Les corrélations

Corrélation

$$\bar{x} = \left(\frac{1}{N}\right) \times \sum_{i=1}^{N} x_{i}$$

$$\sigma_{x} = \sqrt{\left(\frac{1}{N}\right) \times \sum_{i=1}^{N} \left(x_{i} - \bar{x}\right)^{2}}$$

$$\sigma_{xy} = \frac{1}{N} \times \sum_{i=1}^{N} \left[\left(x_{i} - \bar{x}\right) \cdot \left(y_{i} - \bar{y}\right)\right]$$

$$R_{xy} = \frac{\sigma_{xy}}{\left(\sigma_{x}\sigma_{y}\right)}$$

Auto-corrélation

n=décallage échantillons

$$C_{x}[n] = \sum_{m=0}^{M} x[m] \times x[m-n]$$

Inter-corrélation

$$C_{fg}(n) = \sum_{m=0}^{M} f(m) \times g(m-n)$$

Corrélation normalisée

$$C_{fg}(n) = \frac{\sum_{m=0}^{M} f(m) \times g(m-n)}{\sqrt{\sum_{m=0}^{M} f(m)^{2} \times \sum_{m=0}^{M} g(m)^{2}}}$$

Corrélation centrée

$$C_{fg}(n) = \sum_{m=0}^{M} [f(m) - \overline{f}] \times [g(m-n) - \overline{g}]$$

Corrélation normalisée centrée

$$C_{fg}(n) = \frac{\sum_{m=0}^{M} [f(m) - \bar{f}] \times [g(m-n) - \bar{g}]}{\sqrt{\sum_{m=0}^{M} [f(m) - \bar{f}]^2 \times \sum_{m=0}^{M} [g(m) - \bar{g}]^2}}$$

Les moyennes

Moyenne simple
$$m = \frac{1}{N} \times \sum_{i=0}^{N} x[i]$$

Moyenne à fenêtre glissante
$$m: \frac{Taille de la fenêtre}{2}$$

$$k: 2m+1$$

$$x_m[k] = \frac{1}{2m+1} \times \sum_{l=-m}^{m} x[k+l]$$