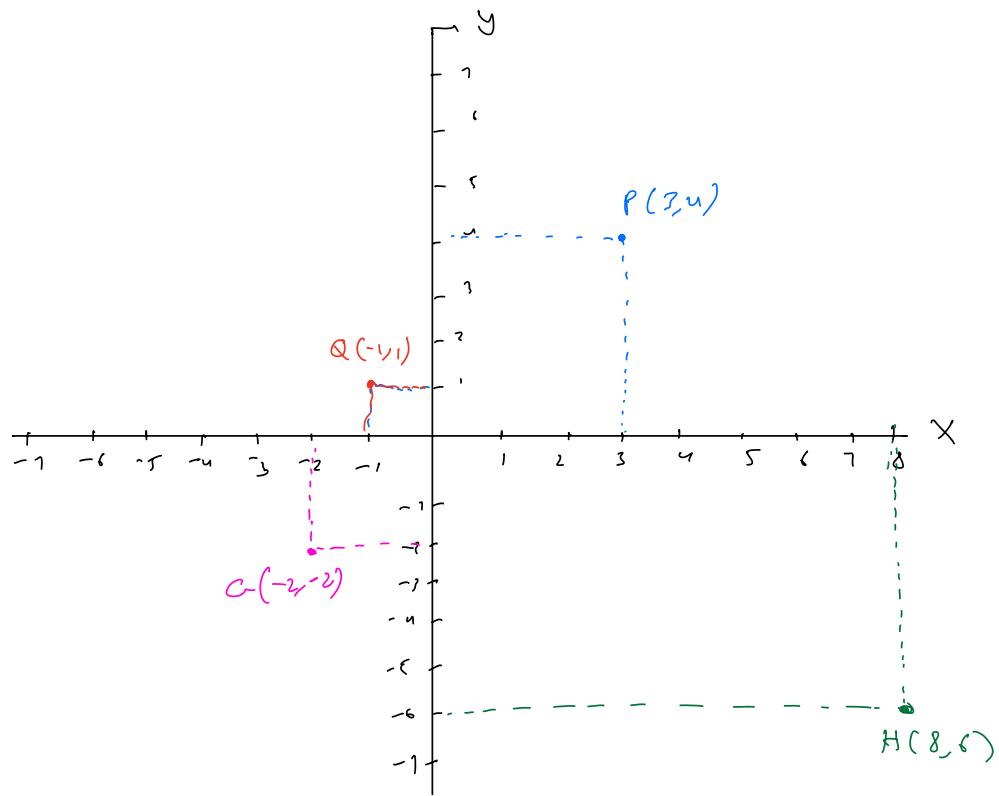
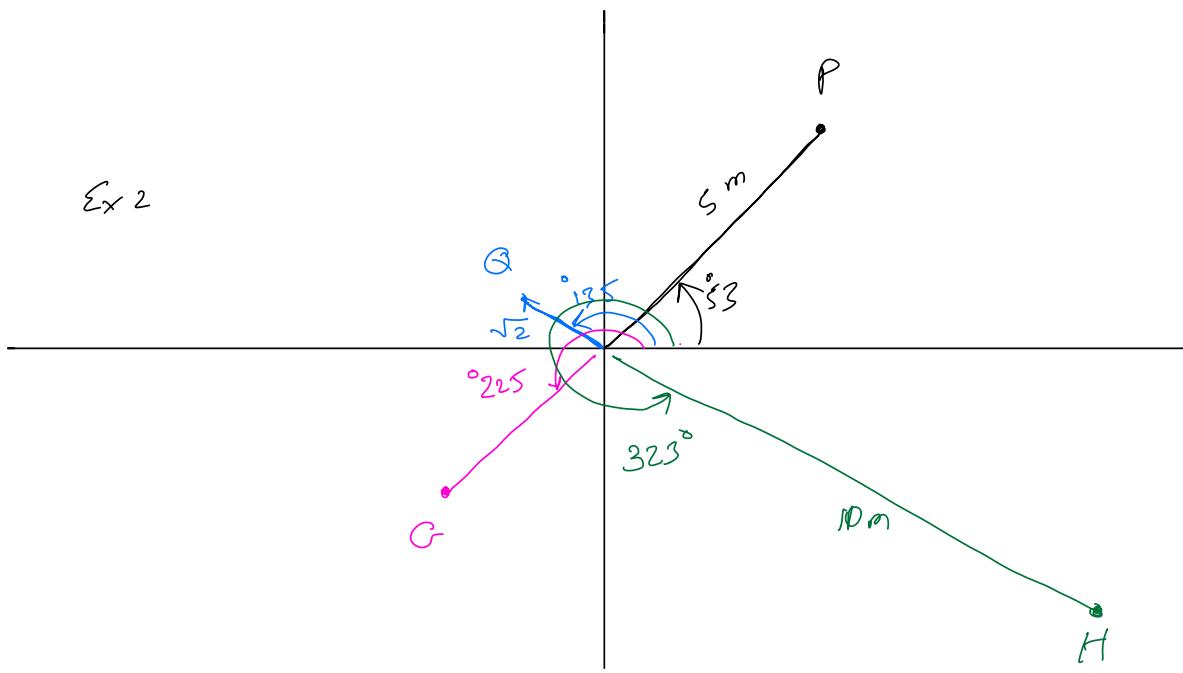


Ex1



Ex 2

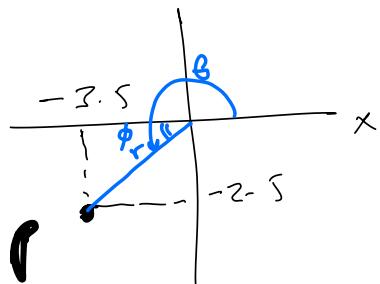


Ex 3.1
 $P(5\text{m}, (-3.5, -2.5)) \rightarrow P(r, \theta) ?$

$$\Rightarrow x = -3.5 \text{ m}$$

$$y = -2.5 \text{ m}$$

y



$$r = \sqrt{x^2 + y^2}$$

$$= \sqrt{(-3.5)^2 + (-2.5)^2}$$

$$= 4.3 \text{ m}$$

$$\tan \phi = \frac{y}{x} = \frac{-2.5}{-3.5} = 0.714$$

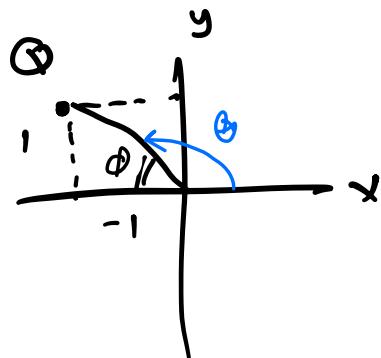
$$\phi = 35.54^\circ \approx 36^\circ \quad \rightarrow \theta = 180^\circ + \phi = 180^\circ + 36^\circ$$

$$\therefore P(-3.5, -2.5) \Rightarrow P(4.3 \text{ m}, 216^\circ)$$

Ex 3

$$Q(-1, 1) \rightarrow \begin{matrix} x = -1 \\ y = 1 \end{matrix} m$$

$$\begin{aligned} r &= \sqrt{x^2 + y^2} \\ &= \sqrt{(-1)^2 + 1^2} \\ &= \sqrt{2} m \end{aligned}$$



$$\tan \phi = \frac{1}{-1} = -1 \rightarrow \phi = \tan^{-1} 1 = 45^\circ$$

$$\begin{aligned} \theta &= 180 - \phi \\ &= 180 - 45 \end{aligned}$$

$$\therefore Q(-1, 1) \rightarrow Q(\sqrt{2}m, 135^\circ)$$

Ex 4

$$C(\sqrt{8} \text{ m}, 225^\circ)$$

$$r = \sqrt{8} \text{ m} \quad \theta = 225^\circ$$

$$\begin{aligned} x = r \cos \theta &\Rightarrow r = \sqrt{8} \cos 225^\circ \\ &= 2\sqrt{2} \left(-\frac{1}{\sqrt{2}}\right) \\ &= -2 \text{ m} \end{aligned}$$

$$\begin{aligned} y &= r \sin \theta \\ &= 2\sqrt{2} \sin 225^\circ \\ &= 2\sqrt{2} \cdot \frac{1}{\sqrt{2}} = 2 \text{ m} \end{aligned}$$

$$\therefore C(\sqrt{8} \text{ m}, 225^\circ) \rightarrow C(-2, 2) \text{ m}$$

Ex 6

$$r = 10 \text{ mm}$$

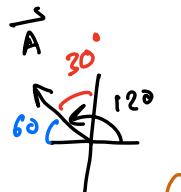
$$\theta = 37^\circ + 270^\circ = 323^\circ$$

$$\text{or } \theta = 360^\circ - 37^\circ = 323^\circ$$

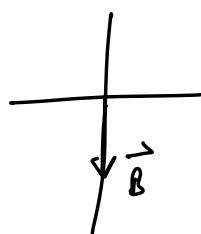
$$\begin{array}{l|l} x = r \cos \theta & y = r \sin \theta \\ = 10 \cos 323^\circ & = 10 \sin 323^\circ \\ = (10)(0.8) & = 10(0.6) \\ = 8 \text{ mm} & = -6 \text{ mm} \end{array}$$

$$\therefore H(10 \text{ mm}, 323^\circ) \rightarrow H(8, -6) \text{ mm.}$$

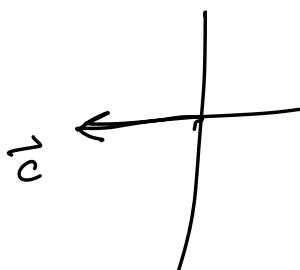
Ex 6



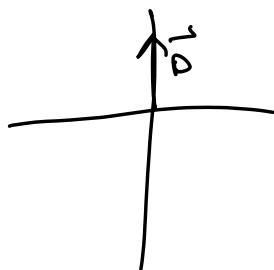
- \vec{A} سريل از احمد متوجه 5m بجهه 120° سالبيه سمح لشي طرحب ($180^\circ - 30^\circ$ غرب) ($180^\circ - 60^\circ$ شمال غرب)



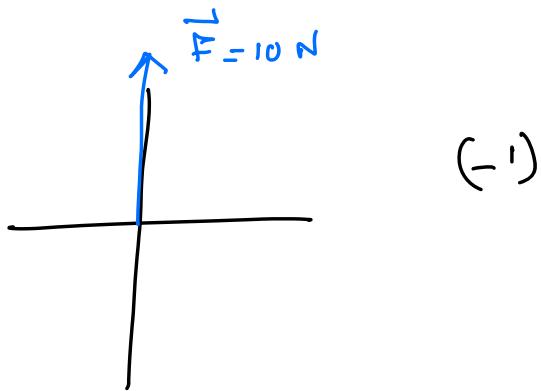
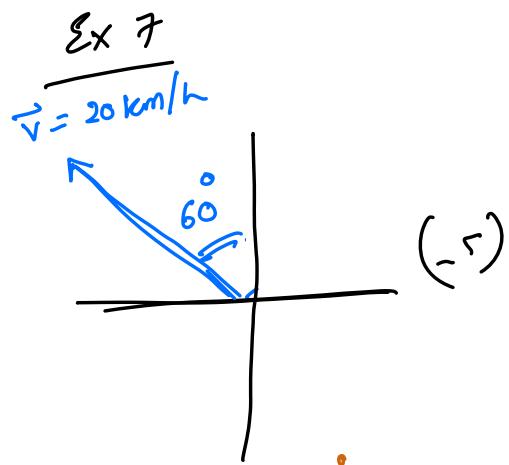
- \vec{B} متوجه سارقا متوجه سارقا بجهه كنفر



- \vec{C} سريل سره متوجه سره سره بجهه كنفر

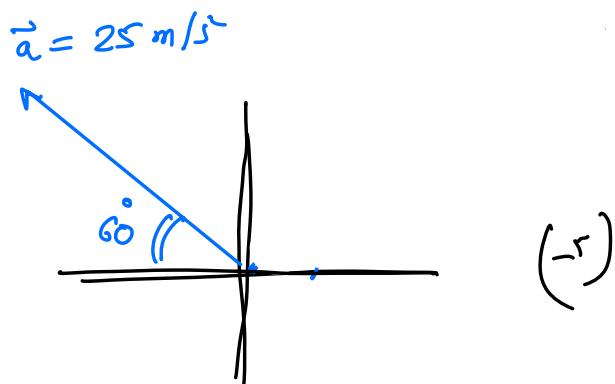
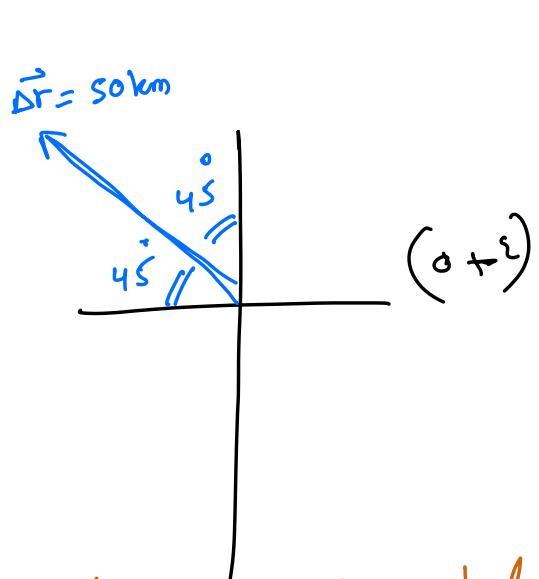


- \vec{D} سريل حركه متوجه حركه سره سره بجهه كنفر



$$\vec{v} = 20 \text{ km/h}, 60^\circ \text{ west of north}$$

$$= 20 \text{ km/h}, 150^\circ$$

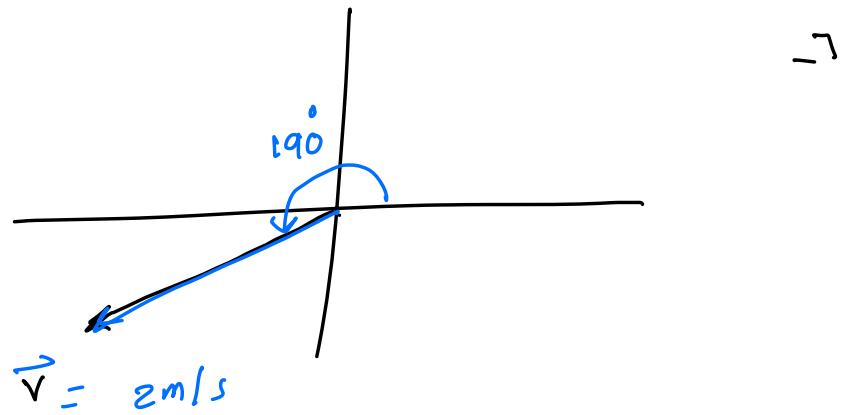


$$\vec{dr} = 50 \text{ km, } 45^\circ \text{ west of north}$$

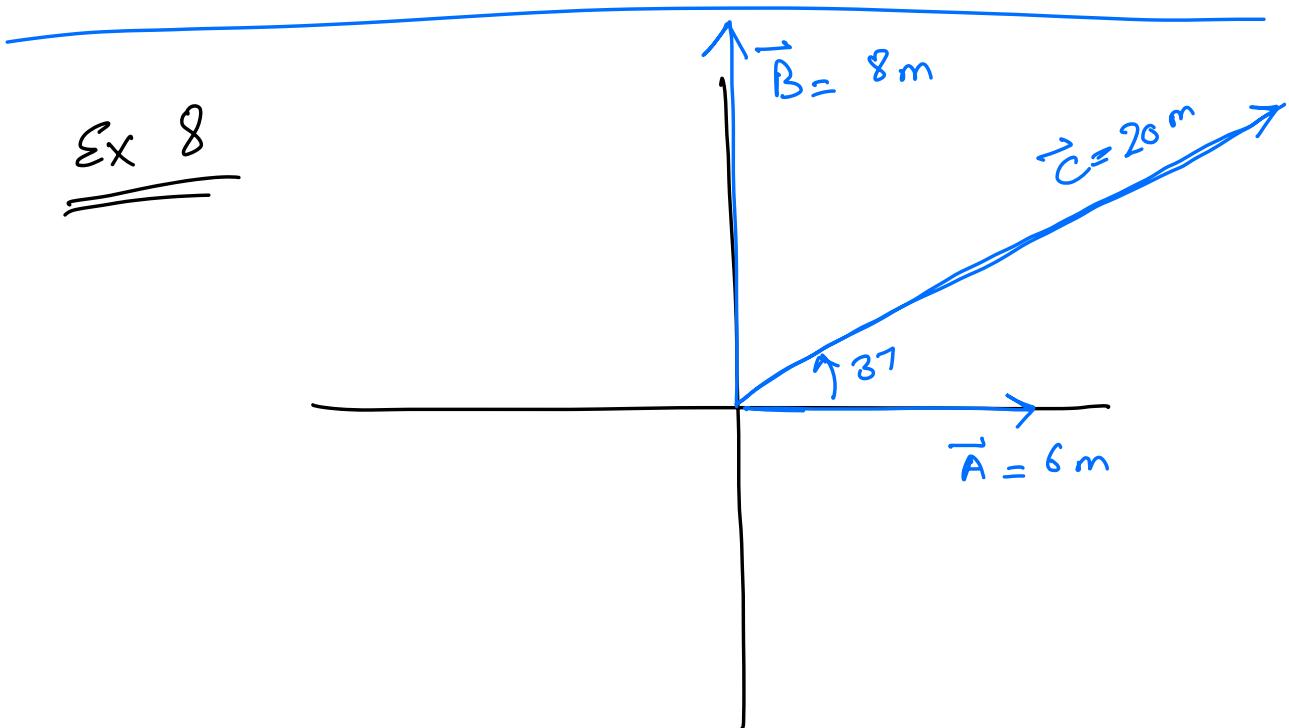
$$= 50 \text{ km, } 135^\circ$$

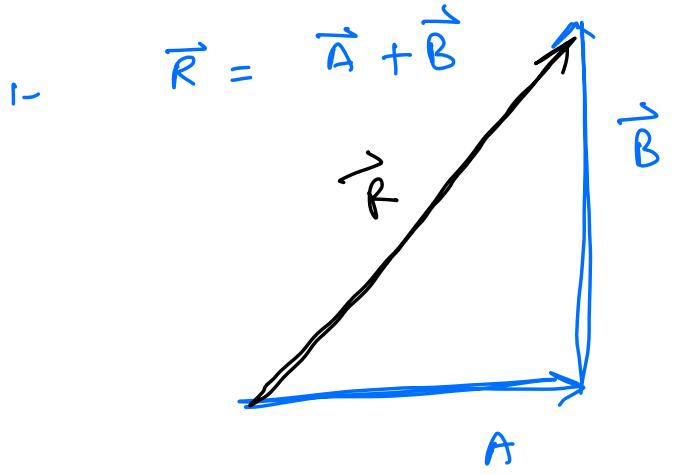
$$\vec{a} = 25 \text{ m/s}^2, 60^\circ \text{ north of west}$$

$$= 25 \text{ m/s}^2, 120^\circ$$

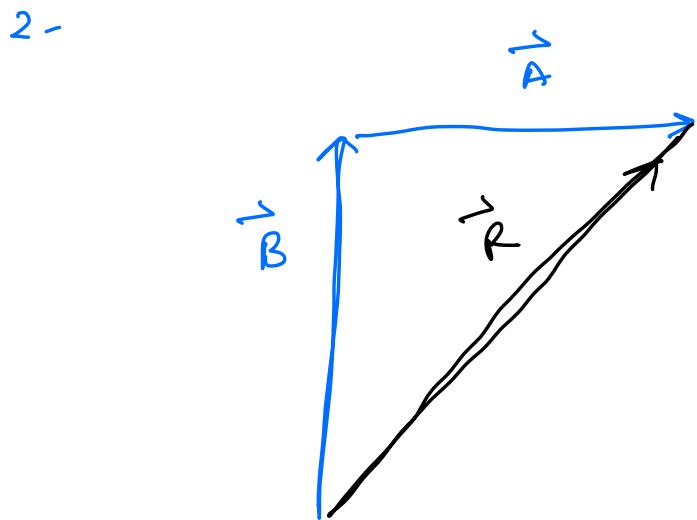


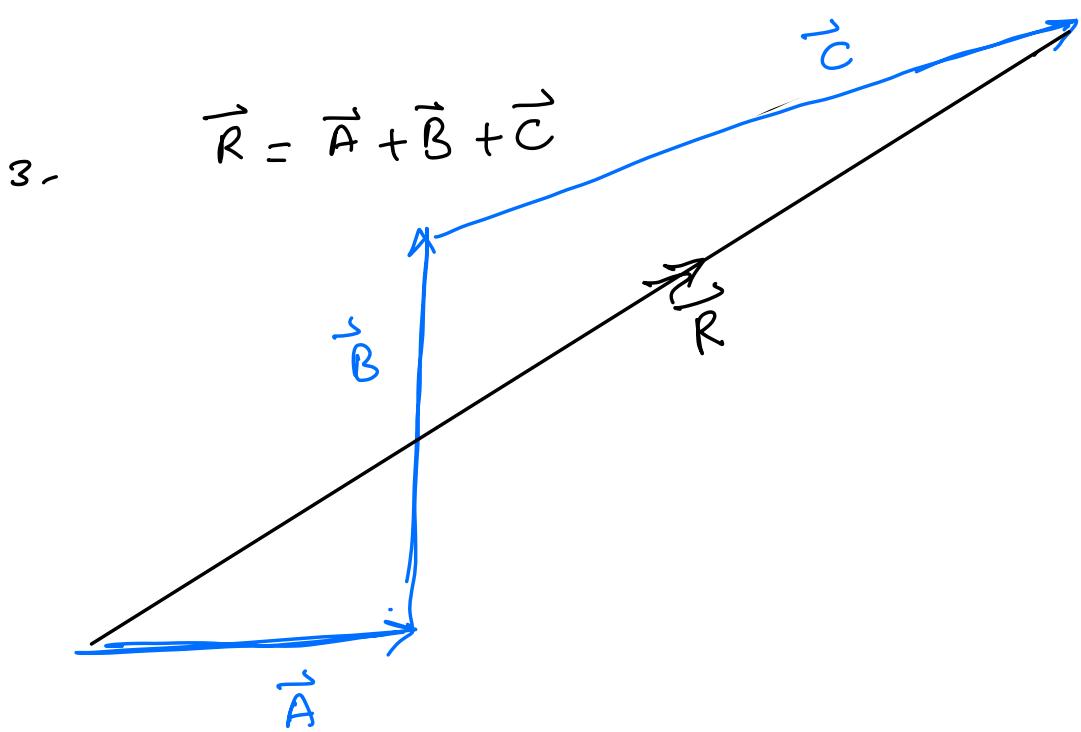
$$\begin{aligned}
 \vec{v} &= 2 \text{ m/s}, 190^\circ \\
 &= 2 \text{ m/s} - 10^\circ \text{ south of west} \\
 &= 2 \text{ m/s} - 80^\circ \text{ west of south}
 \end{aligned}$$





$$\vec{R} = \vec{B} + \vec{A}$$





Ex 9

- كون \vec{A} على عد ٣ و \vec{B} على عد ٤ و \vec{C} على عد ٦
المتجهات متوازية، يعني (زاوية 0°)
معنى ذلك:

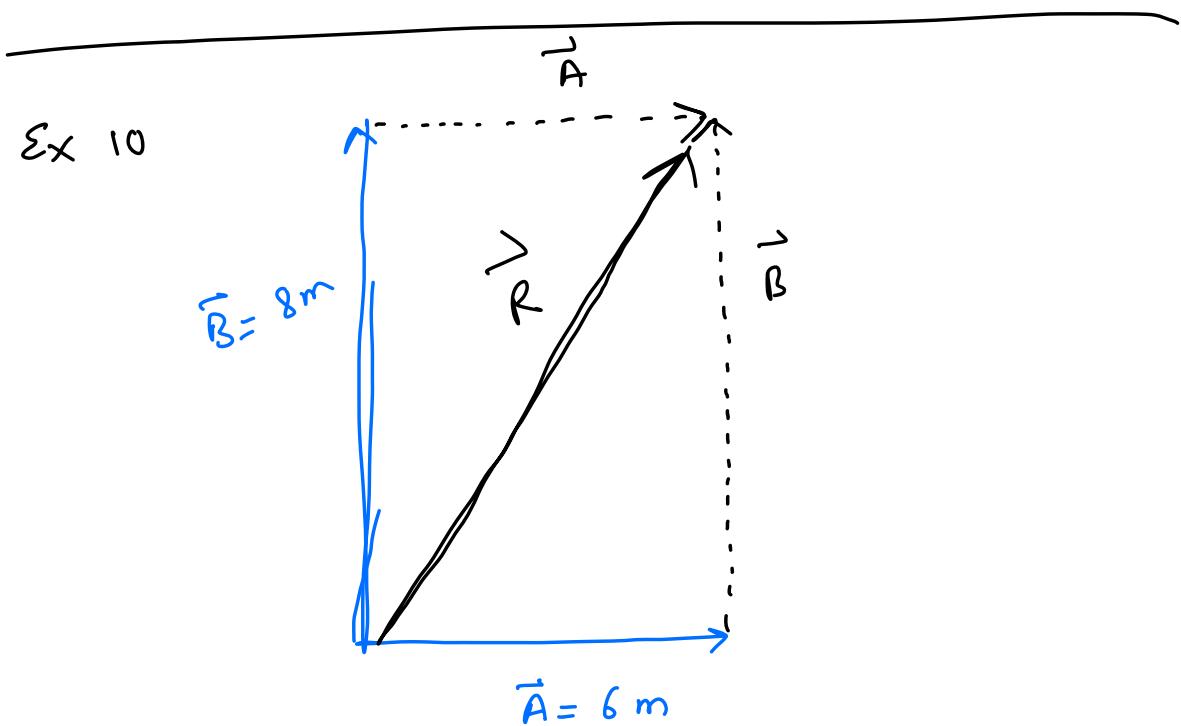
\vec{A} \vec{B} \vec{C}
ذلك يعني $\vec{A} + \vec{B} + \vec{C}$ ص. م. ل.

$$\vec{R} = 3+4 = 7 \text{ units}$$

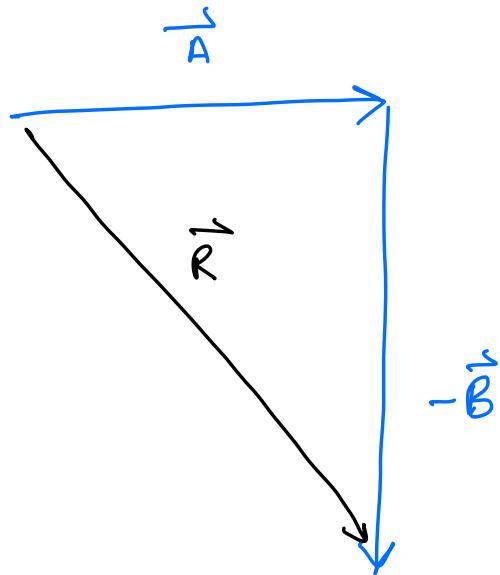
عن كل اتجاه

۲- در نی کهنه عکس طبقه ای از سایر مکانات
 (موزه ایران) موزه ایران
 (۱۸۰°)

ایک جگہ سے شروع ہوئے دو فکری وکٹروں کا نمونہ۔ وکٹر A بھرپور راستے پر اور وکٹر B بھرپور راستے پر مخالف راستے پر ہے۔ وکٹروں کے درمیانی فاصلہ 1 یونٹ ہے۔



Ex 11



Ex 12 $\vec{A} = 6 \text{ m/s}, 0^\circ$

$$\vec{B} = 8 \text{ m/s}, 90^\circ$$

$$\vec{C} = 20 \text{ m/s}, 37^\circ$$

1- $3\vec{A} = 18 \text{ m/s}, 0^\circ$

2- $\frac{1}{2}\vec{B} = 4 \text{ m/s}, 90^\circ$

3- $-2\vec{A} = 12 \text{ m/s}, 180^\circ$

4- $-\frac{1}{3}\vec{A} = 2 \text{ m/s}, 180^\circ$

5- $-\frac{1}{4}\vec{C} = 5 \text{ m/s}, (37^\circ + 180^\circ) \rightarrow 5 \text{ m/s}, 217^\circ$

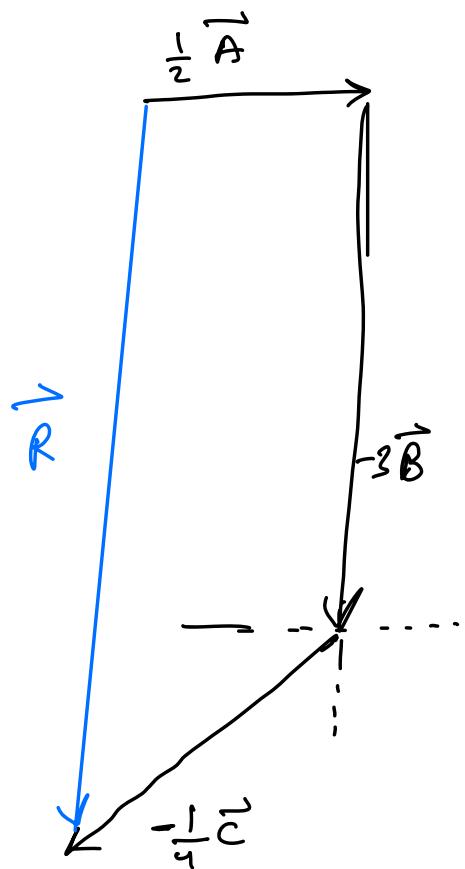
Ex 13

$$\frac{1}{2}\vec{A} = 3 \text{ m/s}, 0^\circ$$

$$3\vec{B} = 24 \text{ m/s}, 90^\circ \rightarrow -3\vec{B} = 24 \text{ m/s}, 270^\circ$$

$$\frac{1}{4}\vec{C} = 5 \text{ m/s}, 87^\circ \rightarrow -\frac{1}{4}\vec{C} = 5 \text{ m/s}, 217^\circ$$

$$\vec{R} = \frac{1}{2}\vec{A} + (-3\vec{B}) + \left(-\frac{1}{4}\vec{C}\right)$$



Ex 14

$$\vec{A} = 10 \text{ units}, 37^\circ$$

$$A_x = A \cos 37^\circ \\ = (10)(0.8) = 8 \text{ units}$$

$$A_y = A \sin 37^\circ \\ = (10)(0.6) = 6 \text{ units}$$

$$\vec{B} = 100 \text{ units}, 37 + 90^\circ \Rightarrow 100 \text{ units}, 127^\circ$$

$$B_x = B \cos 127^\circ = (100)(-0.6) \\ = -60 \text{ units}$$

or

$$B_x = -B \sin 37^\circ \\ = (-100)(0.6) = -60 \text{ units}$$

$$B_y = B \sin 127^\circ = (100)(0.8) = \\ = 80 \text{ units}$$

or

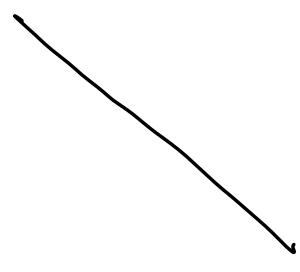
$$B_y = +B \cos 37^\circ \\ = (100)(0.8) \\ = 80 \text{ units}$$

$$\vec{C} = 20\sqrt{2} \text{ units}, 270 - 45^\circ \rightarrow 20\sqrt{2} \text{ units}, 225^\circ$$

$$C_x = C \cos 225^\circ \\ = 20\sqrt{2} \times \frac{1}{\sqrt{2}} = -20 \text{ units}$$

or

$$C_x = -C \sin 45^\circ = -20 \text{ units}$$



$$\begin{aligned}C_y &= C \sin 225^\circ \\&= 20\sqrt{2} \left(-\frac{1}{\sqrt{2}}\right) \\&= -20 \text{ units}\end{aligned}$$

or $C_y = -C \sin 45^\circ$
 $= -20 \text{ units}$

Ex 15

$$\vec{A} = 50 \text{ units}, 0^\circ$$

$$\begin{aligned}A_x &= 50 \cos 0^\circ = 50 \text{ units} \\A_y &= 50 \sin 0^\circ = 0\end{aligned}$$

$$\begin{aligned}\vec{B} &= 50 \text{ units}, 90^\circ \\B_x &= B \cos 90^\circ = 0 \\B_y &= B \sin 90^\circ = 50 \text{ units}\end{aligned}$$

$$\vec{C} = 50 \text{ units}, 180^\circ$$

$$\begin{aligned}C_x &= C \cos 180^\circ = -50 \text{ units} \\C_y &= C \sin 180^\circ = 0\end{aligned}$$

$$\vec{D} = 50 \text{ units}, 270^\circ$$

$$\begin{aligned}D_x &= D \cos 270^\circ = 0 \\D_y &= D \sin 270^\circ = -50 \text{ units}\end{aligned}$$

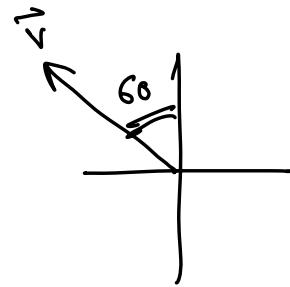
Ex 16

1- $\vec{F} = 10 \text{ N}, 90^\circ$

$$F_x = 10 \cos 90^\circ = 0$$

$$F_y = 10 \sin 90^\circ = 10 \text{ N}$$

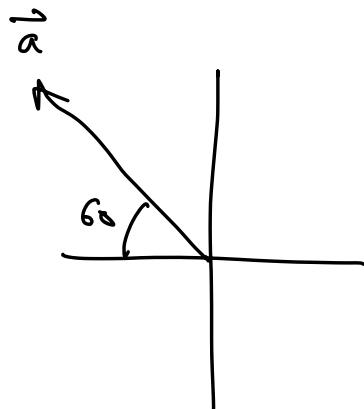
2- $\vec{v} = 20 \text{ km/h}, 60^\circ \text{ west of north}$



$$\begin{aligned} v_x &= -20 \sin 60^\circ \\ &= (-20)(0.866) \\ &\approx -17.3 \text{ km/h} \end{aligned}$$

$$\begin{aligned} v_y &= +20 \cos 60^\circ \\ &= (20)\left(\frac{1}{2}\right) = 10 \text{ km/h} \end{aligned}$$

3- $\vec{a} = 25 \text{ m/s}^2, 60^\circ \text{ north of west}$

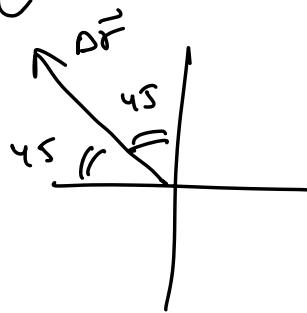


$$\begin{aligned} a_x &= (25)(\cos 60^\circ) \\ &= (25)(0.5) \\ &= -12.5 \text{ m/s}^2 \end{aligned}$$

$$\begin{aligned} a_y &= (+25)(\sin 60^\circ) \\ &= (25)(0.866) \\ &\approx 21.7 \text{ m/s}^2 \end{aligned}$$

$$4+5) \quad \Delta \vec{r} = 50 \text{ km, north west}$$

$$\text{or } \Delta r = 50 \text{ km, west north}$$



$$\begin{aligned}\Delta r_x &= \Delta x = -50 \cos 45^\circ \\ &= (-50)(0.7) \\ &\approx -35 \text{ km}\end{aligned}$$

$$\begin{aligned}\Delta r_y &= \Delta y = 50 \cos 45^\circ \\ &= (50)(0.7) \\ &\approx 35 \text{ km}\end{aligned}$$

$$6- \quad \vec{v} = 2 \text{ m/s, } 190^\circ$$

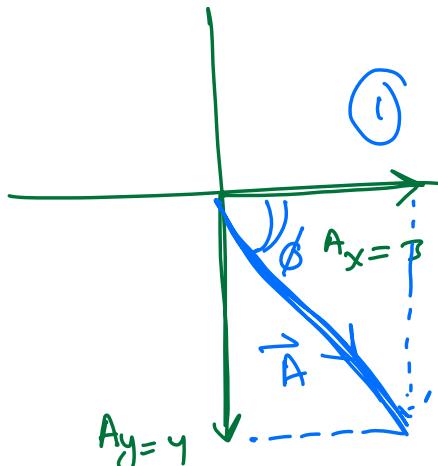
$$\begin{aligned}v_x &= (2) \cos 190^\circ \\ &= (2)(-0.98) \\ &\approx -1.97 \text{ m/s}\end{aligned}$$

$$\begin{aligned}v_y &= (2) \sin 190^\circ \\ &= (2)(-0.17) \\ &\approx -0.34 \text{ m/s}\end{aligned}$$

Ex 17 $\vec{A} = 3\hat{i} - 4\hat{j}$ $A_x = 3 \text{ m}$
 $A_y = -4 \text{ m}$

②

$$\begin{aligned} |\vec{A}| &= \sqrt{A_x^2 + A_y^2} \\ &= \sqrt{9+16} \\ &= \sqrt{25} = 5 \text{ m} \end{aligned}$$



① $\tan \phi = \frac{|A_y|}{|A_x|} = \frac{4}{3} \rightarrow \phi = \tan^{-1}$
 $\phi \approx 53^\circ$

$$\begin{aligned} \therefore \theta &= 360 - 53 \\ &= 306^\circ \end{aligned}$$

Ex 18 $\vec{A} = 3\hat{i} - 4\hat{j} + 3\hat{k} \text{ m}$

$$\vec{B} = 3\hat{i} - 4\hat{j} \text{ m} \rightarrow 2\vec{B} = 6\hat{i} - 8\hat{j} \text{ m}$$

$$\vec{C} = -5\hat{j} - 6\hat{k} \rightarrow -3\vec{C} = 15\hat{j} + 18\hat{k} \text{ m}$$

$$\vec{R} = \vec{A} + 2\vec{B} + 3\vec{C} = 9\hat{i} + 3\hat{j} + 21\hat{k}$$

Ex 19

| | x-comp | y-comp. | |
|-----------|---|---|--|
| \vec{A} | $A_x = 10 \cos 37$ $= (10)(0.8) = 8 \text{ m}$ | $A_y = (10) \sin 37$ $= (10)(0.6) = 6 \text{ m}$ | $\vec{A} = 8\hat{i} + 6\hat{j} \text{ m}$ |
| \vec{B} | $B_x = 5 \cos 53$ $= (5)(0.6) = 3 \text{ m}$ | $B_y = -5 \sin 53$ $= (-5)(0.8) = -4 \text{ m}$ | $\vec{B} = 3\hat{i} - 4\hat{j} \text{ m}$ |
| \vec{C} | $C_x = -20\sqrt{2} \sin 45$ $= -20\sqrt{2} \cancel{\frac{1}{\sqrt{2}}}$ $= -20 \text{ m}$ | $C_y = 20\sqrt{2} \cos 45$ $= 20\sqrt{2} \frac{1}{\sqrt{2}}$ $= 20 \text{ m}$ | $\vec{C} = -20\hat{i} + 20\hat{j} \text{ m}$ |
| \vec{D} | $D_x = -3 \text{ m}$ | $D_y = 0$ | $\vec{D} = -3\hat{i} \text{ m}$ |
| \vec{E} | $E_x = 0$ | $E_y = 4 \text{ m}$ | $\vec{E} = 4\hat{j} \text{ m}$ |

$$1 - (\vec{A} + \vec{B})_x = A_x + B_x = 8 + 3 = 11 \text{ m}$$

$$2 - (\vec{A} + \vec{B})_y = A_y + B_y = 6 + -4 = 2 \text{ m}$$

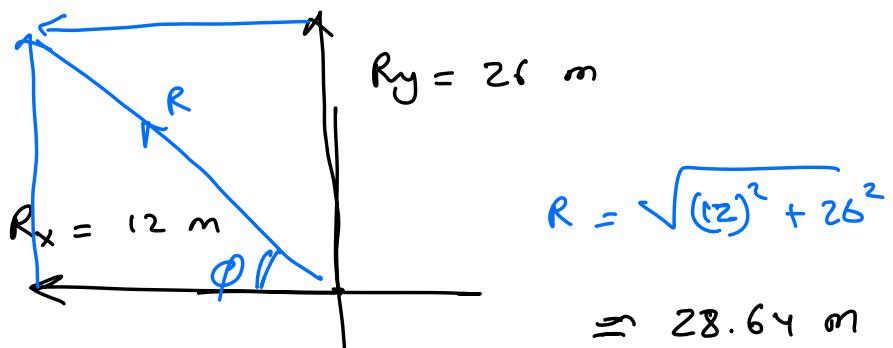
3- \vec{R}

$$R_x = A_x + B_x + C_x + D_x + E_x$$

$$= 8 + 3 + -20 + -3 + 0 = -12 \text{ m}$$

$$R_y = A_y + B_y + C_y + D_y + E_y$$

$$= 6 + -4 + 20 + 0 + 4 = 26 \text{ m}$$



$$\tan \phi = \frac{|R_y|}{|R_x|} = \frac{26}{12} =$$

$$\phi \approx 65.22^\circ$$

$$\theta = 180 - \phi = 180 - 65.22$$

$$\approx 114.8^\circ$$

$\therefore \vec{R} = 28.64 \text{ m}, 114.8^\circ$

Ex 20

$$\vec{A} = 3\hat{i} - 4\hat{j} + 3\hat{k} \text{ m} \rightarrow |\vec{A}| = \sqrt{9+16+9} = \sqrt{34} \text{ m}$$

$$\vec{B} = 3\hat{i} - 4\hat{j} \text{ m} \rightarrow |\vec{B}| = \sqrt{9+16} = 5 \text{ m}$$

$$\vec{C} = -5\hat{j} - 6\hat{k} \text{ m} \rightarrow |\vec{C}| = \sqrt{25+36} = \sqrt{61} \text{ m}$$

$$1- \vec{A} \cdot \vec{B} = A_x B_x + A_y B_y + A_z B_z = 9 + 16 = 25$$

$$2- \vec{B} \cdot \vec{A} = B_x A_x + B_y A_y + B_z A_z = 9 + 16 = 25$$

$$3- \vec{A} \cdot \vec{A} = A^2 = A_x A_x + A_y A_y + A_z A_z = 9 + 16 + 9 = 34$$

$$4- \vec{C} \cdot \vec{B} = C_x B_x + C_y B_y + C_z B_z = 0 + 20 + 0 = 20$$

$$5- -2\vec{A} \cdot 3\vec{C} = (-6)(0) + (8)(15) + (3)(-18)$$

$$= 0 + 120 + 108 = 228$$

$$6- \vec{A} \cdot \vec{B} = A B \cos \alpha$$

$$25 = (\sqrt{34})(5) \cos \alpha \rightarrow \alpha = \cos^{-1} \frac{5}{\sqrt{34}} = 31^\circ$$

$$7- \vec{A} \cdot \vec{C} = A C \cos \alpha$$

$$(3)(0) + (-4)(-5) + (3)(-6) = (\sqrt{34})(\sqrt{61}) \cos \alpha$$

$$\alpha = \cos^{-1} \frac{2}{(\sqrt{61})(\sqrt{34})} = 87.5^\circ$$

$$8- \vec{A} \cdot \hat{k} = |\vec{A}| |\hat{k}| \cos \alpha$$

$$3 = (\sqrt{34})(1) \cos \alpha$$

$$\alpha = \cos^{-1} \frac{3}{\sqrt{34}} = 59^\circ$$

$$9 - \vec{C} \cdot \vec{D} = |\vec{C}| |\vec{D}| \cos \alpha$$

$$\alpha = \sqrt{61} \cos \alpha$$

$$\alpha = \cos^{-1} 0 = 90^\circ$$

$$10 - \vec{A} \cdot \vec{D} \Rightarrow A_x D_x + A_y D_y + A_z D_z = |A| |\vec{D}| \cos 90^\circ$$

$$(3)(0) + (-4)(-5) + (3)\beta = 0$$

$$0 + 20 + 3\beta = 0$$

$$\beta = -\frac{20}{3}$$

Ex 21 $\vec{A} = 3\hat{i} - 4\hat{j} + 3\hat{k} \text{ m}$

$$\vec{B} = 3\hat{i} - 4\hat{j} \text{ m}$$

$$\vec{C} = -5\hat{j} - 6\hat{k} \text{ m}$$

$$1 - \vec{A} \times \vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & -4 & 3 \\ 3 & -4 & 0 \end{vmatrix}$$

$$= \hat{i}(0+12) - \hat{j}(0-9) + \hat{k}(-12+12)$$

$$= 12\hat{i} + 9\hat{j}$$

$$2 - \vec{B} \times \vec{A} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & -4 & 0 \\ 3 & -1 & 3 \end{vmatrix}$$

$$= \hat{i} (-12 - 0) - \hat{j} (9 - 0) + \hat{k} (-12 + 12)$$

$$= -12\hat{i} - 9\hat{j}$$

$$3 - \vec{A} \times \vec{A} = |\vec{A}| |\vec{A}| \sin 0 = 0$$

$$4 - \vec{C} \times \vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & -5 & -6 \\ 3 & -1 & 0 \end{vmatrix}$$

$$= \hat{i} (0 - 24) - \hat{j} (0 + 15) + \hat{k} (0 + 15)$$

$$= -24\hat{i} - 15\hat{j} + 15\hat{k}$$

$$5 - 2\hat{c} \times 2\vec{B} = 2\hat{c} \times [6\hat{i} - 8\hat{j}] = 0 - 24\hat{k}$$

$$\therefore (3\hat{c} \times 2\vec{B}) - 3\vec{c}$$

$$-24\hat{k} - (-15\hat{j} - 18\hat{k}) = 15\hat{j} - 6\hat{k}$$