

HElib (Detailed Description)

by

1. Basheir khan (FALL-16/RIS-007)
2. Sahibzada Shuja (FALL-16/RIS-015)

HElib

Implementing Homomorphic Encryption

AltCRT Class Reference

Alternative implementation of integer polynomials.

```
#include <AltCRT.h>
```

Public Member Functions

	AltCRT (const AltCRT &other)
	AltCRT (const ZZX &poly, const FHEcontext &_context, const IndexSet &indexSet)
	AltCRT (const ZZX &poly, const FHEcontext &_context)
	AltCRT (const ZZX &poly)
	AltCRT (const FHEcontext &_context, const IndexSet &indexSet)
	AltCRT (const FHEcontext &_context)
AltCRT &	operator= (const AltCRT &other)
AltCRT &	operator= (const ZZX &poly)
AltCRT &	operator= (const ZZ &num)
AltCRT &	operator= (const long num)

long	getOneRow (Vec< long > &row, long idx, bool positive=false) const Get one row of a polynomial.
long	getOneRow (zz_pX &row, long idx) const
void	toPoly (ZZX &p, const IndexSet &s, bool positive=false) const
void	toPoly (ZZX &p, bool positive=false) const
bool	operator== (const AltCRT &other) const
bool	operator!= (const AltCRT &other) const
AltCRT &	SetZero ()
AltCRT &	SetOne ()
void	breakIntoDigits (vector< AltCRT > &dgts, long n) const
void	addPrimes (const IndexSet &s1)
double	addPrimesAndScale (const IndexSet &s1)
void	removePrimes (const IndexSet &s1)
AltCRT &	Negate (const AltCRT &other)
AltCRT &	Negate ()
AltCRT &	operator+= (const AltCRT &other)

AltCRT &	operator+= (const ZZX &poly)
AltCRT &	operator+= (const ZZ &num)
AltCRT &	operator+= (long num)
AltCRT &	operator-= (const AltCRT &other)
AltCRT &	operator-= (const ZZX &poly)
AltCRT &	operator-= (const ZZ &num)
AltCRT &	operator-= (long num)
AltCRT &	operator++ ()
AltCRT &	operator-- ()
void	operator++ (int)
void	operator-- (int)
AltCRT &	operator*= (const AltCRT &other)
AltCRT &	operator*= (const ZZX &poly)
AltCRT &	operator*= (const ZZ &num)
AltCRT &	operator*= (long num)
void	Add (const AltCRT &other, bool matchIndexSets=true)

void	Sub (const AltCRT &other, bool matchIndexSets=true)
void	Mul (const AltCRT &other, bool matchIndexSets=true)
AltCRT &	operator/= (const ZZ &num)
AltCRT &	operator/= (long num)
void	Exp (long k)
void	automorph (long k)
AltCRT &	operator>>= (long k)
const FHEcontext &	getContext () const
const IndexMap < zz_pX > &	getMap () const
const IndexSet &	getIndexSet () const
void	randomize (const ZZ *seed=NULL)
void	sampleSmall ()
void	sampleHWt (long Hwt)
void	sampleGaussian (double stdev=0.0)
void	sampleUniform (const ZZ &B)
void	scaleDownToSet (const IndexSet &s, long ptxtSpace)

void **reduce** () const

Friends

ostream & **operator<<** (ostream &s, const [AltCRT](#) &d)

istream & **operator>>** (istream &s, [AltCRT](#) &d)

Detailed Description

Alternative implementation of integer polynomials.

The documentation for this class was generated from the following files:

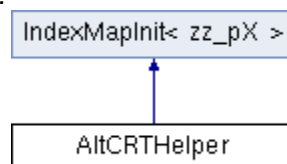
- src/[AltCRT.h](#)
- src/AltCRT.cpp

AltCRTHelper Class Reference

A helper class to enforce consistency within an [AltCRTHelper](#) object

```
#include <AltCRT.h>
```

Inheritance diagram for AltCRTHelper:



Public Member Functions

	AltCRTHelper (const FHEcontext &context)
virtual void	init (zz_pX &v)
	Initialization function, override with initialization code.
virtual IndexMapInit < zz_pX > *	clone () const
	Cloning a pointer, override with code to create a fresh copy.

Detailed Description

A helper class to enforce consistency within an [AltCRTHelper](#) object.

See Section 2.6.2 of the design document ([IndexMap](#))

The documentation for this class was generated from the following file:

- src/[AltCRT.h](#)
-

BipartiteGraph Class Reference

A bipartite flow graph.

```
#include <matching.h>
```

Public Member Functions

void	addEdge (long from, long to, long label, long color=0)
------	---

void	partitionToMatchings ()
------	--------------------------------

void	printout ()
------	--------------------

Public Attributes

vector< LabeledVertex >	left
---	-------------

Detailed Description

A bipartite flow graph.

The documentation for this class was generated from the following files:

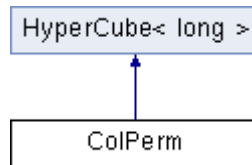
- src/[matching.h](#)
- src/matching.cpp

ColPerm Class Reference

Permuting a single dimension (column) of a hypercube. [More...](#)

```
#include <permutations.h>
```

Inheritance diagram for ColPerm:



Public Member Functions

	ColPerm (const CubeSignature &_sig)
long	getPermDim () const
void	setPermDim (long _dim)
void	makeExplicit (Permut &out) const
long	getShiftAmounts (Permut &out) const
void	getBenesShiftAmounts (Vec< Permut > &out, Vec< bool > &idID, const Vec< long > &benesLvls) const
void	printout (ostream &s)
	A test/debugging method.

► Public Member Functions inherited from [HyperCube< long >](#)

Detailed Description

Permuting a single dimension (column) of a hypercube.

[ColPerm](#) is derived from a [HyperCube<long>](#), and it uses the cube object to store the actual permutation data. The interpretation of this data, however, depends on the data member dim.

The cube is partitioned into columns of size $n = \text{getDim}(\text{dim})$: a single column consists of the n entries whose indices i have the same coordinates in all dimensions other than dim . The entries in any such column form a permutation on $[0..n)$.

For a given [ColPerm](#) perm, one way to access each column is as follows: for slice_index = [0..perm.getProd(0, dim)) [CubeSlice](#) slice(perm, slice_index, dim) for col_index = [0..perm.getProd(dim+1)) getHyperColumn(column, slice, col_index)

Another way is to use the getCoord and addCoord methods.

For example, permuting a 2x3x2 cube along dim=1 (the 2nd dimension), we could have the data vector as [1 1 0 2 2 0 2 0 1 1 0 2]. This means the four columns are permuted by the permutations [1 0 2] [1 2 0] [2 1 0] [0 1 2]. Written explicitly, we get: [2 3 0 5 4 1 10 7 8 9 6 11].

Another representation that we provide is by "shift amount": how many slots each element needs to move inside its small permutation. For the example above, this will be: [1 -1 0] [2 -1 -1] [2 0 -2] [0 0 0] so we write the permutation as [1 1 -1 1 0 -2 2 0 0 0 -2 0].

Member Function Documentation

```
void ColPerm::getBenesShiftAmounts ( Vec< Permut > & out,  
                                     Vec< bool > & idID,  
                                     const Vec< long > & benesLvls  
                                     ) const
```

Get multiple layers of a Benes permutation network. Returns in out[i][j] the shift amount to move item j in the i'th layer. Also isID[i]=true if the i'th layer is the identity (i.e., contains only 0 shift amounts).

```
long ColPerm::getShiftAmounts ( Permut & out ) const
```

For each position in the data vector, compute how many slots it should be shifted inside its small permutation. Returns zero if all the shift amount are zero, nonzero values otherwise.

The documentation for this class was generated from the following files:

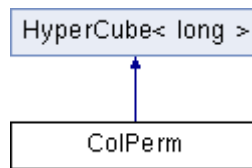
- src/[permutations.h](#)
- src/permutations.cpp

ColPerm Class Reference

Permuting a single dimension (column) of a hypercube.

```
#include <permutations.h>
```

Inheritance diagram for ColPerm:



Public Member Functions

	ColPerm (const CubeSignature &_sig)
long	getPermDim () const
void	setPermDim (long _dim)
void	makeExplicit (Permut &out) const
long	getShiftAmounts (Permut &out) const
void	getBenesShiftAmounts (Vec< Permut > &out, Vec< bool > &idID, const Vec< long > &benesLvls) const
void	printout (ostream &s)
	A test/debugging method.

► Public Member Functions inherited from [HyperCube< long >](#)

Detailed Description

Permuting a single dimension (column) of a hypercube.

[ColPerm](#) is derived from a [HyperCube<long>](#), and it uses the cube object to store the actual permutation data. The interpretation of this data, however, depends on the data member dim.

The cube is partitioned into columns of size $n = \text{getDim}(\text{dim})$: a single column consists of the n entries whose indices i have the same coordinates in all dimensions other than dim . The entries in any such column form a permutation on $[0..n)$.

For a given [ColPerm](#) perm, one way to access each column is as follows: for $\text{slice_index} = [0..\text{perm.getProd}(0, \text{dim})]$ [CubeSlice](#) slice(perm, slice_index, dim) for $\text{col_index} = [0..\text{perm.getProd}(\text{dim}+1)]$ getHyperColumn(column, slice, col_index)

Another way is to use the getCoord and addCoord methods.

For example, permuting a 2x3x2 cube along $\text{dim}=1$ (the 2nd dimension), we could have the data vector as $[1\ 1\ 0\ 2\ 2\ 0\ 2\ 0\ 1\ 1\ 0\ 2]$. This means the four columns are permuted by the permutations $[1\ 0\ 2][1\ 2\ 0][2\ 1\ 0][0\ 1\ 2]$. Written explicitly, we get: $[2\ 3\ 0\ 5\ 4\ 1\ 10\ 7\ 8\ 9\ 6\ 11]$.

Another representation that we provide is by "shift amount": how many slots each element needs to move inside its small permutation. For the example above, this will be: $[1\ -1\ 0][2\ -1\ -1][2\ 0\ -2][0\ 0\ 0]$ so we write the permutation as $[1\ 1\ -1\ 1\ 0\ -2\ 2\ 0\ 0\ 0\ -2\ 0]$.

Member Function Documentation

```
void ColPerm::getBenesShiftAmounts ( Vec< Permut > & out,
                                     Vec< bool > & idID,
                                     const Vec< long > & benesLvls
                                     ) const
```

Get multiple layers of a Benes permutation network. Returns in $\text{out}[i][j]$ the shift amount to move item j in the i 'th layer. Also $\text{idID}[i]=\text{true}$ if the i 'th layer is the identity (i.e., contains only 0 shift amounts).

```
long ColPerm::getShiftAmounts ( Permut & out ) const
```

For each position in the data vector, compute how many slots it should be shifted inside its small permutation. Returns zero if all the shift amount are zero, nonzero values otherwise.

The documentation for this class was generated from the following files:

- src/[permutations.h](#)
- src/permutations.cpp

Ctxt Class Reference

A [Ctxt](#) object holds a single ciphertext. [More...](#)

```
#include <Ctxt.h>
```

Public Member Functions

	Ctxt (const FHEPubKey &newPubKey, long newPtxtSpace=0)
	Ctxt (ZeroCtxtLike_type, const Ctxt &ctxt)
void	DummyEncrypt (const ZZx &ptxt, double size=-1.0)
	Dummy encryption, just encodes the plaintext in a Ctxt object.
Ctxt &	operator= (const Ctxt &other)
bool	operator== (const Ctxt &other) const
bool	operator!= (const Ctxt &other) const
bool	equalsTo (const Ctxt &other, bool comparePkeys=true) const
Ciphertext arithmetic	
void	negate ()
Ctxt &	operator+= (const Ctxt &other)
Ctxt &	operator-= (const Ctxt &other)
void	addCtxt (const Ctxt &other, bool negative=false)
Ctxt &	operator*= (const Ctxt &other)

void	automorph (long k)
Ctxt &	operator>>= (long k)
void	smartAutomorph (long k)
	automorphism with re-linearization
void	frobeniusAutomorph (long j)
	applies the automorphism p^j using smartAutomorphism
void	addConstant (const DoubleCRT &dcrt, double size=-1.0)
void	addConstant (const ZZx &poly, double size=-1.0)
void	addConstant (const ZZ &c)
void	multByConstant (const DoubleCRT &dcrt, double size=-1.0)
void	multByConstant (const ZZx &poly, double size=-1.0)
void	multByConstant (const ZZ &c)
void	divideByP ()
void	multByP (long e=1)
void	divideBy2 ()
void	extractBits (vector< Ctxt > &bits, long nBits2extract=0)
void	multiplyBy (const Ctxt &other)

void	multiplyBy2 (const Ctxt &other1, const Ctxt &other2)
void	square ()
void	cube ()

Ciphertext maintenance

Reduce plaintext space to a divisor of the original plaintext space

void	reducePtxtSpace (long newPtxtSpace)
void	reLinearize (long keyIdx=0)
void	cleanUp ()
void	reduce () const
void	blindCtxt (const ZZx &poly) Add a high-noise encryption of the given constant.
xdouble	modSwitchAddedNoiseVar () const Estimate the added noise variance.
long	findBaseLevel () const Find the "natural level" of a ciphertext. More...
void	modUpToSet (const IndexSet &s) Modulus-switching up (to a larger modulus). Must have primeSet <= s, and s must contain either all the special primes or none of them.
void	modDownToSet (const IndexSet &s)

	Modulus-switching down (to a smaller modulus). mod-switch down to primeSet s, after this call we have primeSet<=s. s must contain either all special primes or none of them.
void	<u>modDownToLevel</u> (long lvl)
	Modulus-switching down.
double	<u>rawModSwitch</u> (vector< ZZX > &zzParts, long toModulus) const
	Special-purpose modulus-switching for bootstrapping.
void	<u>findBaseSet</u> (<u>IndexSet</u> &s) const
	Find the "natural prime-set" of a cipehrtext. Find the highest <u>IndexSet</u> so that mod-switching down to that set results in the dominant noise term being the additive term due to rounding.
void	<u>evalPoly</u> (const ZZX &poly)
	compute the power X, X^2, \dots, X^n
Utility methods	
void	clear ()
bool	<u>isEmpty</u> () const
	Is this an empty cipehrtext without any parts.
bool	<u>inCanonicalForm</u> (long keyID=0) const
	A canonical cipherttext has (at most) handles pointing to (1,s)
bool	<u>isCorrect</u> () const
	Would this cipherttext be decrypted without errors?

const FHEContext &	getContext () const
const FHEPubKey &	getPubKey () const
const IndexSet &	getPrimeSet () const
const xdouble &	getNoiseVar () const
const long	getPtxtSpace () const
const long	getKeyID () const
const long	effectiveR () const
double	log_of_ratio () const
	Returns $\log(\text{noise-variance})/2 - \log(q)$

Friends

class	FHEPubKey
class	FHESecKey
istream &	operator>> (istream &str, Ctxt &ctxt)
ostream &	operator<< (ostream &str, const Ctxt &ctxt)

Detailed Description

A [Ctxt](#) object holds a single ciphertext.

The class [Ctxt](#) includes a `vector<CtxtPart>`: For a [Ctxt](#) `c`, `c[i]` is the *i*'th ciphertext part, which can be used also as a [DoubleCRT](#) object (since [CtxtPart](#) is derived from [DoubleCRT](#)). By convention, `c[0]`, the first [CtxtPart](#) object in the vector, has `skHndl` that points to 1 (i.e., it is just added in upon decryption, without being multiplied by anything). We maintain the invariance that all the parts of a ciphertext are defined relative to the same set of primes.

A ciphertext contains also pointers to the general parameters of this FHE instance and the public key, and an estimate of the noise variance. The noise variance is determined by the norm of the canonical embedding of the noise polynomials, namely their evaluations in roots of the ring polynomial (which are the complex primitive roots of unity). We consider each such evaluation point as a random variable, and estimate the variances of these variables. This estimate is heuristic, assuming that various quantities "behave like independent random variables". The variance is added on addition, multiplied on multiplications, remains unchanged for automorphism, and is roughly scaled down by mod-switching with some added factor, and similarly scaled up by key-switching with some added factor. The `noiseVar` data member of the class keeps the estimated variance.

Member Function Documentation

void Ctxt::divideByP ()

Divide a ciphertext by p , for plaintext space p^r , $r > 1$. It is assumed that the ciphertext encrypts a polynomial which is zero mod p . If this is not the case then the result will not be a valid ciphertext anymore. As a side-effect, the plaintext space is reduced from p^r to p^{r-1} .

void Ctxt::evalPoly (const ZZx & poly)

compute the power X, X^2, \dots, X^n

Evaluate the cleartext poly on the encrypted ciphertext

long Ctxt::findBaseLevel () const

Find the "natural level" of a ciphertext.

How many levels in the "base-set" for that ciphertext.

void Ctxt::multByP (long e = 1)

inline

Multiply ciphertext by p^e , for plaintext space p^r . This also has the side-effect of increasing the plaintext space to p^{r+e} .

```
double Ctxt::rawModSwitch ( vector< ZZx > & zzParts,  
                           long           toModulus  
                           )           Const
```

Special-purpose modulus-switching for bootstrapping.

Mod-switch to an externally-supplied modulus. The modulus need not be in the moduli-chain in the context, and does not even need to be a prime. The ciphertext *this is not affected, instead the result is returned in the zzParts vector, as a vector of ZZx'es. Returns an estimate for the noise variance after mod-switching.

The documentation for this class was generated from the following files:

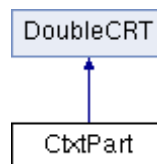
- src/[Ctxt.h](#)
- src/Ctxt.bak.cpp
- src/Ctxt.cpp

CtxtPart Class Reference

One entry in a ciphertext vector.

```
#include <Ctxt.h>
```

Inheritance diagram for CtxtPart:



Public Member Functions

bool	operator== (const CtxtPart &other) const
------	---

bool	operator!= (const CtxtPart &other) const
------	---

	CtxtPart (const FHEcontext &_context)
	CtxtPart (const FHEcontext &_context, const IndexSet &s)
	CtxtPart (const FHEcontext &_context, const IndexSet &s, const SKHandle &otherHandle)
	CtxtPart (const DoubleCRT &other)
	CtxtPart (const DoubleCRT &other, const SKHandle &otherHandle)

► Public Member Functions inherited from [DoubleCRT](#)

Public Attributes

SKHandle	skHandle
	The handle is a public data member.

Detailed Description

One entry in a ciphertext vector.

A ciphertext part consists of a polynomial (element of the ring R_Q) and a handle to the corresponding secret-key polynomial.

The documentation for this class was generated from the following files:

- src/[Ctxt.h](#)
- src/Ctxt.bak.cpp
- src/Ctxt.cpp

CubeSignature Class Reference

Holds a vector of dimensions for a hypercube and some additional data.

```
#include <hypercube.h>
```

Public Member Functions

	CubeSignature (const Vec< long > &_dims)
	CubeSignature (const PAlgebra &alg)
	Build a CubeSignature to reflect the hypercube structure of $Z_m^* / (p)$
void	initSignature (const Vec< long > &_dims)
long	getSize () const
	total size of cube
long	getNumDims () const
	number of dimensions
long	getDim (long d) const
	size of dimension d
long	getProd (long d) const
	product of sizes of dimensions d, d+1, ...
long	getProd (long from, long to) const
	product of sizes of dimensions from, from+1, ..., to-1
long	getCoord (long i, long d) const
	get coordinate in dimension d of index i

long	<code>addCoord</code> (long i, long d, long offset) const
	add offset to coordinate in dimension d of index i
long	<code>numSlices</code> (long d=1) const
	number of slices
long	<code>sliceSize</code> (long d=1) const
	size of one slice
long	<code>numCols</code> () const
	number of columns

Friends

ostream &	<code>operator<<</code> (ostream &s, const <code>CubeSignature</code> &sig)
-----------	--

Detailed Description

Holds a vector of dimensions for a hypercube and some additional data.

The documentation for this class was generated from the following files:

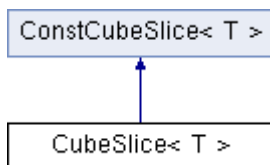
- src/[`hypercube.h`](#)
- src/PAlgebra.cpp

CubeSlice< T > Class Template Reference

A lower-dimension slice of a hypercube.

```
#include <hypercube.h>
```

Inheritance diagram for `CubeSlice< T >`:



Public Member Functions

	CubeSlice (HyperCube < T > &_cube)
	CubeSlice (Vec< T > &_data, const CubeSignature &_sig)
	CubeSlice (const CubeSlice < T > &bigger, long i, long _dimOffset=1)
	CubeSlice (HyperCube < T > &_cube, long i, long _dimOffset=1)
void	copy (const ConstCubeSlice < T > &other) const
T &	at (long i) const
T &	operator[] (long i) const

► Public Member Functions inherited from [ConstCubeSlice< T >](#)

Detailed Description

```
template<class T>
class CubeSlice< T >
```

A lower-dimension slice of a hypercube.

The documentation for this class was generated from the following files:

- [src/hypercube.h](#)
- [src/hypercube.cpp](#)

deep_clone< X > Class Template Reference

Deep copy: initialize with clone.

```
#include <cloned\_ptr.h>
```

Static Public Member Functions

static X *	apply (const X *x)
------------	---------------------------

Detailed Description

```
template<class X>  
class deep_clone< X >
```

Deep copy: initialize with clone.

Template Parameters

X The class to which this points

The documentation for this class was generated from the following file:

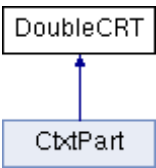
- [src/cloned_ptr.h](#)

DoubleCRT Class Reference

Implementatigs polynomials (elements in the ring R_Q) in double-CRT form.


```
#include <DoubleCRT.h>
```

Inheritance diagram for DoubleCRT:



Public Member Functions

	DoubleCRT (const ZZ X &poly, const FHEcontext &_context, const IndexSet &indexSet)
	Initializing DoubleCRT from a ZZ X polynomial.
	DoubleCRT (const ZZ X &poly, const FHEcontext &_context)
	DoubleCRT (const ZZ X &poly)
	Context is not specified, use the "active context".
	DoubleCRT (const FHEcontext &_context)
	DoubleCRT (const FHEcontext &_context, const IndexSet &indexSet)
	Also specify the IndexSet explicitly.
DoubleCRT &	operator= (const DoubleCRT &other)
DoubleCRT &	operator= (const ZZ X &poly)
DoubleCRT &	operator= (const ZZ &num)
DoubleCRT &	operator= (const long num)
long	getOneRow (Vec< long > &row, long idx, bool positive=false)

	const
	Get one row of a polynomial.
long	getOneRow (zz_pX &row, long idx) const
void	toPoly (ZZX &p, const IndexSet &s, bool positive=false) const
	Recovering the polynomial in coefficient representation. This yields an integer polynomial with coefficients in $[-P/2, P/2]$, unless the positive flag is set to true, in which case we get coefficients in $[0, P-1]$ (P is the product of all moduli used). Using the optional IndexSet param we compute the polynomial reduced modulo the product of only the primes in that set.
void	toPoly (ZZX &p, bool positive=false) const
bool	operator== (const DoubleCRT &other) const
bool	operator!= (const DoubleCRT &other) const
DoubleCRT &	SetZero ()
DoubleCRT &	SetOne ()
void	breakIntoDigits (vector< DoubleCRT > &dgts, long n) const
	Break into n digits, according to the primeSets in context.digits. See Section 3.1.6 of the design document (re-linearization)
void	addPrimes (const IndexSet &s1)
	Expand the index set by s1. It is assumed that s1 is disjoint from the current index set.

double	addPrimesAndScale (const IndexSet &s1)
	Expand index set by s1, and multiply by $\text{Prod}_{\{q \text{ in } s1\}}$. s1 is disjoint from the current index set, returns $\log(\text{product})$.
void	removePrimes (const IndexSet &s1)
	Remove s1 from the index set.
const FHEcontext &	getContext () const
const IndexMap < vec_long > &	getMap () const
const IndexSet &	getIndexSet () const
void	randomize (const ZZ *seed=NULL)
	Fills each row i with random ints mod pi, uses NTL's PRG.
void	sampleSmall ()
	Coefficients are -1/0/1, Prob[0]=1/2.
void	sampleHWt (long Hwt)
	Coefficients are -1/0/1 with pre-specified number of nonzeros.
void	sampleGaussian (double stdev=0.0)
	Coefficients are Gaussians.
void	sampleUniform (const ZZ &B)
	Coefficients are uniform in [-B..B].
void	scaleDownToSet (const IndexSet &s, long ptxtSpace)

void	FFT (const ZZ \mathbb{X} &poly, const IndexSet &s)
------	---

void	reduce () const
------	------------------------

Arithmetic operation

Only the "destructive" versions are used, i.e., $a += b$ is implemented but not $a + b$.

DoubleCRT &	Negate (const DoubleCRT &other)
-----------------------------	--

DoubleCRT &	Negate ()
-----------------------------	------------------

DoubleCRT &	operator+= (const DoubleCRT &other)
-----------------------------	--

DoubleCRT &	operator+= (const ZZ \mathbb{X} &poly)
-----------------------------	---

DoubleCRT &	operator+= (const ZZ &num)
-----------------------------	-----------------------------------

DoubleCRT &	operator+= (long num)
-----------------------------	------------------------------

DoubleCRT &	operator-= (const DoubleCRT &other)
-----------------------------	--

DoubleCRT &	operator-= (const ZZ \mathbb{X} &poly)
-----------------------------	---

DoubleCRT &	operator-= (const ZZ &num)
-----------------------------	-----------------------------------

DoubleCRT &	operator-= (long num)
-----------------------------	------------------------------

DoubleCRT &	operator++ ()
-----------------------------	----------------------

DoubleCRT &	operator-- ()
-----------------------------	----------------------

void	operator++ (int)
------	-------------------------

	void	operator-- (int)
	DoubleCRT &	operator*= (const DoubleCRT &other)
	DoubleCRT &	operator*= (const ZZX &poly)
	DoubleCRT &	operator*= (const ZZ &num)
	DoubleCRT &	operator*= (long num)
	void	Add (const DoubleCRT &other, bool matchIndexSets=true)
	void	Sub (const DoubleCRT &other, bool matchIndexSets=true)
	void	Mul (const DoubleCRT &other, bool matchIndexSets=true)
	DoubleCRT &	operator/= (const ZZ &num)
	DoubleCRT &	operator/= (long num)
	void	Exp (long k)
		Small-exponent polynomial exponentiation.
	void	automorph (long k)
	DoubleCRT &	operator>>= (long k)

Friends

ostream &	operator<< (ostream &s, const DoubleCRT &d)
istream &	operator>> (istream &s, DoubleCRT &d)

Detailed Description

Implementatigs polynomials (elements in the ring R_Q) in double-CRT form.

Double-CRT form is a matrix of L rows and $\phi(m)$ columns. The i 'th row contains the FFT of the element wrt the i th prime, i.e. the evaluations of the polynomial at the primitive m th roots of unity mod the i th prime. The polynomial thus represented is defined modulo the product of all the primes in use.

The list of primes is defined by the data member `indexMap`. `indexMap.getIndexSet()` defines the set of indices of primes associated with this [DoubleCRT](#) object: they index the primes stored in the associated `FHEContext`.

Arithmetic operations are computed modulo the product of the primes in use and also modulo $\Phi_m(X)$. Arithmetic operations can only be applied to [DoubleCRT](#) objects relative to the same context, trying to add/multiply objects that have different `FHEContext` objects will raise an error.

Constructor & Destructor Documentation

```
DoubleCRT::DoubleCRT ( const ZZx &      poly,  
                      const FHEcontext & _context,  
                      const IndexSet &   indexSet  
                      )
```

Initializing [DoubleCRT](#) from a `ZZx` polynomial.

Parameters

poly The ring element itself, zero if not specified
_context The context for this [DoubleCRT](#) object, use "current active context" if not specified
indexSet Which primes to use for this object, if not specified then use all of them

The documentation for this class was generated from the following files:

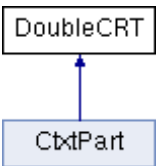
- `src/DoubleCRT.h`
- `src/DoubleCRT.cpp`

DoubleCRT Class Reference

Implementatigs polynomials (elements in the ring R_Q) in double-CRT form. [More...](#)

```
#include <DoubleCRT.h>
```

Inheritance diagram for DoubleCRT:



Public Member Functions

	DoubleCRT (const ZZ X &poly, const FHEcontext &_context, const IndexSet &indexSet)
	Initializing DoubleCRT from a ZZ X polynomial. More...
	DoubleCRT (const ZZ X &poly, const FHEcontext &_context)
	DoubleCRT (const ZZ X &poly)
	Context is not specified, use the "active context".
	DoubleCRT (const FHEcontext &_context)
	DoubleCRT (const FHEcontext &_context, const IndexSet &indexSet)
	Also specify the IndexSet explicitly.
DoubleCRT &	operator= (const DoubleCRT &other)
DoubleCRT &	operator= (const ZZ X &poly)
DoubleCRT &	operator= (const ZZ &num)

DoubleCRT &	operator= (const long num)
long	getOneRow (Vec< long > &row, long idx, bool positive=false) const
	Get one row of a polynomial.
long	getOneRow (zz_pX &row, long idx) const
void	toPoly (ZZX &p, const IndexSet &s, bool positive=false) const
	Recovering the polynomial in coefficient representation. This yields an integer polynomial with coefficients in $[-P/2, P/2]$, unless the positive flag is set to true, in which case we get coefficients in $[0, P-1]$ (P is the product of all moduli used). Using the optional IndexSet param we compute the polynomial reduced modulo the product of only the ptimes in that set.
void	toPoly (ZZX &p, bool positive=false) const
bool	operator== (const DoubleCRT &other) const
bool	operator!= (const DoubleCRT &other) const
DoubleCRT &	SetZero ()
DoubleCRT &	SetOne ()
void	breakIntoDigits (vector< DoubleCRT > &dgts, long n) const
	Break into n digits, according to the primeSets in context.digits. See Section 3.1.6 of the design document (re-linearization)

void	addPrimes (const IndexSet &s1)
	Expand the index set by s1. It is assumed that s1 is disjoint from the current index set.
double	addPrimesAndScale (const IndexSet &s1)
	Expand index set by s1, and multiply by $\text{Prod}_{\{q \text{ in } s1\}}$. s1 is disjoint from the current index set, returns $\log(\text{product})$.
void	removePrimes (const IndexSet &s1)
	Remove s1 from the index set.
const FHEcontext &	getContext () const
const IndexMap < vec_long > &	getMap () const
const IndexSet &	getIndexSet () const
void	randomize (const ZZ *seed=NULL)
	Fills each row i with random ints mod pi, uses NTL's PRG.
void	sampleSmall ()
	Coefficients are -1/0/1, Prob[0]=1/2.
void	sampleHWt (long Hwt)
	Coefficients are -1/0/1 with pre-specified number of nonzeros.
void	sampleGaussian (double stdev=0.0)
	Coefficients are Gaussians.

void	sampleUniform (const ZZ &B)
	Coefficients are uniform in [-B..B].
void	scaleDownToSet (const IndexSet &s, long ptxtSpace)
void	FFT (const ZZx &poly, const IndexSet &s)
void	reduce () const

Arithmetic operation

Only the "destructive" versions are used, i.e., $a += b$ is implemented but not $a + b$.

DoubleCRT &	Negate (const DoubleCRT &other)
DoubleCRT &	Negate ()
DoubleCRT &	operator+= (const DoubleCRT &other)
DoubleCRT &	operator+= (const ZZx &poly)
DoubleCRT &	operator+= (const ZZ &num)
DoubleCRT &	operator+= (long num)
DoubleCRT &	operator-= (const DoubleCRT &other)
DoubleCRT &	operator-= (const ZZx &poly)
DoubleCRT &	operator-= (const ZZ &num)
DoubleCRT &	operator-= (long num)
DoubleCRT &	operator++ ()

<u>DoubleCRT</u> &	operator-- ()
void	operator++ (int)
void	operator-- (int)
<u>DoubleCRT</u> &	operator*= (const <u>DoubleCRT</u> &other)
<u>DoubleCRT</u> &	operator*= (const ZZx &poly)
<u>DoubleCRT</u> &	operator*= (const ZZ &num)
<u>DoubleCRT</u> &	operator*= (long num)
void	Add (const <u>DoubleCRT</u> &other, bool matchIndexSets=true)
void	Sub (const <u>DoubleCRT</u> &other, bool matchIndexSets=true)
void	Mul (const <u>DoubleCRT</u> &other, bool matchIndexSets=true)
<u>DoubleCRT</u> &	operator/= (const ZZ &num)
<u>DoubleCRT</u> &	operator/= (long num)
void	<u>Exp</u> (long k)
	Small-exponent polynomial exponentiation.
void	automorph (long k)
<u>DoubleCRT</u> &	operator>>= (long k)

Friends

ostream &	operator<< (ostream &s, const DoubleCRT &d)
-----------	--

istream &	operator>> (istream &s, DoubleCRT &d)
-----------	--

Detailed Description

Implementatigs polynomials (elements in the ring R_Q) in double-CRT form.

Double-CRT form is a matrix of L rows and $\phi(m)$ columns. The i 'th row contains the FFT of the element wrt the i th prime, i.e. the evaluations of the polynomial at the primitive m th roots of unity mod the i th prime. The polynomial thus represented is defined modulo the product of all the primes in use.

The list of primes is defined by the data member `indexMap`. `indexMap.getIndexSet()` defines the set of indices of primes associated with this [DoubleCRT](#) object: they index the primes stored in the associated `FHEContext`.

Arithmetic operations are computed modulo the product of the primes in use and also modulo $\Phi_m(X)$. Arithmetic operations can only be applied to [DoubleCRT](#) objects relative to the same context, trying to add/multiply objects that have different `FHEContext` objects will raise an error.

Constructor & Destructor Documentation

```
DoubleCRT::DoubleCRT ( const ZZx &          poly,  
                      const FHEcontext & _context,  
                      const IndexSet &      indexSet  
                      )
```

Initializing [DoubleCRT](#) from a `ZZx` polynomial.

Parameters

poly The ring element itself, zero if not specified

_context The context for this [DoubleCRT](#) object, use "current active context" if not specified

indexSet Which primes to use for this object, if not specified then use all of them

The documentation for this class was generated from the following files:

- src/[DoubleCRT.h](#)
- src/DoubleCRT.cpp

DynamicCtxtPowers Class Reference

Store powers of X, compute them dynamically as needed. [More...](#)

```
#include <polyEval.h>
```

Public Member Functions

	DynamicCtxtPowers (const Ctxt &c, long nPowers)
Ctxt &	getPower (long e)
	Returns the e'th power, computing it as needed.
Ctxt &	at (long i)
	dp.at(i) and dp[i] both return the i+1st power
Ctxt &	operator[] (long i)
const vector< Ctxt > &	getVector () const
long	size () const
bool	isPowerComputed (long i)

Detailed Description

Store powers of X , compute them dynamically as needed.

The documentation for this class was generated from the following files:

- src/[polyEval.h](#)
- src/polyEval.cpp

EncryptedArray Class Reference

A simple wrapper for a smart pointer to an [EncryptedArrayBase](#). This is the interface that higher-level code should use. [More...](#)

```
#include <EncryptedArray.h>
```

Public Member Functions

	EncryptedArray (const FHEcontext &context, const ZZx &G=ZZx(1, 1))
	constructor: G defaults to the monomial X, PAlgebraMod from context
	EncryptedArray (const FHEcontext &context, const PAlgebraMod &_alMod)
	constructor: G defaults to F0, PAlgebraMod explicitly given
EncryptedArray &	operator= (const EncryptedArray &other)
template<class type >	
const EncryptedArrayDerived < type > &	getDerived (type) const
	downcast operator example: const EncryptedArrayDerived<PA_GF2>& rep = ea.getDerived(PA_GF2());

Direct access to EncryptedArrayBase methods

const FHEcontext &	getContext () const
const PAlgebraMod &	getAlMod () const
const long	getDegree () const
void	rotate (Ctxt &ctxt, long k) const
void	shift (Ctxt &ctxt, long k) const
void	rotate1D (Ctxt &ctxt, long i, long k, bool dc=false) const
void	shift1D (Ctxt &ctxt, long i, long k) const
void	mat_mul_dense (Ctxt &ctxt, const PlaintextMatrixBaseInterface &mat) const
void	mat_mul (Ctxt &ctxt, const PlaintextMatrixBaseInterface &mat) const
void	mat_mul1D (Ctxt &ctxt, const PlaintextMatrixBaseInterface &mat, long dim) const
void	mat_mul1D (Ctxt &ctxt, const PlaintextBlockMatrixBaseInterface &mat, long dim) const
void	mat_mul (Ctxt &ctxt, const PlaintextBlockMatrixBaseInterface &mat) const
void	compMat (CachedPtxtMatrix &cmat, const PlaintextMatrixBaseInterface &mat) const

void	compMat (CachedDCRTPtxtMatrix &cmat, const PlaintextMatrixBaseInterface &mat) const
void	compMat (CachedPtxtBlockMatrix &cmat, const PlaintextBlockMatrixBaseInterface &mat) const
void	compMat (CachedDCRTPtxtBlockMatrix &cmat, const PlaintextBlockMatrixBaseInterface &mat) const
void	compMat1D (CachedPtxtMatrix &cmat, const PlaintextMatrixBaseInterface &mat, long dim) const
void	compMat1D (CachedPtxtBlockMatrix &cmat, const PlaintextBlockMatrixBaseInterface &mat, long dim) const
void	compMat1D (CachedDCRTPtxtMatrix &cmat, const PlaintextMatrixBaseInterface &mat, long dim) const
void	compMat1D (CachedDCRTPtxtBlockMatrix &cmat, const PlaintextBlockMatrixBaseInterface &mat, long dim) const
void	encode (ZZX &ptxt, const vector< long > &array) const
void	encode (ZZX &ptxt, const vector< ZZX > &array) const
void	encode (ZZX &ptxt, const PlaintextArray &array) const
void	encodeUnitSelector (ZZX &ptxt, long i) const
void	decode (vector< long > &array, const ZZX &ptxt) const

void	decode (vector< ZZX > &array, const ZZX &ptxt) const
void	decode (PlaintextArray &array, const ZZX &ptxt) const
void	random (vector< long > &array) const
void	random (vector< ZZX > &array) const
void	encrypt (Ctxt &ctxt, const FHEPubKey &pKey, const vector< long > &ptxt) const
void	encrypt (Ctxt &ctxt, const FHEPubKey &pKey, const vector< ZZX > &ptxt) const
void	encrypt (Ctxt &ctxt, const FHEPubKey &pKey, const PlaintextArray &ptxt) const
void	decrypt (const Ctxt &ctxt, const FHESecKey &sKey, vector< long > &ptxt) const
void	decrypt (const Ctxt &ctxt, const FHESecKey &sKey, vector< ZZX > &ptxt) const
void	decrypt (const Ctxt &ctxt, const FHESecKey &sKey, PlaintextArray &ptxt) const
void	skEncrypt (Ctxt &ctxt, const FHESecKey &sKey, const vector< long > &ptxt, long skIdx=0) const
void	skEncrypt (Ctxt &ctxt, const FHESecKey &sKey, const vector< ZZX > &ptxt, long skIdx=0) const
void	skEncrypt (Ctxt &ctxt, const FHESecKey &sKey, const PlaintextArray &ptxt, long skIdx=0) const

	void	select (Ctxt &ctxt1, const Ctxt &ctxt2, const vector< long > &selector) const
	void	select (Ctxt &ctxt1, const Ctxt &ctxt2, const vector< ZZX > &selector) const
	void	select (Ctxt &ctxt1, const Ctxt &ctxt2, const PlaintextArray &selector) const
	void	buildLinPolyCoeffs (vector< ZZX > &C, const vector< ZZX > &L) const
	void	restoreContext () const
	void	restoreContextForG () const
	long	size () const
	long	dimension () const
	long	sizeOfDimension (long i) const
	long	nativeDimension (long i) const
	long	coordinate (long i, long k) const
	long	addCoord (long i, long k, long offset) const
template<class U >		
	void	rotate1D (vector< U > &out, const vector< U > &in, long i, long offset) const
		rotate an array by offset in the i'th dimension (output should

not alias input)

Detailed Description

A simple wrapper for a smart pointer to an [EncryptedArrayBase](#). This is the interface that higher-level code should use.

The documentation for this class was generated from the following file:

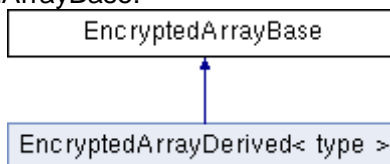
- src/[EncryptedArray.h](#)

EncryptedArrayBase Class Reference abstract

virtual class for data-movement operations on arrays of slots [More...](#)

```
#include <EncryptedArray.h>
```

Inheritance diagram for EncryptedArrayBase:



Public Member Functions

virtual EncryptedArrayBase *	clone () const =0
--	--------------------------

virtual const FHEcontext &	getContext () const =0
--	-------------------------------

virtual const long	getDegree () const =0
--------------------	------------------------------

virtual void	rotate (Ctxt &ctxt, long k) const =0
--------------	--

Right rotation as a linear array. E.g., rotating ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(n 1 2 ... n-1)

virtual void	shift (Ctxt &ctxt, long k) const =0
	Non-cyclic right shift with zero fill E.g., shifting ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(0 1 2... n-1)
virtual void	rotate1D (Ctxt &ctxt, long i, long k, bool dc=false) const =0
	right-rotate k positions along the i'th dimension More...
virtual void	shift1D (Ctxt &ctxt, long i, long k) const =0
	Right shift k positions along the i'th dimension with zero fill.
virtual void	buildLinPolyCoeffs (vector< ZZX > &C, const vector< ZZX > &L) const =0
	Linearized polynomials. L describes a linear map M by describing its action on the standard power basis: $M(x^j \bmod G) = (L[j] \bmod G)$, for $j = 0..d-1$. The result is a coefficient vector C for the linearized polynomial representing M: a polynomial h in $Z/(p^r)[X]$ of degree $< d$ is sent to .
virtual void	restoreContext () const =0
virtual void	restoreContextForG () const =0
long	size () const
	Total size (# of slots) of hypercube.
long	dimension () const
	Number of dimensions of hypercube.

long	<u>sizeOfDimension</u> (long i) const
	Size of given dimension.

bool	<u>nativeDimension</u> (long i) const
	Is rotations in given dimension a "native" operation?

long	<u>coordinate</u> (long i, long k) const
	returns coordinate of index k along the i'th dimension

long	<u>addCoord</u> (long i, long k, long offset) const
	adds offset to index k in the i'th dimension

template<class U >	
void	<u>rotate1D</u> (vector< U > &out, const vector< U > &in, long i, long offset) const
	rotate an array by offset in the i'th dimension (output should not alias input)

Matrix multiplication routines

virtual void	<u>mat_mul_dense</u> (<u>Ctxt</u> &ctxt, const <u>PlaintextMatrixBaseInterface</u> &mat) const =0
	Multiply ctx by plaintext matrix. <u>Ctxt</u> is treated as a row matrix v, and replaced by an encryption of v * mat. Optimized for dense matrices.

virtual void	compMat_dense (CachedPtxtMatrix &cmat, const <u>PlaintextMatrixBaseInterface</u> &mat) const =0
--------------	--

virtual void	compMat_dense (CachedDCRTPtxtMatrix &cmat, const <u>PlaintextMatrixBaseInterface</u> &mat) const =0
--------------	--

virtual void	mat_mul (Ctxt &ctxt, const PlaintextMatrixBaseInterface &mat) const =0
	Multiply ctx by plaintext matrix. Ctxt is treated as a row matrix v, and replaced by an encryption of $v * mat$. Optimized for sparse diagonals.
virtual void	compMat (CachedPtxtMatrix &cmat, const PlaintextMatrixBaseInterface &mat) const =0
virtual void	compMat (CachedDCRTPtxtMatrix &cmat, const PlaintextMatrixBaseInterface &mat) const =0
virtual void	mat_mul (Ctxt &ctxt, const PlaintextBlockMatrixBaseInterface &mat) const =0
	Multiply ctx by plaintext block matrix (over the base field/ring). Ctxt is treated as a row matrix v, and replaced by an encryption of $v*mat$. Optimized for sparse diagonals.
virtual void	compMat (CachedPtxtBlockMatrix &cmat, const PlaintextBlockMatrixBaseInterface &mat) const =0
virtual void	compMat (CachedDCRTPtxtBlockMatrix &cmat, const PlaintextBlockMatrixBaseInterface &mat) const =0
virtual void	mat_mul1D (Ctxt &ctxt, const PlaintextMatrixBaseInterface &mat, long dim) const =0
	Multiply ctx by plaintext matrix. Ctxt is treated as a row matrix v, and replaced by an encryption of $v * mat'$ where mat' is the block-diagonal matrix defined by mat in dimension dim. Here, mat should represent a $D \times D$ matrix, where D is the order of generator dim. We also allow dim to be one greater than the number of generators in zMStar, as if there were an implicit generator of order 1, this is convenient in some applications.

virtual void	compMat1D (CachedPtxtMatrix &cmat, const PlaintextMatrixBaseInterface &mat, long dim) const =0
virtual void	compMat1D (CachedDCRTPtxtMatrix &cmat, const PlaintextMatrixBaseInterface &mat, long dim) const =0
virtual void	mat_mul1D (Ctxt &ctxt, const PlaintextBlockMatrixBaseInterface &mat, long dim) const =0
virtual void	compMat1D (CachedPtxtBlockMatrix &cmat, const PlaintextBlockMatrixBaseInterface &mat, long dim) const =0
virtual void	compMat1D (CachedDCRTPtxtBlockMatrix &smat, const PlaintextBlockMatrixBaseInterface &mat, long dim) const =0
Encoding/decoding methods	
virtual void	encode (ZZX &ptxt, const vector< long > &array) const =0
virtual void	encode (ZZX &ptxt, const vector< ZZX > &array) const =0
virtual void	encode (ZZX &ptxt, const PlaintextArray &array) const =0
virtual void	decode (vector< long > &array, const ZZX &ptxt) const =0
virtual void	decode (vector< ZZX > &array, const ZZX &ptxt) const =0
virtual void	decode (PlaintextArray &array, const ZZX &ptxt) const =0
virtual void	random (vector< long > &array) const =0
virtual void	random (vector< ZZX > &array) const =0

long	decode1Slot (const ZZX &ptxt, long i) const
void	decode1Slot (ZZX &slot, const ZZX &ptxt, long i) const
virtual void	<u>encodeUnitSelector</u> (ZZX &ptxt, long i) const =0
	Encodes a vector with 1 at position i and 0 everywhere else.

Encoding+encryption/decryption+decoding

virtual void	encrypt (<u>Ctxt</u> &ctxt, const <u>FHEPubKey</u> &pKey, const vector< long > &ptxt) const =0
virtual void	encrypt (<u>Ctxt</u> &ctxt, const <u>FHEPubKey</u> &pKey, const vector< ZZX > &ptxt) const =0
virtual void	encrypt (<u>Ctxt</u> &ctxt, const <u>FHEPubKey</u> &pKey, const <u>PlaintextArray</u> &ptxt) const =0
virtual void	decrypt (const <u>Ctxt</u> &ctxt, const <u>FHESecKey</u> &sKey, vector< long > &ptxt) const =0
virtual void	decrypt (const <u>Ctxt</u> &ctxt, const <u>FHESecKey</u> &sKey, vector< ZZX > &ptxt) const =0
virtual void	decrypt (const <u>Ctxt</u> &ctxt, const <u>FHESecKey</u> &sKey, <u>PlaintextArray</u> &ptxt) const =0
virtual void	skEncrypt (<u>Ctxt</u> &ctxt, const <u>FHESecKey</u> &sKey, const vector< long > &ptxt, long skIdx=0) const =0
virtual void	skEncrypt (<u>Ctxt</u> &ctxt, const <u>FHESecKey</u> &sKey, const vector< ZZX > &ptxt, long skIdx=0) const =0
virtual void	skEncrypt (<u>Ctxt</u> &ctxt, const <u>FHESecKey</u> &sKey,

	const PlaintextArray &ptxt, long skIdx=0) const =0
long	decrypt1Slot (const Ctxt &ctxt, const FHESecKey &sKey, long i) const
void	decrypt1Slot (ZZX &slot, const Ctxt &ctxt, const FHESecKey &sKey, long i) const
virtual void	select (Ctxt &ctxt1, const Ctxt &ctxt2, const vector< long > &selector) const =0
	MUX: ctxt1 = ctxt1*selector + ctxt2*(1-selector)
virtual void	select (Ctxt &ctxt1, const Ctxt &ctxt2, const vector< ZZX > &selector) const =0
virtual void	select (Ctxt &ctxt1, const Ctxt &ctxt2, const PlaintextArray &selector) const =0

Detailed Description

virtual class for data-movement operations on arrays of slots

An object ea of type [EncryptedArray](#) stores information about an [FHEcontext](#) context, and a monic polynomial G. If context defines parameters m, p, and r, then ea is a helper object that supports encoding/decoding and encryption/decryption of vectors of plaintext slots over the ring $(\mathbb{Z}/(p^r)[X])/(G)$.

The polynomial G should be irreducible over $\mathbb{Z}/(p^r)$ (this is not checked). The degree of G should divide the multiplicative order of p modulo m (this is checked). Currently, the following restriction is imposed:

either $r == 1$ or $\deg(G) == 1$ or $G == \text{factors}[0]$.

ea stores objects in the polynomial ring $\mathbb{Z}/(p^r)[X]$.

Just as for the class `PAlegebraMod`, if $p == 2$ and $r == 1$, then these polynomials are represented as GF2X's, and otherwise as `zz_pX`'s. Thus, the types of these objects are not determined until run time. As such, we need to use a class heirarchy, which mirrors that of [PAlegebraMod](#), as follows.

[EncryptedArrayBase](#) is a virtual class

`EncryptedArrayDerived<type>` is a derived template class, where `type` is either `PA_GF2` or `PA_zz_p`.

The class [EncryptedArray](#) is a simple wrapper around a smart pointer to an [EncryptedArrayBase](#) object: copying an [EncryptedArray](#) object results in a "deep copy" of the underlying object of the derived class.

Member Function Documentation

```
virtual void EncryptedArrayBase::rotate1D ( Ctxt & ctxt,  
                                           long i,  
                                           long k,  
                                           bool dc = false  
                                           ) const
```

pure virtual

right-rotate `k` positions along the `i`'th dimension

Parameters

dc means "don't care", which means that the caller guarantees that only zero elements rotate off the end – this allows for some optimizations that would not otherwise be possible

Implemented in [EncryptedArrayDerived< type >](#).

The documentation for this class was generated from the following file:

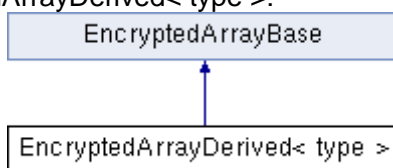
- `src/`[EncryptedArray.h](#)

EncryptedArrayDerived< type > Class Template Reference

Derived concrete implementation of [EncryptedArrayBase](#). [More...](#)

```
#include <EncryptedArray.h>
```

Inheritance diagram for EncryptedArrayDerived< type >:



Public Member Functions

	EncryptedArrayDerived (const FHEcontext &_context, const RX &_G, const PAlgebraMod &_tab)
	EncryptedArrayDerived (const EncryptedArrayDerived &other)
EncryptedArrayDerived &	operator= (const EncryptedArrayDerived &other)
virtual EncryptedArrayBase *	clone () const
const RX &	getG () const
const Mat< R > &	getNormalBasisMatrix () const
const Mat< R > &	getNormalBasisMatrixInverse () const
void	initNormalBasisMatrix () const
virtual void	restoreContext () const
virtual void	restoreContextForG () const
virtual const FHEcontext &	getContext () const
virtual const long	getDegree () const

const PAlgebraModDerived < type > &	getTab () const
virtual void	rotate (Ctxt &ctxt, long k) const
	Right rotation as a linear array. E.g., rotating ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(n 1 2 ... n-1)
virtual void	shift (Ctxt &ctxt, long k) const
	Non-cyclic right shift with zero fill E.g., shifting ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(0 1 2... n-1)
virtual void	rotate1D (Ctxt &ctxt, long i, long k, bool dc=false) const
	right-rotate k positions along the i'th dimension More...
virtual void	shift1D (Ctxt &ctxt, long i, long k) const
	Right shift k positions along the i'th dimension with zero fill.
void	rec_mul (long dim, Ctxt &res, const Ctxt &pdata, const vector< long > &idx, const PlaintextMatrixInterface < type > &mat, const vector< long > &dimx) const
virtual void	mat_mul_dense (Ctxt &ctxt, const PlaintextMatrixBaseInterface &mat) const
	Multiply ctx by plaintext matrix. Ctxt is treated as a row matrix v, and replaced by an encryption of v * mat. Optimized for dense matrices.
virtual void	compMat_dense (CachedPtxtMatrix &cmat, const PlaintextMatrixBaseInterface &mat) const
virtual void	compMat_dense (CachedDCRTPtxtMatrix &cmat,

	const PlaintextMatrixBaseInterface &mat) const
virtual void	mat_mul (Ctxt &ctxt, const PlaintextMatrixBaseInterface &mat) const
	Multiply ctx by plaintext matrix. Ctxt is treated as a row matrix v, and replaced by an encryption of $v * \text{mat}$. Optimized for sparse diagonals.
virtual void	compMat (CachedPtxtMatrix &cmat, const PlaintextMatrixBaseInterface &mat) const
virtual void	compMat (CachedDCRTPtxtMatrix &cmat, const PlaintextMatrixBaseInterface &mat) const
virtual void	mat_mul (Ctxt &ctxt, const PlaintextBlockMatrixBaseInterface &mat) const
	Multiply ctx by plaintext block matrix (over the base field/ring). Ctxt is treated as a row matrix v, and replaced by an encryption of $v * \text{mat}$. Optimized for sparse diagonals.
virtual void	compMat (CachedPtxtBlockMatrix &cmat, const PlaintextBlockMatrixBaseInterface &mat) const
virtual void	compMat (CachedDCRTPtxtBlockMatrix &cmat, const PlaintextBlockMatrixBaseInterface &mat) const
virtual void	mat_mul1D (Ctxt &ctxt, const PlaintextMatrixBaseInterface &mat, long dim) const
	Multiply ctx by plaintext matrix. Ctxt is treated as a row matrix v, and replaced by an encryption of $v * \text{mat}'$ where mat' is the block-diagonal matrix defined by mat in dimension dim. Here, mat should represent a $D \times D$

	matrix, where D is the order of generator dim. We also allow dim to be one greater than the number of generators in zMStar, as if there were an implicit generator of order 1, this is convenient in some applications.
virtual void	compMat1D (CachedPtxtMatrix &cmat, const PlaintextMatrixBaseInterface &mat, long dim) const
virtual void	compMat1D (CachedDCRTPtxtMatrix &cmat, const PlaintextMatrixBaseInterface &mat, long dim) const
virtual void	mat_mul1D (Ctxt &ctxt, const PlaintextBlockMatrixBaseInterface &mat, long dim) const
virtual void	compMat1D (CachedPtxtBlockMatrix &cmat, const PlaintextBlockMatrixBaseInterface &mat, long dim) const
virtual void	compMat1D (CachedDCRTPtxtBlockMatrix &cmat, const PlaintextBlockMatrixBaseInterface &mat, long dim) const
virtual void	encode (ZZX &ptxt, const vector< long > &array) const
virtual void	encode (ZZX &ptxt, const vector< ZZX > &array) const
virtual void	encode (ZZX &ptxt, const PlaintextArray &array) const
virtual void	encodeUnitSelector (ZZX &ptxt, long i) const
	Encodes a vector with 1 at position i and 0 everywhere

	else.
virtual void	decode (vector< long > &array, const ZZx &ptxt) const
virtual void	decode (vector< ZZx > &array, const ZZx &ptxt) const
virtual void	decode (PlaintextArray &array, const ZZx &ptxt) const
virtual void	random (vector< long > &array) const
virtual void	random (vector< ZZx > &array) const
virtual void	encrypt (Ctxt &ctxt, const FHEPubKey &pKey, const vector< long > &ptxt) const
virtual void	encrypt (Ctxt &ctxt, const FHEPubKey &pKey, const vector< ZZx > &ptxt) const
virtual void	encrypt (Ctxt &ctxt, const FHEPubKey &pKey, const PlaintextArray &ptxt) const
virtual void	decrypt (const Ctxt &ctxt, const FHESecKey &sKey, vector< long > &ptxt) const
virtual void	decrypt (const Ctxt &ctxt, const FHESecKey &sKey, vector< ZZx > &ptxt) const
virtual void	decrypt (const Ctxt &ctxt, const FHESecKey &sKey, PlaintextArray &ptxt) const
virtual void	skEncrypt (Ctxt &ctxt, const FHESecKey &sKey, const vector< long > &ptxt, long skIdx=0) const
virtual void	skEncrypt (Ctxt &ctxt, const FHESecKey &sKey, const

	vector< ZZX > &ptxt, long skIdx=0) const
virtual void	skEncrypt (Ctxt &ctxt, const FHESecKey &sKey, const PlaintextArray &ptxt, long skIdx=0) const
virtual void	select (Ctxt &ctxt1, const Ctxt &ctxt2, const vector< long > &selector) const
	MUX: ctxt1 = ctxt1*selector + ctxt2*(1-selector)
virtual void	select (Ctxt &ctxt1, const Ctxt &ctxt2, const vector< ZZX > &selector) const
virtual void	select (Ctxt &ctxt1, const Ctxt &ctxt2, const PlaintextArray &selector) const
virtual void	buildLinPolyCoeffs (vector< ZZX > &C, const vector< ZZX > &L) const
	<p>Linearized polynomials. L describes a linear map M by describing its action on the standard power basis: $M(x^j \bmod G) = (L[j] \bmod G)$, for $j = 0..d-1$. The result is a coefficient vector C for the linearized polynomial representing M: a polynoamial h in $\mathbb{Z}/(p^r)[X]$ of degree < d is sent to</p> <p>.</p>
void	encode (ZZX &ptxt, const vector< RX > &array) const
void	decode (vector< RX > &array, const ZZX &ptxt) const
void	random (vector< RX > &array) const

void	encrypt (Ctxt &ctxt, const FHEPubKey &pKey, const vector< RX > &ptxt) const
void	decrypt (const Ctxt &ctxt, const FHESecKey &sKey, vector< RX > &ptxt) const
void	skEncrypt (Ctxt &ctxt, const FHESecKey &sKey, const vector< RX > &ptxt, long skIdx=0) const
virtual void	buildLinPolyCoeffs (vector< RX > &C, const vector< RX > &L) const

► Public Member Functions inherited from [EncryptedArrayBase](#)

Detailed Description

template<class type>
class EncryptedArrayDerived< type >

Derived concrete implementation of [EncryptedArrayBase](#).

Member Function Documentation

template<class type >

```
void EncryptedArrayDerived< type >::rotate1D ( Ctxt & ctxt,
                                             long i,
                                             long k,
                                             bool dc = false
                                             ) const
```

virtual

right-rotate k positions along the i'th dimension

Parameters

dc means "don't care", which means that the caller guarantees that only zero elements rotate

off the end – this allows for some optimizations that would not otherwise be possible

Implements [EncryptedArrayBase](#).

The documentation for this class was generated from the following files:

- src/[EncryptedArray.h](#)
- src/EncryptedArray.cpp

EvalMap Class Reference

Class that provides the functionality for the linear transforms used in bootstrapping. The constructor is invoked with three arguments: [More...](#)

```
#include <EvalMap.h>
```

Public Member Functions

EvalMap (const EncryptedArray &_ea, const Vec< long > &mvec, bool _invert, bool normal_basis=true)

void	apply (Ctxt &ctxt) const
------	--

Detailed Description

Class that provides the functionality for the linear transforms used in bootstrapping. The constructor is invoked with three arguments:

- an [EncryptedArray](#) object ea
- an integer vector mvec
- a boolean flag invert The mvec vector specifies the factorization of m to use in the "powerful basis" decomposition.

If the invert flag is false, the forward transformation is used. This transformation views the slots as being packed with powerful-basis coefficients and performs a multi-point polynomial evaluation. This is the second transformation used in bootstrapping.

If invert flag is true, the inverse transformation is used. In addition, the current implementation folds into the inverse transformation a transformation that moves the coefficients in each slot into a normal-basis representation, which helps with the unpacking procedure.

The constructor precomputes certain values, but the linear transformation itself is effected using the apply method.

Note that the factorization in mvec must correspond to the generators used in [PAlgebra](#). The best way to ensure this is to use directly the output of the params program, which will supply values for mvec (to be used here), and gens and ords (to be used in initialize the [FHEcontext](#)).

The documentation for this class was generated from the following files:

- src/[EvalMap.h](#)
- src/EvalMap.cpp

EvalMap Class Reference

Class that provides the functionality for the linear transforms used in bootstrapping. The constructor is invoked with three arguments: [More...](#)

```
#include <EvalMap.h>
```

Public Member Functions

EvalMap (const EncryptedArray &_ea, const Vec< long > &mvec, bool _invert, bool normal_basis=true)

void	apply (Ctxt &ctxt) const
------	--

Detailed Description

Class that provides the functionality for the linear transforms used in bootstrapping. The constructor is invoked with three arguments:

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The constructor precomputes certain values, but the linear transformation itself is effected using the apply method.

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The documentation for this class was generated from the following files:

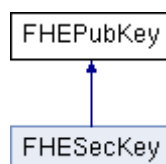
- src/[EvalMap.h](#)
- src/EvalMap.cpp

FHEPubKey Class Reference

The public key. [More...](#)

```
#include <FHE.h>
```

Inheritance diagram for FHEPubKey:



Public Member Functions

	FHEPubKey (const FHEcontext &_context)
	FHEPubKey (const FHEPubKey &other)
void	clear ()
bool	operator== (const FHEPubKey &other) const
bool	operator!= (const FHEPubKey &other) const
const FHEcontext &	getContext () const
long	getPtxtSpace () const
bool	keyExists (long keyID)
long	getSKeyWeight (long keyID=0) const
	The Hamming weight of the secret key.
bool	isReachable (long k, long keyID=0) const
	Is it possible to re-linearize the automorphism $X \rightarrow X^k$ See Section 3.2.2 in the design document (KeySwitchMap)
void	setKeySwitchMap (long keyID=0)
	Compute the reachability graph of key-switching matrices See Section 3.2.2 in the design document (KeySwitchMap)
long	Encrypt (Ctxt &ciphertext, const ZZx &plaintext, long ptxtSpace=0, bool highNoise=false) const

	Encrypts plaintext, result returned in the ciphertext argument. The returned value is the plaintext-space for that ciphertext. When called with highNoise=true, returns a ciphertext with noise level~q/8.
--	--

bool	isBootstrappable () const
------	----------------------------------

void	reCrypt (Ctxt &ctxt)
------	--

Find key-switching matrices

const KeySwitch &	getKeySWmatrix (const SKHandle &from, long toID=0) const
	Find a key-switching matrix by its indexes. If no such matrix exists it returns a dummy matrix with toKeyID== -1.

const KeySwitch &	getKeySWmatrix (long fromSPower, long fromXPower, long fromID=0, long toID=0) const
-----------------------------------	--

bool	haveKeySWmatrix (const SKHandle &from, long toID=0) const
------	--

bool	haveKeySWmatrix (long fromSPower, long fromXPower, long fromID=0, long toID=0) const
------	---

const KeySwitch &	getAnyKeySWmatrix (const SKHandle &from) const
	Is there a matrix from this key to <i>any</i> base key?

bool	haveAnyKeySWmatrix (const SKHandle &from) const
------	--

const KeySwitch &	getNextKSWmatrix (long fromXPower, long fromID=0) const
	Get the next matrix to use for multi-hop automorphism See Section 3.2.2 in the design document.

Static Public Member Functions

static long	ePlusR (long p)
-------------	------------------------

Friends

class	FHESecKey
ostream &	operator<< (ostream &str, const FHEPubKey &pk)
istream &	operator>> (istream &str, FHEPubKey &pk)

Detailed Description

The public key.

The documentation for this class was generated from the following files:

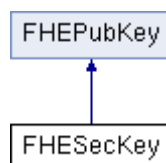
- src/[FHE.h](#)
- src/FHE.cpp
- src/recryption.cpp

FHESecKey Class Reference

The secret key. [More...](#)

```
#include <FHE.h>
```

Inheritance diagram for FHESecKey:



Public Member Functions

FHESecKey (const FHEcontext &_context)

bool	operator== (const FHESecKey &other) const
bool	operator!= (const FHESecKey &other) const
void	clear ()
long	ImportSecKey (const DoubleCRT &sKey, long hwt, long ptxtSpace=0, bool onlyLinear=false)
long	GenSecKey (long hwt, long ptxtSpace=0, bool onlyLinear=false)
void	GenKeySWmatrix (long fromSPower, long fromXPower, long fromKeyIdx=0, long toKeyIdx=0, long ptxtSpace=0)
void	Decrypt (ZZX &plaintext, const Ctxt &ciphertext) const
void	Decrypt (ZZX &plaintext, const Ctxt &ciphertext, ZZX &f) const Debugging version, returns in f the polynomial before reduction modulo the ptxtSpace.
long	Encrypt (Ctxt &ctxt, const ZZX &ptxt, long ptxtSpace=0, long skIdx=0) const Symmetric encryption using the secret key.
long	genRecryptData () Generate bootstrapping data if needed, returns index of key.

► Public Member Functions inherited from [FHEPubKey](#)

Public Attributes

vector< DoubleCRT >	sKeys
-------------------------------------	--------------

Friends

ostream &	operator<< (ostream &str, const FHESecKey &sk)
-----------	---

istream &	operator>> (istream &str, FHESecKey &sk)
-----------	---

Additional Inherited Members

► Static Public Member Functions inherited from [FHEPubKey](#)

Detailed Description

The secret key.

Member Function Documentation

```
void FHESecKey::GenKeySWmatrix ( long fromSPower,  
                                long fromXPower,  
                                long fromKeyIdx = 0,  
                                long toKeyIdx = 0,  
                                long ptxtSpace = 0  
                                )
```

Generate a key-switching matrix and store it in the public key. The i 'th column of the matrix encrypts $\text{fromKey} * B_1 * B_2 * \dots * B_{i-1} * Q$ under toKey , relative to the largest modulus (i.e., all primes) and plaintext space p . Q is the product of special primes, and the B_i 's are the products of primes in the i 'th digit. The plaintext space defaults to 2^r , as defined by `context.mod2r`.

```
long FHESecKey::GenSecKey ( long hwt,  
                           long ptxtSpace = 0,  
                           bool onlyLinear = false  
                           )
```

inline

Key generation: This procedure generates a single secret key, pushes it onto the sKeys list using ImportSecKey from above.

```
long FHESecKey::ImportSecKey ( const DoubleCRT & sKey,  
                                long hwt,  
                                long ptxtSpace = 0,  
                                bool onlyLinear = false  
                                )
```

We allow the calling application to choose a secret-key polynomial by itself, then insert it into the [FHESecKey](#) object, getting the index of that secret key in the sKeys list. If this is the first secret-key for this object then the procedure below also generates a corresponding public encryption key. It is assumed that the context already contains all parameters.

The documentation for this class was generated from the following files:

- src/[FHE.h](#)
- src/FHE.cpp

FHEtimer Class Reference

A simple class to accumulate time. [More...](#)

```
#include <timing.h>
```

Public Member Functions

	FHEtimer (const char *_name, const char *_loc)
void	reset ()
double	getTime () const
long	getNumCalls () const

Public Attributes

const char *	name
const char *	loc
FHE_atomic_ulong	counter
FHE_atomic_long	numCalls

Detailed Description

A simple class to accumulate time.

The documentation for this class was generated from the following files:

- src/[timing.h](#)
- src/timing.cpp

FlowEdge Class Reference

An edge in a flow graph. [More...](#)

```
#include <matching.h>
```

Public Member Functions

FlowEdge (long c=0, long f=0)

Public Attributes

long	capacity
------	-----------------

long **flow**

Detailed Description

An edge in a flow graph.

The documentation for this class was generated from the following file:

- src/[matching.h](#)

FullBinaryTree< T > Class Template Reference

A simple implementation of full binary trees (each non-leaf has 2 children) [More...](#)

```
#include <permutations.h>
```

Public Member Functions

	FullBinaryTree (long _aux=0)
--	-------------------------------------

	FullBinaryTree (const T &d, long _aux=0)
--	---

void	putDataInRoot (const T &d)
------	-----------------------------------

long	size ()
------	----------------

TreeNode < T > &	operator[] (long i)
----------------------------------	----------------------------

const TreeNode < T > &	operator[] (long i) const
--	----------------------------------

<u>TreeNode</u> < T > &	at (long i)
const <u>TreeNode</u> < T > &	at (long i) const
T &	DataOfNode (long i)
const T &	DataOfNode (long i) const
long	getAuxKey () const
void	setAuxKey (long _aux)
long	getNleaves () const
long	firstLeaf () const
long	nextLeaf (long i) const
long	prevLeaf (long i) const
long	lastLeaf () const
long	rootIdx () const
long	parentIdx (long i) const

long	leftChildIdx (long i) const
long	rightChildIdx (long i) const
void	printout (ostream &s, long idx=0) const
long	<u>addChildren</u> (long prntIdx, const T &leftData, const T &rightData)
void	<u>collapseToRoot</u> ()
	Remove all nodes in the tree except for the root.

Detailed Description

```
template<class T>
class FullBinaryTree< T >
```

A simple implementation of full binary trees (each non-leaf has 2 children)

Member Function Documentation

```
template<class T >
```

```
long FullBinaryTree< T >::addChildren ( long      prntIdx,
                                     const T & leftData,
                                     const T & rightData
                                     )
```

If the parent is a leaf, add to it the children with the given data, else just update the data of the two children of this parent. Returns the index of the left child, the right-child index is one more than the left-child index.

The documentation for this class was generated from the following file:

- src/[permutations.h](#)

GenDescriptor Class Reference

A minimal description of a generator for the purpose of building tree. [More...](#)

```
#include <permutations.h>
```

Public Member Functions

GenDescriptor (long _order, bool _good, long gen=0)
--

Public Attributes

long	genIdx
------	---------------

long	order
------	--------------

bool	good
------	-------------

Detailed Description

A minimal description of a generator for the purpose of building tree.

The documentation for this class was generated from the following file:

- src/[permutations.h](#)

GeneralBenesNetwork Class Reference

Implementation of generalized Benes Permutation Network. [More...](#)

```
#include <permutations.h>
```

Public Member Functions

long	getDepth () const
long	getSize () const
long	getNumLevels () const
const Vec< short > &	getLevel (long i) const
long	levelToDepthMap (long i) const
long	shamt (long i) const
	GeneralBenesNetwork (const Permut &perm)
bool	testNetwork (const Permut &perm) const

Static Public Member Functions

static long	depth (long n)
static long	levelToDepthMap (long n, long k, long i)
static long	shamt (long n, long k, long i)

Detailed Description

Implementation of generalized Benes Permutation Network.

Member Function Documentation

static long GeneralBenesNetwork::depth (long *n*)

inline static

computes recursion depth *k* for generalized Benes network of size *n*. the actual number of levels in the network is 2^{k-1}

**static long GeneralBenesNetwork::levelToDepthMap (long *n*,
long *k*,
long *i*
)**

inline static

maps a level number $i = 0..2^{k-2}$ to a recursion depth $d = 0..k-1$ using the formula $d = (k-1) - |(k-1)-i|$

**static long GeneralBenesNetwork::shamt (long *n*,
long *k*,
long *i*
)**

inline static

shift amount for level number $i=0..2^{k-2}$ using the formula $\text{ceil}(\text{floor}(n/2^d) / 2)$, where $d = \text{levelToDepthMap}(i)$

The documentation for this class was generated from the following files:

- src/[permutations.h](#)
- src/BenesNetwork.cpp

GeneratorTrees Class Reference

A vector of generator trees, one per generator in $Z_m^*/(p)$ [More...](#)

```
#include <permutations.h>
```

Public Member Functions

long	numLayers () const
long	numTrees () const
long	getSize () const
OneGeneratorTree &	operator[] (long i)
const OneGeneratorTree &	operator[] (long i) const
OneGeneratorTree &	at (long i)
const OneGeneratorTree &	at (long i) const
OneGeneratorTree &	getGenTree (long i)
const OneGeneratorTree &	getGenTree (long i) const
const Permut &	mapToCube () const
const Permut &	mapToArray () const
Permut &	mapToCube ()
Permut &	mapToArray ()
long	mapToCube (long i) const
long	mapToArray (long i) const

void	getCubeDims (Vec< long > &dims) const
void	getCubeSubDims (Vec< long > &dims) const
long	buildOptimalTrees (const Vec< GenDescriptor > &vec, long depthBound)
void	ComputeCubeMapping ()
	Computes permutations mapping between linear array and the cube. More...

Friends

ostream &	operator<< (ostream &s, const GeneratorTrees &t)
-----------	---

Detailed Description

A vector of generator trees, one per generator in $Z_m^{*}/(p)$

Member Function Documentation

```
long GeneratorTrees::buildOptimalTrees ( const Vec< GenDescriptor > & vec,
                                         long
                                         depthBound
                                         )
```

Compute the trees corresponding to the "optimal" way of breaking a permutation into dimensions, subject to some constraints. Returns the cost (# of 1D shifts) of this colution. Returns NTL_MAX_LONG if no solution

```
void GeneratorTrees::ComputeCubeMapping ( )
```

Computes permutations mapping between linear array and the cube.

If the cube dimensions (i.e., leaves of tree) are n_1, n_2, \dots, n_t and $N = n_j$ is the size of the cube, then an integer i can be represented in either the mixed base of the n_j 's or in "CRT basis" relative to the leaves: Namely either $i = \{j \leq t\} i_j * \{k > j\} n_k$, or $i = i'_{\text{leaf}} * \text{leaf.e mod } N$.

The `breakPermByDim` procedure expects its input in the mixed-base representation, and the maps are used to convert back and forth. Specifically, let (i'_1, \dots, i'_t) be the CRT representation of i in this cube, and $j = \{j=1\}^t i'_j * \{k > j\} n_k$, then we have `map2cube[i]=j` and `map2array[j]=i`.

`void GeneratorTrees::getCubeDims (Vec< long > & dims) const`

Get the "crude" cube dimensions corresponding to the vector of trees, the ordered vector with one dimension per tree

`void GeneratorTrees::getCubeSubDims (Vec< long > & dims) const`

Get the "fine" cube dimensions corresponding to the vector of trees, the ordered vector with one dimension per leaf in all the trees.

The documentation for this class was generated from the following files:

- [src/permutations.h](#)
- [src/OptimizePermutations.cpp](#)
- [src/permutations.cpp](#)

HyperCube< T > Class Template Reference

A multi-dimensional cube. [More...](#)

```
#include <hypercube.h>
```

Public Member Functions

	HyperCube (const CubeSignature &_sig)
	initialzie a HyperCube with a CubeSignature

<u>HyperCube</u> &	<u>operator=</u> (const <u>HyperCube</u> < T > &other)
	assignment: signatures must be the same
bool	<u>operator==</u> (const <u>HyperCube</u> < T > &other) const
	equality testing: signatures must be the same
bool	<u>operator!=</u> (const <u>HyperCube</u> < T > &other) const
const <u>CubeSignature</u> &	<u>getSig</u> () const
	const ref to signature
Vec< T > &	<u>getData</u> ()
const Vec< T > &	<u>getData</u> () const
	read-only ref to data vector
long	<u>getSize</u> () const
	total size of cube
long	<u>getNumDims</u> () const
	number of dimensions
long	<u>getDim</u> (long d) const
	size of dimension d

long	<u>getProd</u> (long d) const
	product of sizes of dimensions d, d+1, ...
long	<u>getProd</u> (long from, long to) const
	product of sizes of dimensions from, from+1, ..., to-1
long	<u>getCoord</u> (long i, long d) const
	get coordinate in dimension d of index i
long	<u>addCoord</u> (long i, long d, long offset) const
	add offset to coordinate in dimension d of index i
long	<u>numSlices</u> (long d=1) const
	number of slices
long	<u>sliceSize</u> (long d=1) const
	size of one slice
long	<u>numCols</u> () const
	number of columns
T &	<u>at</u> (long i)
	reference to element at position i, with bounds check
T &	<u>operator[]</u> (long i)

	reference to element at position i, without bounds check
const T &	<u>at</u> (long i) const
	read-only reference to element at position i, with bounds check
const T &	<u>operator[]</u> (long i) const
	read-only reference to element at position i, without bounds check
void	<u>rotate1D</u> (long i, long k)
	rotate k positions along the i'th dimension
void	<u>shift1D</u> (long i, long k)
	Shift k positions along the i'th dimension with zero fill.

Detailed Description

```
template<class T>
class HyperCube< T >
```

A multi-dimensional cube.

Such an object is initialized with a [CubeSignature](#): a reference to the signature is stored with the cube, and so the signature must remain alive during the lifetime of the cube, to prevent dangling pointers.

Member Function Documentation

```
template<class T>
```

Vec<T>& [HyperCube](#)< T >::getData ()

inline

read/write ref to the data vector. Note that the length of data is fixed upon construction, so it cannot be changed through this ref.

The documentation for this class was generated from the following files:

- src/[hypercube.h](#)
- src/hypercube.cpp

IndexMap< T > Class Template Reference

IndexMap<T> implements a generic map indexed by a dynamic index set. [More...](#)

```
#include <IndexMap.h>
```

Public Member Functions

	IndexMap ()
	The empty map.
	IndexMap (IndexMapInit< T > *_init)
	A map with an initialization object. This associates a method for initializing new elements in the map. When a new index j is added to the index set, an object t of type T is created using the default constructor for T, after which the function _init->init(t) is called (t is passed by reference). To use this feature, you need to derive a subclass of IndexMapInit<T> that defines the init function. This "helper object" should be created using operator new, and the pointer is "exclusively owned" by the map object.
const IndexSet &	getIndexSet () const

	Get the underlying index set.
T &	operator[] (long j)
	Access functions: will raise an error if j does not belong to the current index set.
const T &	operator[] (long j) const
void	insert (long j)
	Insert indexes to the IndexSet . Insertion will cause new T objects to be created, using the default constructor, and possibly initilized via the IndexMapInit<T> pointer.
void	insert (const IndexSet &s)
void	remove (long j)
	Delete indexes from IndexSet , may cause objects to be destroyed.
void	remove (const IndexSet &s)
void	clear ()

Detailed Description

```
template<class T>
class IndexMap< T >
```

IndexMap<T> implements a generic map indexed by a dynamic index set.

Additionally, it allows new elements of the map to be initialized in a flexible manner.

The documentation for this class was generated from the following file:

- src/[IndexMap.h](#)

IndexMapInit< T > Class Template Reference abstract

Initializing elements in an [IndexMap](#). [More...](#)

```
#include <IndexMap.h>
```

Public Member Functions

virtual void	init (T &)=0
	Initialization function, override with initialization code.
virtual IndexMapInit < T > *	clone () const =0
	Cloning a pointer, override with code to create a fresh copy.

Detailed Description

```
template<class T>  
class IndexMapInit< T >
```

Initializing elements in an [IndexMap](#).

The documentation for this class was generated from the following file:

- src/[IndexMap.h](#)

IndexSet Class Reference

A dynamic set of non-negative integers. [More...](#)

```
#include <IndexSet.h>
```

Public Member Functions

	IndexSet (long low, long high)
	IndexSet (long j)
long	first () const
	Returns the first element, 0 if the set is empty.
long	last () const
	Returns the last element, -1 if the set is empty.
long	next (long j) const
	Returns the next element after j, if any; otherwise j+1.
long	prev (long j) const
long	card () const
	The cardinality of the set.
bool	contains (long j) const
	Returns true iff the set contains j.
bool	contains (const IndexSet &s) const
	Returns true iff the set contains s.

bool	disjointFrom (const IndexSet &s) const
	Returns true iff the set is disjoint from s.
bool	operator== (const IndexSet &s) const
bool	operator!= (const IndexSet &s) const
void	clear ()
	Set to the empty set.
void	insert (long j)
	Add j to the set.
void	remove (long j)
	Remove j from the set.
void	insert (const IndexSet &s)
	Add s to the set (union)
void	remove (const IndexSet &s)
	Remove s from the set (set minus)
void	retain (const IndexSet &s)
	Retains only those elements that are also in s (intersection)
bool	isInterval () const
	Is this set a contiguous interval?

Static Public Member Functions

static const IndexSet &	emptySet ()
---	-----------------------------

	Read-only access to an empty set.
--	-----------------------------------

Detailed Description

A dynamic set of non-negative integers.

You can iterate through a set as follows:

```
for (long i = s.first(); i <= s.last(); i = s.next(i)) ...
for (long i = s.last(); i >= s.first(); i = s.prev(i)) ...
```

The documentation for this class was generated from the following files:

- src/[IndexSet.h](#)
- src/IndexSet.cpp

KeySwitch Class Reference

Key-switching matrices. [More...](#)

```
#include <FHE.h>
```

Public Member Functions

	KeySwitch (long sPow=0, long xPow=0, long fromID=0, long toID=0, long p=0)
--	---

	KeySwitch (const SKHandle &_fromKey, long fromID=0, long toID=0, long p=0)
--	---

bool	operator== (const KeySwitch &other) const
------	--

bool	operator!= (const KeySwitch &other) const
------	--

unsigned long	NumCols () const
void	verify (FHESecKey &sk)
	A debugging method.
void	readMatrix (istream &str, const FHEcontext &context)
	Read a key-switching matrix from input.

Static Public Member Functions

static const KeySwitch &	dummy ()
	returns a dummy static matrix with toKeyld == -1

Public Attributes

SKHandle	fromKey
long	toKeyID
long	ptxtSpace
vector< DoubleCRT >	b
ZZ	prgSeed

Detailed Description

Key-switching matrices.

There are basically two approaches for how to do key-switching: either decompose the mod-q ciphertext into bits (or digits) to make it low-norm, or perform the key-switching operation mod $Q \gg q$. The tradeoff is that when decomposing the (coefficients of the) ciphertext into t digits, we need to

increase the size of the key-switching matrix by a factor of t (and the running time similarly grows). On the other hand if we do not decompose at all then we need to work modulo $Q > q^2$, which means that the bitsize of our largest modulus q_0 more than doubles (and hence also the parameter m more than doubles). In general if we decompose into digits of size B then we need to work with $Q > q^B$.)

The part of the spectrum where we expect to find the sweet spot is when we decompose the ciphertext into digits of size $B = q_0^{1/t}$ for some small constant t (maybe $t=2,3$ or so). This means that our largest modulus has to be $Q > q_0^{1+1/t}$, which increases also the parameter m by a factor $(1+1/t)$. It also means that for key-switching in the top levels we would break the ciphertext to t digits, hence the key-switching matrix will have t columns.

A key-switch matrix $W[s' \rightarrow s]$ converts a ciphertext-part with respect to secret-key polynomial s' into a canonical ciphertext (i.e. a two-part ciphertext with respect to $(1,s)$). The matrix W is a 2 -by- t matrix of [DoubleCRT](#) objects. The bottom row are just (pseudo)random elements. Then for column i , if the bottom element is a_i then the top element is set as $b_i = P \cdot B_i \cdot s' + p \cdot e_i - s \cdot a_i \bmod P \cdot q_0$, where p is the plaintext space (i.e. 2 or 2^r) and B_i is the product of the digits-sizes corresponding to columns $0 \dots i-1$. (For example if we have digit sizes $3,5,7$ then $B_0=1$, $B_1=3$, $B_2=15$ and $B_3=105$.) Also, q_0 is the product of all the "ciphertext primes" and P is roughly the product of all the special primes. (Actually, if Q is the product of all the special primes then $P = Q \cdot (Q^{-1} \bmod p)$.)

In this implementation we save some space, by keeping only a PRG seed for generating the pseudo-random elements, rather than the elements themselves.

To convert a ciphertext part R , we break R into digits $R = \sum_i B_i R_i$, then set $(q_0, q_1)^T = \sum_i R_i \cdot \text{column-}i$. Note that we have $\langle (1,s), (q_0, q_1) \rangle = \sum_i R_i (s \cdot a_i - s \cdot a_i + p \cdot e_i + P \cdot B_i \cdot s') = P \cdot \sum_i B_i \cdot R_i \cdot s' + p \sum_i R_i \cdot e_i = P \cdot R \cdot s' + p \cdot \text{a-small-element} \bmod P \cdot q_0$ where the last element is small since the e_i 's are small and $|R_i| < B$. Note that if the ciphertext is encrypted relative to plaintext space p' and then key-switched with matrices W relative to plaintext space p , then we get a new ciphertext with noise $p' \cdot \text{small} + p \cdot \text{small}$, so it is valid relative to plaintext space $\text{GCD}(p', p)$.

The matrix W is defined modulo $Q > t \cdot B \cdot \sigma \cdot q_0$ (with σ a bound on the size of the e_i 's), and Q is the product of all the small primes in our moduli chain. However, if p is much smaller than B then it is enough to use $W \bmod Q_i$ with Q_i a smaller modulus, $Q > p \cdot \sigma \cdot q_0$. Also note that if $p < B^r$ then we will be using only first r columns of the matrix W .

The documentation for this class was generated from the following files:

- [src/FHE.h](#)
- [src/FHE.cpp](#)

LabeledEdge Class Reference

A generic directed edge in a graph with some labels. [More...](#)

```
#include <matching.h>
```

Public Member Functions

LabeledEdge (long f, long t, long l=0, long c=0)

Public Attributes

long	from
------	-------------

long	to
------	-----------

long	label
------	--------------

long	color
------	--------------

Detailed Description

A generic directed edge in a graph with some labels.

The documentation for this class was generated from the following file:

- src/[matching.h](#)

LabeledVertex Class Reference

A generic node in a graph with some labels. [More...](#)

```
#include <matching.h>
```


Public Member Functions

	LabeledVertex (long n, long l=0)
void	addEdge (long nn, long l=0, long c=0)
void	addNeighbor (long nn, long l=0, long c=0)

Public Attributes

long	name
long	label
LNeighborList	neighbors

Detailed Description

A generic node in a graph with some labels.

The documentation for this class was generated from the following file:

- src/[matching.h](#)

MappingData< type > Class Template Reference

Auxilliary structure to support encoding/decoding slots. [More...](#)

```
#include <PAlgebra.h>
```

Public Member Functions

const RX &	getG () const
------------	----------------------

long	getDegG () const
void	restoreContextForG () const

Friends

class	PAlgebraModDerived < type >
-------	------------------------------------

Detailed Description

template<class type>
class MappingData< type >

Auxilliary structure to support encoding/decoding slots.

The documentation for this class was generated from the following file:

- src/[PAlgebra.h](#)

PAlgebra Class Reference

The structure of $(\mathbb{Z}/m\mathbb{Z})^* / (p)$ [More...](#)

```
#include <PAlgebra.h>
```

Public Member Functions

	PAlgebra (unsigned long mm, unsigned long pp=2, const vector< long > &_gens=vector< long >(), const vector< long > &_ords=vector< long >())
--	--

bool	operator== (const PAlgebra &other) const
bool	operator!= (const PAlgebra &other) const
void	printout () const
	Prints the structure in a readable form.
unsigned long	getM () const
	Returns m.
unsigned long	getP () const
	Returns p.
unsigned long	getPhiM () const
	Returns phi(m)
unsigned long	getOrdP () const
	The order of p in $(\mathbb{Z}/m\mathbb{Z})^*$.
unsigned long	getNSlots () const
	The number of plaintext slots = $\text{phi}(m)/\text{ord}(p)$
const ZZ[X] &	getPhimX () const
	The cyclotomic polynomial $\Phi_m(X)$
void	set_cM (double c)
	The ring constant cM.
const double	get_cM () const

unsigned long	<u>numOfGens</u> () const
	The prime-power factorization of m. More...

unsigned long	<u>ZmStarGen</u> (unsigned long i) const
	the i'th generator in $(\mathbb{Z}/m\mathbb{Z})^* / (p)$ (if any)

unsigned long	<u>OrderOf</u> (unsigned long i) const
	The order of i'th generator (if any)

bool	<u>SameOrd</u> (unsigned long i) const
	Is ord(i'th generator) the same as its order in $(\mathbb{Z}/m\mathbb{Z})^*$?

Translation between index, represnetatives, and exponents

unsigned long	<u>ith_rep</u> (unsigned long i) const
	Returns the i'th element in T.

long	<u>indexOfRep</u> (unsigned long t) const
	Returns the index of t in T.

bool	<u>isRep</u> (unsigned long t) const
	Is t in T?

long	<u>indexInZmstar</u> (unsigned long t) const
	Returns the index of t in $(\mathbb{Z}/m\mathbb{Z})^*$.

bool	<u>inZmStar</u> (unsigned long t) const
	Is t in $[0, m-1]$ with $(t, m) = 1$?

long	<u>coordinate</u> (long i, long k) const
------	--

	Returns ith coordinate of index k along the i'th dimension. See Section 2.4 in the design document.
long	addCoord (long i, long k, long offset) const
	adds offset to index k in the i'th dimension
unsigned long	exponentiate (const vector< unsigned long > &exps, bool onlySameOrd=false) const
	Returns $\prod_i g_i^{\text{exps}[i]} \bmod m$. If onlySameOrd=true, use only generators that have the same order as in $(\mathbb{Z}/m\mathbb{Z})^*$.
const long *	dLog (unsigned long t) const
	Inverse of exponentiate.
unsigned long	gGrpOrd (bool onlySameOrd=false) const
bool	nextExpVector (vector< unsigned long > &exps) const

Detailed Description

The structure of $(\mathbb{Z}/m\mathbb{Z})^* / (p)$

A [PAlgebra](#) object is determined by an integer m and a prime p , where p does not divide m . It holds information describing the structure of $(\mathbb{Z}/m\mathbb{Z})^*$, which is isomorphic to the Galois group over $A = \mathbb{Z}[X]/\Phi_m(X)$.

We represent $(\mathbb{Z}/m\mathbb{Z})^*$ as $(\mathbb{Z}/m\mathbb{Z})^* = (p) \times (g_1, g_2, \dots) \times (h_1, h_2, \dots)$ where the group generated by g_1, g_2, \dots consists of the elements that have the same order in $(\mathbb{Z}/m\mathbb{Z})^*$ as in $(\mathbb{Z}/m\mathbb{Z})^* / (p, g_1, \dots, g_{i-1})$, and h_1, h_2, \dots generate the remaining quotient group $(\mathbb{Z}/m\mathbb{Z})^* / (p, g_1, g_2, \dots)$.

We let $T \subset (\mathbb{Z}/m\mathbb{Z})^*$ be a set of representatives for the quotient group $(\mathbb{Z}/m\mathbb{Z})^* / (p)$, defined as $T = \{ \prod_i g_i^{e_i} * \prod_j h_j^{e_j} \}$ where the e_i 's range over $0, 1, \dots, \text{ord}(g_i)-1$ and the e_j 's range over $0, 1, \dots, \text{ord}(h_j)-1$ (these last orders are in $(\mathbb{Z}/m\mathbb{Z})^* / (p, g_1, g_2, \dots)$).

$\Phi_m(X)$ is factored as $\Phi_m(X) = \prod_{t \in T} F_t(X) \pmod p$, where the F_t 's are irreducible modulo p . An arbitrary factor is chosen as F_1 , then for each t in T we associate with the index t the factor $F_t(X) = \text{GCD}(F_1(X^t), \Phi_m(X))$.

Note that fixing a representation of the field $R = (\mathbb{Z}/p\mathbb{Z})[X]/F_1(X)$ and letting z be a root of F_1 in R (which is a primitive m -th root of unity in R), we get that F_t is the minimal polynomial of $z^{1/t}$.

Member Function Documentation

bool PAlgebra::nextExpVector (vector< unsigned long > & **exps) const**

`exps` is an array of exponents (the `dLog` of some t in T), this function increment `exps` lexicographic order, return false if it cannot be incremented (because it is at its maximum value)

unsigned long PAlgebra::numOfGens () const

inline

The prime-power factorization of m .

The number of generators in $(\mathbb{Z}/m\mathbb{Z})^* / (p)$

unsigned long PAlgebra::qGrpOrd (bool **onlySameOrd = false) const**

inline

The order of the quotient group $(\mathbb{Z}/m\mathbb{Z})^* / (p)$ (if `flag=false`), or the subgroup of elements with the same order as in $(\mathbb{Z}/m\mathbb{Z})^*$ (if `flag=true`)

The documentation for this class was generated from the following files:

- [src/PAlgebra.h](#)
- [src/PAlgebra.cpp](#)

PAlgebraMod Class Reference

The structure of $\mathbb{Z}[X]/(\Phi_m(X), p)$ [More...](#)

```
#include <PAlgebra.h>
```

Public Member Functions

	PAgebraMod (const PAgebra &zMStar, long r)
template<class type >	
const PAgebraModDerived < type > &	getDerived (type) const
bool	operator== (const PAgebraMod &other) const
bool	operator!= (const PAgebraMod &other) const
PA_tag	getTag () const
	Returns the type tag: PA_GF2_tag or PA_zz_p_tag.
const PAgebra &	getZMStar () const
	Returns reference to underlying PAgebra object.
const vector< ZZX > &	getFactorsOverZZ () const
	Returns reference to the factorization of $\Phi_m(X)$ mod p^r , but as ZZX's.
long	getR () const
	The value r.
long	getPPowR () const
	The value p^r .
void	restoreContext () const
	Restores the NTL context for p^r .

Detailed Description

The structure of $Z[X]/(\Phi_m(X), p)$

An object of type [PAlgebraMod](#) stores information about a [PAlgebra](#) object `zmStar`, and an integer `r`. It also provides support for encoding and decoding plaintext slots.

the [PAlgebra](#) object `zmStar` defines $(Z/mZ)^*/(0)$, and the [PAlgebraMod](#) object stores various tables related to the polynomial ring $Z/(p^r)[X]$. To do this most efficiently, if $p == 2$ and $r == 1$, then these polynomials are represented as GF2X's, and otherwise as `zz_pX`'s. Thus, the types of these objects are not determined until run time. As such, we need to use a class heirarchy, as follows.

- [PAlgebraModBase](#) is a virtual class
- `PAlegbraModDerived<type>` is a derived template class, where `type` is either `PA_GF2` or `PA_zz_p`.
- The class [PAlgebraMod](#) is a simple wrapper around a smart pointer to a [PAlgebraModBase](#) object: copying a [PAlgebra](#) object results is a "deep copy" of the underlying object of the derived class. It provides `dDirect` access to the virtual methods of [PAlgebraModBase](#), along with a "downcast" operator to get a reference to the object as a derived type, and also `==` and `!=` operators.

Member Function Documentation

template<class type >

const [PAlgebraModDerived](#)<type>& PAlgebraMod::getDerived (type) const

inline

Downcast operator example: `const PAlgebraModDerived<PA_GF2>& rep = alMod.getDerived(PA_GF2());`

The documentation for this class was generated from the following file:

- `src/PAlgebra.h`

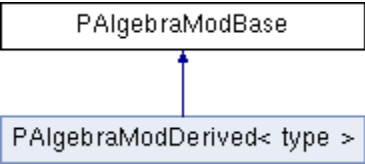
PAlgebraModBase Class Reference

abstract

Virtual base class for [PAlgebraMod](#). [More...](#)

```
#include <PAlgebra.h>
```

Inheritance diagram for PAlgebraModBase:



Public Member Functions

virtual PAlgebraModBase *	clone () const =0
virtual PA_tag	getTag () const =0
	Returns the type tag: PA_GF2_tag or PA_zz_p_tag.
virtual const PAlgebra &	getZMStar () const =0
	Returns reference to underlying PAlgebra object.
virtual const vector< ZZX > &	getFactorsOverZZ () const =0
	Returns reference to the factorization of $\Phi_m(X) \bmod p^r$, but as ZZX's.
virtual long	getR () const =0
	The value r.
virtual long	getPPowR () const =0
	The value p^r .
virtual void	restoreContext () const =0
	Restores the NTL context for p^r .

Detailed Description

Virtual base class for [PAlgebraMod](#).

The documentation for this class was generated from the following file:

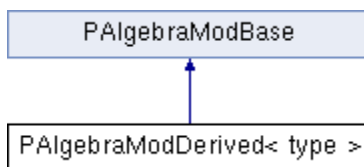
- src/[PAlgebra.h](#)

PAlgebraModDerived< type > Class Template Reference

A concrete instantiation of the virtual class. [More...](#)

```
#include <PAlgebra.h>
```

Inheritance diagram for PAlgebraModDerived< type >:



Public Member Functions

	PAlgebraModDerived (const PAlgebra &zMStar, long r)
	PAlgebraModDerived (const PAlgebraModDerived &other)
PAlgebraModDerived &	operator= (const PAlgebraModDerived &other)
virtual PAlgebraModBase *	clone () const
	Returns a pointer to a "clone".
virtual PA_tag	getTag () const

	Returns the type tag: PA_GF2_tag or PA_zz_p_tag.
virtual const PAlgebra &	getZMStar () const
	Returns reference to underlying PAlgebra object.
virtual const vector< ZZX > &	getFactorsOverZZ () const
	Returns reference to the factorization of $\Phi_m(X) \bmod p^r$, but as ZZX's.
virtual long	getR () const
	The value r.
virtual long	getPPowR () const
	The value p^r .
virtual void	restoreContext () const
	Restores the NTL context for p^r .
const RXModulus &	getPhimXMod () const
	Returns reference to an RXModulus representing $\Phi_m(X) \bmod p^r$
const vec_RX &	getFactors () const
	Returns reference to the factors of $\Phi_m(X)$ modulo p^r .
const vec_RX &	getCrtCoeffs () const

	Returns the CRT coefficients: element i contains $(\prod_{j \neq i} F_j)^{-1} \bmod F_i$, where $F_0 F_1 \dots$ is the factorization of $\Phi_m(X) \bmod p^r$.
--	--

<code>const vector< vector< RX > > &</code>	<code>getMaskTable</code> () const
	Returns ref to maskTable, which is used to implement rotations (in the EncryptedArray module). More...

Embedding in the plaintext slots and decoding back

In all the functions below, G must be irreducible mod p , and the order of G must divide the order of p modulo m (as returned by `zMStar.getOrdP()`). In addition, when $r > 1$, G must be the monomial X ($RX(1, 1)$)

void	<code>CRT_decompose</code> (vector< RX > &crt, const RX &H) const
	Returns a vector crt[] such that $\text{crt}[i] = H \bmod F_t$ (with $t = T[i]$)

void	<code>CRT_reconstruct</code> (RX &H, vector< RX > &crt) const
	Returns H in $R[X]/\Phi_m(X)$ s.t. for every $i < n\text{Slots}$ and $t = T[i]$, we have $H == \text{crt}[i] \pmod{F_t}$

void	<code>mapToSlots</code> (MappingData < type > &mappingData, const RX &G) const
	Compute the maps for all the slots. In the current implementation, we if $r > 1$, then we must have either $\deg(G) == 1$ or $G == \text{factors}[0]$.

void	<code>embedInAllSlots</code> (RX &H, const RX &alpha, const MappingData < type > &mappingData) const
	Returns H in $R[X]/\Phi_m(X)$ s.t. for every $t \in T$, the element $H_t = (H \bmod F_t)$ in $R[X]/F_t(X)$ represents the same element as

		alpha in $R[X]/G(X)$. More...
	void	embedInSlots (RX &H, const vector< RX > &alphas, const MappingData < type > &mappingData) const
		Returns H in $R[X]/\Phi_m(X)$ s.t. for every t in T, the element $H_t = (H \bmod F_t)$ in $R[X]/F_t(X)$ represents the same element as $\text{alphas}[i]$ in $R[X]/G(X)$. More...
	void	decodePlaintext (vector< RX > &alphas, const RX &ptxt, const MappingData < type > &mappingData) const
		Return an array such that $\text{alphas}[i]$ in $R[X]/G(X)$ represent the same element as $r_t = (H \bmod F_t)$ in $R[X]/F_t(X)$ where $t=T[i]$. More...
	void	buildLinPolyCoeffs (vector< RX > &C, const vector< RX > &L, const MappingData < type > &mappingData) const
		Returns a coefficient vector C for the linearized polynomial representing M. More...

Detailed Description

template<class type>
class PAlgebraModDerived< type >

A concrete instantiation of the virtual class.

Member Function Documentation

template<class type >	
void PAlgebraModDerived < type	(vector< RX > & C,

>::buildLinPolyCoeffs

```
const vector< RX > & L,  
const MappingData< type > & mappingData  
) const
```

Returns a coefficient vector C for the linearized polynomial representing M.

For h in $\mathbb{Z}/(p^r)[X]$ of degree < d,

G is assumed to be defined in mappingData, with $d = \deg(G)$. L describes a linear map M by describing its action on the standard power basis: $M(x^j \bmod G) = (L[j] \bmod G)$, for $j = 0..d-1$.

```
template<class type >
```

```
void PAlgebraModDerived< type  
>::decodePlaintext ( vector< RX > & alphas,  
const RX & ptxt,  
const MappingData< type > & mappingData  
) const
```

Return an array such that $\text{alphas}[i]$ in $R[X]/G(X)$ represent the same element as $rt = (H \bmod Ft)$ in $R[X]/Ft(X)$ where $t=T[i]$.

The mappingData argument should contain the output of mapToSlots(G).

```
template<class type >
```

```
void PAlgebraModDerived< type  
>::embedInAllSlots ( RX & H,  
const RX & alpha,
```

const [MappingData](#)< type > & mappingData

) const

Returns H in $R[X]/\Phi_m(X)$ s.t. for every t in T , the element $H_t = (H \bmod F_t)$ in $R[X]/F_t(X)$ represents the same element as α in $R[X]/G(X)$.

Must have $\deg(\alpha) < \deg(G)$. The `mappingData` argument should contain the output of `mapToSlots(G)`.

`template<class type >`

void [PAlgebraModDerived](#)< type

>::embedInSlots

(RX & H,

const vector< RX > & alphas,

const [MappingData](#)< type > & mappingData

) const

Returns H in $R[X]/\Phi_m(X)$ s.t. for every t in T , the element $H_t = (H \bmod F_t)$ in $R[X]/F_t(X)$ represents the same element as `alphas[i]` in $R[X]/G(X)$.

Must have $\deg(\alpha[i]) < \deg(G)$. The `mappingData` argument should contain the output of `mapToSlots(G)`.

`template<class type>`

const vector< vector< RX > > & [PAlgebraModDerived](#)< type >::getMaskTable () const inline

Returns ref to `maskTable`, which is used to implement rotations (in the [EncryptedArray](#) module).

`maskTable[i][j]` is a polynomial representation of a mask that is 1 in all slots whose i 'th coordinate is at least j , and 0 elsewhere. We have:

```
maskTable.size() == zMStar.numOfGens() // # of generators
for i = 0..maskTable.size()-1:
    maskTable[i].size() == zMStar.OrderOf(i) // order of generator i
```

The documentation for this class was generated from the following files:

- src/[PAlgebra.h](#)
- src/PAlgebra.cpp

PermNetLayer Class Reference

The information needed to apply one layer of a permutation network. [More...](#)

```
#include <permutations.h>
```

Public Member Functions

long	getGenIdx () const
long	getE () const
const Vec< long > &	getShifts () const
bool	isIdentity () const

Friends

class	PermNetwork
ostream &	operator<< (ostream &s, const PermNetwork &net)

Detailed Description

The information needed to apply one layer of a permutation network.

The documentation for this class was generated from the following file:

- src/[permutations.h](#)

PermNetwork Class Reference

A full permutation network. [More...](#)

```
#include <permutations.h>
```

Public Member Functions

	PermNetwork (const Permut &pi, const GeneratorTrees &trees)
long	depth () const
void	buildNetwork (const Permut &pi, const GeneratorTrees &trees)
void	applyToCtxt (Ctxt &c, const EncryptedArray &ea) const
	Apply network to permute a ciphertext.
void	applyToCube (HyperCube < long > &v) const
	Apply network to array, used mostly for debugging.
void	applyToPtxt (ZZX &p, const EncryptedArray &ea) const
	Apply network to plaintext polynomial, used mostly for debugging.
const PermNetLayer &	getLayer (long i) const

Friends

ostream &	operator<< (ostream &s, const PermNetwork &net)
-----------	--

Detailed Description

A full permutation network.

Member Function Documentation

```
void PermNetwork::buildNetwork ( const Permut & pi,  
                                const GeneratorTrees & trees  
                                )
```

Take as input a permutation pi and the trees of all the generators, and prepares the permutation network for this pi

The documentation for this class was generated from the following files:

- src/[permutations.h](#)
- src/PermNetwork.cpp

PlaintextArray Class Reference

A simple wrapper for a pointer to a [PlaintextArrayBase](#). This is the interface that higher-level code should use. [More...](#)

```
#include <EncryptedArray.h>
```

Public Member Functions

	PlaintextArray (const EncryptedArray &ea)
--	--

template<class type >

const PlaintextArrayDerived	
< type > &	getDerived (type) const

template<class type >

<u>PlaintextArrayDerived</u> < type > &	getDerived (type)
const <u>EncryptedArray</u> &	<u>getEA</u> () const
	Get the EA object (which is needed for the encoding/decoding routines)
void	<u>rotate</u> (long k)
	Rotation/shift as a linear array.
void	<u>shift</u> (long k)
	Non-cyclic shift with zero fill.
void	<u>encode</u> (const vector< long > &array)
	Encode/decode arrays into plaintext polynomials.
void	encode (const vector< ZZx > &array)
void	decode (vector< long > &array) const
void	decode (vector< ZZx > &array) const
void	<u>encode</u> (long val)
	Encode with the same value replicated in each slot.
void	encode (const ZZx &val)
void	<u>random</u> ()
	Generate a uniformly random element.
bool	<u>equals</u> (const <u>PlaintextArray</u> &other) const

	Equality testing.
bool	equals (const vector< long > &other) const
bool	equals (const vector< ZZX > &other) const
void	add (const PlaintextArray &other)
void	sub (const PlaintextArray &other)
void	negate ()
void	mul (const PlaintextArray &other)
void	mat_mul (const PlaintextMatrixBaseInterface &mat)
void	alt_mul (const PlaintextMatrixBaseInterface &mat)
void	mat_mul (const PlaintextBlockMatrixBaseInterface &mat)
void	replicate (long i)
	Replicate coordinate i at all coordinates.
void	frobeniusAutomorph (long j)
void	frobeniusAutomorph (const Vec< long > &vec)
virtual void	applyPerm (const Vec< long > &pi)
void	print (ostream &s) const

Detailed Description

A simple wrapper for a pointer to a [PlaintextArrayBase](#). This is the interface that higher-level code should use.

The documentation for this class was generated from the following file:

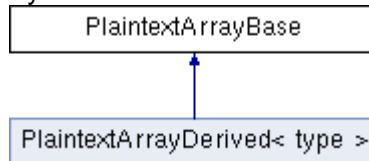
- src/[EncryptedArray.h](#)

PlaintextArrayBase Class Reference abstract

Virtual class for array of slots, not encrypted. [More...](#)

```
#include <EncryptedArray.h>
```

Inheritance diagram for PlaintextArrayBase:



Public Member Functions

virtual PlaintextArrayBase *	clone () const =0
virtual const EncryptedArray &	getEA () const =0 Get the EA object (which is needed for the encoding/decoding routines)
virtual void	rotate (long k)=0 Rotation/shift as a linear array.
virtual void	shift (long k)=0 Non-cyclic shift with zero fill.

virtual void	encode (const vector< long > &array)=0
	Encode/decode arrays into plaintext polynomials.
virtual void	encode (const vector< ZZX > &array)=0
virtual void	decode (vector< long > &array) const =0
virtual void	decode (vector< ZZX > &array) const =0
virtual void	encode (long val)=0
	Encode with the same value replicated in each slot.
virtual void	encode (const ZZX &val)=0
virtual void	random ()=0
	Generate a uniformly random element.
virtual bool	equals (const PlaintextArrayBase &other) const =0
	Equality testing.
virtual bool	equals (const vector< long > &other) const =0
virtual bool	equals (const vector< ZZX > &other) const =0
virtual void	add (const PlaintextArrayBase &other)=0
virtual void	sub (const PlaintextArrayBase &other)=0
virtual void	mul (const PlaintextArrayBase &other)=0

virtual void	negate ()=0
virtual void	mat_mul (const PlaintextMatrixBaseInterface &mat)=0
virtual void	alt_mul (const PlaintextMatrixBaseInterface &mat)=0
virtual void	mat_mul (const PlaintextBlockMatrixBaseInterface &mat)= 0
virtual void	replicate (long i)=0 Replicate coordinate i at all coordinates.
virtual void	frobeniusAutomorph (long j)=0 apply $x \rightarrow x^{p^j}$ at all coordinates
virtual void	frobeniusAutomorph (const Vec< long > &vec)=0 apply $x \rightarrow x^{p^{\text{vec}[i]}}$ to slot i
virtual void	applyPerm (const Vec< long > &pi)=0 apply a permutation: $\text{new}[i] = \text{old}[\text{pi}[i]]$
virtual void	print (ostream &s) const =0

Detailed Description

Virtual class for array of slots, not encrypted.

An object pa of type [PlaintextArray](#) stores information about an [EncryptedArray](#) object ea. The object pa stores a vector of plaintext slots, where each slot is an element of the polynomial ring $(\mathbb{Z}/(p^r)[X])/(G)$, where p, r, and G are as defined in ea. Support for arithmetic on [PlaintextArray](#) objects is provided.

Mirroring [PAlgebraMod](#) and [EncryptedArray](#), we have the following class heirarchy:

[PlaintextArrayBase](#) is a virtual class

PlaintextArrayDerived<type> is a derived template class, where type is either PA_GF2 or PA_zz_p.

The class [PlaintextArray](#) is a simple wrapper around a smart pointer to a [PlaintextArray](#) object: copying a [PlaintextArray](#) object results is a "deep copy" of the underlying object of the derived class.

The documentation for this class was generated from the following file:

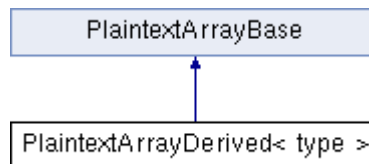
- src/[EncryptedArray.h](#)

PlaintextArrayDerived< type > Class Template Reference

Derived concrete implementation of [PlaintextArrayBase](#). [More...](#)

```
#include <EncryptedArray.h>
```

Inheritance diagram for PlaintextArrayDerived< type >:



Public Member Functions

virtual PlaintextArrayBase *	clone () const
virtual const EncryptedArray &	getEA () const
	Get the EA object (which is needed for the encoding/decoding routines)
	PlaintextArrayDerived (const EncryptedArray &_ea)

	PlaintextArrayDerived (const PlaintextArrayDerived &other)
PlaintextArrayDerived &	operator= (const PlaintextArrayDerived &other)
virtual void	rotate (long k)
	Rotation/shift as a linear array.
virtual void	shift (long k)
	Non-cyclic shift with zero fill.
virtual void	encode (const vector< long > &array)
	Encode/decode arrays into plaintext polynomials.
virtual void	encode (const vector< ZZx > &array)
virtual void	decode (vector< long > &array) const
virtual void	decode (vector< ZZx > &array) const
virtual void	encode (long val)
	Encode with the same value replicated in each slot.
virtual void	encode (const ZZx &val)
virtual void	random ()

	Generate a uniformly random element.
virtual bool	equals (const PlaintextArrayBase &other) const
	Equality testing.
virtual bool	equals (const vector< long > &other) const
virtual bool	equals (const vector< ZZx > &other) const
virtual void	add (const PlaintextArrayBase &other)
virtual void	sub (const PlaintextArrayBase &other)
virtual void	negate ()
virtual void	mul (const PlaintextArrayBase &other)
virtual void	mat_mul (const PlaintextMatrixBaseInterface &mat)
virtual void	alt_mul (const PlaintextMatrixBaseInterface &mat)
virtual void	mat_mul (const PlaintextBlockMatrixBaseInterface &mat)
virtual void	replicate (long i)
	Replicate coordinate i at all coordinates.

virtual void	frobeniusAutomorph (long j)
	apply $x \rightarrow x^{p^j}$ at all coordinates
virtual void	frobeniusAutomorph (const Vec< long > &vec)
	apply $x \rightarrow x^{p^{\text{vec}[i]}}$ to slot i
virtual void	applyPerm (const Vec< long > &pi)
	apply a permutation: $\text{new}[i] = \text{old}[\text{pi}[i]]$
virtual void	print (ostream &s) const
const vector< RX > &	getData () const
void	setData (const vector< RX > &_data)

Static Public Member Functions

static void	rec_mul (long dim, const EncryptedArray &ea, vector< RX > &res, const vector< RX > &pdata, const vector< long > &idx, const PlaintextMatrixInterface < type > &mat)
-------------	--

Friends

template<class tt >	
ostream &	operator<< (ostream &os, const PlaintextArrayDerived < tt > &pt)

Detailed Description

template<class type>

class PlaintextArrayDerived< type >

Derived concrete implementation of [PlaintextArrayBase](#).

The documentation for this class was generated from the following file:

- src/[EncryptedArray.h](#)

PlaintextBlockMatrixBaseInterface Class Reference abstract

An abstract interface for linear transformations. [More...](#)

```
#include <EncryptedArray.h>
```

Inheritance diagram for PlaintextBlockMatrixBaseInterface:



Public Member Functions

virtual const [EncryptedArray](#) & **getEA** () const =0

Detailed Description

An abstract interface for linear transformations.

A block matrix implements linear transformation over the base field/ring (e.g., \mathbb{Z}_2 , \mathbb{Z}_3 , \mathbb{Z}_{2^8} , etc.) Any class implementing this interface should be linked to a specific [EncryptedArray](#) object, a reference to which is returned by the `getEA()` method – this method will generally be invoked by an [EncryptedArray](#) object to verify consistent use.

The documentation for this class was generated from the following file:

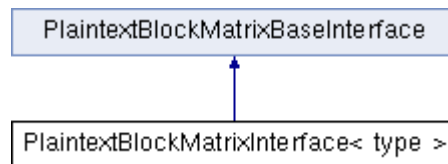
- src/[EncryptedArray.h](#)

PlaintextBlockMatrixInterface< type > Class Template Reference abstract

A somewhat less abstract interface for linear transformations. [More...](#)

```
#include <EncryptedArray.h>
```

Inheritance diagram for PlaintextBlockMatrixInterface< type >:



Public Member Functions

virtual bool	get (mat_R &out, long i, long j) const =0
--------------	--

► Public Member Functions inherited from [PlaintextBlockMatrixBaseInterface](#)

Detailed Description

template<class type>
class PlaintextBlockMatrixInterface< type >

A somewhat less abstract interface for linear transformations.

A block matrix implements linear transformation over the base field/ring (e.g., \mathbb{Z}_2 , \mathbb{Z}_3 , \mathbb{Z}_{2^8} , etc.) The method `get(out, i, j)` copies the element at row `i` column `j` of a matrix into the variable `out`. The type of `out` is `mat_R` (so either `mar_GF2` or `mat_zz_p`). A return value of `true` means that the entry is zero, and `out` is not touched.

The documentation for this class was generated from the following file:

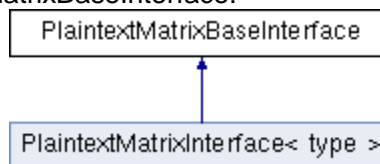
- src/[EncryptedArray.h](#)

PlaintextMatrixBaseInterface Class Reference abstract

An abstract interface for linear transformations. [More...](#)

```
#include <EncryptedArray.h>
```

Inheritance diagram for PlaintextMatrixBaseInterface:



Public Member Functions

virtual const EncryptedArray &	getEA () const =0
--	--------------------------

Detailed Description

An abstract interface for linear transformations.

A matrix implements linear transformation over an extension field/ring (e.g., $GF(2^d)$ or $Z_{2^8}[X]/G(X)$ for irreducible G). Any class implementing this interface should be linked to a specific [EncryptedArray](#) object, a reference to which is returned by the `getEA()` method – this method will generally be invoked by an [EncryptedArray](#) object to verify consistent use.

The documentation for this class was generated from the following file:

- src/[EncryptedArray.h](#)
-

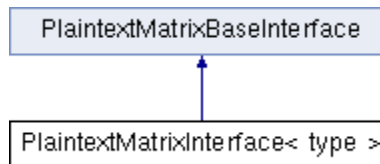
PlaintextMatrixInterface< type > Class Template Reference

abstract

A somewhat less abstract interface for linear transformations. [More...](#)

```
#include <EncryptedArray.h>
```

Inheritance diagram for PlaintextMatrixInterface< type >:



Public Member Functions

virtual bool **get** (RX &out, long i, long j) const =0

► Public Member Functions inherited from [PlaintextMatrixBaseInterface](#)

Detailed Description

```
template<class type>
class PlaintextMatrixInterface< type >
```

A somewhat less abstract interface for linear transformations.

A matrix implements linear transformation over an extension field/ring (e.g., $GF(2^d)$ or $Z_{2^8}[X]/G(X)$ for irreducible G). The method `get(out, i, j)` copies the element at row i column j of a matrix into the variable `out`. The type of `out` is `RX`, which is `GF2X` if `type` is `PA_GF2`, and `zz_pX` if `type` is `PA_zz_p`. A return value of `true` means that the entry is zero, and `out` is not touched.

The documentation for this class was generated from the following file:

- src/[EncryptedArray.h](#)

PowerfulConversion Class Reference

Conversion between powerful representation in $R_m/(q)$ and zz_pX . [More...](#)

```
#include <powerful.h>
```

Public Member Functions

	PowerfulConversion (const PowerfulTranslationIndexes &ind)
void	initPConv (const PowerfulTranslationIndexes &ind)
void	restoreModulus () const
const CubeSignature &	getLongSig () const
const CubeSignature &	getShortSig () const
long	powerfulToPoly (zz_pX &poly, const HyperCube < zz_p > &powerful) const
long	polyToPowerful (HyperCube < zz_p > &powerful, const zz_pX &poly) const

Detailed Description

Conversion between powerful representation in $R_m/(q)$ and zz_pX .

Usage pattern is as follows:

```
// compute tables for index translation PowerfulTranslationIndexes ind(mvec); // mvec is some factorization of m
```

```
// ... set the current zz_p::modulus to something before initializing PowerfulConversion pConv(ind);
```



```
// Alternatively use // PowerfulConversion pConv(); pConv.initPConv(ind); // Only the latter call  
needs zz_p::modulus to be defined
```

```
// A powerful basis is defined wrt same modulus and cube signature HyperCube<zz_p>  
powerful(pConv.getShortSig());
```

```
// ... some code here to initialize powerful // code can also do other stuff, perhaps changing  
zz_p::modulus
```

```
pConv.restoreModulus(); // restore zz_p::modulus zz_pX poly; // defined relative to the same  
modulus pConv.powerfulToPoly(poly, powerful);
```

```
// ... some more code here, perhaps changing zz_p::modulus again
```

```
pConv.restoreModulus(); // restore zz_p::modulus pConv.polyToPowerful(powerful, poly);
```

Member Function Documentation

```
long PowerfulConversion::powerfulToPoly ( zz_pX & poly,  
                                           const HyperCube< zz_p > & powerful  
                                           ) const
```

The conversion routines return the value of the modulus q. It is assumed that the modulus is already set before calling them

The documentation for this class was generated from the following files:

- src/[powerful.h](#)
 - src/powerful.cpp
-

PowerfulDCRT Class Reference

Conversion between powerful representation, [DoubleCRT](#), and ZZx. [More...](#)

```
#include <powerful.h>
```

Public Member Functions

	PowerfulDCRT (const FHEcontext &_context, const Vec< long > &mvec)
const PowerfulTranslationIndexes &	getIndexTranslation () const
const PowerfulConversion &	getPConv (long i) const
void	dcrtToPowerful (Vec< ZZ > &powerful, const DoubleCRT &dcrt) const
void	powerfulToDCRT (DoubleCRT &dcrt, const Vec< ZZ > &powerful) const
void	ZZXtoPowerful (Vec< ZZ > &powerful, const ZZX &poly, IndexSet s= IndexSet::emptySet ()) const
void	powerfulToZZX (ZZX &poly, const Vec< ZZ > &powerful, IndexSet s= IndexSet::emptySet ()) const

Detailed Description

Conversion between powerful representation, [DoubleCRT](#), and ZZX.

The documentation for this class was generated from the following files:

- src/[powerful.h](#)
 - src/powerful.cpp
-

PowerfulTranslationIndexes Class Reference

Holds index tables for translation between powerful and zz_pX. [More...](#)

```
#include <powerful.h>
```

Public Member Functions

PowerfulTranslationIndexes (const Vec< long > &mv)

Public Attributes

long	M
------	----------

long	Phim
------	-------------

Vec< long >	Mvec
-------------	-------------

Vec< long >	Phivec
-------------	---------------

Vec< long >	Divvec
-------------	---------------

Vec< long >	Invvec
-------------	---------------

CubeSignature	longSig
-------------------------------	----------------

CubeSignature	shortSig
-------------------------------	-----------------

Vec< long >	polyToCubeMap
-------------	----------------------

Vec< long >	cubeToPolyMap
-------------	----------------------

Vec< long >	shortToLongMap
Vec< ZZX >	cycVec
ZZX	phimX

Detailed Description

Holds index tables for translation between powerful and zz_pX.

The documentation for this class was generated from the following files:

- src/[powerful.h](#)
 - src/powerful.cpp
-

RandomState Class Reference

Facility for "restoring" the NTL PRG state

```
#include <NumbTh.h>
```

Public Member Functions

void	restore ()
	Restore the PRG state of NTL.

Detailed Description

Facility for "restoring" the NTL PRG state.

NTL's random number generation facility is pretty limited, and does not provide a way to save/restore the state of a pseudo-random stream. This class gives us that ability: Constructing a [RandomState](#) object uses the PRG to generate 512 bits and stores them. Upon destruction (or an explicit call to [restore\(\)](#)), these bits are used to re-set the seed of the PRG. A typical usage of this class is as follows:

```
{
RandomState r; // save the random state
SetSeed(something); // set the PRG seed to something
... // more code that uses the new PRG seed
} // The destructor is called implicitly, PRG state is restored
```

The documentation for this class was generated from the following file:

- src/[NumbTh.h](#)
-

RecryptData Class Reference

A structure to hold recryption-related data inside the [FHEcontext](#)

```
#include <recryption.h>
```

Public Member Functions

void	init (const FHEcontext &context, const Vec< long > &mvec_, long t=0, bool consFlag=false)
------	---

Initialize the recryption data in the context.

bool	operator== (const RecryptData &other) const
------	--

bool	operator!= (const RecryptData &other) const
------	--

Public Attributes

Vec< long >	<u>mvec</u>
	Some data members that are only used for I/O.
long	<u>hwt</u>
	partition of m into co-prime factors
bool	<u>conservative</u>
	Hamming weight of recryption secret-key.
long	<u>e</u>
	flag for choosing more conservatice parameters <u>More...</u>
long	ePrime
long	<u>skHwt</u>
	Hamming weight of recryption secret key.
double	<u>alpha</u>
	an optimization parameter
<u>PAgebraMod</u> *	<u>alMod</u>
	for plaintext space $p^{\{e-e'+r\}}$
<u>EncryptedArray</u> *	<u>ea</u>
	for plaintext space $p^{\{e-e'+r\}}$
<u>EvalMap</u> *	<u>firstMap</u>
	linear maps

EvalMap *	secondMap
PowerfulDCRT *	p2dConv
	conversion between ZZx and Powerful
vector< ZZx >	unpackSlotEncoding
	linPolys for uppacking the slots

Static Public Attributes

static const long	defSkHwt =56
	default Hamming weight of reryption key

Detailed Description

A structure to hold reryption-related data inside the [FHEcontext](#).

Member Data Documentation

long RecryptData::e

flag for choosing more conservatice parameters

skey encrypted wrt space $p^{e-e'+r}$

The documentation for this class was generated from the following files:

- src/[recryption.h](#)
- src/recryption.cpp

ReplicateHandler Class Reference abstract

A virtual class to handle call-backs to get the output of replicate. [More...](#)

```
#include <replicate.h>
```

Public Member Functions

virtual void	handle (const Ctxt &ctxt)=0
--------------	--

Detailed Description

A virtual class to handle call-backs to get the output of replicate.

The documentation for this class was generated from the following file:

- src/[replicate.h](#)

shallow_clone< X > Class Template Reference

Shallow copy: initialize with copy constructor.

```
#include <cloned\_ptr.h>
```

Static Public Member Functions

static X *	apply (const X *x)
------------	---------------------------

Detailed Description

```
template<class X>
class shallow_clone< X >
```

Shallow copy: initialize with copy constructor.

Template Parameters

X The class to which this points

The documentation for this class was generated from the following file:

- src/[cloned_ptr.h](#)
-

SKHandle Class Reference

A handle, describing the secret-key element that "matches" a part, of the form s^r(X^t). [More...](#)

```
#include <Ctxt.h>
```

Public Member Functions

	SKHandle (long newPowerOfS=0, long newPowerOfX=1, long newSecretKeyID=0)
void	setBase (long newSecretKeyID=-1)
	Set powerOfS=powerOfX=1.
bool	isBase (long ofKeyID=0) const
	Is powerOfS==powerOfX==1?
void	setOne (long newSecretKeyID=-1)
	Set powerOfS=0, powerOfX=1.

bool	<code>isOne</code> () const
	Is powerOfS==0?
bool	operator== (const <code>SKHandle</code> &other) const
bool	operator!= (const <code>SKHandle</code> &other) const
long	getPowerOfS () const
long	getPowerOfX () const
long	getSecretKeyID () const
bool	<code>mul</code> (const <code>SKHandle</code> &a, const <code>SKHandle</code> &b)
	Computes the "product" of two handles. More...

Friends

class	Ctxt
istream &	operator>> (istream &s, <code>SKHandle</code> &handle)

Detailed Description

A handle, describing the secret-key element that "matches" a part, of the form $s^r(X^t)$.

Member Function Documentation

```
bool SKHandle::mul ( const SKHandle & a,
                    const SKHandle & b
```

inline

)

Computes the "product" of two handles.

The key-ID's and powers of X must match, else an error state arises, which is represented using a key-ID of -1 and returning false. Also, note that inputs may alias outputs.

To determine if the resulting handle can be re-linearized using some key-switching matrices from the public key, use the method `pubKey.haveKeySWmatrix(handle, handle.secretKeyID)`, from the class [FHEPubKey](#) in [FHE.h](#)

The documentation for this class was generated from the following file:

- src/[Ctxt.h](#)
-

SubDimension Class Reference

A node in a tree relative to some generator

```
#include <permutations.h>
```

Public Member Functions

	SubDimension (long sz=0, bool gd=false, long ee=0, const Vec< long > &bns1=dummyBenes, const Vec< long > &bns2=dummyBenes)
--	---

long	totalLength () const
------	-----------------------------

Public Attributes

long	Size
------	-------------

bool	Good
long	E
Vec< long >	frstBenes
Vec< long >	scndBenes

Friends

ostream &	operator<< (ostream &s, const SubDimension &tree)
-----------	--

Detailed Description

A node in a tree relative to some generator.

The documentation for this class was generated from the following files:

- src/[permutations.h](#)
- src/permutations.cpp

TreeNode< T > Class Template Reference

A node in a full binary tree.

```
#include <permutations.h>
```

Public Member Functions

	TreeNode (const T &d)
--	------------------------------

T &	getData ()
const T &	getData () const
long	getParent () const
long	getLeftChild () const
long	getRightChild () const
long	getPrev () const
long	getNext () const

Friends

class	FullBinaryTree< T >
-------	----------------------------------

Detailed Description

```
template<class T>
class TreeNode< T >
```

A node in a full binary tree.

These nodes are in a vector, so we use indexes rather than pointers

The documentation for this class was generated from the following file:

- src/[permutations.h](#)

zz_pXModulus1 Class Reference

Auxiliary classes to facillitiate faster reduction mod $\Phi_m(X)$ when the input has degree less than m . [More...](#)

```
#include <NumbTh.h>
```

Public Member Functions

	zz_pXModulus1 (long _m, const zz_pX &_f)
const zz_pXModulus &	upcast () const

Public Attributes

long	M
zz_pX	F
long	N
bool	specialLogic
long	K
long	k1

fftRep	R0
fftRep	R1
zz_pXModulus	Fm

Detailed Description

Auxiliary classes to facillitiate faster reduction mod $\Phi_m(X)$ when the input has degree less than m .

The documentation for this class was generated from the following files:

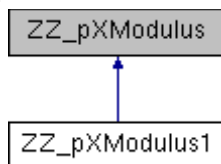
- src/[NumbTh.h](#)
- src/NumbTh.cpp

ZZ_pXModulus1 Class Reference

placeholder for pXModulus ...no optimizations [More...](#)

```
#include <NumbTh.h>
```

Inheritance diagram for ZZ_pXModulus1:



Public Member Functions

	ZZ_pXModulus1 (long $_m$, const ZZ_pX & $_f$)
const ZZ_pXModulus &	upcast () const

Detailed Description

placeholder for pXModulus ...no optimizations

The documentation for this class was generated from the following file:

- src/[NumbTh.h](#)
-