## Homework Assignment 2 Loss Functions and Support Vector Machines

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**1. Equivalence of negative log probability and logistic loss (10 points)** After replacing the label set from  $\{0,1\}$  to  $\{-1,1\}$ , we introduced the log loss

$$D_{\log}(y, \mathbf{x}; M) = \frac{1}{\log 2} \log(1 + \exp(-s(y, \mathbf{x}; M))),$$

as an alternative to the logistic regression distance function above. Show that these two are equivalent up to a constant multiplication for logistic regression.

**2. Hinge loss gradients (10 points)** Unlike the log loss, the hinge loss, defined below, is not differentiable everywhere:

$$D_{\text{hinge}}(y, \mathbf{x}; M) = \max(0, 1 - s(y, \mathbf{x}; M)).$$

Does it mean that we cannot use a gradient-based optimization algorithm for finding a solution that minimizes the hinge loss? If not, what can we do about it?

**3. Model Selection (20 points due to importance)** Consider that we are learning a logistic regression  $M^{(1)}$  and a perceptron  $M^{(2)}$ , and we have three dataset partitions: a training set  $D_{\text{train}}$ , a validation set  $D_{\text{val}}$ , and a test set  $D_{\text{test}}$ .

The two models are iteratively optimized on  $D_{\text{train}}$  over T steps, and now we have T logistic regression parameter configurations (i.e. weights and biases)  $M_1^{(1)}, M_2^{(1)}, \dots, M_T^{(1)}$  and T perceptron configurations  $M_1^{(2)}, M_2^{(2)}, \dots, M_T^{(2)}$ , all with different parameters. We now evaluate the expected cost for all the 2T models on training set, validation

We now evaluate the expected cost for all the 2T models on training set, validation set, and test set. So we have 6T quantities  $\tilde{R}_{\text{train},t}^{(i)}$ ,  $\tilde{R}_{\text{val},t}^{(i)}$ ,  $\tilde{R}_{\text{test},t}^{(i)}$  where i=1,2 and  $t=1,\ldots,T$ .

- (a) Which i and t should we pick as the best model? (10 points)
- (b) How should we report the generalization error? (10 points)

**4. Image Recovery & Numerical Stability (20 points)** Please download https: //github.com/nyu-dl/Intro\_to\_ML\_Lecture\_Note/blob/master/homeworks/hw2.ipynb and follow its instructions.