Problem Solving as Search

CS161

Prof. Guy Van den Broeck

What is search?

- Basic Al problem
- Long history, active topic
- Basis for games, SAT, advanced reasoning
- Used in many other fields
- UCLA plays key role in history of search ©

Graduate CS class offered by Prof. Korf

What is search?

Structure: Search 'engine'



- Sensitive to
 - problem formulation (today)
 - choice of strategy (next lectures)

Examples

- Puzzles
 - 8-puzzle
 - Missionaries and Cannibals
 - N-Queens
 - Crypto arithmetic
 - Rubik's cube
- Planning
 - Practical industry applications
 (e.g., Amazon delivery, Uber route and match, etc.)

How would you solve these?

Search Problem Formulation

- Common elements:
 - Initial state
 - Final/goal state or goal test/predicate
 - Actions
 - Transition model/successors
 - (Costs)
- <u>Task</u>: find sequence of actions to move from initial to goal state.
- Optimal solution has lowest cost

Search Problem Formulation

- Notions of state and action are not sharp!
- Design problem: art

Example: 8-puzzle?



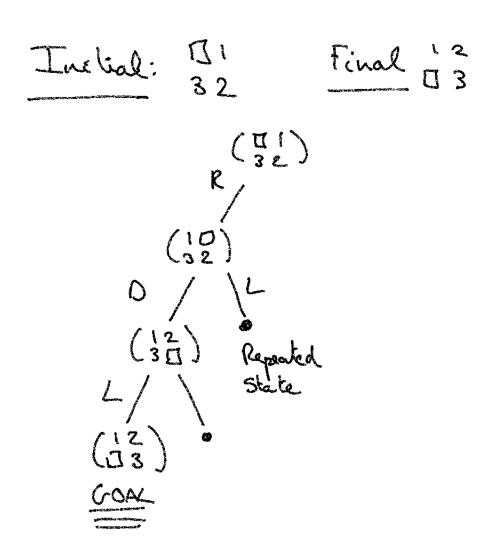
- States are atomic (no internal structure)
- States are discrete
- No percepts
- Deterministic transitions
- How many unique states? 9! = 362,880
 15! = 10^12
- Choice of action space is important
 - Move tile x up, down, left, right?
 - Move blank up, down, left, right?
 More elegant, fewer actions!
- Actions may not be applicable to all states

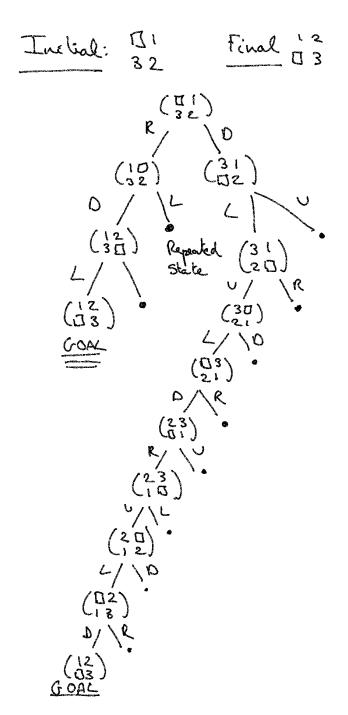
Search Trees

• Example: 8-puzzle?



- Some paths include the goal state
- Solving the search problem is finding such path
- Some paths are infinite (tree infinite)
- Beware: Repeated states
- Different solutions with different qualities
- Search space vs. search tree

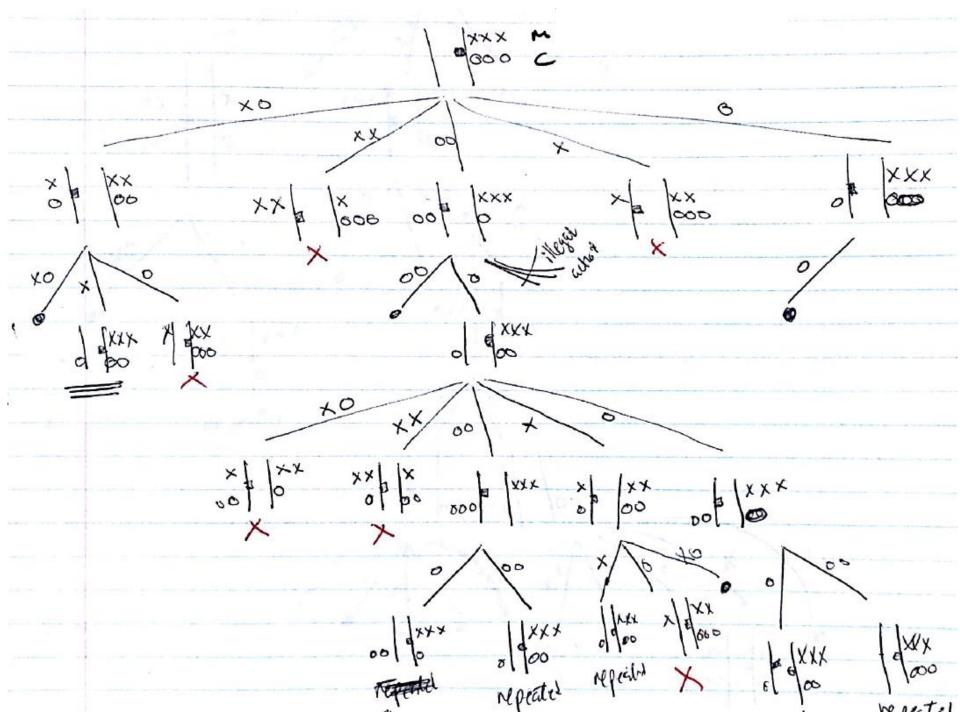


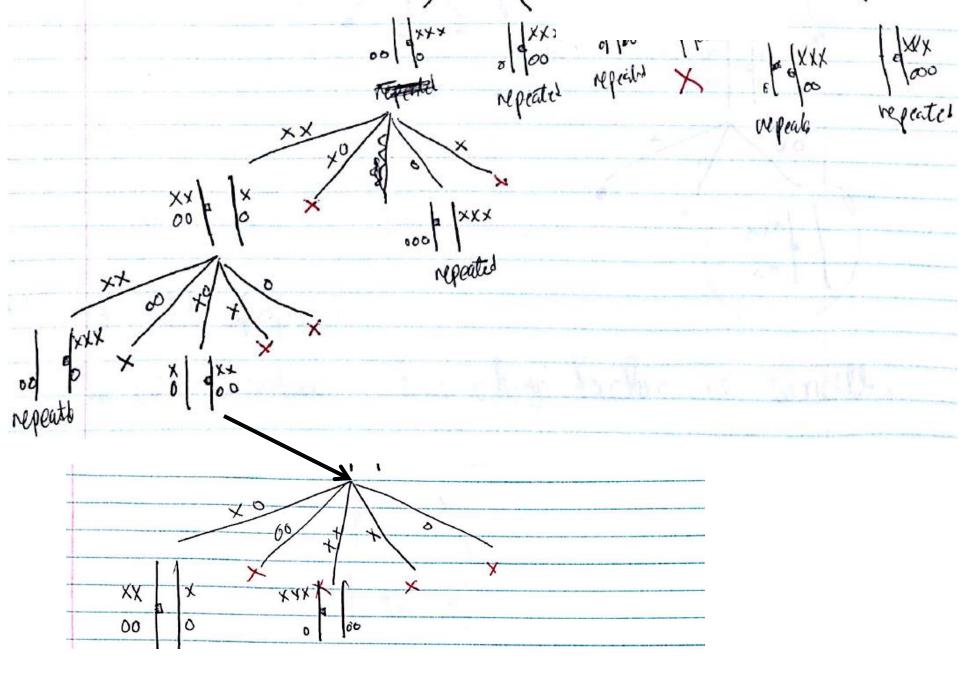


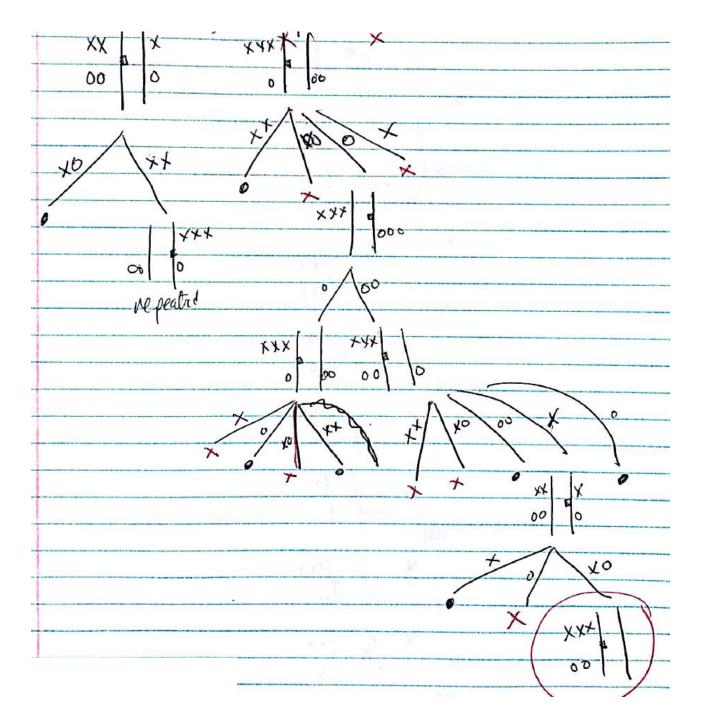
- Avoid repeated states or run into infinite loop
- Two solutions: cost 3 and cost 9
- Difficulty of problem: measured by parameters
 - Number of states
 - Branching factor
 - Solution depth
- 15-puzzle has 1.3 trillion states: few ms to solve
- 24-puzzle has 10^25 states: one day to solve
- Solving sliding block puzzles is NP-complete!

Example: Missionaries and Cannibals?

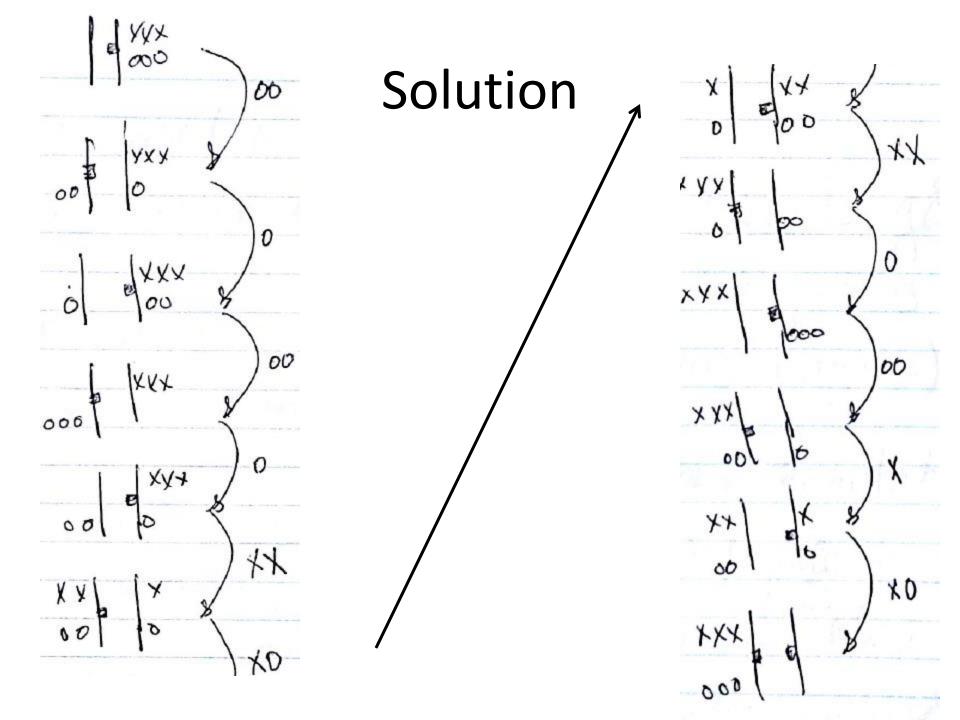








- Many choices for
 - State description
 - Actions
- Many correct, some better than others
- Find correct level of abstraction



• Example: 8-Queens?



- State formulation:
 - Incremental state
 - Complete state
- May or may not allow bad intermediate states
- No goal state => goal predicate
- Solution cost:
 - Incremental state: 8
 - Complete state: 0-8 (Can be solved in 0 moves!)

Example: Crypt-arithmetic?

FORTY	\longrightarrow	29786
TEN		850
TEN		850
+		+
SIXTY		31486



- Assign numbers to letters in fixed order (better: smallest number of remaining values)
- Incremental or complete state

- Example: Knut's Problem?
- Start: 4
- Actions
 - Factorial: x!
 - Sqrt: \sqrt{x}
 - Floor: |x|
- Transitions: math
- Goal: 5 => HOW?



- Conjecture:
 Any positive integer can be reached
- No bound on intermediate representation
- Infinite state space

- Example of class of problems: recursively defined objects
 - Circuits, proofs, programs, etc.

More Real-World Search Problems

Route finding

Amazon, computer networks, travel planning, airline planning, navigation systems

Traveling salesperson problems

Planning circuit board drill movements, mail delivery, street cleaning, etc.

What is a state?

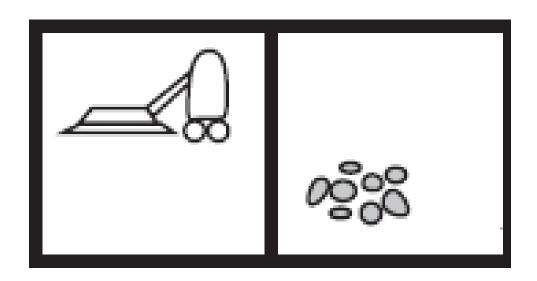
- Hardware layout
- Continuous robot navigation
- Scheduling
- Theorem proving

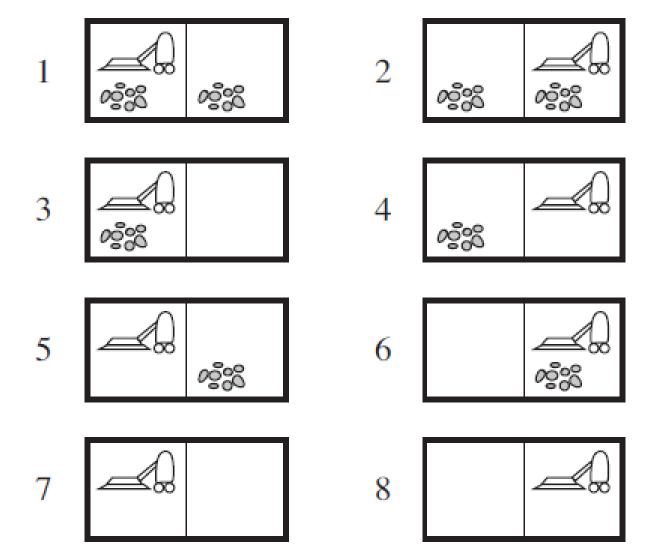
Extensions/Complications

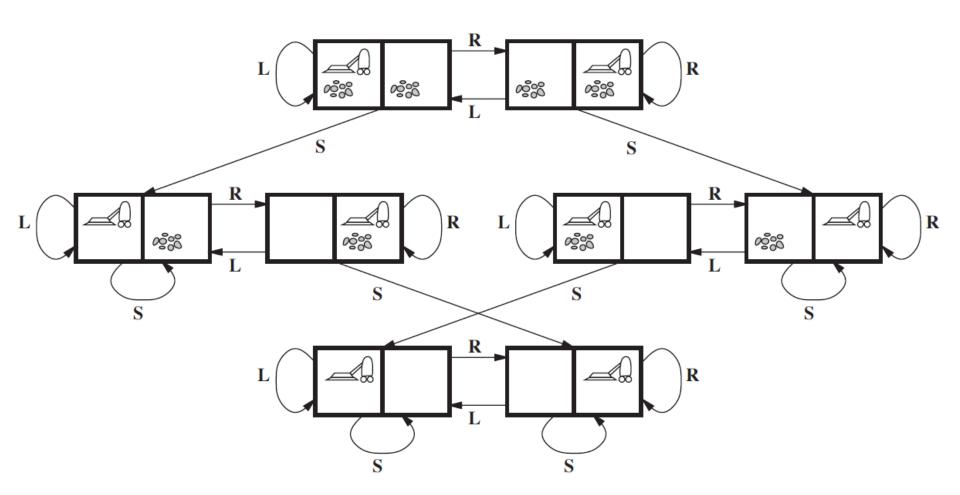
- Minimizing solution cost ('optimal solution')
 - Cost of solution is sum of action costs
- Note sure about effect of actions
 - Non-determinism (see probability later)
- Note sure about initial state

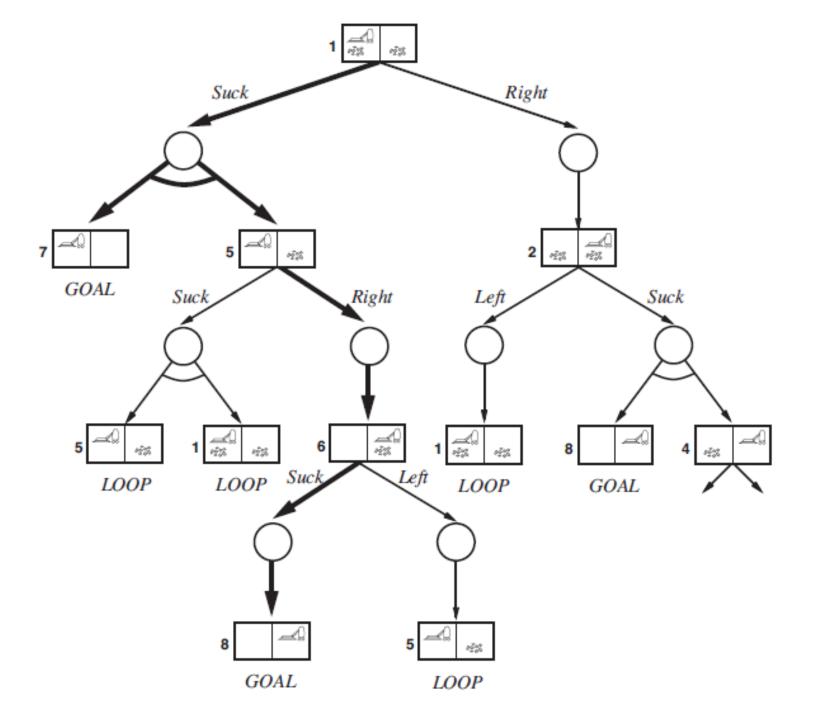
- Contingent planning: action based on sensing
- Conformant planning: plan without sensors
 Example: Not knowing initial state (see next)

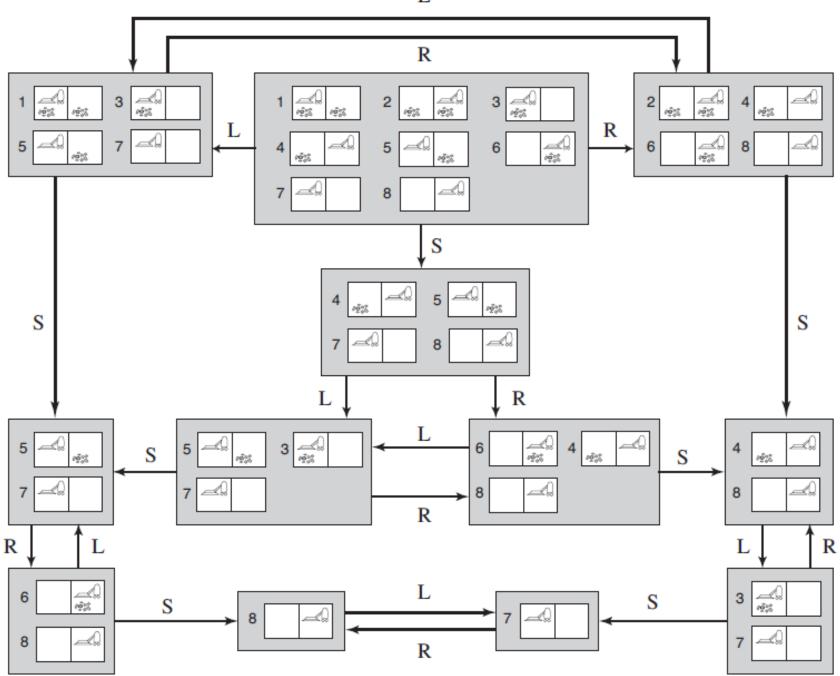
Vacuum Cleaner World











- When uncertain about initial state, use belief states.
- Belief state is a set of deterministic states