

FunSearch & AlphaEvolve

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The Reasoning Reading Group @ FAIR

Motivation

Preconditions:

- A problem of finding optimal heuristic/program.
- A pre-trained, coding-capable LLM.
- An automated evaluator returning a scalar score.

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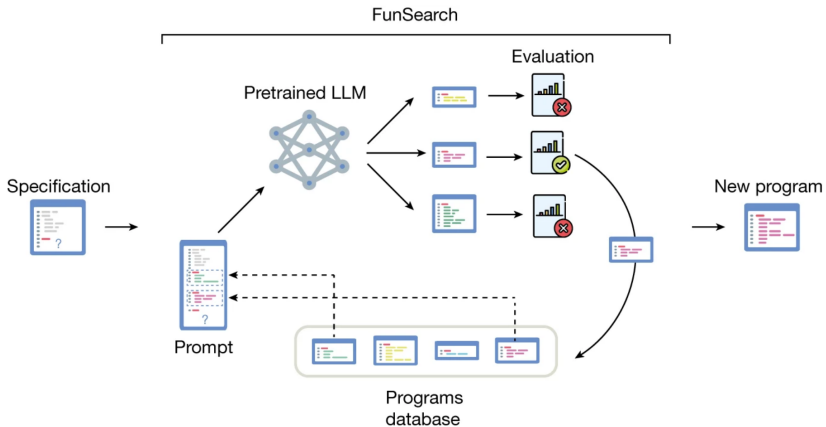
But instead of sampling independently, can we **incorporate the evaluator feedback** into subsequent generations?

FunSearch

Key ingredients:

- *best-shot* prompting,
- a growing database of programs,
- an evolutionary strategy acting on it.

FunSearch



Database of programs

- Several island/subpopulations growing independently.
- Higher-scoring programs, but also shorter ones, are prioritized.

Best-shot prompting

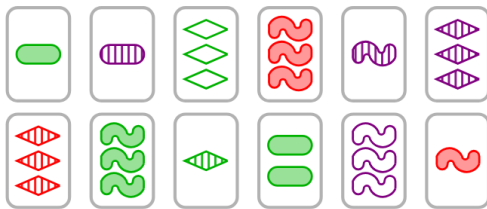
- k good programs per prompt sampled, for each island.
- Information which one is better incorporated into the prompt.

Cap set problem

What is the the largest possible set of vectors in \mathbb{Z}_3^n (*cap set*) such that no three vectors sum to zero?

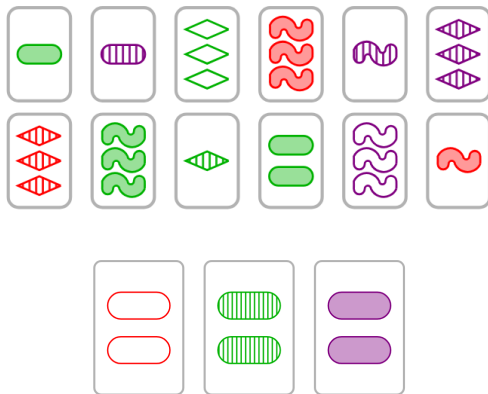
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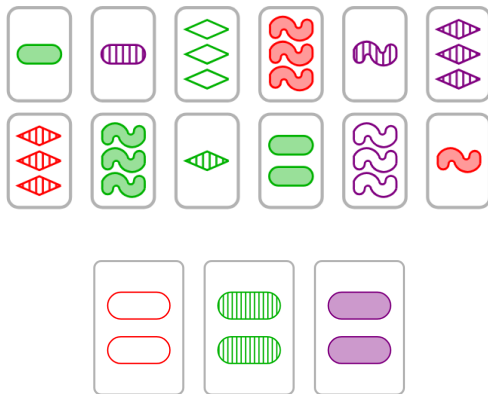
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n	3	4	5	6	7	8
Best known	9	20	45	112	236	496
FunSearch	9	20	45	112	236	512

Cap set solution template

```
"""Finds large cap sets."""
import numpy as np
import utils_capset

# Function to be executed by FunSearch.
def main(n):
    """Runs `solve` on `n`-dimensional cap set and
    ↳ evaluates the output."""
    solution = solve(n)
    return evaluate(solution, n)

def evaluate(candidate_set, n):
    """Returns size of candidate_set if it is a cap
    ↳ set, None otherwise."""
    if utils_capset.is_capset(candidate_set, n):
        return len(candidate_set)
    else:
        return None

def solve(n):
    """Builds a cap set of dimension `n` using
    ↳ `priority` function."""
    # Precompute all priority scores.
    elements = utils_capset.get_all_elements(n)
    scores = [priority(el, n) for el in elements]
    # Sort elements according to the scores.
    elements = elements[np.argsort(scores,
    ↳ kind='stable')[:-1]]

    # Build `capset` greedily, using scores for
    ↳ prioritization.
    capset = []
    for element in elements:
        if utils_capset.can_be_added(element, capset):
            capset.append(element)
    return capset

# Function to be evolved by FunSearch.
def priority(element, n):
    """Returns the priority with which we want to add
    ↳ `element` to the cap set."""
    return 0.0
```

Cap set solution (priority function)

```
def priority(el: tuple[int,...],  
↳ n: int) -> float:  
    score = n  
    in_el = 0  
    el_count = el.count(0)  
  
    if el_count == 0:  
        score += n**2  
        if el[1] == el[-1]:  
            score *= 1.5  
        if el[2] == el[-2]:  
            score *= 1.5  
        if el[3] == el[-3]:  
            score *= 1.5  
    else:  
        if el[1] == el[-1]:  
            score *= 0.5  
        if el[2] == el[-2]:  
            score *= 0.5  
  
    for e in el:  
        if e == 0:  
            if in_el == 0:  
                score *= n * 0.5  
            elif in_el == el_count - 1:  
                score *= 0.5  
            else:  
                score *= n * 0.5 ** in_el
```

AlphaEvolve

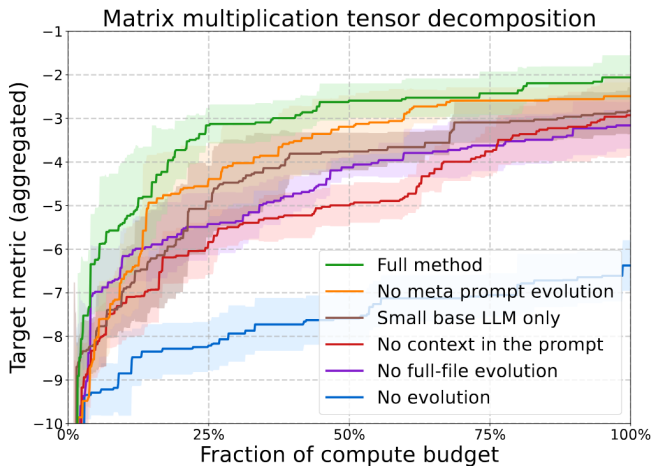
tldr: FunSearch scaled-up in multiple dimensions.

<i>FunSearch</i> [83]	<i>AlphaEvolve</i>
evolves single function	evolves entire code file
evolves up to 10-20 lines of code	evolves up to hundreds of lines of code
evolves code in Python	evolves any language
needs fast evaluation (≤ 20 min on 1 CPU)	can evaluate for hours, in parallel, on accelerators
millions of LLM samples used	thousands of LLM samples suffice
small LLMs used; no benefit from larger	benefits from SOTA LLMs
minimal context (only previous solutions)	rich context and feedback in prompts
optimizes single metric	can simultaneously optimize multiple metrics

Optimizong matrix multiplications

$\langle m, n, p \rangle$	best known [reference]	<i>AlphaEvolve</i>
$\langle 2, 4, 5 \rangle$	33 [42]	32
$\langle 2, 4, 7 \rangle$	46 [93]	45
$\langle 2, 4, 8 \rangle$	52 [93]	51
$\langle 2, 5, 6 \rangle$	48 [93]	47
$\langle 3, 3, 3 \rangle$	23 [52]	23
$\langle 3, 4, 6 \rangle$	56 [48]	54
$\langle 3, 4, 7 \rangle$	66 [91]	63
$\langle 3, 4, 8 \rangle$	75 [91]	74
$\langle 3, 5, 6 \rangle$	70 [48]	68
$\langle 3, 5, 7 \rangle$	82 [91]	80
$\langle 4, 4, 4 \rangle$	49 [95]	48
$\langle 4, 4, 5 \rangle$	62 [47]	61
$\langle 4, 4, 7 \rangle$	87 [93]	85
$\langle 4, 4, 8 \rangle$	98 [95]	96
$\langle 4, 5, 6 \rangle$	93 [48]	90
$\langle 5, 5, 5 \rangle$	93 [72]	93

Ablations



Closing remarks

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