

Bashundhara
Exercise Book
Write Your Future

Digital Image Processing(CSE -4245)
Naima Islam Nodi SMS

Ref. Book :

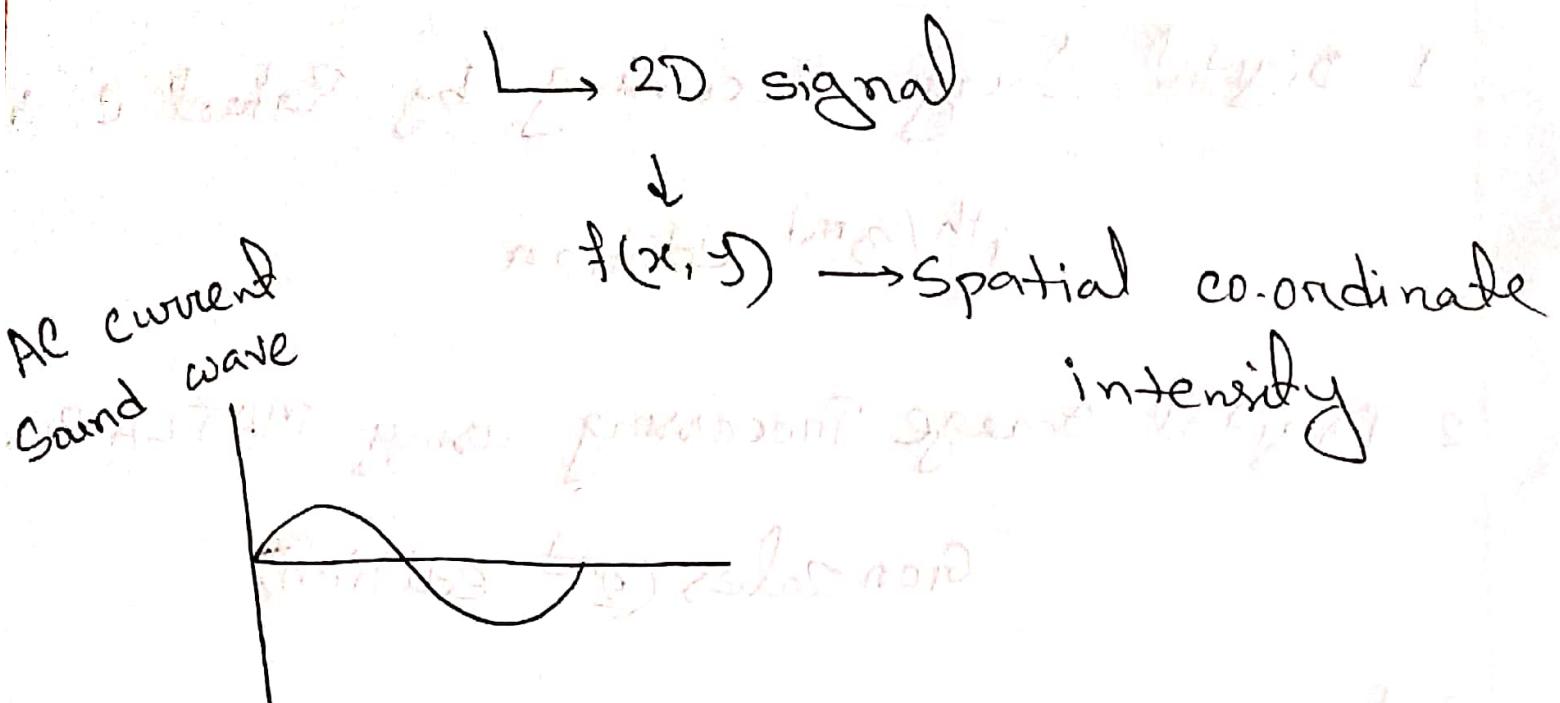
Image Processing

1. Digital Image Processing by Rafael C. Gonzales
4th / 3rd edition
2. Digital Image Processing using MATLAB,
Gonzales (2nd edition)
3. Image Processing using Python, web reference.
to apply something on image

Objectives:

1. Explain how digital images are represented & manipulated in a computer.
2. Mathematical description of image processing techniques & algorithms.

Digital image



pixel → picture element

1 bit → 0 } Representation

Gray Scale Image:



Color image: → RGB

→
Different
Intensity value.

Source of Image:

Digital camera

X-Ray

Painting

Computer Vision

AI

ML

* Image Processing:

Image enhancement

Image filtering

Special Domain filtering

Frequency

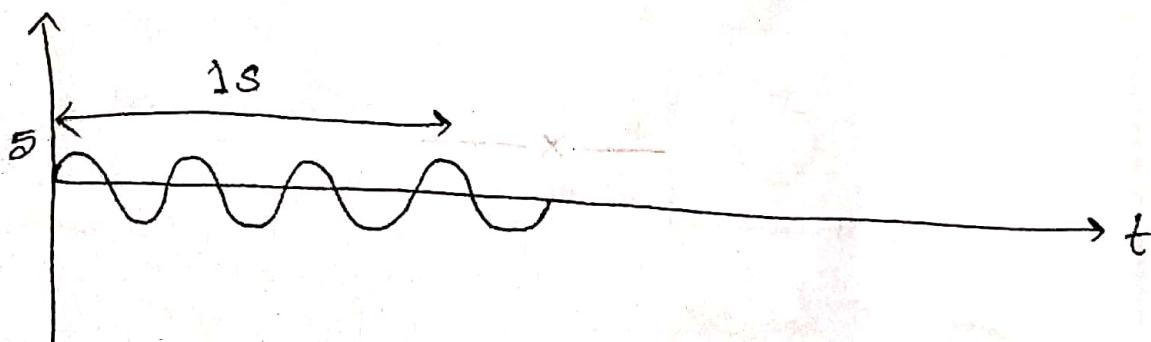
Image Restoration

Image compression

Image Segmentation

Morphological Analysis

Object Recognition



Time Domain Representation

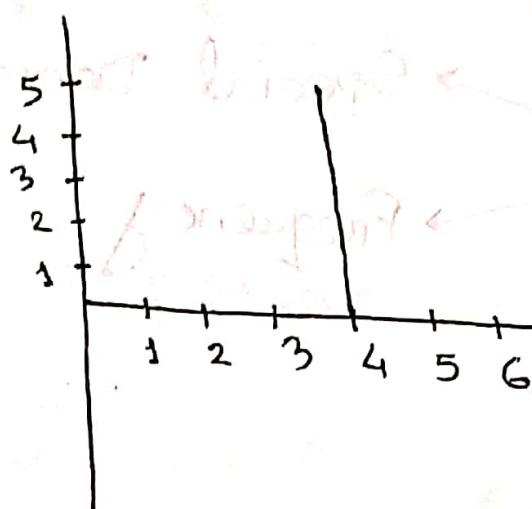
$$s(t) = A \sin(\omega t + \phi)$$

Amplitude

Angular Frequency

Phase Angle

$$f = \frac{1}{T} = \frac{1}{4} = 0.25 \text{ Hz}$$



Frequency Domain

Representation

$$\text{if } T = 0.25$$

$$\text{then, } f = \frac{1}{0.25}$$

$$= 4 \text{ Hz}$$

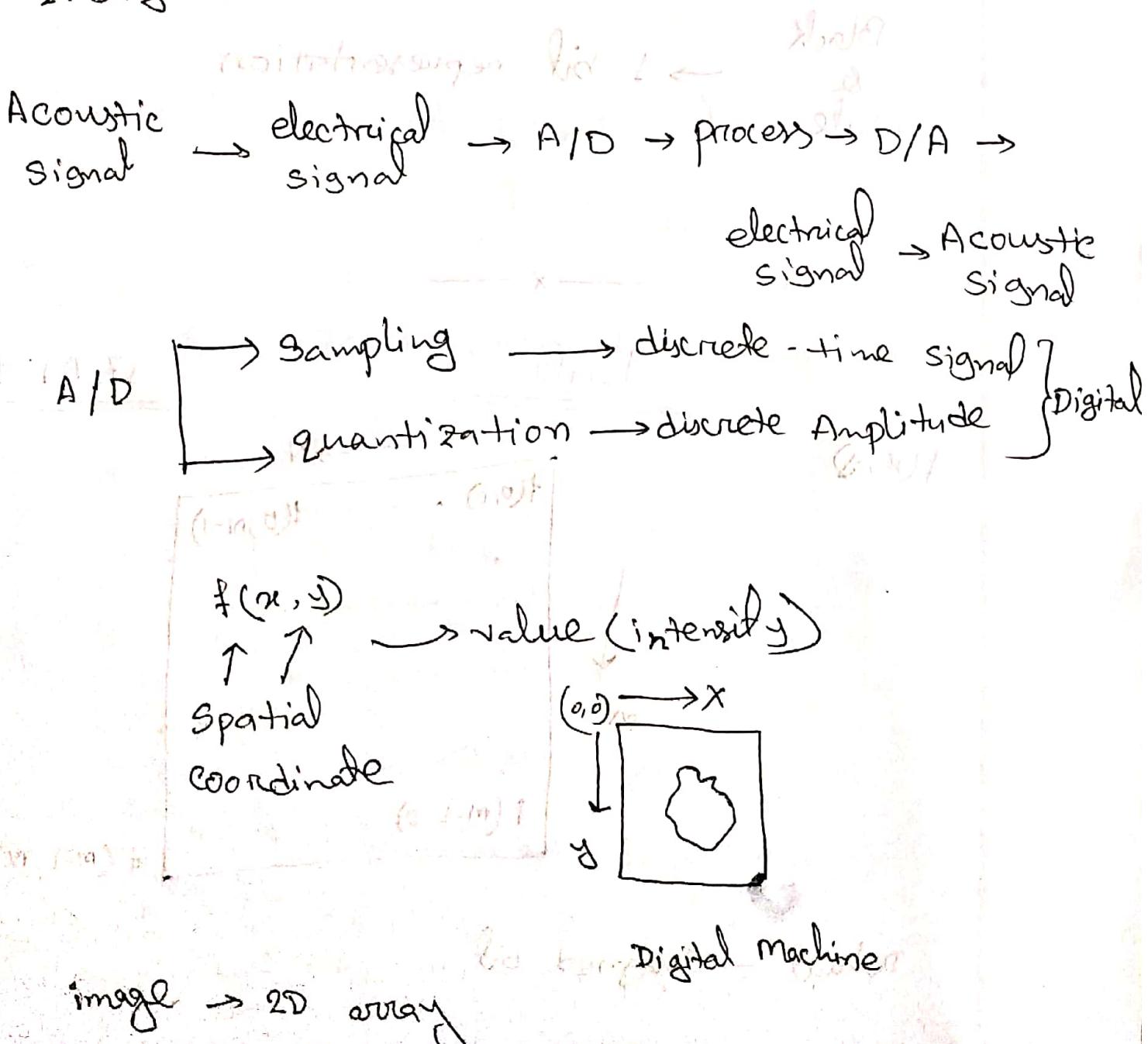
16.01.19.

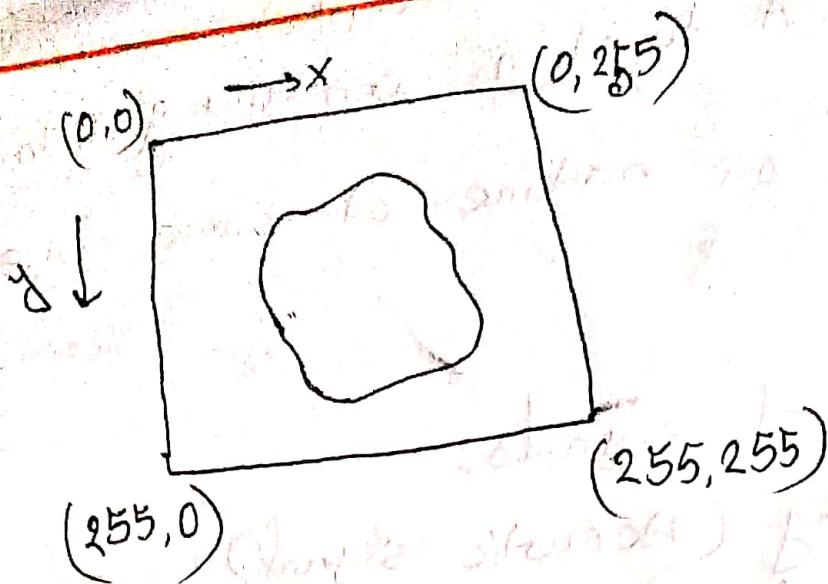
$$x(t) \quad x(t_1, t_2)$$

Signals: A function containing information about the behavior or nature of some phenomenon of interest.

2 types of signals:

- 1. Analog (Acoustic signal)
- 2. Digital



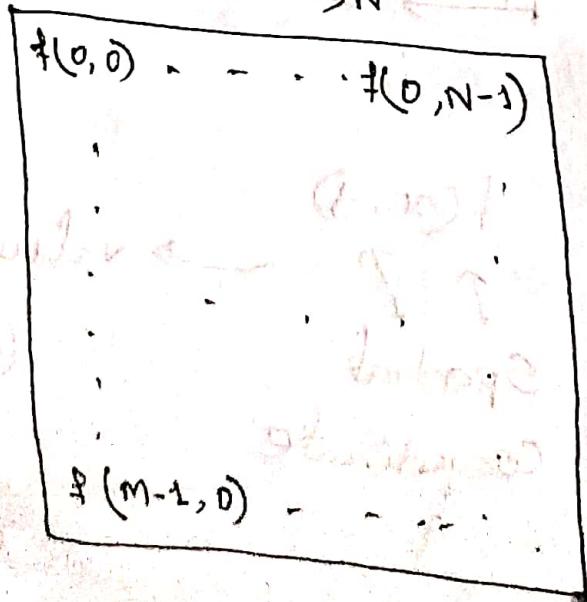


Black & white → 1 bit representation

— x —

17.01.19

$f(x, y)$



Default → Unsigned int

$I = \text{imread}('my.png');$

$I = 272 \times 394 \times 3$

$I = \text{imread}('my.png')$

$K = 272 \times 394$

$\text{subplot}(2, 1, 1);$

$\text{imshow}(I);$

$\text{subplot}(2, 1, 2);$

$K = \text{rgb2gray}(I);$

$\text{imshow}(K);$

Command window

help imread

$\text{Subplot}(2, 1, 1)$

row col

$\text{Subplot}(2, 2, 1)$

1	2	3	4
row	col		

row all col.

$P = K(3, :)$

all row

$q = K(:, 2)$

col.

$r = K(2, 3)$

row col.

Agenda:

1. Introduction
2. Project plan.

Image transformation, 5, 6

Challenges:

1. Identity (detection)
2. Gender / age / Profile identification
3. Representation
4. Freshness Detection

1200 dpi (dot per inch)

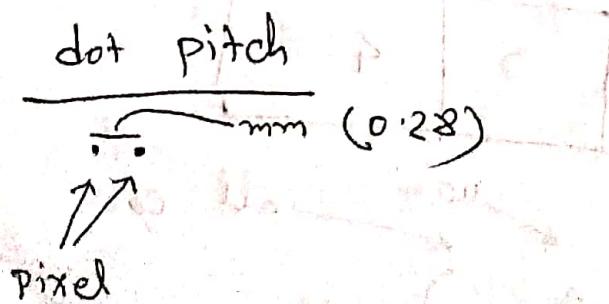
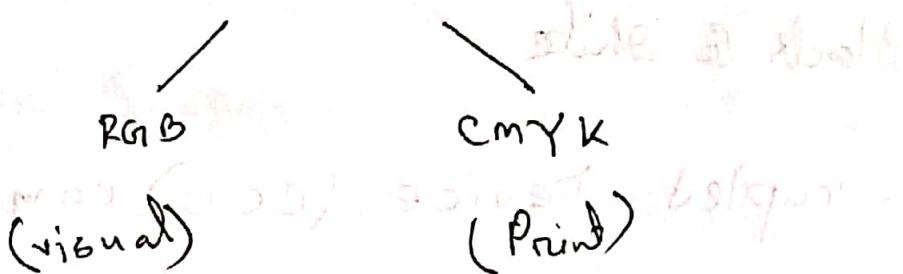
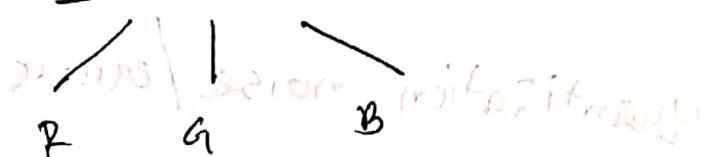


Image compression

Color Scheme



Color TV



3 electron gun

Project 3D object

Image formation:

1. Geometry of image formation.

2. Physics of light

$$v = n \lambda$$

$$\Rightarrow \lambda = \frac{v}{n}$$

AR

→ Augmented reality

* Image acquisition & manipulation.

* Monochromatic images

Black & White

Charged - coupled Device (CCD) cameras

Frame Grabber

Image digitization

quantization noise / error.

Image file formats

PGM format

*

Project list :

1. Facial expression recognition
2. Visual detection of autonomous driving
3. System Based on deep learning
4. Traffic signs recognition
5. Target stealth
6. Gait Analysis
7. A study on Image segmentation
8. Activity Recognition
9. Eye-tracking & gaze capture

Sigmoid

21.01.19.

Classification of Images:

Reflection Images → scattered & diffused

Emission Images → emitted by atoms/molecules

Absorption Images → absorb & scatter

Electromagnetic (EM) energy spectrum:

Conventional X-ray → Tomography

CT-Scan

PET (Positron Emission Tomography)

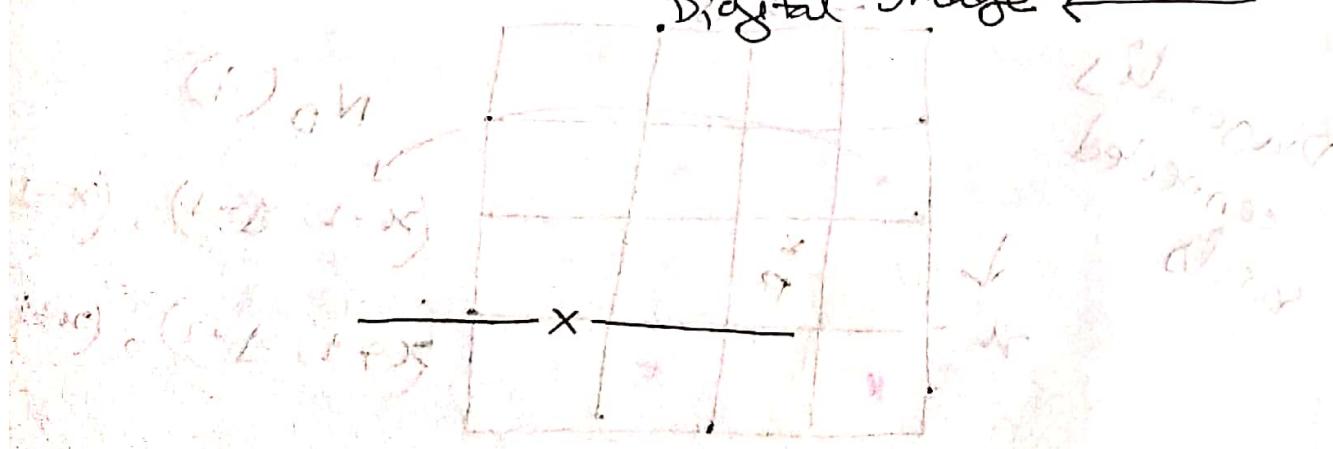
Position, Emission, Tomography

Image acquisition Process:

Scenes → Electromagnetic

Scenes → element → Imaging system → Image Plan

Digital Image ←



Digital Image:

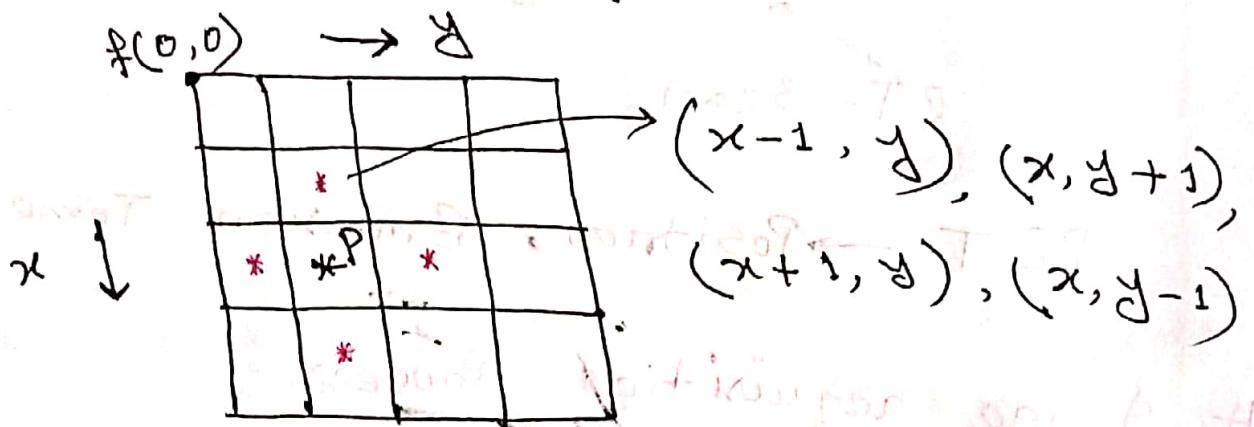
Sampling → Discretize co-ordinates in 2D array.

Quantization → Discretize amplitude or intensity

pixel → smallest picture element. value.

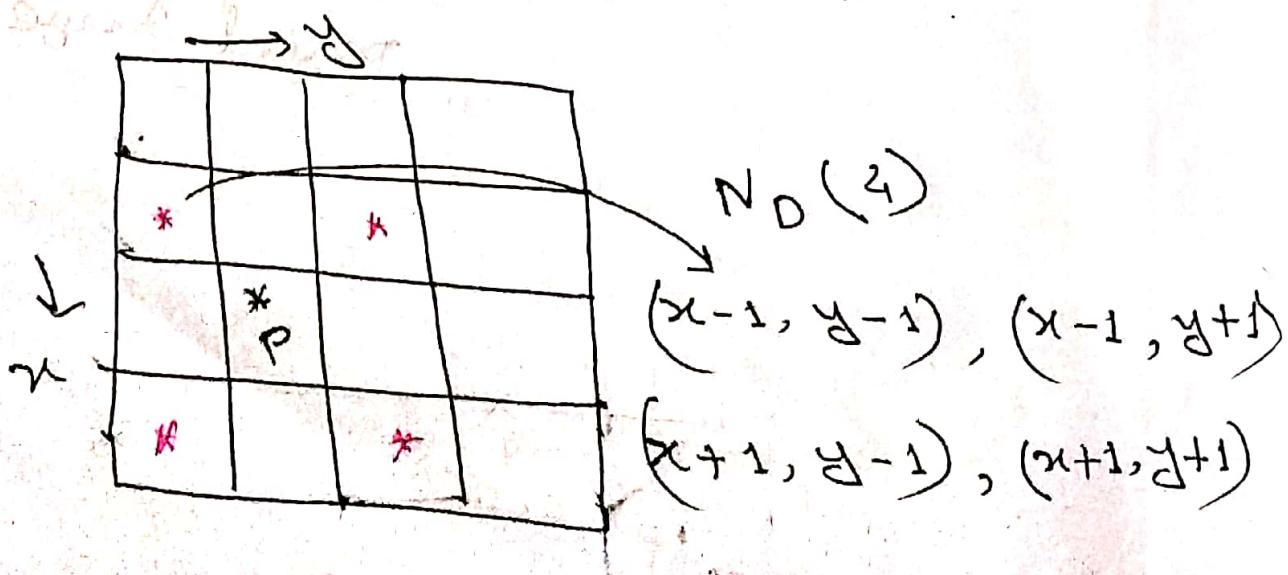
Basic Relationship between pixel:

* Neighbors of a pixel (4 Neighbors) $\rightarrow N_4(p)$



→ Horizontally & vertically connected pixels.

diagonally connected pixels



8-Neighbors:

$$N_8(P)$$

$$N_4(P) + N_D(P)$$

$N_8(P) = 8$

Adjacency:

1. 4-adjacency:

(Depends on intensity value)

0	1	1
0	P	0
0	0	1

$$V = \{1\}$$

This pixel is the only 4-adjacent of P.

* To be 4-adjacency, the pixel value should exist in set and must be a 4-neighbor.

1. Two pixel p & q with values from V are 4-adjacency if q is in set $N_4(p)$.

2. 8-adjacency:

Two pixel p & q with values from V are 8-adjacency if q is in set $N_8(p)$.

m -adjacency:

1. q is in $N_4(P)$

2. q is in $N_D(P)$ and $N_4(P) \cap N_4(q) = \emptyset$
 NULL

0	1*	1 _q
0	1	0
0	0	1

$$V = \{1\}$$

$$N_D(P)$$

$$N_4(P)$$

$$N_8(P)$$

Here P & q are not m -adjacent,

as (*) this pixel falls in both $N_4(P)$ and $N_4(q)$. So $N_4(P) \cap N_4(q) \neq \emptyset$.

Exercise (2.1.1) \rightarrow H.W.

2.11

Given two sub sets S_1 & S_2 are.

	S_1	S_2	
0	0 0 0 0 0	0 0 1 1 0	0
1	0 0 1 0 0	0 1 0 0 1	1
1	0 0 1 0 1	1 1 0 0 0	0
0	0 1 1 1 0	0 0 0 0 1	0
	0 0 1 1 1 0	0 1 1 1 1	

For, $V = \{1\}$, let p and q be two pixels.

- (a) For two different subsets S_1 and S_2 , p and q are not 4-adjacent as none p is in the set of $N_4(q)$, neither q is in the set of $N_4(p)$.

- (b) Here p and q are not 8-adjacent, as both of their values are not in set of $V = \{1\}$ and q is but p is not in set $N_8(p)$.

- (c) p and q are not m-adjacent, as q is not in $N_4(p)$.

Here, again, if we consider P and q ,

	s_1	s_2	
0	0 0 0 0 0	0 0 1 1 0	0
1	0 0 1 0 0	0 1 0 0 0	0 1 0 0
1	0 0 1 0 0	(1) 1 0 0 0	0 1
0	0 1 1 1 0	0 0 0 0 0	0 0
	0 1 0 1 0 1 1 0 0 1 0		

- Out of all 8 nodes of the graph, q is not 4-connected as q is not in the set $N_4(P)$.

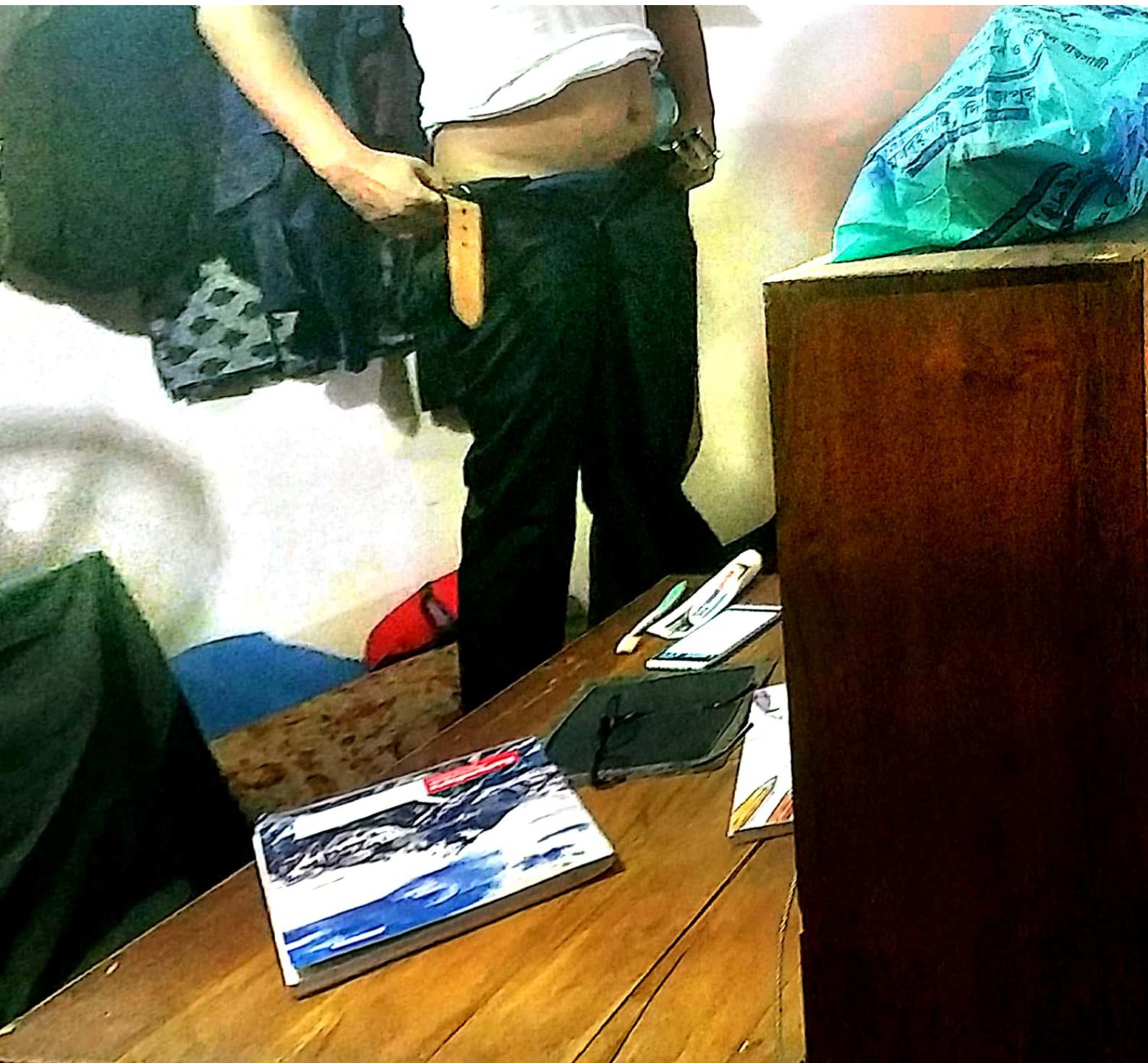
- (b) ~~$s_2 \neq s_1$~~ and s_2 are 8-connected because, q is in the set $N_8(P)$.

- (c) s_1 and s_2 are m-connected, as

(i) q is in $N_8(P)$ and

(ii) the set $N_4(P) \cap N_4(q) = \emptyset$.

(Ans).



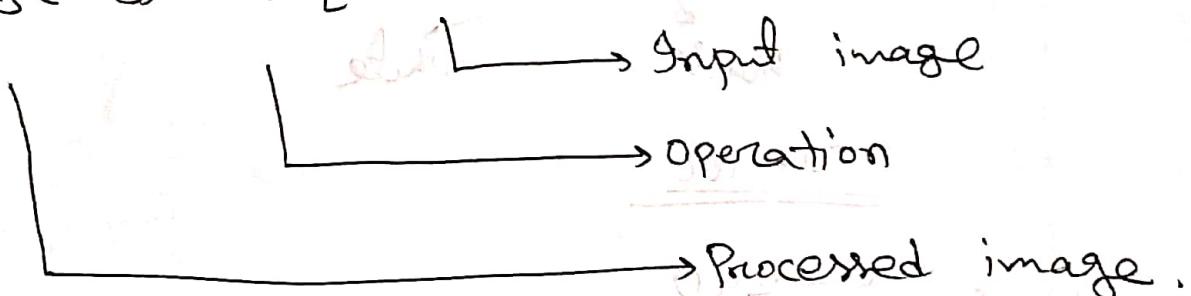
Spatial Domain Vs. Transform Domain

Image enhancement

1. Spatial Domain (co-ordinate value)

2. Frequency Domain (Fourier Transform)

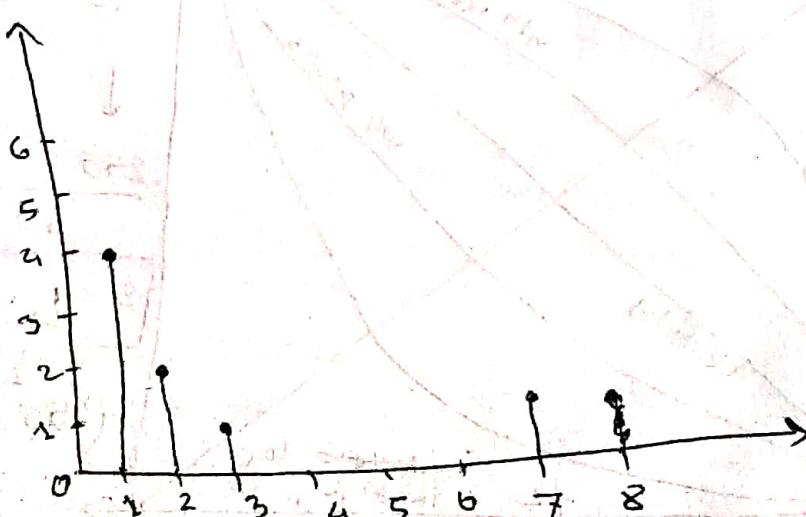
$$g(x,y) = T[f(x,y)]$$



* Point operation (individual pixel)

* Local operation (neighbor pixels)

* Global operation (Histogram) → find frequency



1	1	2
7	0	1
1	2	3

intensity value scale: 0 -

Spatial Domain Process

Intensity transformation function:

$$S = T(R_b)$$

$0 - 255$

Black

White

$50 \sim 100$

$0 - 240$

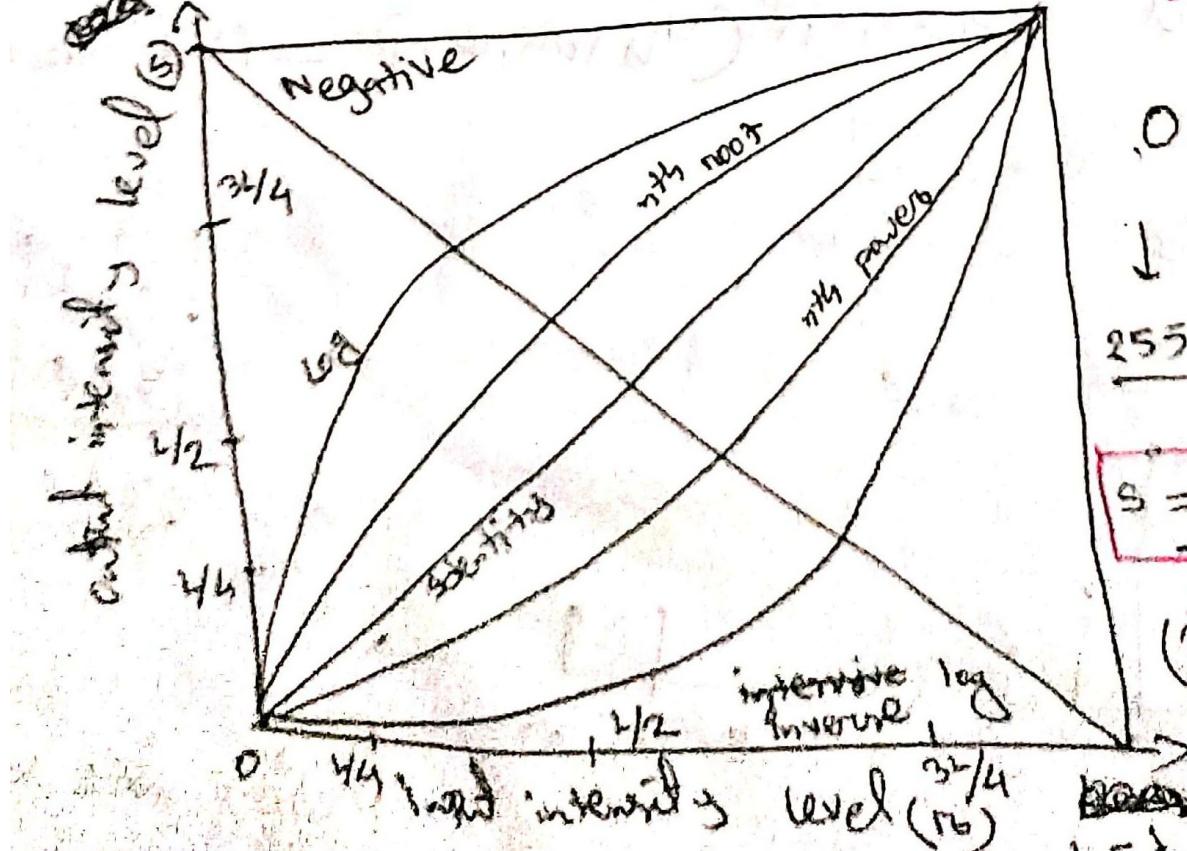
More clear,

more contrast after

stretching (value of intensity increases)

negative

$L = \max$ intensity level.



$0 \quad 255$

\downarrow

255

130

\uparrow

0

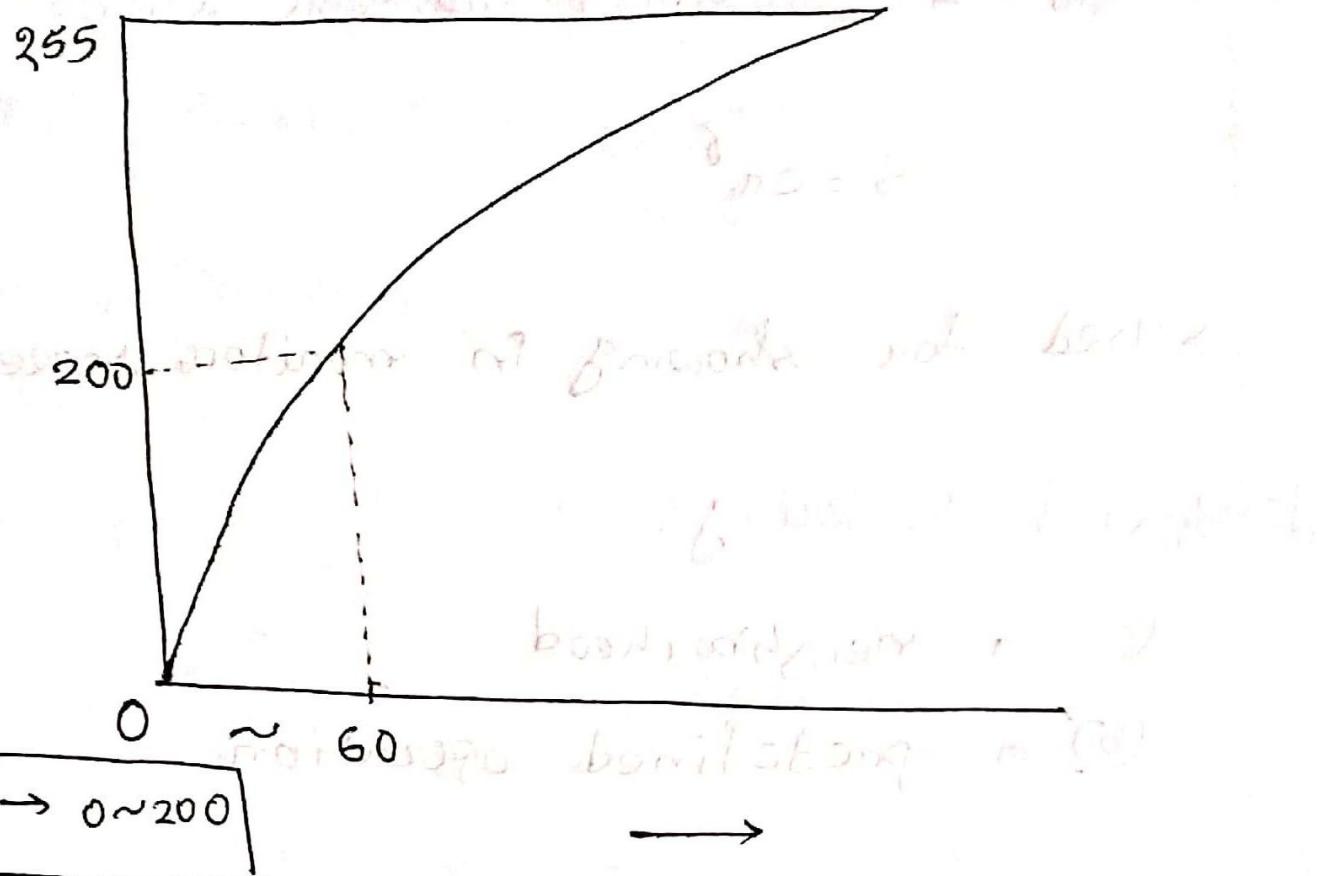
\downarrow

130

\uparrow

130

Log Transform:



$$S = c \log(1 + r_b)$$

Power-Law (Gamma) Transformations:

$$S = C r_b^\gamma$$

06.02.19.

Till tomorrow's class.

Power-Law (Gamma) Transformations:

$$S = cR^{\gamma}$$

→ used for showing in monitor screen.

Spatial Filtering:

- (a) a neighborhood
- (b) a predefined operation.

* Histograms

Contrast Stretching:

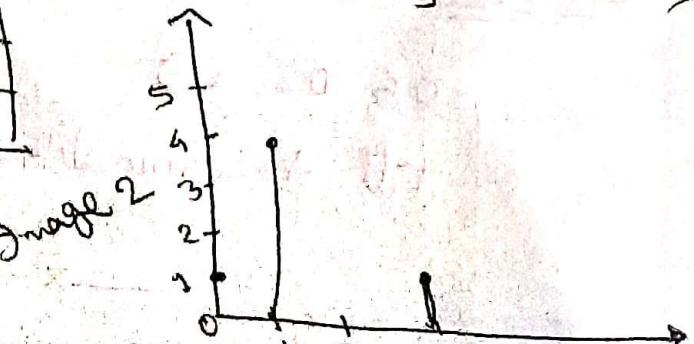
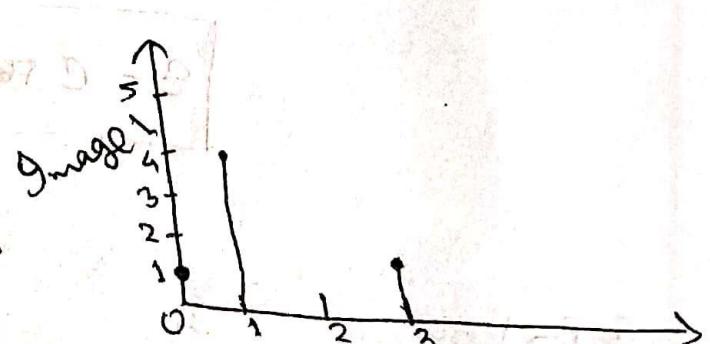
* To identify different images or frequency range.

Image 1

1	1
3	0
1	1

Image 2

0	1
1	1
3	1



* Same Histogram for both images which are different.

We can not identify image through histogram, but can have idea on its contrast level.

Frequency Domain

Spatial "

Spatial Filtering:

$$g(x, y) = \sum_{s=-a}^a \sum_{t=-b}^b w(s, t) f(x+s, y+t)$$

linear spatial filtering of an image of size $m \times N$ with a filter of $m \times n$.

Image smoothing

" Sharpening

— X —

"LAB"

31.01.19

After image

negative image

subplot (2, 1, 1);

imshow (I)

subplot (2, 1, 2);

V = rgb2gray (I);

imshow (V)

(0, K, 255) = (256 - I - K);

imshow (S).

In negative to grayscale image convert

Log Transformation:

$g = c \cdot \log (1 + f)$

$c = 1$

$f = \text{image}$

$g = \log (1 + \text{double} (f)) * 1;$

subplot (2, 2, 4);

imshow (g)

Powers-law (Gamma) Transformations:

$$S = c \cdot I^{\gamma}$$

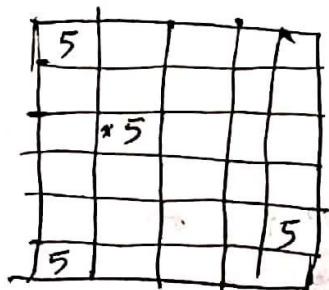
$$f = \text{uint}(10 * (K \cdot I^2)),$$

subplot (3, 3, 5);

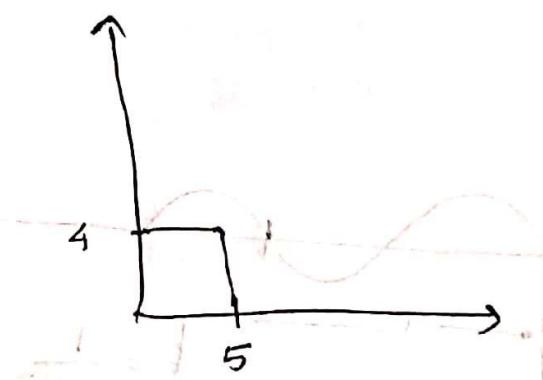
imshow(f)

$$\text{on, } f = \text{uint}(10 * (I^2));$$

Image Histogram:



$$g = \delta(3, 2) = 5$$



$$[row, col, d] = \text{size}(k)$$

for c = 1: col

H.C. \rightarrow ① Image Histogram Plot

② Normalize Histogram

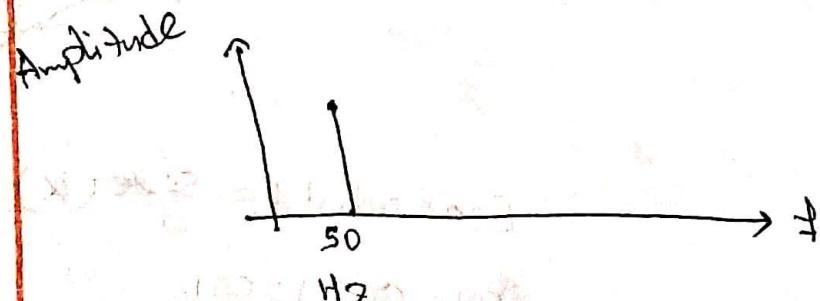
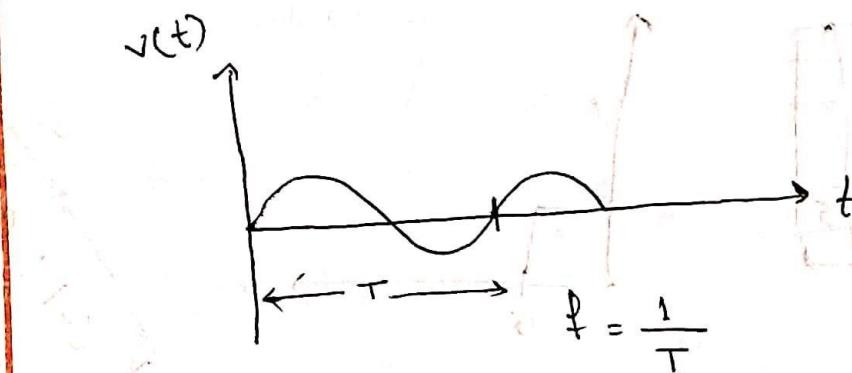
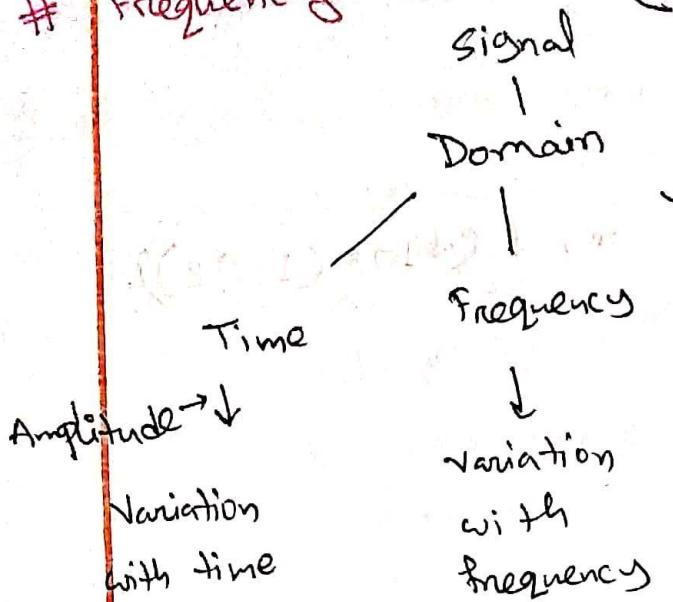
$$\text{value} = k(n, c)$$

↓
Plot (probability plotting)

31.01.19

"Akhtar Sir"

Frequency Domain; (Image enhancement)



Time, frequency, Amplitude → Spectrogram

i Analog signal $\xrightarrow{\text{Fourier Transformation}}$ Discrete / Digital Signal.

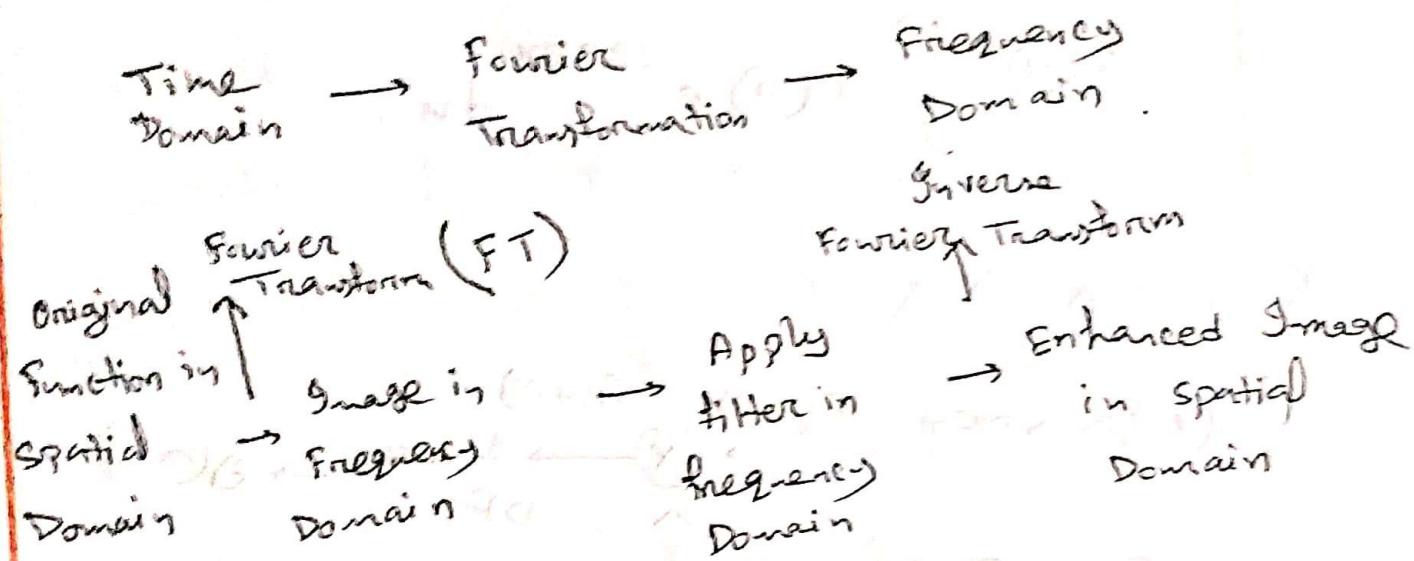


Fig: Processes in Fourier Transform.

1-D FT \rightarrow Signal processing

2D " \rightarrow Image "

3D " \rightarrow Computer vision.

* Application:

1. Image enhancement

2. " restoration

3. " encoding / decoding

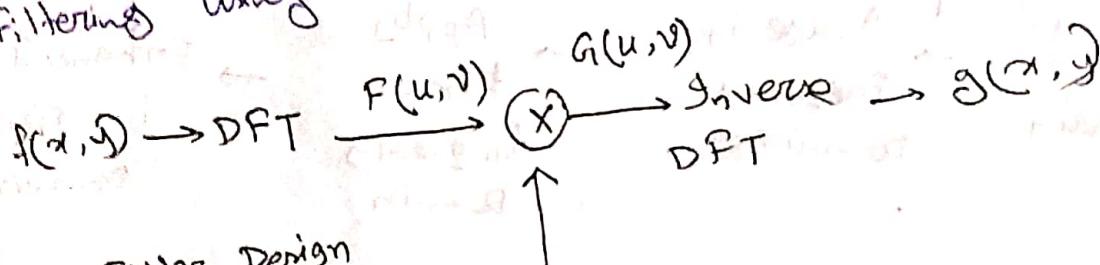
4. " description

* 1D FT:

$$f(u) = \int_{-\infty}^{\infty} f(x) e^{-j2\pi ux} dx \quad \text{where } j = \sqrt{-1}$$

$$f(u) = \int_{-\infty}^{\infty} F(v) e^{j2\pi vx} dv$$

* Filtering Using FT's



Filter Design

$$H(u, v)$$

DFT \rightarrow Discrete FT

* High Pass (HP), Low pass filters (LPF).

1. Ideal
2. Butterworth (Smooth transition between low & high)
3. Gaussian

Tearing effect

Frequency Bands

The Convolution Theorem

$$g = f * h$$

implies

$$G_L = F \cdot H$$

$$g = f \cdot h$$

implies

$$G_L = F * H$$

Low frequency to high frequency \rightarrow Butterworth.

$\uparrow D_0 \rightarrow \downarrow$ Ringing radius + \downarrow blur

~~• Gaussian effect~~

~~Softer blurring + no ringing~~

~~Smoothing \rightarrow low pass filter~~

~~Sharpening \rightarrow High pass filter~~

~~Band Pass filtering \rightarrow certain range pass~~

Band rejection filtering:

Scikit

04.02.19

CT-1 → 11.02.19 (Monday)

- Time : 10:45 AM.
1. Fundamental of digital image processing
 2. Sampling & Quantization

3. Adjacency, Neighborhood

4. Intensity transformation

(Image negative, log transform,
gamma transform)

Frequency Domain Filtering

Image smoothing (low pass)

" Sharpening (High pass)

Spatial Filtering

Spatial convolution

origin (center)

0	0	0	0	0
0	0	0	0	0
0	0	1	0	0
0	0	0	0	0
0	0	0	0	0

original
image.

$w(x, y)$

1	2	3
4	5	6
7	8	9

filter

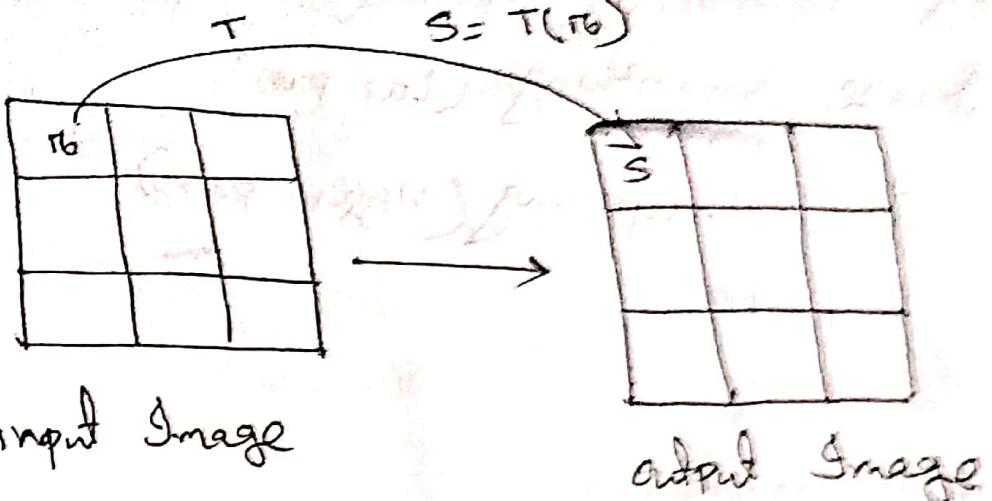
↓ Padding

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

initial
position →

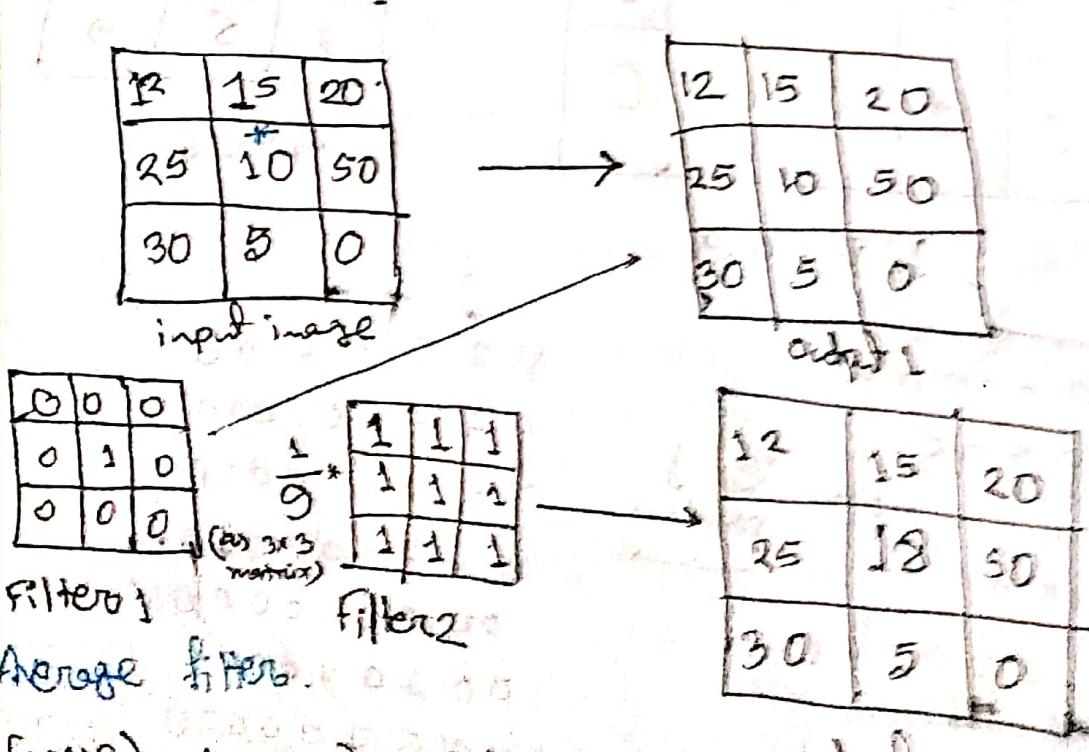
1	2	3	0	0	0	0	0	0	0
4	5	6	0	0	0	0	0	0	0
7	8	9	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

Smoothing Spatial Filters; (to remove noise)



Smoothing \rightarrow Low pass filters

Sharpening \rightarrow High " "



Ans.

$$\frac{1}{9}$$

$$(1 \times 12) + (1 \times 15) + 20 \\ + 25 + 10 + 50 \\ + 30 + 5 + 0$$

Salt & pepper Noise

Median filter

0 85 85 7 12 15 20 25 30 25 5



median 15

12	15	20
25	255	7
30	5	0

Median
filter

12	15	20
25	15	7
30	5	0

—X—

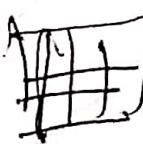
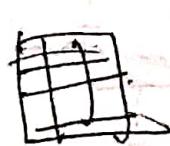
13.02.19

Code: 00010000000000000000000000000000

3x3

$n \times m$ $m \times z$

256x 256



13.02.19

Spatial Filtering:

"LAB"

14.02.19.

Hw. → Image Filtering

(using average, max, min, median)

— X —

18.02.19

Sharpening Spatial Filter:
[High Pass filter]

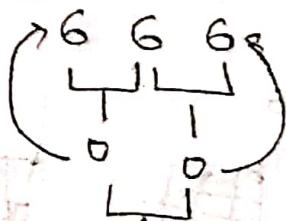
derivative

$$\frac{\partial f}{\partial x} = f(x+1) - f(x)$$

6	6	6	6	5	9	3	2	1	1	1	1	1	1	6	6	6	6
0	0	0	-1	-1	-1	-1	-1	0	0	0	0	0	5	0	0	0	0

$$\frac{\partial^2 f}{\partial x^2}$$

$$0 \ 0 \ -1 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 5 \ -5 \ 0 \ 0$$



$$\begin{aligned}\frac{\partial^2 f}{\partial x^2} &= f(x+1) - f(x) - f(x) + f(x-1) \\ &= f(x+1) + f(x-1) - 2f(x).\end{aligned}$$

Q1 Ans

$$\frac{\partial^3 f}{\partial y} = f(y+1) + f(y-1) - 2f(y)$$

operator

$$\frac{\partial^2 f}{\partial x} + \frac{\partial^2 f}{\partial y} = f(x+1) + f(x-1) - 2f(x) + f(x+1) + f(x-1) - 2f(x)$$
$$= f(x+1, y) + f(x-1, y) + f(x, y+1) + f(x, y-1) - 4f(x, y)$$

Mask:

	1	
1	-4	1

2nd order
derivative.

20.02.19

CT-2

27.02.19

10:30:00 AM

Syllabus:

1 Spatial Filtering

-Image smoothing

-Image sharpening



Notes for

Spatial



"External"

20.02.19.

Agenda:

1. Image enhancement

2. Image processing using python

Image Enhancement in Frequency Domain:

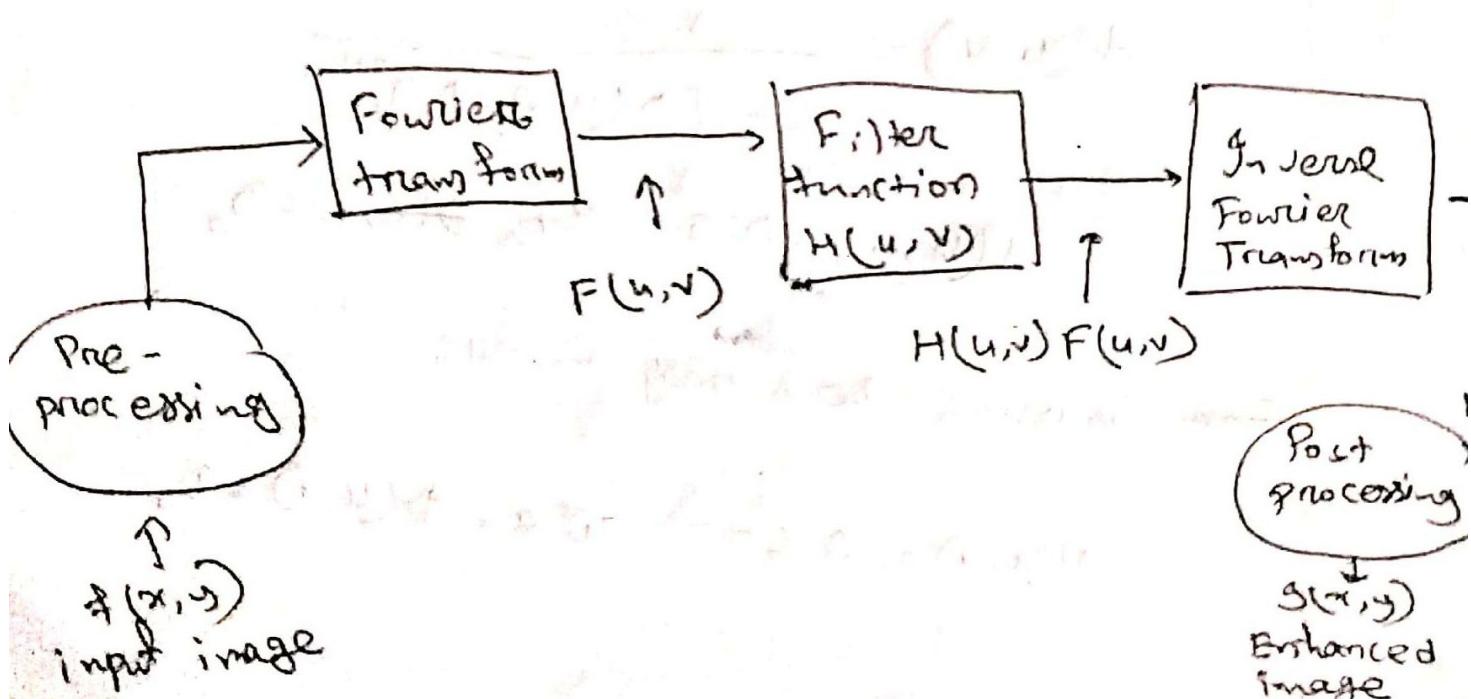
Basics of Frequency Domain Filtering:

continuous time \rightarrow Discrete time \rightarrow Discrete Fourier Transform (DFT)

DFT of the image; $F(u,v) \rightarrow F(u,v) * \text{filter function}$
 $(H(u,v))$

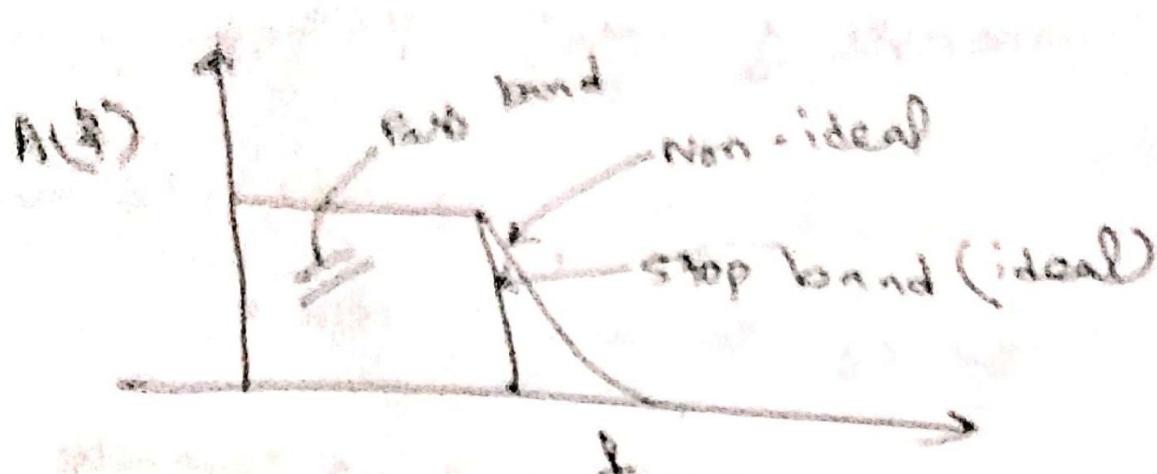
inverse D.F.T

Basic Steps:



Time domain filtering \rightarrow convolution.

Ideal Low Pass Filter:



Smoothing Frequency Domain Filters:

$a(u,v)$

Cut-off Frequency

Buttersworth Lowpass Filter:

Does not have sharp discontinuity,

$$H(u,v) = \frac{1}{1 + [D(u,v)/D_0]^{2n}}$$

$$H(u,v) = 0.5 \text{ when } D(u,v) = D_0$$

Gauss. Gaussian Low pass filter:

$$\pi H(u,v) = 0.607 \text{ when } D(u,v) = D_0$$

* Convolution in the time domain is filtering in frequency domain.

Sharpening Frequency Domain Filters:

High Pass Filtering

$$H_{HP}(u,v) = 1 - H_{LP}(u,v)$$

Smoothing \rightarrow Low pass filters

Sharpening \rightarrow High pass filters.

Does not have sharp discontinuity.

$$H(u,v) = \frac{1}{1 + [D_0 / D(u,v)]^{2n}}$$

Gaussian Highpass Filter:

$$-\sigma^2(u,v)$$

$$\frac{1}{2\sigma^2} e^{-\frac{(u-u_0)^2+(v-v_0)^2}{2\sigma^2}}$$

$$H(u,v) = 1 - e^{-\frac{(u-u_0)^2+(v-v_0)^2}{2\sigma^2}}$$

$$H(u,v) = 0.607 \text{ when } D(u,v) = D_0$$

Open CV (Open Computer vision)

25.02.19

27.02.19

"Histogram Processing"

Histogram equalization

" matching "

Local " processing

using " statistics for Image enhancement.

CT-2 : 14.03.19

10:50 Am

previous syllabus

Histogram Equalization

+ Spatial filtering

(smoothing + sharpening (laplacian))

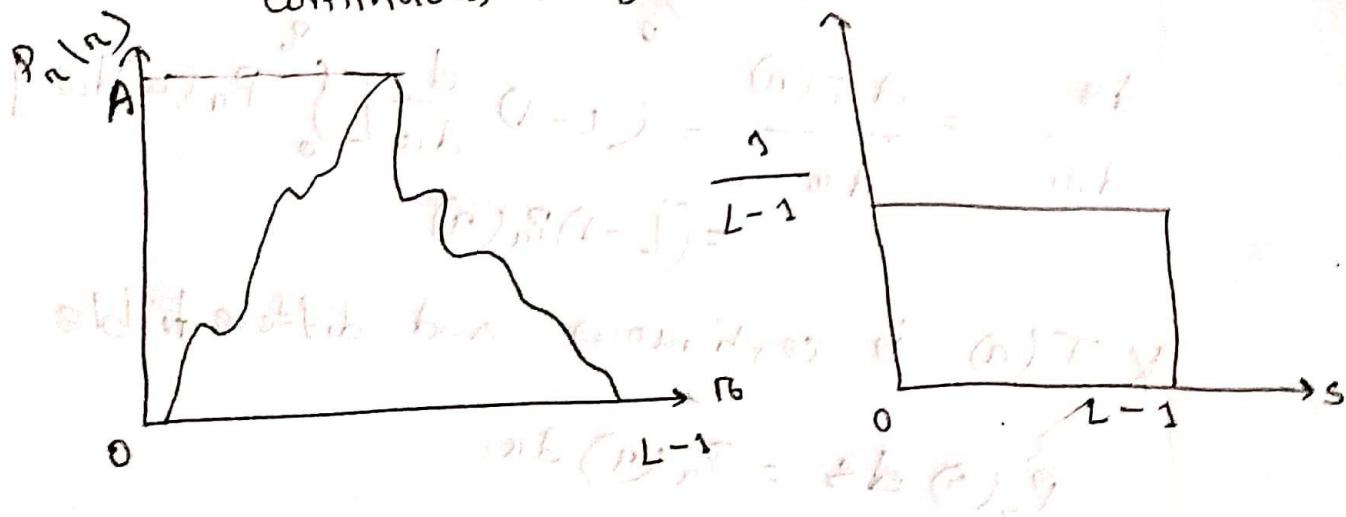
Normalized histogram, $P(r_x) = \frac{n_x}{MN}$

1	1	1
2	50	70
5	7	10

$$\text{For } r_1, \frac{1}{3} \\ n=0.33$$

* Histogram Equalization
 (continuous) Pmf \rightarrow Probability Density Function
 Factors

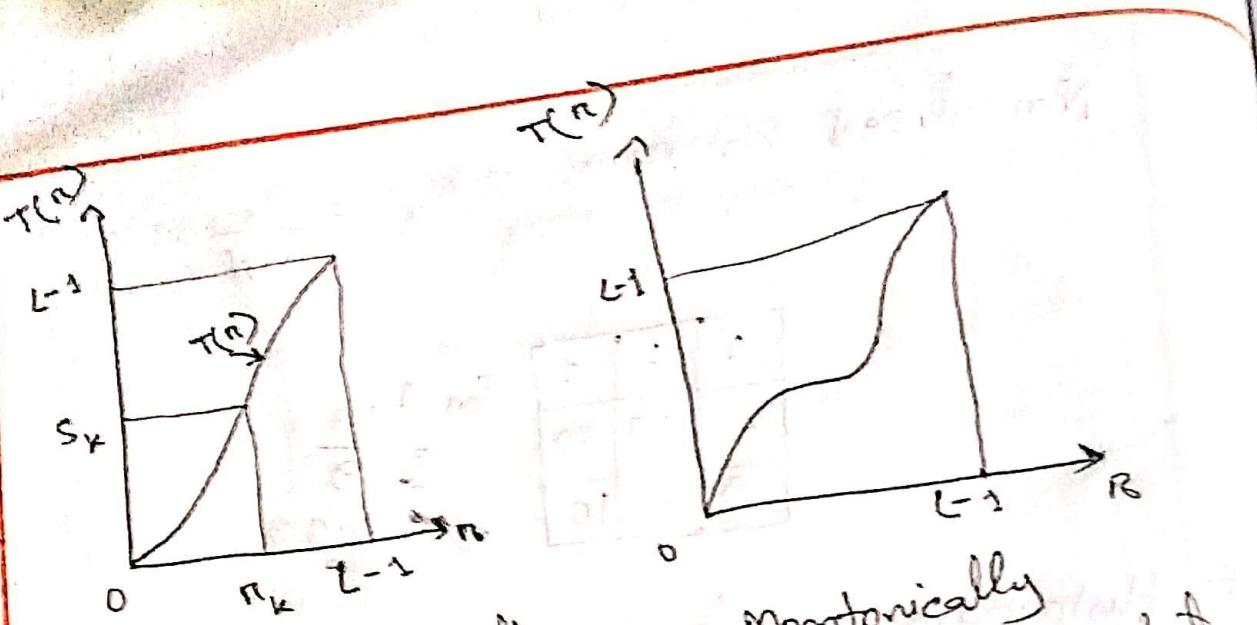
(discrete) Pmf \rightarrow " match
 continuous image.



$$s = T(n)$$

(a) $T(n)$ is strictly monotonically increasing function in the interval $0 \leq n \leq L-1$

(b) $0 \leq T(n) \leq L-1$ for $0 \leq n \leq L-1$.



- (a) strictly monotonically increasing function Monotonically increasing function, but not strictly.

$$S = T(n) = (L-1) \int_0^n P_n(\omega) d\omega$$

$$\frac{ds}{dn} = \frac{d T(n)}{dn} = (L-1) \frac{d}{dn} \left[\int_0^n P_n(\omega) d\omega \right] \\ = (L-1) P_n(n)$$

* $T(n)$ is continuous and differentiable

$$P_s(s) ds = P_n(n) dn$$

$$P_s(s) = \frac{P_n(n) dn}{ds} = P_n(n) / \left(\frac{ds}{dn} \right)$$

$$= P_n(n) / ((L-1) P_n(n)) = \frac{1}{L-1}$$

Derive values:

$$g_k = \Gamma(\mu_k) = (k+1) \sum_{j=0}^k p_n(e^{n_j})$$

$$= (k+1) \sum_{j=0}^k \frac{n_j}{MN} = \frac{k+1}{MN} \sum_{j=0}^k n_j$$

$$k = 0, 1, 2, \dots, k-1.$$