

1. (a) Neither

Smoke	Fire	Smoke \Rightarrow Fire	\neg Smoke \Rightarrow \neg Fire	(Smoke \Rightarrow Fire) \Rightarrow (\neg Smoke \Rightarrow \neg Fire)
T	T	T	T	T
T	F	F	T	T
F	T	T	F	F
F	F	T	T	T

(b) Neither

Smoke	Fire	Heat	Smoke \Rightarrow Fire	(Smoke \vee Heat) \Rightarrow Fire	(Smoke \Rightarrow Fire) \Rightarrow ((Smoke \vee Heat) \Rightarrow Fire)
T	T	T	T	T	T
T	T	F	T	T	T
T	F	T	F	F	T
T	F	F	F	F	T
F	T	T	T	T	T
F	T	F	T	T	T
F	F	T	T	F	F
F	F	F	T	T	T

(c) valid

Smoke	Fire	Heat	(Smoke \wedge Heat) \Rightarrow Fire	(Smoke \Rightarrow Fire) \vee (Heat \Rightarrow Fire)	((Smoke \vee Heat) \Rightarrow Fire) \Leftrightarrow ((Smoke \Rightarrow Fire) \vee (Heat \Rightarrow Fire))
T	T	T	T	T	T
T	T	F	T	T	T
T	F	T	F	F	T
T	F	F	T	T	T
F	T	T	T	T	T
F	T	F	T	T	T
F	F	T	T	T	F
F	F	F	T	T	T

2.

- a. mythical \Rightarrow immortal (S1)
 \neg mythical $\Rightarrow \neg$ immortal \wedge mammal (S2)
immortal \vee mammal \Rightarrow horned (S3)
horned \Rightarrow magical (S4)
- b. S1 = \neg mythical \vee immortal
S2 = mythical \vee (\neg immortal \wedge mammal) =
(\neg immortal \vee mythical) (S5)
 \wedge (mammal \vee mythical) (S6)
S3 = \neg (immortal \vee mammal) \vee horned =
(\neg immortal \vee horned) (S7)
 \wedge (\neg mammal \vee horned) (S8)
S4 = \neg horned \vee magical
- c. We are able to prove unicorn is horned and magical, but we are not able to prove the unicorn is mythical.

To prove horned, we add S9: \neg horned
 Resolve S9 with S7, giving: S10: \neg immortal
 Resolve S9 with S8, giving: S11: \neg mammal
 Resolve S11 with S6, giving: S12: mythical
 Resolve S12 with S1, giving: S13: immortal
 Resolve S10 with S13, empty clause.

To prove magical, we add S9: \neg magical
 Resolve S9 with S4, giving: S10: \neg horned
 Go through above procedure to get empty clause.

3.

- a. $\{x/A, y/B, z/B\}$
- b. It is not unifiable, because x cannot be substituted by both A and B
- c. $\{y/John, x/John\}$
- d. It is not unifiable

4.

- a. $A \ x \ (Food(x) \Rightarrow Likes(John, x))$
 $Food(Apples)$
 $Food(Chicken)$
 $A \ x \ A \ y \ (Eats(x, y) \ \& \ \neg Killed(x, y) \Rightarrow Food(y))$
 $A \ x \ (E \ y \ Killed(x, y)) \Rightarrow \neg Alive(x)$
 $Eats(Bill, Peanuts) \ \& \ Alive(Bill)$
 $A \ x \ Eats(Bill, x) \Rightarrow Eats(Sue, x)$
- b. $\neg Food(x) \mid Likes(John, x)$ (S1)
 $Food(Apples)$ (S2)
 $Food(Chicken)$ (S3)
 $\neg Eats(x, y) \mid Killed(x, y) \mid Food(y)$ (S4)
 $\neg Killed(x, y) \mid \neg Alive(x)$ (S5)
 $Eats(Bill, Peanuts)$ (S6)
 $Alive(Bill)$ (S7)
 $\neg Eats(Bill, x) \mid Eats(Sue, x)$ (S8)
- c. To prove John likes peanuts, we add S9: $\neg Likes(John, Peanuts)$
 Resolve S9 with S1 $\{x/Peanuts\}$, giving S10: $\neg Food(Peanuts)$
 Resolve S10 with S4 $\{y/Peanuts\}$, giving S11: $\neg Eats(x, Peanuts) \mid Killed(x, Peanuts)$
 Resolve S11 with S5 $\{y/Peanuts\}$, giving S12: $\neg Eats(x, Peanuts) \mid \neg Alive(x)$
 Resolve S7 with S12 $\{x/Bill\}$, giving S13: $\neg Eats(Bill, Peanuts)$
 Resolve S13 with S6, empty clause.
- d. To figure out “what food does Sue eat?” ($E \ x \ Food(x) \ \& \ Eats(Sue, x)$), we add its negation S9: $\neg Food(x) \mid \neg Eats(Sue, x)$
 Resolve S9 with S8, giving S10: $\neg Eats(Bill, x) \mid \neg Food(x)$
 Resolve S6 with S10 $\{x/Peanuts\}$, giving S11: $\neg Food(Peanuts)$

Go through the procedure in (c), getting an empty clause.
So, Sue eats Peanuts.

e. Now, we have:

-Food(x) Likes(John, x)		(S1)
Food(Apples)		(S2)
Food(Chicken)		(S3)
-Eats(x, y) Killed(x, y) Food(y)		(S4)
-Killed(x, y) -Alive(x)		(S5)
-Eats(Bill, x) Eats(Sue, x)		(S6)
$\forall x \forall y \neg \text{Eats}(x, y) \Rightarrow \text{Die}(x)$	=	$\text{Eats}(x, y) \text{Die}(x)$ (S7)
$\forall x \text{Die}(x) \Rightarrow \neg \text{Alive}(x)$	=	$\neg \text{Die}(x) \neg \text{Alive}(x)$ (S8)
Alive(Bill)		(S9)

We add S10: $\neg \text{Food}(z) | \neg \text{Eats}(\text{Sue}, z)$
 Resolve S10 with S6 $\{x/z\}$, giving S11: $\neg \text{Eats}(\text{Bill}, z) | \neg \text{Food}(z)$
 Resolve S11 with S7 $\{x/\text{Bill}, y/z\}$, giving S12: $\text{Die}(\text{Bill}) | \neg \text{Food}(z)$
 Resolve S12 with S8 $\{x/\text{Bill}\}$, giving S13: $\neg \text{Alive}(\text{Bill}) | \neg \text{Food}(z)$
 Resolve S13 with S9, giving S14: $\neg \text{Food}(z)$
 Resolve S14 with S4 $\{z/y\}$, giving S15: $\neg \text{Eats}(x, y) | \text{Killed}(x, y)$
 Resolve S15 with S5, giving S16: $\neg \text{Eats}(x, y) | \neg \text{Alive}(x)$
 Resolve S16 with S9 $\{x/\text{Bill}\}$, giving S17: $\neg \text{Eats}(\text{Bill}, y)$
 Resolve S17 with S7 $\{x/\text{Bill}\}$, giving S18: $\text{Die}(\text{Bill})$
 Resolve S18 with S8 $\{x/\text{Bill}\}$, giving S19: $\neg \text{Alive}(\text{Bill})$
 Resolve S19 with S9, empty clause.

So, Sue just eats everything Bill eats.