a]_b \\ (\boldsymbol{\sigma}, g, \mathbf{o}) & \text{otherwise} \end{cases}$	
				$oldsymbol{\sigma}^* \equiv oldsymbol{\sigma} ext{except} oldsymbol{\sigma}^*[I_a]_b = oldsymbol{\sigma}[I_a]_b - oldsymbol{\mu}_{\mathbf{s}}[2]$ $oldsymbol{\mu}_g' \equiv oldsymbol{\mu}_g + g'$	
				$\mu_{\mathbf{s}}'[0] \equiv x$	
				where $x = 0$ if the code execution for this operation failed due to lack of gas or if $\mu_{\mathbf{s}}[2] > \sigma[I_a]_b$; $x = 1$ otherwise.	
				$\mu'_i \equiv \max(\mu_i, \lceil \max(\mu_s[3] + \mu_s[4], \mu_s[5] + \mu_s[6]) \div 32 \rceil)$ Thus the operand order is: gas, to, value, in offset, in size, out offset, out size.	
0xf2	RETURN	2	0	Halt execution returning output data.	
				$H_{\text{RETURN}}(\boldsymbol{\mu}) \equiv \boldsymbol{\mu}_{\mathbf{m}}[\boldsymbol{\mu}_{\mathbf{s}}[0] \dots (\boldsymbol{\mu}_{\mathbf{s}}[0] + \boldsymbol{\mu}_{\mathbf{s}}[1] - 1)]$ This has the effect of halting the execution at this point with output defined. See section 9. $\boldsymbol{\mu}_i' \equiv \max(\boldsymbol{\mu}_i, \lceil (\boldsymbol{\mu}_{\mathbf{s}}[0] + \boldsymbol{\mu}_{\mathbf{s}}[1]) \div 32 \rceil)$	
0xff	SUICIDE	1	0	Halt execution and obliterate account.	
				$oldsymbol{\sigma}'[oldsymbol{\mu}_{\mathbf{s}}[0]]_b \equiv oldsymbol{\sigma}[oldsymbol{\mu}_{\mathbf{s}}[0]]_b + oldsymbol{\sigma}[I_a]_b \ oldsymbol{\sigma}'[I_a] \equiv arnothing$	

APPENDIX H. WIRE PROTOCOL

The wire-protocol specifies a network-level protocol for how two peers can communicate. It includes handshake procedures and the means for transferring information such as peers, blocks and transactions. Peer-to-peer communications between nodes running Ethereum clients are designed to be governed by a simple wire-protocol making use of existing Ethereum technologies and standards such as RLP wherever practical.

Ethereum nodes may connect to each other over TCP only. Peers are free to advertise and accept connections on any port(s) they wish, however, a default port on which the connection may be listened and made will be 30303.

Though TCP provides a connection-oriented medium, Ethereum nodes communicate in terms of packets. These packets are formed as a 4-byte synchronisation token (0x22400891), a 4-byte "payload size", to be interpreted as a big-endian integer and finally an N-byte **RLP-serialised** data structure, where N is the aforementioned "payload size". To be clear, the payload size specifies the number of bytes in the packet "following" the first 8.

There are a number of different types of message that may be sent. This "type" is always determined by the first entry of the structure, represented as a scalar. The structure of each message type is described below.

00s: Session control

Value Mnemonic Expected Reply Packet Format

0x00 Hello

 $(0x00, v \in \mathbb{P}, n \in \mathbb{P}, \mathbf{i} \in \mathbb{B}, c \in \mathbb{P}, p \in \mathbb{P}, u \in \mathbb{B}_{64})$

This is the first packet sent over the connection, and sent once by both sides. No other messages may be sent until a Hello is received.

- v is the Protocol Version. See the latest documentation for which version is current.
- n is the Network Id should be 0.
- i is the Client Id and specifies the client software identity as a human-readable string (e.g. "Ethereum(++)/1.0.0").
- c is the client's Capabilities and specifies the capabilities of the client as a set of flags;
 presently three bits are used:

0x01: Client provides peer discovery service;

0x02: Client provides transaction relaying service;

0x04: Client provides block-chain querying service.

- p is the Listen Port and specifies the port that the client is listening on (on the interface that the present connection traverses). If 0 it indicates the client is not listening.
- \bullet u is the Unique Identity of the node and specifies a 512-bit hash that identifies this node.

peer.

0x01 DISCONNECT

 $(0x01, r \in \mathbb{P})$

Inform the peer that a disconnection is imminent; if received, a peer should disconnect immediately. When sending, well-behaved hosts give their peers a fighting chance (read: wait 2 seconds) to disconnect to before disconnecting themselves.

 \bullet r is an integer specifying one of a number of reasons for disconnect:

0x00: Disconnect requested;

0x01: TCP sub-system error;

0x02: Bad protocol;

0x03: Useless peer;

0x04: Too many peers;

0x05: Already connected;

0x06: Wrong genesis block;

0x07: Incompatible network protocols;

0x08: Client quitting.

0x02	Ping	Pong	(0x02)
	Requests a	n immediate reply	of Pong from the

0x03 Pong Reply to peer's Ping packet. (0x03)

10s: Information

Value	Mnemonic	Expected Reply	Packet Format
0x10	GETPEERS Request the peer to peer itself.	Peers enumerate some known pee	(0x10) rs for us to connect to. This should include the
011	Drang		(0-11 (- CD - CD : CD) (- CD - CD : CD)

0x11 Peers

 $(0x11, (a_0 \in \mathbb{B}_4, p_0 \in \mathbb{P}, i_0 \in \mathbb{B}_{64}), (a_1 \in \mathbb{B}_4, p_1 \in \mathbb{P}, i_1 \in \mathbb{B}_{64}), ...)$

Specifies a number of known peers.

- a_0 , a_1 , ... is the node's IPv4 address, a 4-byte array that should be interpreted as the IP address $a_0[0].a_0[1].a_0[2].a_0[3]$.
- p_0, p_1, \dots is the node's Port and is an integer.
- i₀, i₁, ... is the node's Unique Identifier and is the 512-bit hash that serves to identify
 the node.

0x12 Transactions

 $(0x12, L_T(T_0), L_T(T_1), ...)$

where L_T is the transaction preparation function, as specified in section 4.3.

Specify a transaction or transactions that the peer should make sure is included on its transaction queue. The items in the list (following the first item 0x12) are transactions in the format described in the main Ethereum specification.

• T_0, T_1, \dots are the transactions that should be assimilated.

0x13 Blocks

 $(0x13, L_B(b_0), L_B(b_1), ...)$

Where L_B is the block preparation function, as specified in section 4.3.

Specify a block or blocks that the peer should know about. The items in the list (following the first item, 0x13) are blocks as described in the format described in the main specification.

• b_0, b_1, \dots are the blocks that should be assimilated.

0x14 GetChain

BLOCKS OF NOTINCHAIN $(0x14, p_0 \in \mathbb{B}_{32}, p_1 \in \mathbb{B}_{32}, ..., c \in \mathbb{P})$

Request the peer to send c blocks in the current canonical block chain that are children of one of a number of given blocks, according to a preferential order with p_0 being the most prefered. If the designated parent is the present block chain head, an empty reply should be sent. If none of the parents are in the current canonical block chain, then a NotInChain message should be sent along with p_n , the least preferential parent. If no parents are passed, then a reply need not be made.

- p_0 , p_1 , ... are the SHA3 hashes of the parents of blocks that we should be informed of with a BLOCKS reply. Typically, these will be specified in increasing age (or decreasing block number).
- c is the number of children blocks of the most preferred parent that we should be informed of through the corresponding Blocks reply.

0x15 NotInChain

 $(0x15, p \in \mathbb{B}_{32})$

Inform the peer that a particular block was not found in its block chain.

• p is the SHA3 hash of the block that was not found in the block chain. Typically, this will be the least preferential (oldest) block hash given in a previous GETCHAIN message.

0x16 GetTransactions Transactions

(0x16)

Request the peer to send all transactions currently in the queue. See Transactions.

APPENDIX I. GENESIS BLOCK

The genesis block is 13 items, and is specified thus:

$$((0256, SHA3(RLP(())), 0160, stateRoot, 0, 222, 0, 0, 1000000, 0, 0, 0, SHA3((42))), (), ())$$

Where 0_{256} refers to the parent hash, a 256-bit hash which is all zeroes; 0_{160} refers to the coinbase address, a 160-bit hash which is all zeroes; 2^{22} refers to the difficulty; 0 refers to the timestamp (the Unix epoch); the transaction trie root and extradata are both 0, being equivalent to the empty byte array. The sequences of both uncles and transactions are empty and represented by (). SHA3((42)) refers to the SHA3 hash of a byte array of length one whose first and only byte is of value 42. SHA3(RLP(())) value refers to the hash of the uncle lists in RLP, both empty lists.

The proof-of-concept series include a development premine, making the state root hash some value *stateRoot*. The latest documentation should be consulted for the value of the state root.

APPENDIX J. JAVASCRIPT API

The JavaScript API provides a consistent API across multiple scenarios including each of the clients' web-based in-process DApp frameworks and the out-of-process RPC-based infrastructure. All key access takes places though the special eth object, part of the global namespace.

- J.1. Values. There are no special object types in the API; all values are strings. As strings, values may be of several forms, and are interpreted by the API according to a series of rules:
 - (1) If the string contains only digits from 0-9, then it is interpreted as a decimal integer;
 - (2) if the string begins with the characters 0x, then it is interpreted as a hexadecimal integer;
 - (3) it is interpreted as a binary string otherwise.

The only exception to this are for parameters that expect a binary string; in this case the string is always interpreted as such.

Values are implicitly converted between integers and hashes/byte-arrays; when this happens, integers are interpreted as big-endian as is standard for Ethereum. The following forms are allowed; they are all interpreted in the same way:

- (1) "4276803"
- (2) "0x414243"
- (3) "ABC"

In each case, they are interpreted as the number 4276803. The first two values may be alternated between with the additional String methods bin() and unbin().

As byte arrays, values may be concatenated with the + operator as is normal for strings.

Strings also have a number of additional methods to help with conversion and alignment when switching between addresses, 256-bit integers and free-form byte-arrays for transaction data:

- bin(): Converts the string to binary format.
- pad(1): Converts the string to binary format (ready for data parameters) and pads with zeroes until it is of width 1. Will pad to the left if the original string is numeric, or to the right if binary. If 1 is less than the width of the string, it is resized accordingly.
- pad(a, b): Converts the string to binary format (ready for data parameters) and pads with zeroes on the left size until it is of width a. Then pads with zeroes on the right side until it has grown to size b. If b is less hat the width of the string, it is resized accordingly.
- unbin(): Converts the string from binary format to hex format.
- unpad(): Converts the string from binary format to hex format, first removing any zeroes from the right side.
- dec(): Converts the string to decimal format (typically from hex).

J.2. The eth object.

- J.2.1. *Properties.* For each such item, there is also an asynchronous method, taking a parameter of the callback function, itself taking a single parameter of the property's return value and of the same name but prefixed with get and recapitalised, e.g. getCoinbase(fn).
 - coinbase Returns the coinbase address of the client.
 - isListening Returns true if and only if the client is actively listening for network connections.
 - isMining Returns true if and only if the client is actively mining new blocks.
 - gasPrice Returns the client's present price of gas.
 - key Returns the special key-pair object corresponding to the preferred account owned by the client.
 - keys Returns a list of the special key-pair objects corresponding to all accounts owned by the client.
 - peerCount Returns the number of peers currently connected to the client.
- J.2.2. Synchronous Getters. For each such item, there is also an asynchronous method, taking an additional parameter of the callback function, itself taking a single parameter of the synchronous method's return value and of the same name but prefixed with get and recapitalised, e.g. getBalanceAt(a, fn).
 - balanceAt(a) Returns the balance of the account of address given by the address a.
 - storageAt(a, x) Returns the value in storage at position given by the number x of the account of address given by the address a.
 - txCountAt(a) Returns the number of transactions send from the account of address given by a.
 - isContractAt(a) Returns true if the account of address given by a has associated code.

J.2.3. Transactions.

- create(sec, xEndowment, bCode, xGas, xGasPrice, fn) Creates a new contract-creation transaction, given parameters:
 - sec, the secret-key for the sender;
 - xEndowment, the number equal to the account's endowment;
 - bCode, the binary string (byte array) of EVM-bytecode for the initialisation of the account;
 - xGas, the number equal to the amount of gas to purchase for the transaction (unused gas is refunded);
 - xGasPrice, the number equal to the price of gas for this transaction. Returns the special address object representing the new account; and

- fn, the callback function, called on completion of the transaction.
- transact(sec, xValue, aDest, bData, xGas, xGasPrice, fn) Creates a new message-call transaction, given parameters:
 - sec, the secret-key for the sender;
 - xValue, the value transferred for the transaction (in Wei);
 - aDest, the address representing the destination address of the message;
 - bData, the binary string (byte array), containing the associated data of the message;
 - xGas, the amount of gas to purchase for the transaction (unused gas is refunded);
 - xGasPrice, the price of gas for this transaction; and
 - fn, the callback function, called on completion of the transaction.

J.2.4. Events.

- watch(a, fn): Registers fn as a callback for whenever anything about the state of the account at address a changes, and also on the initial load.
- watch(a, x, fn): Registers fn as a callback for whenever the storage location x of the account at address a changes, and also on the initial load.
- newBlock(fn): Registers fn as a callback for whenever the state changes, and also on the initial load.

${\rm J.2.5.}\ Misc.$

• secretToAddress(a): Determines the address from the secret key a.