

Board Questions

Fourth Session, Sep 26th

1 Bernoulli RVs

1. Prove: if $X \sim \text{Bernoulli}(p)$ then $\text{var}(X) = p(1 - p)$
2. Prove: if $X \sim \text{bin}(n, p)$ then $\text{var}(X) = np(1 - p)$
3. Suppose X_1, \dots, X_n are independent and all have the same standard deviation $\sigma = 2$. Let \bar{X} be the average of X_1, \dots, X_n . What is the standard deviation of \bar{X} ?

2 Probability Table

$X \backslash Y$	1	2	3	4	5	6
1	1/36	1/36	1/36	1/36	1/36	1/36
2	1/36	1/36	1/36	1/36	1/36	1/36
3	1/36	1/36	1/36	1/36	1/36	1/36
4	1/36	1/36	1/36	1/36	1/36	1/36
5	1/36	1/36	1/36	1/36	1/36	1/36
6	1/36	1/36	1/36	1/36	1/36	1/36

Compute $F(3.5, 4)$.

3 Computing Covariance

Flip a fair coin 3 times. Let X be the number of heads in the first two flips and Y be the number of heads in the last two flips. Compute $\text{Cov}(X, Y)$.

4 Concept Question

Toss a fair coin $2n + 1$ times. Let X be the number of heads on the first $n + 1$ trials and Y be the number of heads on the last $n + 1$ trials. If $n = 1000$ then $\text{Cov}(X, Y)$ is

- a) 0
- b) $1/4$
- c) $1/2$
- d) 1
- e) more than 1
- f) tiny but not 0