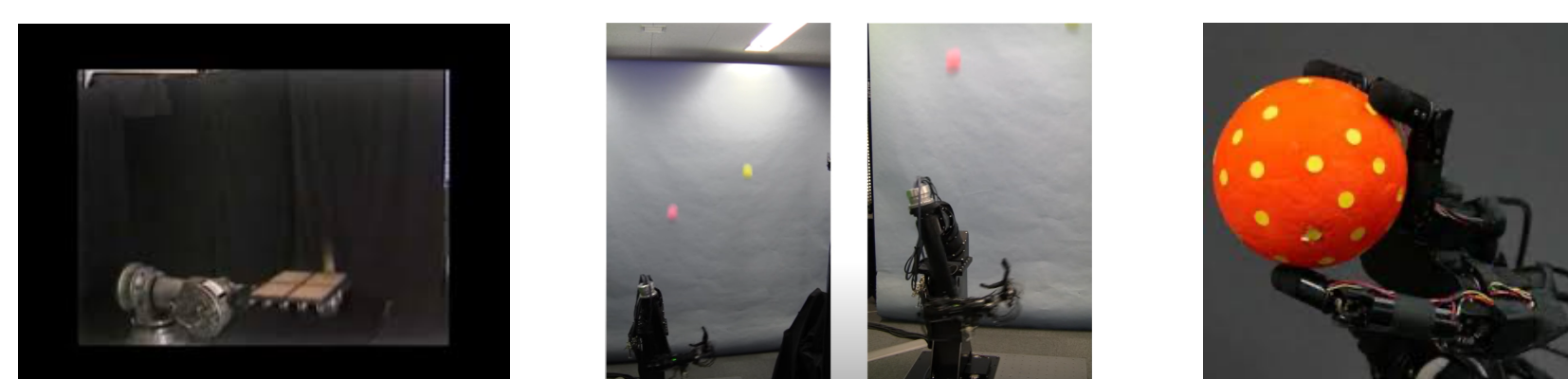


## Introduction

### A. Related Research



paddle juggling

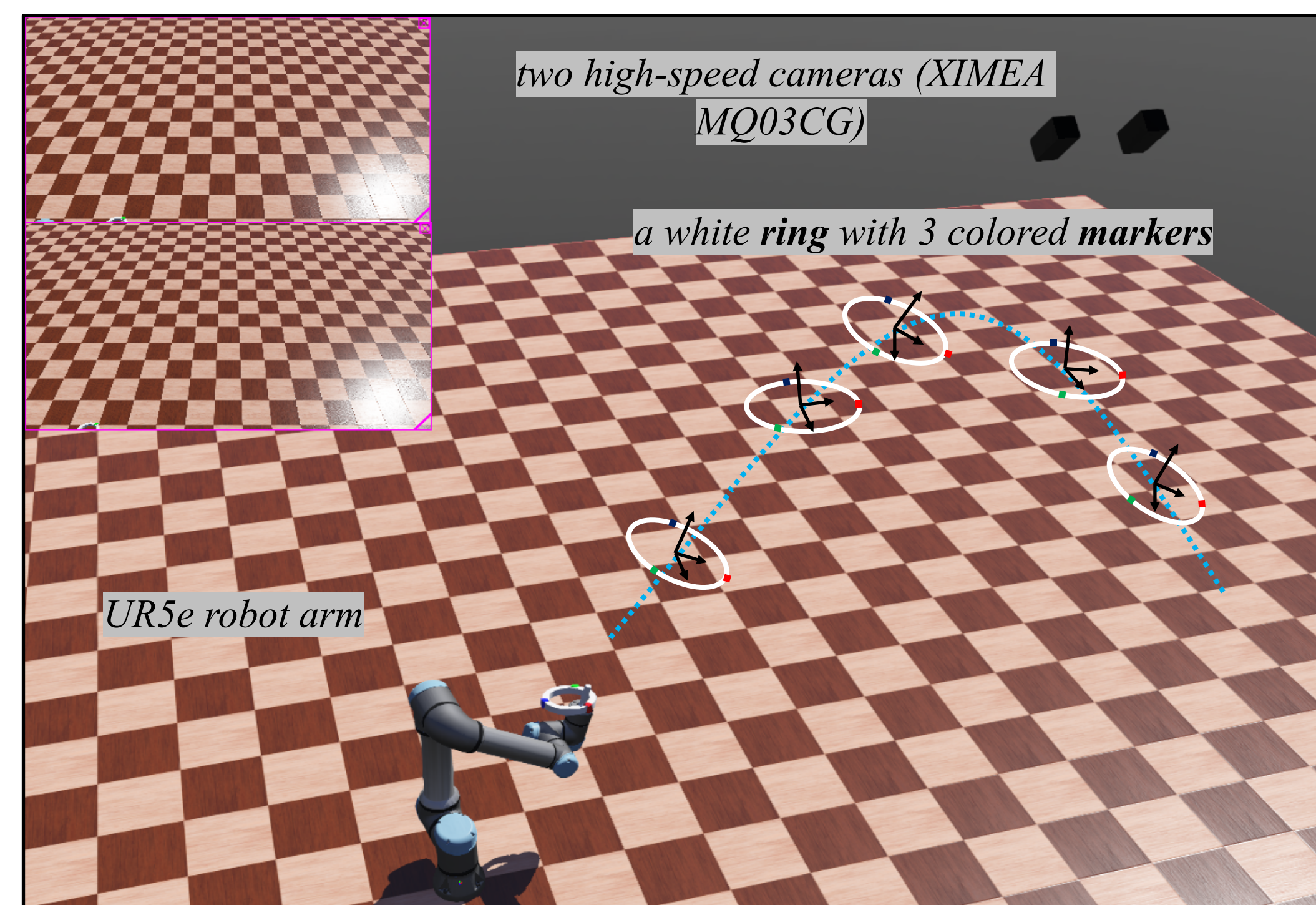
two ball juggling

ball catching

We want to challenge a larger universality and rapidity of object manipulation

### B. Task

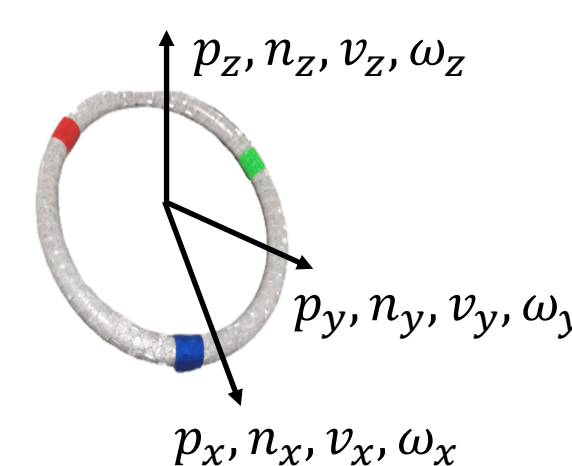
Catching of a Throwing Ring



### C. Challenge

#### Specialty of Ring:

- Position ( $p$ ) and Orientation ( $n$ ), SE(3)
- Linear velocity( $v$ ) and angular velocity( $\omega$ )
- Phenomena of **Nutation**

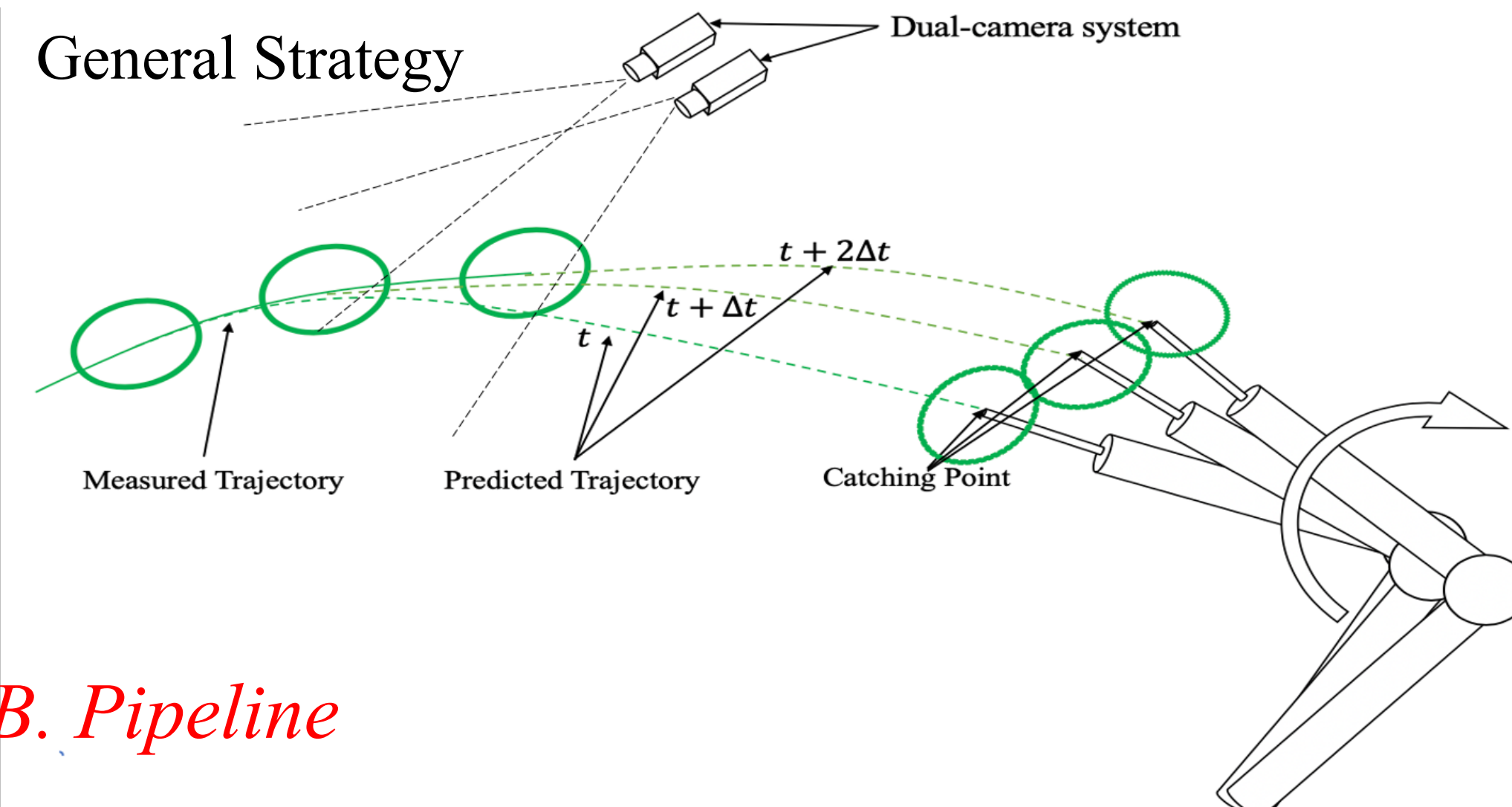


#### High Speed of Task:

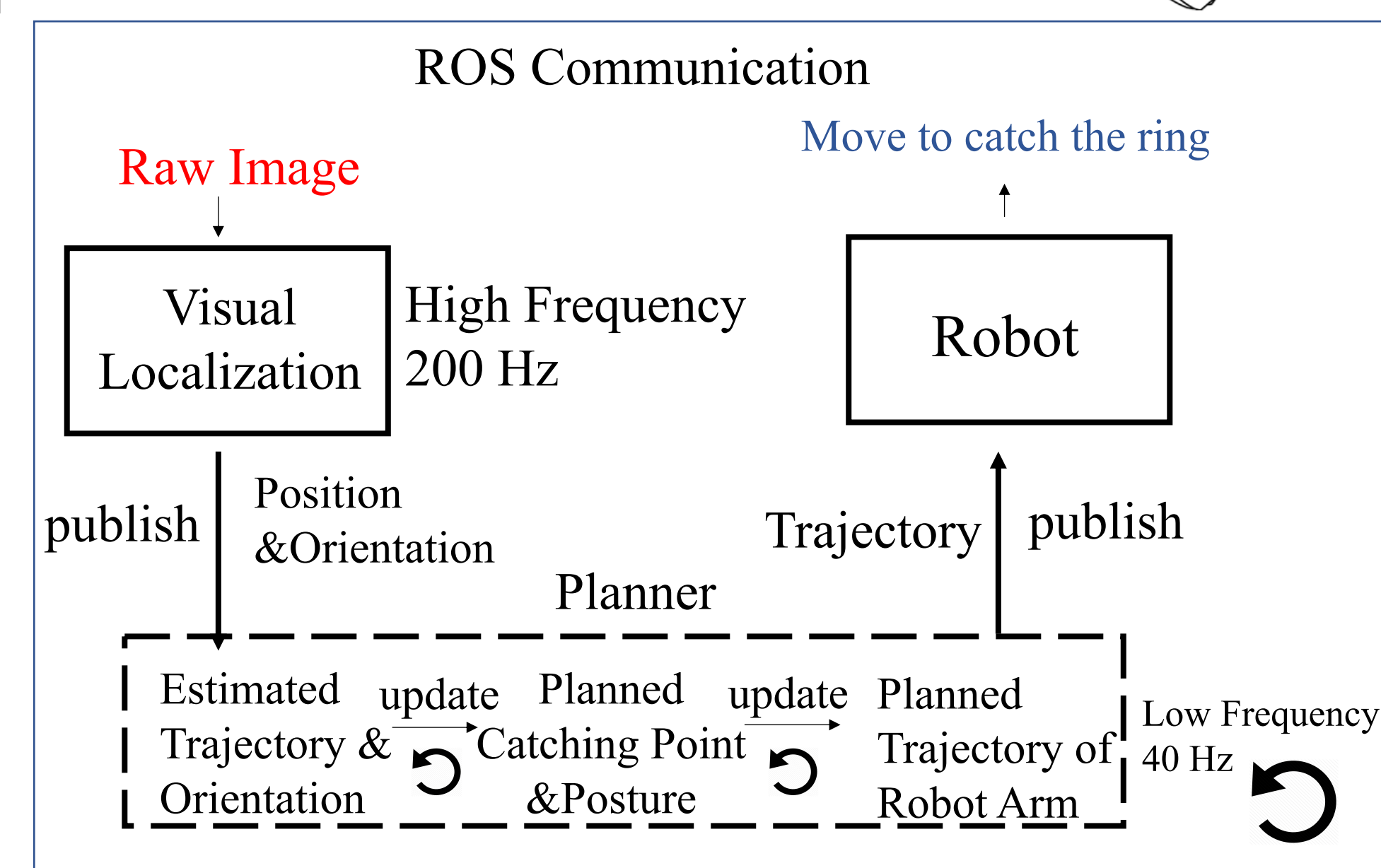
- Appearance duration in the view of camera is **less than 1 second**
- Preparation duration from appearing in view to catching is **less than 1.5 second**

## Methodology

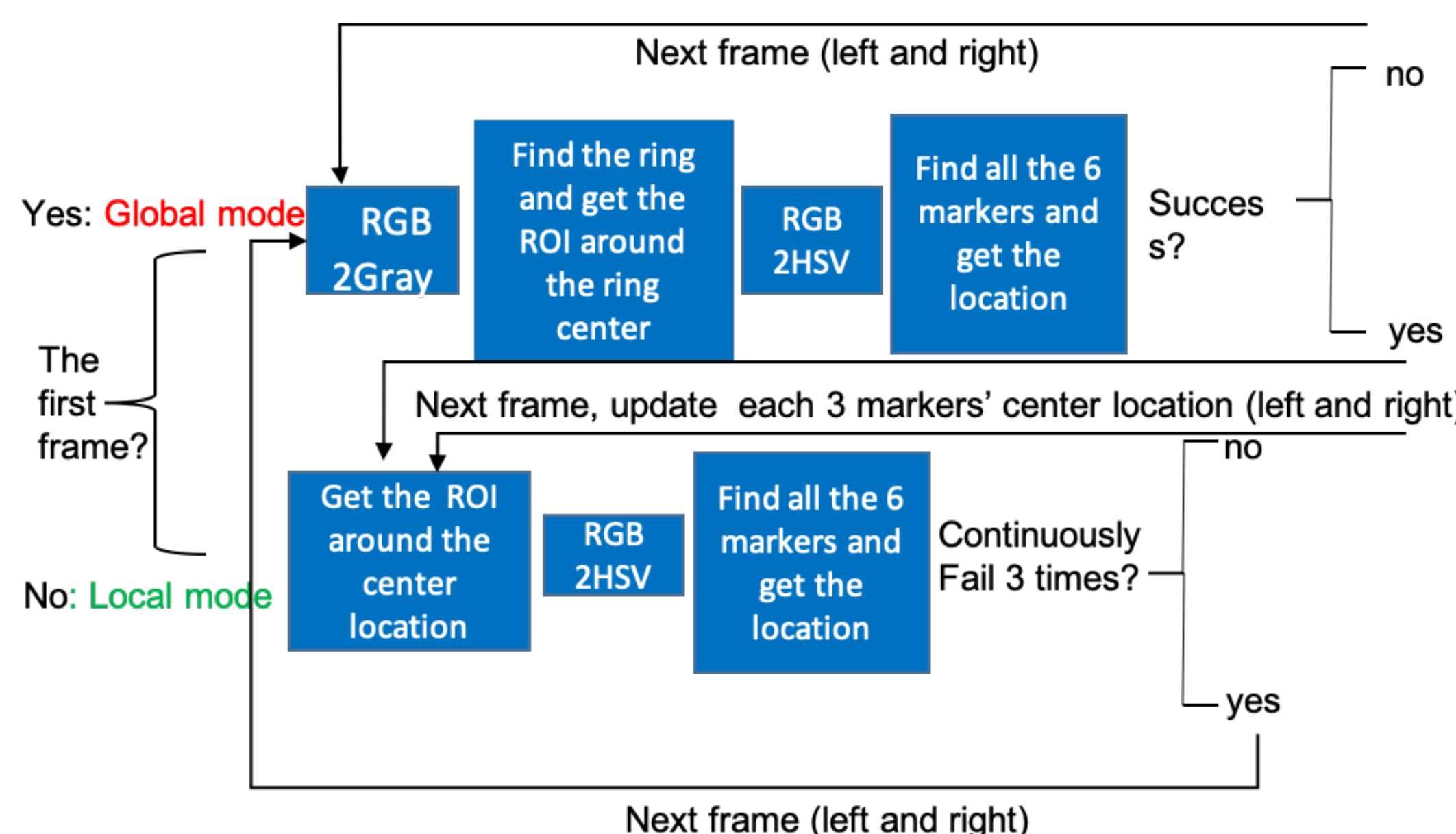
### A. Overall



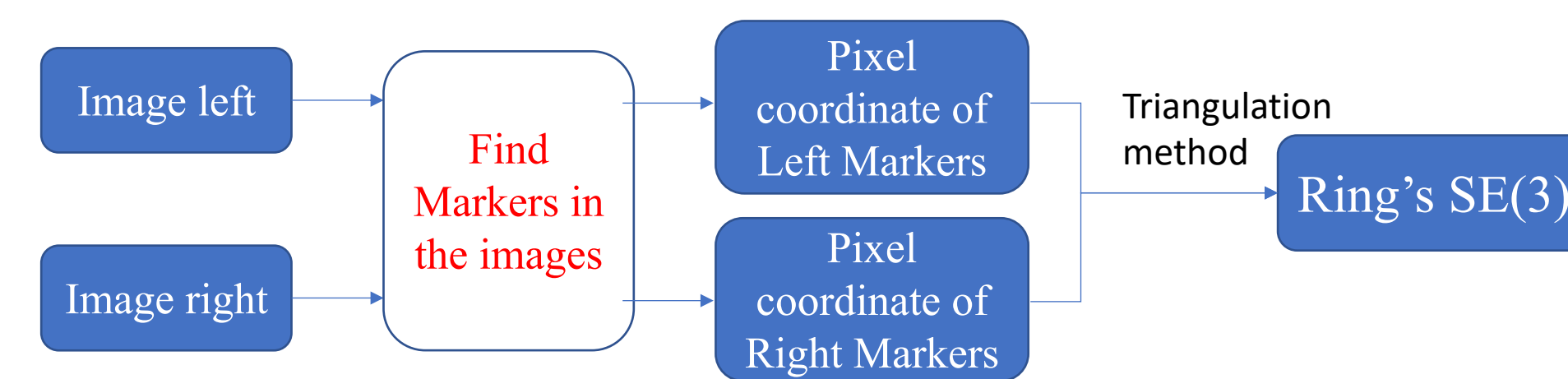
### B. Pipeline



### C. Visual Localization



## Methodology



Performance:

Speed: Global mode 50 Hz Local mode 200 Hz

Ratio of local mode: 97.1%

Successful rate of find all markers: 89.7%.

### D. Trajectory Prediction

Reason: Motion planning and execution needs time

Dynamics analysis

$$m \begin{bmatrix} \ddot{x} \\ \ddot{y} \\ \ddot{z} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ -mg \end{bmatrix} \Rightarrow \begin{aligned} x &= x_0 + v_x t \\ y &= y_0 + v_y t \\ z &= z_0 + v_z t - \frac{1}{2} g t^2 \end{aligned}$$

$$I \begin{bmatrix} \dot{p} \\ \dot{q} \\ \dot{r} \end{bmatrix} + \begin{bmatrix} p \\ q \\ r \end{bmatrix} \times I \begin{bmatrix} p \\ q \\ r \end{bmatrix} = 0$$

$$\begin{aligned} p &= p_0 \cos(r_0 t) + q_0 \sin(r_0 t) \\ q &= q_0 \cos(r_0 t) + p_0 \sin(r_0 t) \\ r &= r_0 \end{aligned}$$

(normal vector of ring)  $\vec{b}_3 = (n_1, n_2, n_3)$

Body-fixed Coordinates

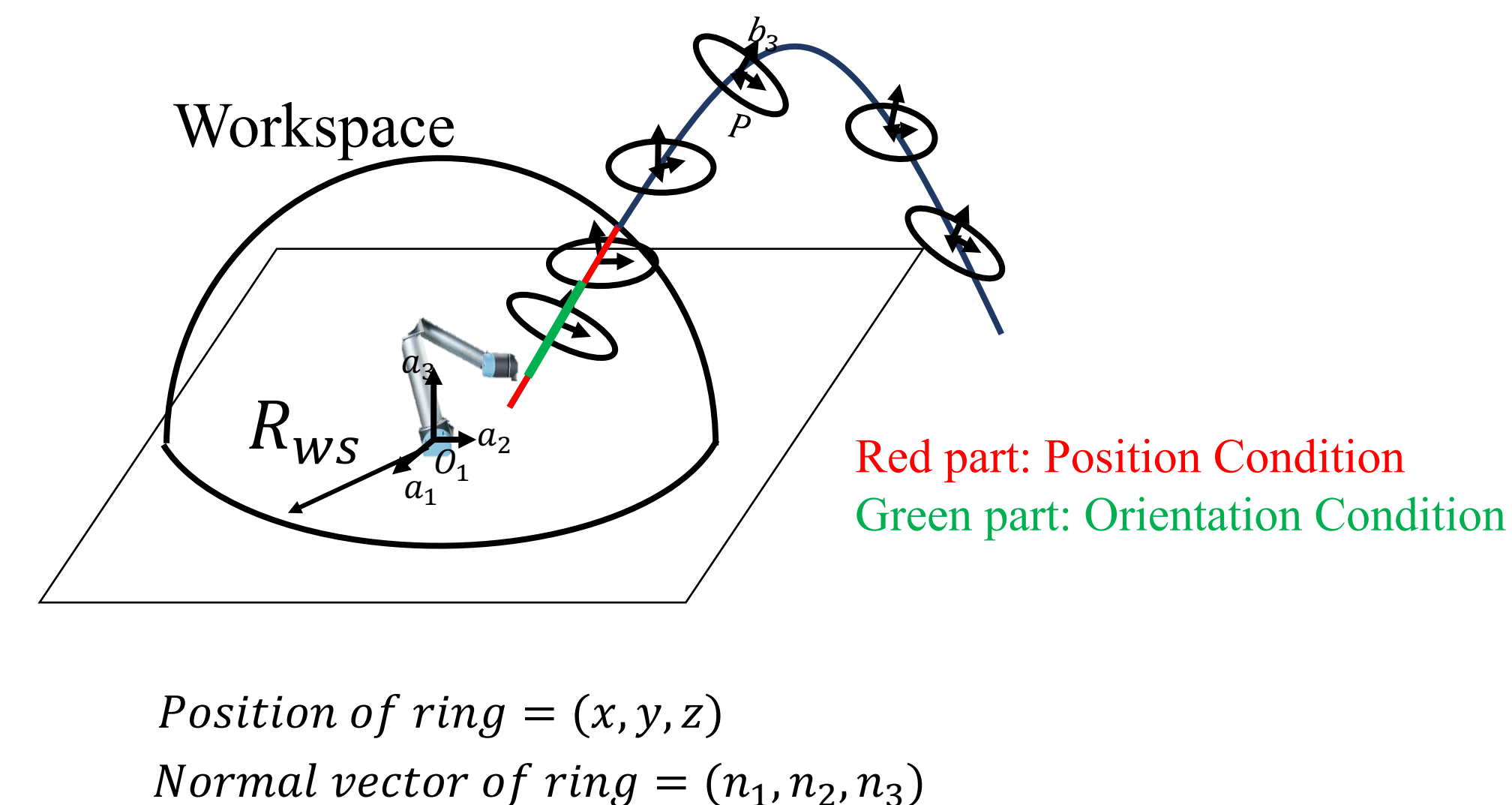
Trajectory Model:

$$\begin{aligned} x &= \theta_0 + \theta_1 t & n_1 &= \theta_7 \sin(\theta_8 t + \theta_9) \\ y &= \theta_2 + \theta_3 t & n_2 &= \theta_{10} \sin(\theta_{11} t + \theta_{12}) \\ z &= \theta_4 + \theta_5 t + \theta_6 t^2 & n_3 &= \theta_{13} \sin(\theta_{14} t + \theta_{15}) \end{aligned}$$

World Coordinates

To catch the ring, its position and its normal vector is considered

### E. Catching Point Planning

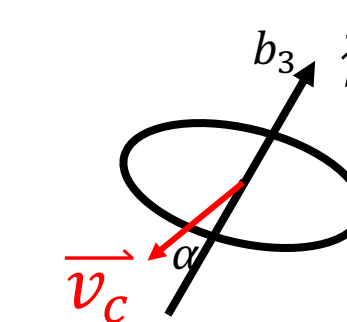


## Methodology

1. Position Condition:

$$P_{catch} \in Working Space$$

$$\begin{cases} (x - x_{robot})^2 + (y - y_{robot})^2 + (z - z_{robot})^2 < R_{ws}^2 \\ z > z_{robot} \end{cases}$$



2. Orientation Condition:

$$\langle \vec{v}_c, -\vec{b}_3 \rangle < \alpha_{threshold}$$

This condition guarantees the orientation of ring and its velocity is close.

## Experiment

Due to the COVID-19, we are sorry that we cannot conduct experiments in the laboratory. Instead, we conduct the experiment in the simulation.

View our demonstration at this website: <https://youtu.be/sY5x89v5OrQ>

